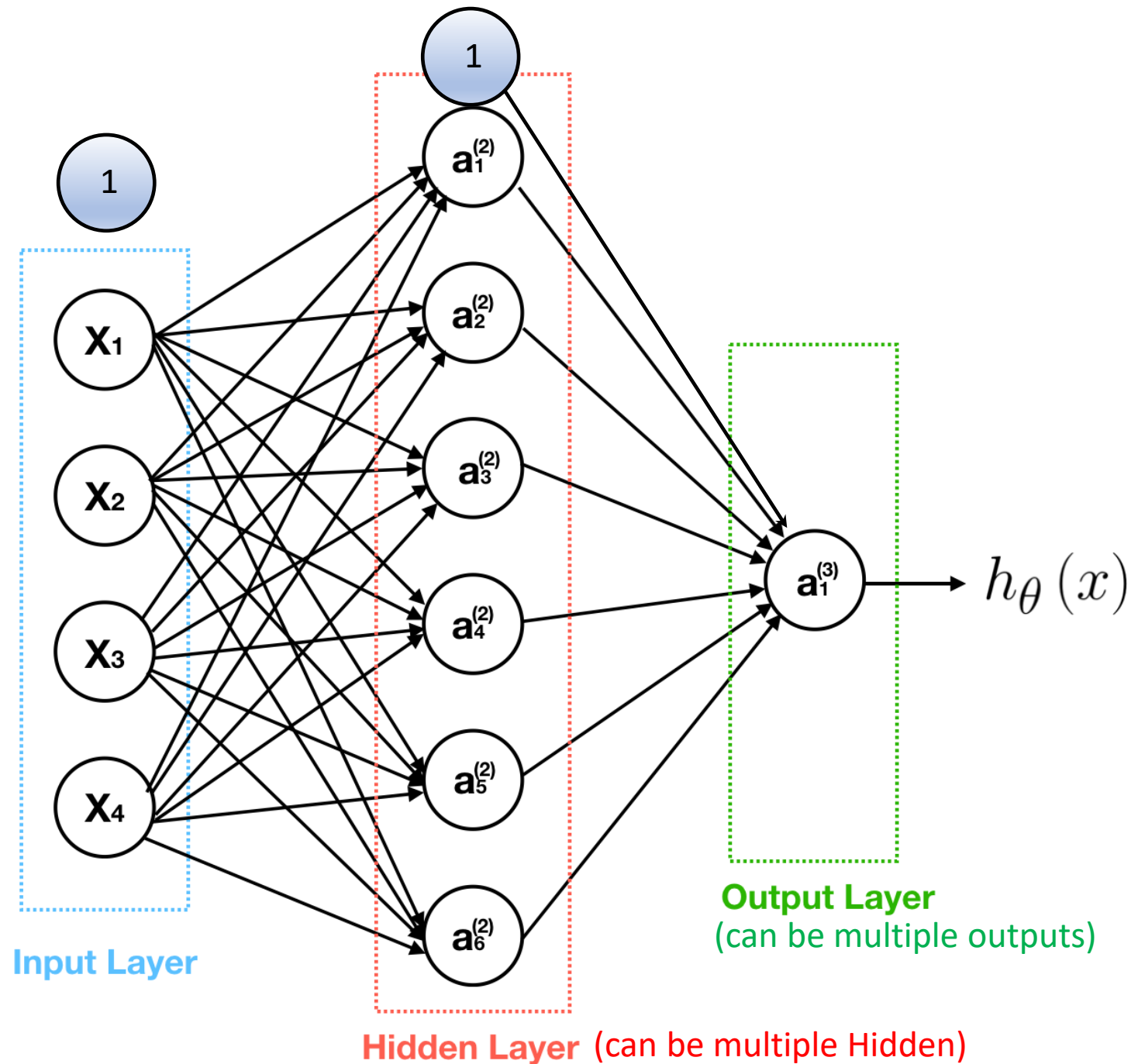


$$\text{Output of neuron} = Y = f(w1.X1 + w2.X2 + b)$$

Neural Network Components



Still remember?



