

Homework 1

SUBJECT 1: OPERATIONS

STUDENT 1: CALOTĂ OVIDIU

$$b_1 = 8$$

$$b_2 = 16$$

$$x = 111650$$

$$y = 66231$$

$$z = 55\text{ECC8}$$

$$f = 7$$

$$X_{(b_1)} + Y_{(b_1)} = S_{(b_1)}$$

$$111650 + 66231 = 200801$$

$$z_{(b_2)} * f_{(b_2)} = p_{(b_2)}$$

$$55\text{ECC8} * 7 = 2597978$$

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Student 1: Ovidiu Calota

Student 2: Jacine-Jane Boulat

Subject 1

$$S = 200101_{(8)}$$

$$p = 2597978_{(16)}$$

$$y = 66231_{(8)}$$

$$f = 7_{(16)}$$

the point means we subtract the result from here

$$\begin{array}{r} 1 \ 7 \ 7 \ 8 \\ 2 \ 0 \ 0 \ 1 \ 0 \end{array} - 6 \ 6 \ 2 \ 3 \ 1 = 1 \ 1 \ 1 \ 6 \ 5 \ 0_{(8)}$$

here, we need 8 because we don't have where to subtract from so it loses 1 unit for the other to have 8 from which it can subtract

$$2597978_{(16)} : 7_{(16)} = ?$$

we calculate p in base 10 \Rightarrow

$$\begin{aligned} \Rightarrow 2597978_{(16)} &= 8 \cdot 16^6 + 7 \cdot 16^5 + 9 \cdot 16^4 + 7 \cdot 16^3 + 9 \cdot 16^2 + 5 \cdot 16^1 + 2 \cdot 16^0 = \\ &= 8 + 112 + 2304 + 28672 + 589824 + 5242880 + 33554432 = \\ &= 120 + 30976 + 5832704 + 33554432 = \\ &= 31096 + 39387136 = \\ &= 39418232_{(10)} \end{aligned}$$

we change bases for f as well $\Rightarrow 7_{(16)} = 7 \cdot 16^0 = 7_{(10)}$

$$\Rightarrow 39418232_{(10)} : 7_{(10)} = 5631176_{(10)}$$

and now we change the result in base 16

| | | | | |
|-----|-----|-----|---------------------|--------|
| 5 | 631 | 176 | 16 \Rightarrow 02 | 8 |
| 351 | 948 | | 16 \Rightarrow 02 | 12 (C) |
| 21 | 996 | | 16 \Rightarrow 02 | 12 (C) |
| 1 | 374 | | 16 \Rightarrow 02 | 14 (E) |
| | 85 | | 16 \Rightarrow 02 | 5 |
| | 5 | | 16 \Rightarrow 02 | 5 |
| | 0 | | | |

we read the answer from down to up

$$551E55ECC8_{(16)} = Z_{(16)}$$

being the answer

Subject 2

$$b=2 \quad h=16$$

the chosen number is

$$1011 \ 1100 \ 1001 \ 1000 \ 0011 \ 1010 \ 1111 \ 0010_{(2)} = BC983, AF2_{(16)}$$

$$1011 = 2^3 + 2^1 + 2^0 = 8 + 2 + 1 = 11 = B$$

$$1100 = 2^3 + 2^2 = 8 + 4 = 12 = C$$

$$1001 = 9$$

$$0011 = 3$$

$$1111 = 2^3 + 2^2 + 2 + 1 = 15 = F$$

$$1000 = 8$$

$$1010 = 10 = A$$

$$0010 = 2$$

SUBJECT 2:

