

Medical image segmentation in a multiple labelers context: Application to the study of histopathology

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Segmentación de imágenes médicas en un contexto de múltiples anotadores: Aplicación al estudio de histopatologías

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ABSTRACT

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CCGP Correlated Chained Gaussian Processes 18
CCGPMA Correlated Chained Gaussian Processes for Multiple Annotators 17, 19
CE Cross Entropy 32
CGP Chained Gaussian Processes 18
CNN Convolutional Neural Networks 3, 14, 22, 23
CT Computed Tomography 11
ELBO Evidence Lower Bound 18
GCE Generalized Cross Entropy 32
GCECDL Generalized Cross-Entropy-based Chained Deep Learning 20, 21
ISS Image Semantic segmentation 2, 3, 6, 11, 13, 21-23
LF Latent Function 18
MAE Mean Absolute Error 32, 33
MITs Medical Imaging Techniques 1
ML Machine Learning 11, 21
MV Majority Voting 11, 12
OCR Optical Character Recognition 11
PET Positron Emission Tomography 14
ROI Region of Interest 2, 6
SLFM Semi-Parametric Latent Factor Model 18
SS Semantic segmentation 3
STAPLE Simultaneous Truth and Performance Level Estimation 12-14
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CAD Computer-Aided Diagnosis 2, 5, 6

WSI Whole Slide Imaging 1, 5, 6, 8, 15

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СНАРТЕГ	137
ONE	138
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INTRODUCTION

1.1 Motivation

Since Roentgen's discovery of X-rays in 1895, medical imaging has advanced significantly, with modalities like radionuclide imaging, ultrasound, CT, MRI, and digital radiography emerging over the past 50 years. Modern imaging extends 144 beyond image production to include processing, display, storage, transmission and 145 analysis. [Zhou et al., 2021]. Other Medical Imaging Techniques (MITs) have arose 146 during the last decades, some of them implying only the examination of certain 147 pieces or tissues instead of complete patients, like histopathological images, which 148 are images of tissue samples obtained from biopsies or surgical resections and are widely used for the diagnosis of diseases like cancer through Whole Slide Imaging (WSI) scanners [Rashmi et al., 2021]. 151

Along with the advances in technologies for medical images acquisition, computational technologies on pattern recognition and artificial intelligence have

also emerged, allowing the development of Computer-Aided Diagnosis (CAD) systems based on machine learning algorithms. These systems aim to assist 155 physicians in the diagnosis and treatment of diseases, by providing a second 156 opinion or by automating the analysis of medical images. [Panayides et al., 2020]. One of the most used tasks in which machine learning technologies is being used in the universe of medical images is Image Semantic segmentation (ISS), which 159 consists of assigning a label to each pixel in an image according to the object it 160 belongs to. This task is crucial for the development of CAD systems, as it allows 161 the identification of Region of Interest (ROI) in the images, which can be used to 162 detect and classify diseases [Azad et al., 2024]. 163

The application of Machine Learning in medical imaging has grown significantly, 164 with key tasks including classification, segmentation, anomaly detection, 165 super-resolution, image registration, and synthetic image generation 166 [Brito-Pacheco et al., 2025]. Among imaging modalities, X-rays and CT scans are 167 widely used for classification and anomaly detection, especially in pulmonary and 168 oncological applications. MRI and ultrasound play a crucial role in segmentation and resolution enhancement, while PET/SPECT imaging is essential for anomaly detection in oncology and neurodegenerative diseases [Brito-Pacheco et al., 2025]. Histopathology is rapidly gaining prominence, particularly in segmentation and feature extraction, where AI-driven techniques aid in automated cancer diagnosis 173 and tissue structure analysis. The integration of Deep Learning in histological 174 image processing is revolutionizing pathology, enabling more precise and efficient 175 diagnostics. A brief comparison of the tasks and medical image types based on 176 recent literature review, can be seen in Figure 1-1. [Yu et al., 2025], [Brito-Pacheco et al., 2025], [Ryou et al., 2025], [Hu et al., 2025], [Elhaminia et al., 2025]

For solving the different requirements of tasks in medical images, a variety of computational techniques have been developed [Zhou et al., 2021]. Initially, these needs were covered with simple morphological filters, which implied no training process or elaborated optimization. However, as the complexity of the tasks increased, the need for more sophisticated techniques arose, leading to the

1.1 Motivation 3

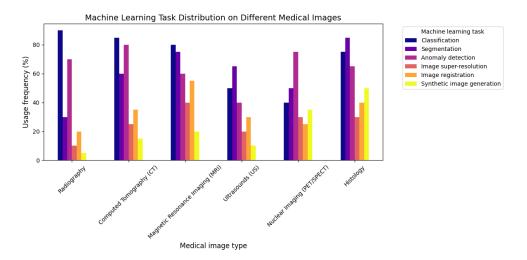


Figure 1-1 Estimation of the tasks and medical image types based on recent literature review (count of referenced terms).

application of advanced statistical tools and machine learning algorithms like Support Vector Machines, Decision Trees, and SGD Neural Networks [Avanzo et al., 2024]. The coevolution of advances in medical image acquisition, computational power (i.e. Moore's law) and statistical/mathematical techniques have led to a convergence for merging state of the art algorithms with medical imaging [Shalf, 2020]. Figure 1-2 shows a brief timeline of coevolution between some conspicuous advances in computational pattern recognition and its medical applications in different scopes (besides medical imaging) [Avanzo et al., 2024].

