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In[98]:= (**Problem 3**)
Remove["Global`*"]

f[x_] :=  $\frac{1}{1+x}$ ;

exact = Integrate[f[x], {x, 0, 1}] // N;

Print["The exact value of the integral is ", exact]
Print["\n"]

TrapRule[a0_, b0_, m0_] :=
Module[{a = N[a0], b = N[b0], m = m0, k},

  h =  $\frac{b-a}{m}$ ;

  sum = 0;

  For[k = 1, k ≤ m-1, k++,
    sum = sum + f[a + h k];];

  Return[ $\frac{h}{2} (f[a] + f[b]) + h \text{ sum}$ ];];

For[n = 10, n ≤ 80, n = 2 n,
  approx = TrapRule[0, 1, n];
  err = Abs[approx - exact];
  Print["n = ", n]
  Print["Approximate Value = ", approx]
  Print["Absolute Error = ", err]
  Print["Absolute Error X n2 = ", err * n2]
  Print["\n"]
]

```

The exact value of the integral is 0.693147

$n = 10$

Approximate Value = 0.693771

Absolute Error = 0.000624223

Absolute Error  $\times n^2 = 0.0624223$

$n = 20$

Approximate Value = 0.693303

Absolute Error = 0.000156201

Absolute Error  $\times n^2 = 0.0624805$

$n = 40$

Approximate Value = 0.693186

Absolute Error = 0.0000390594

Absolute Error  $\times n^2 = 0.0624951$

$n = 80$

Approximate Value = 0.693157

Absolute Error =  $9.76543 \times 10^{-6}$

Absolute Error  $\times n^2 = 0.0624988$

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In[93]:= (**Problem 4**)
Remove["Global`*"]

f[x_] :=  $\frac{1}{1+x}$ ;

exact = Integrate[f[x], {x, 0, 1}] // N;

Simpson[a0_, b0_, m0_] :=
Module[{a = N[a0], b = N[b0], m = m0, k},

  h =  $\frac{b-a}{2 m}$ ;

  SumEven = 0;
  For[k = 1, k ≤ m - 1, k++,
    SumEven = SumEven + f[a + h 2 k];];

  SumOdd = 0;
  For[k = 1, k ≤ m, k++,
    SumOdd = SumOdd + f[a + h (2 k - 1)];];

  Return[ $\frac{h}{3}$  (f[a] + f[b] + 2 SumEven + 4 SumOdd)];];

For[n = 10, n ≤ 80, n = 2 n,
  approx = Simpson[0, 1, n];
  err = Abs[approx - exact];
  Print["n = ", n]
  Print["Approximate Value = ", approx]
  Print["Absolute Error = ", err]
  Print["Absolute Error X n4 = ", err * n4]
  Print["\n"]
]

```

n = 10  
Approximate Value = 0.693147  
Absolute Error =  $1.94105 \times 10^{-7}$   
Absolute Error X  $n^4$  = 0.00194105

n = 20  
Approximate Value = 0.693147  
Absolute Error =  $1.2188 \times 10^{-8}$   
Absolute Error X  $n^4$  = 0.00195008

n = 40  
Approximate Value = 0.693147  
Absolute Error =  $7.62642 \times 10^{-10}$   
Absolute Error X  $n^4$  = 0.00195236

n = 80  
Approximate Value = 0.693147  
Absolute Error =  $4.76791 \times 10^{-11}$   
Absolute Error X  $n^4$  = 0.00195294