Linear Regression

Model definition

$$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i \quad \epsilon \sim N(0, \sigma_\epsilon^2)$$

Estimated (fitted) model

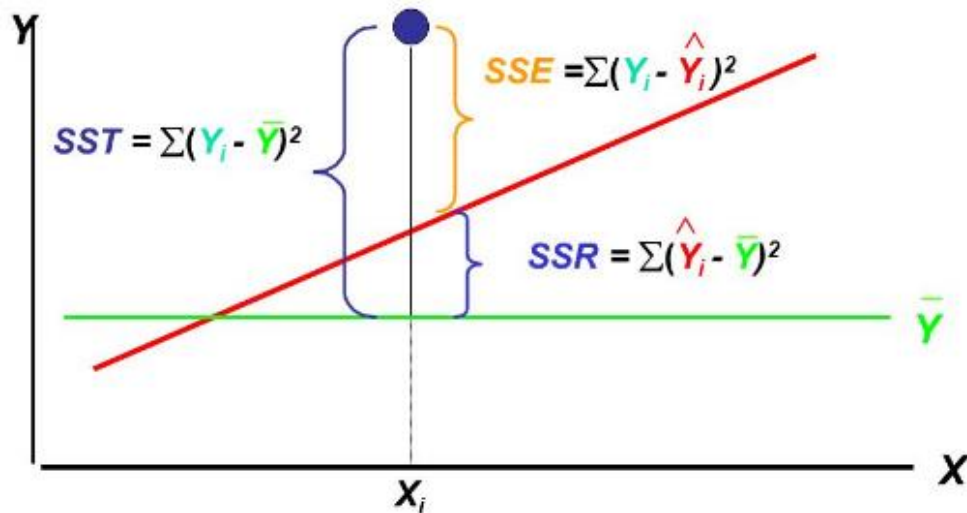
$$\hat{Y}_i = \hat{\beta}_0 + \hat{\beta}_1 X_i$$

Residual errors

$$\hat{\epsilon}_i = Y_i - \hat{Y}_i$$

$$Y_i = \hat{Y}_i + \hat{\epsilon}_i$$

Model Fit, R-square



Logistic regression equation :

Linear regression $Y = b_0 + b_1 \times X_1 + b_2 \times X_2 + \dots + b_K \times X_K$

Sigmoid Function $P = \frac{1}{1 + e^{-Y}}$

By putting Y in Sigmoid function, we get the following result.

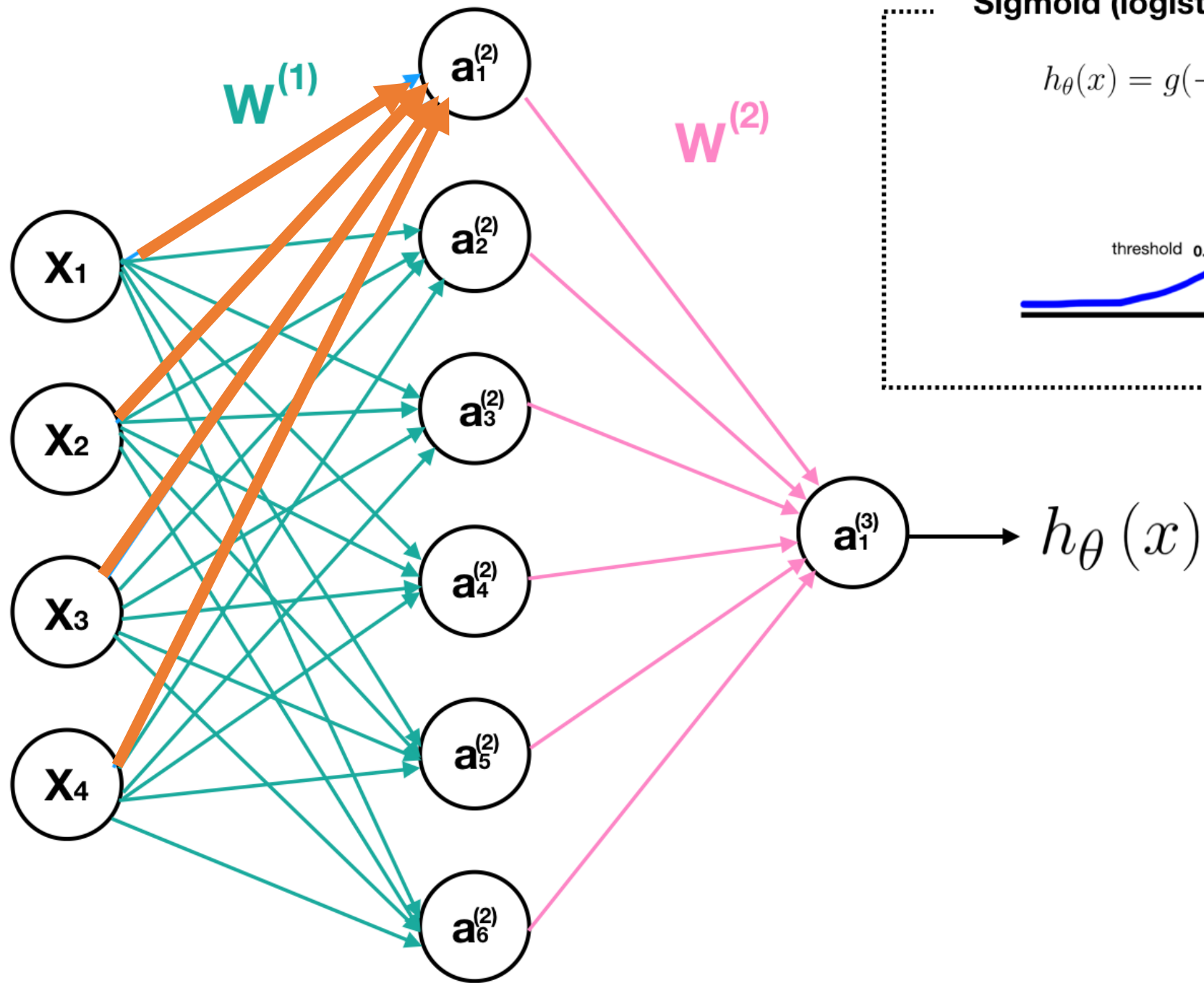
$$\ln\left(\frac{P}{1-P}\right) = b_0 + b_1 \times X_1 + b_2 \times X_2 + \dots + b_K \times X_K$$