Convolutional Neural Networks (CNN) have been widely used in Semantic segmentation (SS) tasks, as they have outperformed traditional machine learning algorithms in this task for both medical and non medical images [Xu et al., 2024] [Sarvamangala and Kulkarni, 2022]. However, most CNN architectures are deep, which imply a necessity of a large amount of data to train them. This introduces a problem since both the acquisition and annotation of medical images are expensive and time-consuming processes. This is especially true for ISS tasks, as they require pixel-level annotations, which is taxing in terms of cost, time and logistics involved [Bhalgat et al., 2018]. Other fashions face this problem through less expensive annotation strategies like bounding boxes or anatomical landmarks

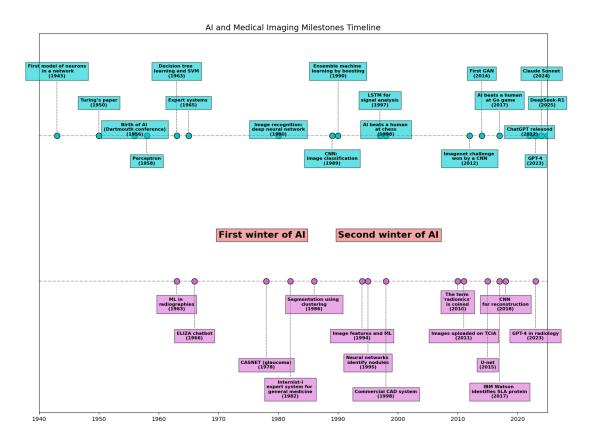


Figure 1-2 AI and machine learning in medical imaging brief timeline.

1.1 Motivation 5

for being used in a semi-supervised strategy [Shah et al., 2018].

Many medical images datasets however, contain a high variability in class sizes and variations in colors, which is specially noticeable in histopathological images because of the usage of different staining and other factors which can affect the color of the images. This variability can lead to a significant loss of efficiency of machine learning models when using a mixed supervision strategy, as the model can be biased towards the most common classes or colors in the dataset [Shah et al., 2018].

This is were other solutions arise to tackle the problem of the weak image annotation while mainlining low costs. One of these solutions is crowdsourcing strategy, which consists of having multiple annotators labeling the same image, and then combining the labels to obtain a consensus label [Lu et al., 2023]. This strategy can lead to a labeling cost reduction when different levels of expertise are combined, since the crowd may be composed of both experts and laymen, being the latter less expensive to hire [López-Pérez et al., 2023].

Recently, diagnosis, prognosis and treatment of cancer have heavily relied on 217 histopathology, where tissue samples are obtained through biopsies or surgical 218 resections and critical information that helps pathologists determine the presence and severity of malignancies [López-Pérez et al., 2024]. The segmentation of histopathological images enables precise identification of structures such as 221 nuclei, glands, and tumors, which are essential for assessing disease progression 222 and treatment response [Rashmi et al., 2021]. Accurate segmentation is 223 particularly crucial in digital pathology, where whole-slide images (WSI) are 224 analyzed using AI-powered CAD systems to support clinical decision-making [López-Pérez et al., 2024]. 226

A major challenge in histopathological image segmentation arises from the variability in annotations provided by different pathologists. Unlike natural images, where object boundaries are often well-defined, histological structures may have ambiguous borders, leading to inconsistencies among annotators

[López-Pérez et al., 2023]. Because of this, crowdsourcing labeling is one of the most popular approaches, as illustrated in Figure 1-3, an example of how histopathological images are segmented by multiple experts, showing some variations in label assignment ¹. These discrepancies highlight the need for models that can handle annotation uncertainty effectively. Leveraging crowdsourcing strategies and machine learning techniques that infer annotator reliability can enhance segmentation performance while reducing costs.

1.2 Problem Statement

Throughout the development of medical technology and CAD, the task of ISS has become a crucial step in delivering precise diagnosis and treatment planning [Giri and Bhatia, 2024]. Particularly, in the area of histopathological studies, the usage of Whole Slide Images (WSI) is rather common since this method delivers high quality imaging and allows for the diagnosis of diseases like cancer [Lin et al., 2024].

ISS task consists of assigning a label to each pixel in an image according to the 244 object it belongs to. Accurate segmentation is essential for the development of 245 CAD systems, as it allows the identification of regions of interest (ROI) in the images, which can be used to detect and classify diseases and hence, treatment planning [Sarvamangala and Kulkarni, 2022]. However, modern computational solutions for ISS tasks involve the use of deep learning, which mostly rely large amounts of labeled data to train the models on supervised learning techniques. 250 This means that the model is trained on a dataset with ground-truth labels, which 251 are assumed to be correct and consistent across all samples. In practice, this 252 assumption is often violated due to the high technical complexity of labeling these 253 segments ².

