

```
In[45]:= (**Programming Language: Wolfram Language (Mathematica)**)
```

```
(**Problem 2**)
```

```
(**Mathematica is weird with how it handles variables  
so people often include this to make it less annoying**)
```

```
Remove["Global`*"]
```

```
f[x_] := x2 - 4 x + 3
```

```
p0 = 1.99;
```

```
p1 = p0;
```

```
tol = 10-5;
```

```
k = 0;
```

```
While[
```

```
  p0 = p1;
```

```
  p1 = p0 -  $\frac{f[p0]}{f'[p0]}$ ;
```

```
  Abs[p1 - p0] >= tol,
```

```
  k = k + 1;
```

```
  Print["p"k, " = ", N[p1, 10]]
```

```
]
```

```
p1 = -48.005
```

```
p2 = -23.0125
```

```
p3 = -10.5262
```

```
p4 = -4.30304
```

```
p5 = -1.23084
```

```
p6 = 0.229819
```

```
p7 = 0.832453
```

```
p8 = 0.987978
```

```
p9 = 0.999929
```

```
p10 = 1.
```

```

In[40]:= p0 = 2.01;
p1 = p0;

tol = 10-5;
k = 0;

While[

  p0 = p1;
  p1 = p0 -  $\frac{f[p0]}{f'[p0]}$ ;
  Abs[p1 - p0] >= tol,

  k = k + 1;

  Print["p"k, " = ", N[p1, 10]]
]
p1 = 52.005
p2 = 27.0125
p3 = 14.5262
p4 = 8.30304
p5 = 5.23084
p6 = 3.77018
p7 = 3.16755
p8 = 3.01202
p9 = 3.00007
p10 = 3.

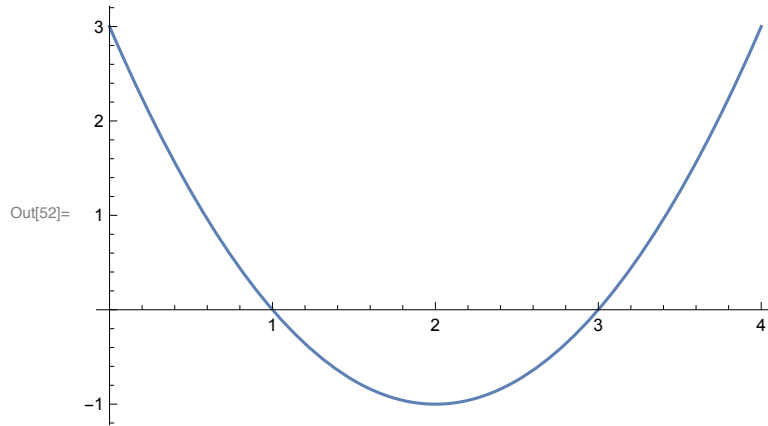
```

```
In[52]:= (**What we find is that this time even though 2.01 is
          close to 1.99 the sequence converges to the other root of 3.**)
```

```
Plot[f[x], {x, 0, 4}]
```

```
Solve[f'[x] == 0, x]
```

```
(**This is because (as shown with the above code)
  the sign of the derivative of f[x] changes at x = 2.**)
```



Out[53]= $\{ \{ x \rightarrow 2 \} \}$

```

(**Problem 3**)

Remove["Global`*"]

(**In Mathematica all reserved names begin with capital letters,
even the constant e!**)
g[x_] := 3 x - E^x

p0 = 1;
p1 = 2;

tol = 10-5;

p2 = p1;
p1 = p0;

k = 0;

(**This expression will be aborted after 30 seconds of attempted evaluation**)
(**If the series doesn't converge within a reasonable
amount of time I think it's safe to say it does not converge**)

TimeConstrained[
  While[
    p0 = p1;
    p1 = p2;

    p2 = p1 -  $\frac{g[p1] (p1 - p0)}{g[p1] - g[p0]}$ ;

    Abs[p2 - p1] >= tol,

    k = k + 1;

    Print["p"k, " = ", N[p2, 10]]
  ]
, 30]

(**In this case the sequence does not converge.**)

p1 = 1.168615340
p2 = 1.311516555
p3 = 1.797043010
p4 = 1.436777893
p5 = 1.486766287
p6 = 1.515325761
p7 = 1.512011934

```

Out[62]= \$Aborted

```

In[63]:= g[x_] := 3 x - E^x

(**Mathematica's answer to this problem
to this problem to see if we are right**)
NSolve[g[x] == 0, x]

(**We choose this points because we know the root is somewhere near 1.5**)
p0 = 2;
p1 = 1.5;

tol = 10-5;

p2 = p1;
p1 = p0;

k = 0;

While[
  p0 = p1;
  p1 = p2;

  p2 = p1 -  $\frac{g[p1] (p1 - p0)}{g[p1] - g[p0]}$ ;

  Abs[p2 - p1] >= tol,

  k = k + 1;
  Print["p"k, " = ", N[p2, 10]]
]

```

NSolve::ifun : Inverse functions are being used by NSolve,
so some solutions may not be found; use Reduce for complete solution information. >>

```
Out[64]= {{x -> 0.619061}, {x -> 1.51213}}
```

```
p1 = 1.50651
```

```
p2 = 1.51224
```

```
p3 = 1.51213
```