$$P :: \textcircled{a^{(1)}} \quad h_{\theta}(x)$$

$$b_0 :: \textcircled{\text{Bias}}$$

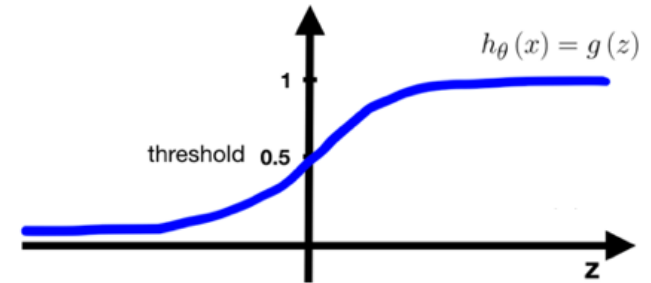
$$b_k :: \textcolor{teal}{w}^{(1)} \quad \textcolor{violet}{w}^{(2)} \quad \theta$$

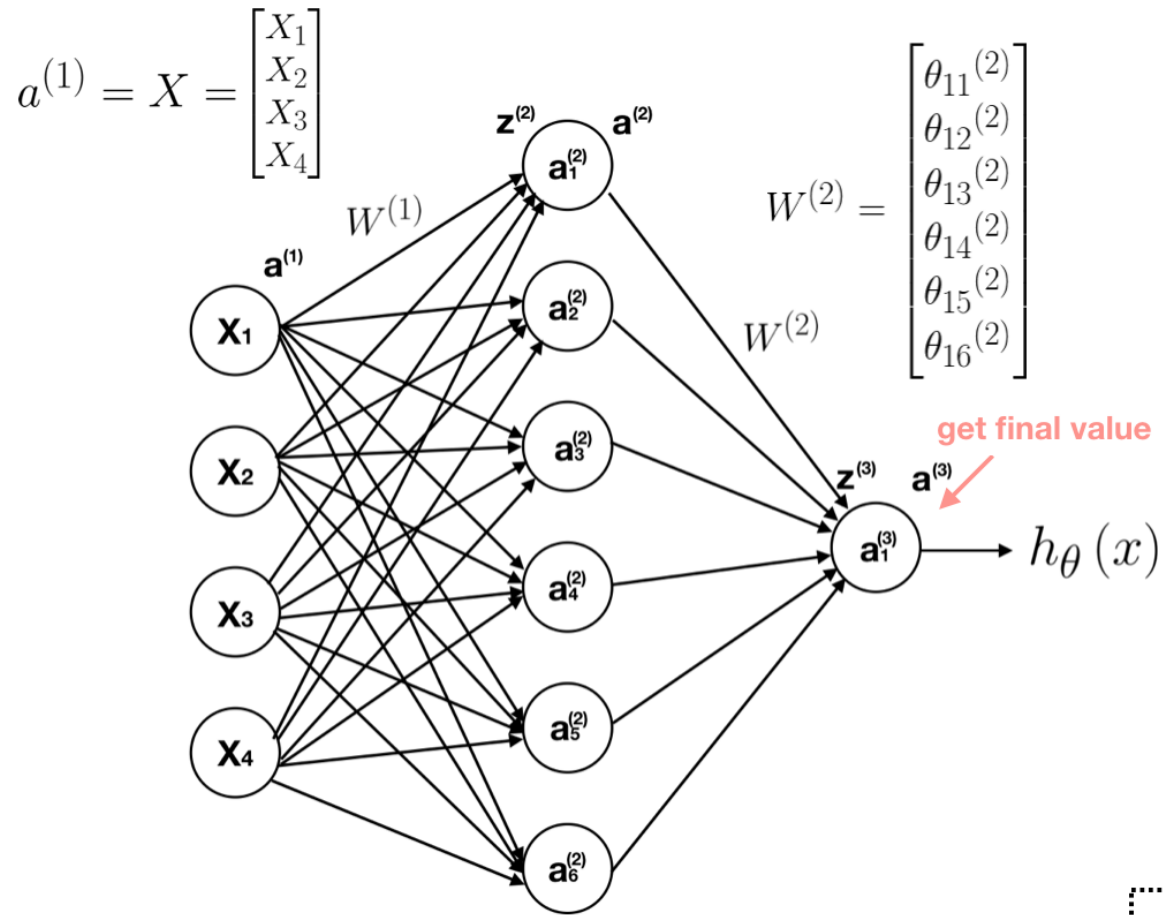
$$\text{SSE} :: J(b) \text{ Loss Functions}$$



Sigmoid (logistic) Activation Function

$$h_\theta(x) = g(-\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$$





$$W^{(1)} = \begin{bmatrix} \theta_{11}^{(1)} & \theta_{21}^{(1)} & \theta_{31}^{(1)} & \theta_{41}^{(1)} & \theta_{51}^{(1)} & \theta_{61}^{(1)} \\ \theta_{12}^{(1)} & \theta_{22}^{(1)} & \theta_{32}^{(1)} & \theta_{42}^{(1)} & \theta_{52}^{(1)} & \theta_{62}^{(1)} \\ \theta_{13}^{(1)} & \theta_{23}^{(1)} & \theta_{33}^{(1)} & \theta_{43}^{(1)} & \theta_{53}^{(1)} & \theta_{63}^{(1)} \\ \theta_{14}^{(1)} & \theta_{24}^{(1)} & \theta_{34}^{(1)} & \theta_{44}^{(1)} & \theta_{54}^{(1)} & \theta_{64}^{(1)} \end{bmatrix}$$