¹obtained from a real world Triple Negative Breast Cancer (TNBC) dataset published in [López-Pérez et al., 2023]

²compared to a more trivial task like image classification on ordinary an well known classes like MNIST

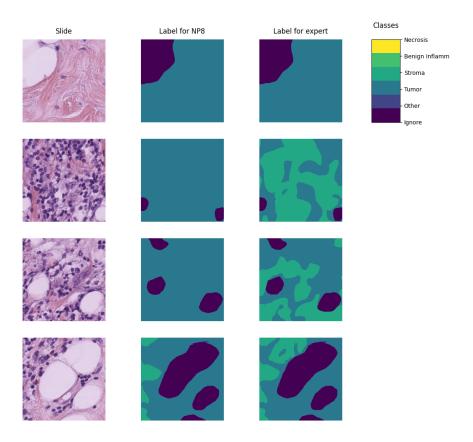


Figure 1-3 Example of a histopathological image segmented by multiple annotators, illustrating variations in label assignment.

The process of labeling medical images is often managed with the help of specialized software tools that allow the annotators to draw the regions, delivering 256 an standard format for the labeled masks [Habis, 2024]. Despite the help of these 257 tools, the labeling process in WSI can have high costs, as it requires long hours of work from specialized personnel. Because of cost constraints in many medical institutions, the labeling processes is often done by multiple labelers with varying 260 levels of expertise, equalizing the cost of the labeling process. However, this 261 strategy can lead to inconsistent labels, as the consensus between the labelers may 262 not be exact due to the diversity in depth of knowledge and experience of the 263 labelers [Xu et al., 2024]. These inconsistencies are mostly represented in the 264 subsections 1.2.1 and 1.2.2.

1.2.1 Variability in Expertise Levels

One of the primary sources of inter-observer variability in medical image segmentation is the difference in expertise levels among annotators [López-Pérez et al., 2023]. Experienced radiologists and pathologists tend to produce highly precise annotations, whereas novice labelers may introduce systematic biases due to their limited familiarity with subtle image features. Studies have demonstrated that annotation accuracy *tends* to improve with experience, yet medical institutions often rely on a mix of annotators to manage costs and workload distribution [Lu et al., 2023].

The training background of annotators and institutional guidelines play a crucial role in shaping labeling practices. Different medical schools and hospitals may adopt distinct segmentation protocols, leading to inconsistencies when datasets are combined from multiple sources [López-Pérez et al., 2023]. For example, some institutions may emphasize conservative delineation of tumor boundaries, while others adopt a more inclusive approach. Such variations contribute to systematic biases in medical image datasets [Banerjee et al., 2025].

Medical images frequently contain structures with ambiguous boundaries, making segmentation inherently subjective. For instance, tumor margins in histopathological slides may not have well-defined edges, leading to variations in how different annotators delineate the regions of interest [Carmo et al., 2025]. These discrepancies arise not only from technical expertise but also from differences in perception and interpretation.

1.2.2 Technical Constraints and Image Quality

Technical constraints in medical imaging, such as resolution differences, noise levels, and contrast variations, can significantly impact segmentation accuracy.

Lower-resolution images may obscure fine structures, leading to inconsistencies in boundary delineation [Zhou et al., 2024].

When combined with long sessions, bad images might also increase the cognitive load of the annotators, leading to fatigue and reduced precision in labeling [Kim et al., 2024]. This is particularly relevant in histopathological studies, where the staining process and tissue preparation can introduce color variations and artifacts that affect image quality, even if the same scanning equipment is used [Karthikeyan et al., 2023].

299 1.2.3 Research Question

Given the challenges posed by inconsistent labels in medical image segmentation, this work aims to address the following research question:

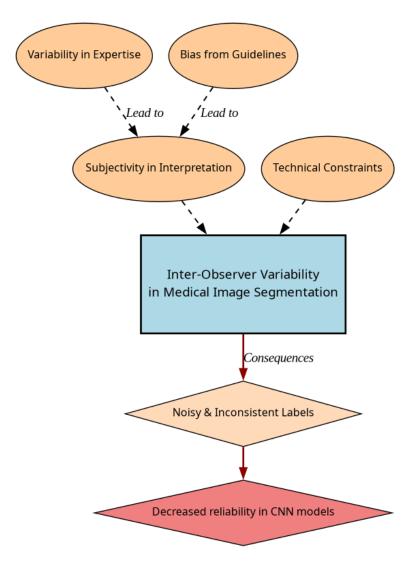


Figure 1-4 Summary diagram for problem Statement

Research Question

How can we develop a learning approach for ISS tasks in medical images that can adapt to inconsistent labels without requiring explicit supervision of labeler performance, while addressing challenges related to variability in expertise levels and technical constraints, and maintaining interpretability, generalization, and computational efficiency?