$$h=16$$

$$b=2$$

$$Y_{(16)} = BC983, AF2$$

$$Y_{(2)} = 1011 \ 1100 \ 1001 \ 1000 \ 0011 \ 1010 \ 1111 \ 0010$$

SUBJECT 3

OPTION 1

$$x = 1111$$

$$y = 11222$$

$$z = 17333$$

$$[X]_{\text{dec}} = 0010 \ 1011 \ 0110 \ 0111$$

$$[Y]_{\text{dec}} = 0010 \ 1011 \ 1101 \ 0110$$

$$[Z]_{\text{dec}} = 0010 \ 1100 \ 0100 \ 0101$$

$$[X]_{\text{inv}} = 0010 \ 1011 \ 0110 \ 0111$$

$$[Y]_{\text{inv}} = 0010 \ 1011 \ 1101 \ 0110$$

$$[Z]_{\text{inv}} = 0010 \ 1100 \ 0100 \ 0101$$

$$[X]_{\text{compl}} = 0010 \ 1011 \ 0110 \ 0111$$

$$[Y]_{\text{compl}} = 0010 \ 1011 \ 1101 \ 0110$$

$$[Z]_{\text{compl}} = 0010 \ 1100 \ 0100 \ 0101$$

$$-x = -1111$$

$$-y = -1122$$

$$-z = -1133$$

$$[-x]_{\text{dec}} = 1101 \ 0100 \ 1001 \ 1001$$

$$[-y]_{\text{dec}} = 1101 \ 0100 \ 0010 \ 1010$$

$$[-z]_{\text{dec}} = 1101 \ 0011 \ 1011 \ 1011$$

$$[-x]_{\text{inv}} = 1101 \ 0100 \ 1001 \ 1000$$

$$[-y]_{\text{inv}} = 1101 \ 0100 \ 0010 \ 1001$$

$$[-z]_{\text{inv}} = 1101 \ 0011 \ 1011 \ 1010$$

$$[-x]_{\text{compl}} = 1101 \ 0100 \ 1001 \ 1001$$

$$[-y]_{\text{compl}} = 1101 \ 0100 \ 0010 \ 1011$$

$$[-z]_{\text{compl}} = 1101 \ 0011 \ 1011 \ 1011$$

Subject 3 $[x]_{\text{compl}} = 0010 \ 1011 \ 0110 \ 0111$

$[y]_{\text{compl}} = 0010 \ 1011 \ 1101 \ 0110$

$[z]_{\text{compl}} = 0010 \ 1100 \ 0100 \ 0101$

$[-x]_{\text{compl}} = 1101 \ 0100 \ 1001 \ 1001$

$[-y]_{\text{compl}} = 1101 \ 0100 \ 0010 \ 1011$

$[-z]_{\text{compl}} = 1101 \ 0011 \ 1011 \ 1011$

we remember that many units we added

$$\begin{array}{r} [x+y]_{\text{compl}} \Rightarrow \begin{array}{cccc} 0010 & 1011 & 0110 & 0111 \\ 0010 & 1011 & 1101 & 0110 \\ \hline 0101 & 0110 & 0011 & 1101 \end{array} \\ [x]_{\text{compl}} + [y]_{\text{compl}} \end{array}$$

$0101 \ 0110 \ 0011 \ 1101 = 1 + 4 + 8 + 16 + 32 + 256 + 512 + 1024 + \dots$

$16384 =$

$= 22333$

$[x-y]_{\text{compl}} = [x+(-y)]_{\text{compl}} \Rightarrow [x]_{\text{compl}} + [-y]_{\text{compl}}$

$$\begin{array}{r} \Rightarrow \begin{array}{cccc} 0010 & 1011 & 0110 & 0111 \\ 1101 & 0100 & 0010 & 1011 \\ \hline 1111 & 1111 & 1001 & 0010 \end{array} \end{array}$$

$-(2^1 + 2^4 + 2^7 + 2^8 + 2^9 + 2^{10} + 2^{11} + 2^{12} + 2^{13} + 2^{14}) =$

$= -(2 + 16 + 128 + 256 + 512 + 1024 + 2048 + 4096 + 8192 + 16384) =$

$= -32658$

$[z-x]_{\text{compl}} = [z+(-x)]_{\text{compl}} \Rightarrow [z]_{\text{compl}} + [-x]_{\text{compl}}$

$$\begin{array}{r} \begin{array}{cccc} 0010 & 1100 & 0100 & 0101 \\ 1101 & 0100 & 1001 & 1001 \\ \hline +0000 & 0000 & 1101 & 1110 \end{array} \end{array} \quad (22)$$

$\Rightarrow 2 + 4 + 8 + 16 + 64 + 128 = 130 + 80 + 12 = 222$

$[-z-x]_{\text{compl}} \Rightarrow [(-z)+(-x)]_{\text{compl}} \Rightarrow [-z]_{\text{compl}} + [-x]_{\text{compl}}$

$$\begin{array}{r} \begin{array}{cccc} 1101 & 0011 & 1011 & 1011 \\ 1101 & 0100 & 1001 & 1001 \\ \hline +1010 & 1000 & 0101 & 0100 \end{array} \end{array} \quad (22) \Rightarrow$$

$$-(2^2 + 2^4 + 2^6 + 2^{11} + 2^{13}) = -(4 + 16 + 64 + 2048 + 8192) = 10320$$