Forward Propagation

$$W^{(1)T} X = z^{(2)}$$

$$a^{(2)} = g(z^{(2)})$$

$$W^{(2)T} a^{(2)} = z^{(3)}$$

$$a^{(3)} = g(z^{(3)})$$

Final value, for prediction

Sigmoid (logistic) Activation Function

$$h_\theta(x) = g(-\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$$

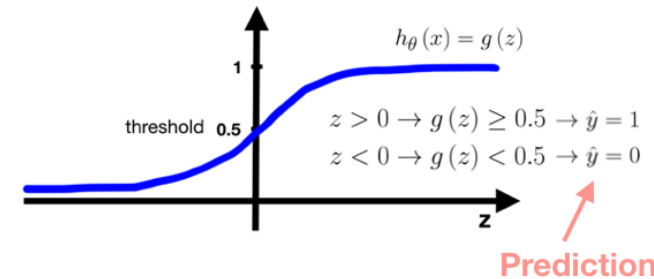


Table 4.1 Choosing the right last-layer activation and loss function for your model

Problem type	Last-layer activation	Loss function
Binary classification	<code>sigmoid</code>	<code>binary_crossentropy</code>
Multiclass, single-label classification	<code>softmax</code>	<code>categorical_crossentropy</code>
Multiclass, multilabel classification	<code>sigmoid</code>	<code>binary_crossentropy</code>
Regression to arbitrary values	None	<code>mse</code>
Regression to values between 0 and 1	<code>sigmoid</code>	<code>mse</code> or <code>binary_crossentropy</code>

Source: Francois Chollet