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1.3 Literature review

Certainly, in general Machine Learning (ML) classification tasks ³ where multiple 304 annotators are involved, Majority Voting (MV) is by far the simplest possible 305 approach to implement. This concept was born multiple times and divergently in multiple fields, but it was described as relevant for ML and pattern recognition labeling for classification in [Lam and Suen, 1997], in which the approach is exposed as simple, yet powerful. The authors describe the MV as a method that 309 can be used to improve the accuracy of classification tasks by combining the labels 310 of multiple annotators. The method is based on the assumption that the majority 311 vote of the annotators is more likely to be correct than the vote of a single 312 annotator. The authors also describe the method as a straightforward way to 313 improve the accuracy of classification tasks without the need for complex 314 algorithms or additional data. The authors also prove this method to deliver very similar results to more complicated approaches (Bayesian, logistic regression, fuzzy integral, and neural network) in the particular task of Optical Character Recognition (OCR). Despite its simplicity, modern solutions for delivering accurate 318 medical image segmentation models still rely on Majority Voting at some stage, 319 like [Elnakib et al., 2020], which uses a majority voting strategy for delivering a 320 final output based on the labels of multiple models (VGG16-Segnet, Resnet-18 and 321 Alexnet) in Computed Tomography (CT) images for Liver Tumor Segmentation, or

³In this work, image segmentation is considered as a particular case of classification in which target classes are assigned pixel-wise.

[López-Pérez et al., 2023], which uses MV for combining noisy annotations as an additional annotator to be included in the deep learning solution. Majority voting as a technique for setting a pseudo ground truth label is a powerful approach for its simplicity in many use cases in which the target to be labeled is not tied to an expertise related task, otherwise, the assumption of equal expertise among the labelers can be a source of bias in the final label, which is not desirable in the case of highly technical annotations like medical images. In subsection 1.3.1, we will be reviewing literature which no longer assumes the naive approach of equal expertise among labelers and face the challenge of learning from inconsistent labels.

1.3.1 Facing annotation variability in medical images

Learning from crowds approaches in general face the challenge of not having a 334 ground truth label and hence, an intrinsic difficulty in measuring the real reliability 335 of the labelers annotations. Some approaches assume beforehand a certain level of 336 expertise for each labeler based on experience as an input, like in [TIAN and Zhu, 337 2015], which introduce the concept of max margin majority voting, using the 338 reliability vector as weights for the weights for the binary and multiclass classifier. The crowdsourcing margin is the minimal difference between the aggregated score of the potential true label and the scores for other alternative labels. Accordingly, 341 the annotators' reliability is estimated as generating the largest margin between 342 the potential true labels and other alternatives. The problem introduced in this 343 approach is assuming an stationary reliability per expert across the whole input 344 space, which is imprecise since annotators performance may change between different tasks or even between different regions of the same image.

47 STAPLE Mechanism

The Simultaneous Truth and Performance Level Estimation (STAPLE) algorithm, introduced in [Warfield et al., 2004] is a probabilistic framework that estimates a

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hidden true segmentation from multiple segmentations provided by different raters. It also estimates the reliability of each rater by computing their sensitivity and specificity.

The STAPLE algorithm's goal is to maximize the log likelihood function:

$$(\mathbf{\dot{p}}, \mathbf{\dot{q}}) = \arg\max_{\mathbf{p}, \mathbf{q}} \ln f(\mathbf{D}, \mathbf{T} \mid \mathbf{p}, \mathbf{q}). \tag{1-1}$$

Where **D** is the set of segmentations provided by the raters, **T** is the hidden true segmentation, p is the sensitivity and q is the specificity of the raters.

This is achieved by using the Expectation-Maximization algorithm to maximize the log likelihood function in equation, which is done iteratively with step computations:

$$\begin{split} (p_{j}^{(k)},q_{j}^{(k)}) &= \arg\max_{p_{j},q_{j}} \sum_{i:D_{ij}=1} W_{i}^{(k-1)} \ln p_{j} \\ &+ \sum_{i:D_{ij}=1} \left(1 - W_{i}^{(k-1)}\right) \ln (1 - q_{j}) \\ &+ \sum_{i:D_{ij}=0} W_{i}^{(k-1)} \ln (1 - p_{j}) \\ &+ \sum_{i:D_{ij}=0} \left(1 - W_{i}^{(k-1)}\right) \ln q_{j}. \end{split} \tag{1-2}$$

The capacity of STAPLE to accurately estimate the true segmentation, even in the presence of a majority of raters generating correlated errors, was demonstrated, which makes it theoretically a strong choice for setting a ground-truth in binary or multiclass medical ISS tasks.

The popularity and performance of STAPLE has led to its usage in modern applications medical image, 3d spatial images due to its assumption of decision

space being based on voxel-wise decisions, like the authors in [Grefve et al., 2024] which applied the algorithm on Positron Emission Tomography (PET) images.

