- 1. (4 points total) Perform a formal proof (as we learned in class, using the Rules of Inference on the front of this sheet) that if $H_1 = \neg p \lor r$, $H_2 = \neg q \lor r$, and $H_3 = p \lor q$, then $H_1 \wedge H_2 \wedge H_3 \rightarrow r$
 - 1. Tpvr Η, 2. 79 V r H2
 - 3. prq Hz
 - 4. gvr resolution 1,3
 - 5. rvr resolution 2,4
 - 6. r logical equivalency

2. (6 points total) Perform a formal proof (as we learned in class, using the Rules of Inference on the front of this sheet) that if $H_1 = (d \lor s) \to p$, $H_2 = c \to \neg p$, $H_3 = \neg c \rightarrow e$, and $H_4 = \neg e$ then $H_1 \wedge H_2 \wedge H_3 \wedge H_4 \rightarrow \neg d$

H,

1.
$$(dvs) \rightarrow p$$

- 2. c → 7p H2
- 3. 7c → e HZ
- H4 4. Te
- modus tollens 3,4
- modus ponens 2,5 6. 7p
- modus tollens 1,6 7. 7 (dvs)
- logically equivalent 7 simplification 8 8. 7d 175
- 9. 7d