Other authors still rely heavily on STAPLE for setting a ground truth consensus for histopathological images, like [Qiu et al., 2022].

However, the STAPLE algorithm has some limitations. It assumes independent rater errors, which may not hold in practice, leading to biased estimates. STAPLE is also sensitive to low-quality annotations, potentially degrading final segmentations if the weights are not initialized correctly. The algorithm tends to over-smooth results, blurring fine details, and struggles with multi-class segmentation. Computationally, it is expensive due to its iterative EM approach. Additionally, STAPLE cannot correct systematic biases in annotations and depends on initial estimates, impacting accuracy. Lastly, the estimated performance levels lack interpretability, making it difficult to assess annotator reliability effectively.

Finally, this work contemplates STAPLE as useful for label aggregation,hence being a good support for other methods, but not that useful for providing annotations of structures on new and unlabeled images.

U-shaped CNNs

Since the introduction of U-Net [Ronneberger et al., 2015] in 2015 for biomedical image segmentation, U-shaped CNNs have become a prevalent architecture in medical image segmentation tasks. The U-Net's success stems from its ability to capture both global and local information through its contracting and expanding paths, making it particularly effective for complex and heterogeneous structures, even with limited annotated data. This architecture has been successfully applied to various medical image segmentation tasks, including organ segmentation, tumor segmentation, and brain structure segmentation.

The U-Net architecture consists of a symmetric encoder-decoder structure with skip connections. The encoder path progressively reduces spatial dimensions

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while increasing feature channels through a series of convolutional and max-pooling layers, capturing high-level semantic information. The decoder path uses transposed convolutions to gradually recover spatial resolution while reducing feature channels. Skip connections between corresponding encoder and decoder layers preserve fine-grained details by concatenating high-resolution features from the encoder with upsampled features in the decoder, enabling precise localization of structures.

U-Net based approaches

In [López-Pérez et al., 2024] two networks are trained for delivering a final segmentation. One network is trained to estimate the annotators reliability and another one is trained to segment the image. The first network is a deep neural network that takes as input features of image and the labelers id encoded as one-hot and outputs a reliability map across the image feature space. This map is then used to weight the contribution of each annotator to the final segmentation.

The second network is the U-Net used for segmentation.

In this approach, it is assumed that the images are labeled for at least one labeler and not all of them, which is closer to a real world scenario, in which it is common to have images with variability in the amount of annotations, per patch. Hence, the input data can be modeled as:

$$\mathcal{D} = (\mathbf{X}, \tilde{\mathbf{Y}}) = \{ (\mathbf{x}_n, \tilde{\mathbf{y}}_n^r) : n = 1, \dots, N; r \in R_n \},$$
(1-3)

Where every \mathbf{x}_n is an input patch from a ROI in one WSI, $\tilde{\mathbf{y}}_n$ is the noisy annotation from the r labeler, N is the number of patches in the dataset and $R_n \subset \{1, \dots, R\}$ is the set of labelers that annotated the image \mathbf{x}_n .

The authors then assume the annotator network to deliver a reliability map $\{\hat{\mathbf{A}}_{\phi}^{(r)}(\mathbf{x})\}_{r\in R_n}$ with different dimensions:

• CR global: a single reliability vector per labeler with dimensions C which represent global reliability of the labeler across all input space.

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- CR image: a single reliability vector per image per labeler with dimensions *C* which represent local reliability of the labeler across the image.
- CR pixel: a reliability matrix per image per labeler, with dimensions C which represent local reliability of the labeler across all the pixels in the image.
- These differences in dimensions are determined by the feature extraction space from segmentation network which feed the input of the annotator network, which the authors vary for experimentation purposes.
- Being $\mathbf{p}_{\theta}(\mathbf{x}_n)$ the estimation of the latent (ground truth) segmentation delivered by the segmentation UNet network, thus, the estimated segmentation probability mask for each annotator is given by the product:

$$\mathbf{p}_{\theta,\phi}^{(r)}(\mathbf{x}_n) := \mathbf{A}_{\phi}^{(r)}(\mathbf{x}) \odot \mathbf{p}(\mathbf{x}_n), \tag{1-4}$$

where \odot is the element-wise product and ϕ and θ are the parameters of the annotator network and the segmentation UNet network, respectively, being the latter initialized with a ResNet34 backbone pre-trained on ImageNet.

The authors propose a loss function involving cross-entropy and a trace based regularization on the reliability map, originally proposed in [Zhang et al., 2020] which combined, looks like:

$$\mathcal{L}(\theta, \phi) := \sum_{n=1}^{N} \sum_{r=1}^{R} \mathbb{I}\left(\tilde{\mathbf{y}}_{n}^{(r)} \in R_{n}\right) \cdot \left[CE\left(\mathbf{A}_{\phi}^{(r)}(\mathbf{x}_{n}) \cdot \mathbf{p}_{\theta}(\mathbf{x}_{n}), \tilde{\mathbf{y}}_{n}^{(r)}\right) + \lambda \cdot tr\left(\mathbf{A}_{\phi}^{(r)}(\mathbf{x}_{n})\right) \right]$$
(1-5)

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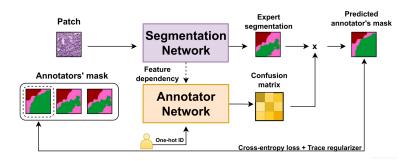


Figure 1-5 Proposed framework for the approach in [López-Pérez et al., 2024].

- Being $\mathbb I$ the indicator function, CE the cross-entropy loss, and λ the regularization parameter.
- When evaluated on a Triple Negative Breast Cancer dataset, this approach achieves a Dice coefficient of 0.7827, outperforming STAPLE (0.7039) and matching expertsupervised performance (0.7723). The CR image reliability modeling proved most effective, as CR pixel, while potentially offering finer-grained reliability estimation, requires significantly more training data.
- Despite the decent performance of the approach, solving the problem of multiple labelers with two networks can be overwhelming for the optimization process, requiring large amounts of annotated data to properly codify the annotators spatial reliabilities, which could be managed by a single model with an appropriate loss function.

Bayesian models

Bayesian approaches are a good choice for handling label noise and uncertainty in the labelers. In [Julián and Álvarez Meza Andrés Marino, 2023] the authors propose a novel approach from Gaussian Processes to model the relationship between the annotators' reliability and the input data, while also preserving the interdependencies among the annotators. This is achieved by introducing Correlated Chained Gaussian Processes for Multiple Annotators (CCGPMA), a 18 Introduction

framework based on the well known Chained Gaussian Processes (CGP). CGP on itself cannot consider inter-annotator dependencies, thus, the authors introduce the Correlated Chained Gaussian Processes (CCGP) to model correlations between the GP latent functions, which are supposed to be generated from a Semi-Parametric Latent Factor Model (SLFM):

$$f_j(\mathbf{x}_n) = \sum_{q=1}^{Q} w_{j,q} \mu_q(\mathbf{x}_n), \tag{1-6}$$

where $f_j: \mathcal{X} \to \mathbb{R}$ is a Latent Function (LF), $\mu_q(\cdot) \sim \mathfrak{GP}(0, k_q(\cdot, \cdot))$ with $k_q: \mathcal{X} \times \mathcal{X} \to \mathbb{R}$ being a kernel function, and $w_{j,q} \in \mathbb{R}$ is a combination coefficient ($Q \in \mathbb{N}$). This leads to a joint distribution of the form:

$$p(\mathbf{y}, \hat{\mathbf{f}}, u | \mathbf{X}) = p(\mathbf{y} | \boldsymbol{\theta}) \prod_{j=1}^{J} p(\mathbf{f}_{j} | \mathbf{u}) p(\mathbf{u}),$$
(1-7)

where \mathbf{y} is the vector of noisy labels, $\hat{\mathbf{f}}$ is the vector of latent functions, u represents the inducing points, and \mathbf{X} is the input data.

Combined with inducing-variables based methods for sparse GP approximations, and maximizing an Evidence Lower Bound (ELBO) for the estimation of the variational parameters, the authors reach a model whose variational expectations are not analytically tractable, and hence, the authors derive a Gaussian-Hermite quadrature approach.

Finally, the authors extend this approach for being applied to classification an regression, reaching the only known approach to involve chained gaussian processes in multiple annotators classification and regression tasks while

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preserving the interdependencies among the annotators, and also outperforming GPC-MV⁴, MA-LFC-C⁵, MA-DGRL⁶, MA-GPC⁷, MA-GPCV⁸, MA-DL⁹, KAAR¹⁰.

473 CCGPMA on itself proposes a good approach for handling label noise and
474 uncertainty in the labelers for regression and classification tasks, while also
475 preserving the interdependencies among the annotators, however, it does not face
476 the image segmentation problem, which is the main focus of this works, however,
477 it does not face the image segmentation problem, which is the main focus of this
478 work. Besides, handling so many latent functions during the optimization process
479 is computationally expensive, making it on itself infeasible for large and high
480 resolution datasets.

1.3.2 Facing noisy annotations and low-quality data

The problem of low-quality data and noisy annotations has been tackled with various strategies. One such approach is the use of deep learning models that incorporate loss functions designed to mitigate the effects of unreliable labels. Traditional methods such as Majority Voting (MV) or Expectation-Maximization (EM) have been widely used for aggregating multiple annotators' inputs. However, they assume a homogeneous reliability of annotators, which may not hold in real-world scenarios.

⁴A GPC using the MV of the labels as the ground truth.

⁵A LRC with constant parameters across the input space.

⁶A multi-labeler approach that considers as latent variables the annotator performance.

⁷A multi-labeler GPC, which is an extension of MA-LFC.

⁸An extension of MA-GPC that includes variational inference and priors over the labelers' parameters.

⁹A Crowd Layer for DL, where the annotators' parameters are constant across the input space.

¹⁰A kernel-based approach that employs a convex combination of classifiers and codes labelers dependencies.

20 Introduction

Loss functions in deep learning models

Loss functions are fundamental components in deep learning models that quantify how well a model's predictions match the ground truth. They serve as the 491 objective function that guides the learning process by measuring the discrepancy between predicted and actual values. In classification tasks, the most common loss functions are Cross-Entropy (CE) and Mean Absolute Error (MAE). CE is 494 particularly effective for classification as it heavily penalizes confident but wrong 495 predictions, though it can be sensitive to noisy labels. MAE, on the other hand, is 496 more robust to outliers and assigns equal weights to all mistakes, but typically 497 requires more training iterations. For image segmentation tasks, specialized loss 498 functions have been developed to handle the unique challenges of pixel-wise 499 classification. The Dice loss, which measures the overlap between predicted and ground truth regions, is widely used in medical image segmentation. recently, the Generalized Cross Entropy (GCE) loss has emerged as a robust alternative that combines the benefits of both CE and MAE, allowing for better 503 handling of noisy labels through a tunable parameter that controls sensitivity to 504 outliers. In multi-annotator scenarios, where multiple experts provide potentially 505 inconsistent segmentations, novel loss functions like the Truncated Generalized 506 Cross Entropy for Semantic Segmentation (TGCE_{SS}) have been developed to 507 account for varying annotator reliability across different image regions. These loss functions are crucial for training accurate segmentation models, especially in medical imaging where precise delineation of anatomical structures is essential for diagnosis and treatment planning.

Generalized Cross-Entropy for multiple annotators classification

A more recent approach was proposed by [Triana-Martinez et al., 2023], introducing a Generalized Cross-Entropy-based Chained Deep Learning (GCECDL) framework. This method addresses the limitations of traditional label aggregation techniques by modeling each annotator's reliability as a function of the input data. 1.4 Aims 21

The approach effectively mitigates the impact of noisy labels by using a noise-robust loss function, balancing Mean Absolute Error (MAE) and Categorical Cross-Entropy (CE). Unlike prior approaches, GCECDL accounts for the dependencies among annotators while encoding their non-stationary behavior across different data samples. Their experiments on multiple datasets demonstrated superior predictive performance compared to state-of-the-art methods, particularly in cases where annotations were highly inconsistent.

The strategy of the authors effectively unlocks the potential of ML models to handle low-quality data and noisy annotations, but it is bounded to classifications tasks only, not being by itself applicable to segmentation tasks. The TGCE equation for handling multiple annotators is defined as:

$$TGCE(\mathbf{y}, f(\mathbf{x}); \tilde{\lambda}_x, \tilde{C}) = \tilde{\lambda}_x \frac{1 - (\mathbf{1}^\top (\mathbf{y} \odot f(\mathbf{x})))^q}{q} + (1 - \tilde{\lambda}_x) \frac{1 - (\tilde{C})^q}{q}, \quad (1-8)$$

where $\tilde{\lambda}_x$ represents the annotator reliability, \tilde{C} is a constant, q is a parameter that controls the balance between MAE and CE behavior, \mathbf{y} is the annotation vector, and $f(\mathbf{x})$ is the model prediction. This approach is more deeply discussed in chapter 4.

1.4 Aims

With the mentioned considerations in section 1.3 in mind, this work proposes a novel approach for ISS tasks in medical images, which aims to train a model whose learning approach is adaptive to the labeler performance. This is done by introducing a loss function capable of inferring the best possible segmentation without needing separate inputs about the labeler performance. This loss function is designed to implicitly weigh the labelers based on their performance, with the presence of an intermediate reliability map allowing the model to learn from the

22 Introduction

most reliable labelers and ignore the noisy labels. This approach differs from existing CNN-based segmentation models, as it does not require explicit supervision of the labeler performance, making it more generalizable and adaptable to different datasets and labelers.

1.4.1 General Aim

The main purpose of this work is to develop a novel approach for ISS tasks in medical images, which can adaptively infer the best possible segmentation without needing separate inputs about the labeler performance. This approach is expected to outperform the segmentation performance of other state of the art approaches, correctly facing the labeler performance inconsistency across the annotators space and the variability of images quality.

50 1.4.2 Specific Aims

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- To develop a novel loss function for ISS tasks in medical images, capable of inferring the best possible segmentation without needing separate inputs about the labeler performance.
- Introducing a tensor map which codifies the reliability of each labeler, allowing the model to implicitly weigh the labelers based on their performance across the mask and classes space.
 - To develop and test a deep learning model for ISS tasks in medical images, which can learn from inconsistent labels and improve the segmentation performance compared to other solutions in state of the art.

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1.5 Outline and Contributions

- As an output of this work, some contributions were made to the field of ISS in medical images. The main contributions are:
- 563 $\,$ $\,$ $\,$ A python package for using the proposed loss function in CNN models for ISS $\,$ tasks in medical images. 11
- \bullet Datasets mapping as lazy loaders for the proposed loss function. 12
 - \bullet A public Github repository with the code used in this work. 13

¹¹https://pypi.org/project/seg_tgce/

¹²https://seg-tgce.readthedocs.io/en/latest/experiments.html

 $^{^{13}} https://github.com/blotero/seg_tgce$

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CONCEPTUAL PRELIMINARIES

2.1 Modern concept of digital image

A digital image is a numerical representation of a visual scene, captured through various imaging devices and stored in a computer. From a mathematical perspective, a digital image can be represented as a function f(x,y) that maps spatial coordinates (x,y) to intensity values. In the discrete domain, this function is sampled at regular intervals, creating a matrix of values known as pixels (picture elements).

2.1.1 Types of digital images

579 Grayscale images

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Grayscale images are the simplest form of digital images, where each pixel represents a single intensity value. Mathematically, a grayscale image can be represented as a 2D matrix I of size $M \times N$, where each element I(i,j) represents the intensity at position (i,j). The intensity values typically range from 0 (black) to 255 (white) in 8-bit images, or from 0 to 65535 in 16-bit images.

585 Color images

Color images extend the grayscale concept by representing each pixel with multiple channels, typically Red, Green, and Blue (RGB). A color image can be represented as a 3D matrix I of size $M \times N \times 3$, where I(i,j,k) represents the intensity of the k-th color channel at position (i,j). Other color spaces like HSV (Hue, Saturation, Value) or CMYK (Cyan, Magenta, Yellow, Key) are also commonly used in different applications.

592 Multispectral images

Multispectral images capture information across multiple wavelength bands beyond the visible spectrum. These images can be represented as a 3D matrix I of size $M \times N \times B$, where B is the number of spectral bands. Each band I(i,j,b) represents the intensity at position (i,j) for the b-th spectral band. This representation is particularly useful in medical imaging, remote sensing, and scientific applications.

599 3D images and volumetric data

Three-dimensional images extend the concept of pixels to voxels (volume elements). A 3D image can be represented as a 3D matrix V of size $M \times N \times D$, where D represents the depth dimension. Each voxel V(i,j,k) represents the intensity at position (i,j,k) in the 3D space. This representation is fundamental in medical imaging (CT, MRI), scientific visualization, and computer graphics.

2.1.2 Mathematical representations

The mathematical foundation of digital images relies on several key concepts:

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- Sampling: The process of converting a continuous image into a discrete representation. According to the Nyquist-Shannon sampling theorem, the sampling frequency must be at least twice the highest frequency present in the image to avoid aliasing.
 - Quantization: The process of converting continuous intensity values into discrete levels. The number of quantization levels determines the image's bit depth and affects its quality and storage requirements.
 - Resolution: The number of pixels per unit length in an image, typically measured in pixels per inch (PPI) or dots per inch (DPI).
 - **Dynamic range**: The ratio between the maximum and minimum measurable light intensities in an image, often expressed in decibels (dB).
- The mathematical representation of a digital image can be expressed as:

$$I(x,y) = \sum_{i=0}^{M-1} \sum_{j=0}^{N-1} f(i,j) \cdot \delta(x-i,y-j)$$
 (2-1)

where I(x,y) is the digital image, f(i,j) represents the intensity values, and $\delta(x-i,y-j)$ is the Kronecker delta function.

For color images, the representation extends to:

$$I(x,y) = \begin{bmatrix} I_R(x,y) \\ I_G(x,y) \\ I_B(x,y) \end{bmatrix}$$
 (2-2)

where I_R , I_G , and I_B represent the red, green, and blue channels respectively.

- 2.1.3 Digital histopathological images
- **2.2** Deep learning fundamentals
- **2.3** Datasets and data sources

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- **3.1** Gaussian processes
- **3.2** Chained Gaussian processes

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TRUNCATED GENERALIZED CROSS ENTROPY FOR SEGMENTATION

4.1 Loss functions for multiple annotators

As mentioned in Section ??, a loss function is a key element for defining the objective function of a deep learning model. The categorical cross-entropy loss is a common loss function for classification tasks. However, in the case of multiple annotators, the categorical cross-entropy loss is not able to handle the varying reliability of the annotators. In this section, we will propose a loss function that is able to handle multiple annotators' segmentation masks while accounting for their varying reliability across different regions of the image.

4.1.1 Generalized Cross Entropy

The Generalized Cross Entropy (GCE) loss function was first introduced by [Zhang and Sabuncu, 2018] as a robust alternative to the standard cross-entropy loss, particularly effective in handling noisy labels. Let us first consider the Cross Entropy (CE) and Mean Absolute Error (MAE) loss functions:

$$MAE(\mathbf{y}, f(\mathbf{x})) = \|\mathbf{y} - f(\mathbf{x})\|_1 \tag{4-1}$$

$$CE(\mathbf{y}, f(\mathbf{x})) = \sum_{k=1}^{K} y_k \log(f_k(\mathbf{x}))$$
(4-2)

where $y_k \in \mathbf{y}$, $f_k(\mathbf{x}) \in f(\mathbf{x})$, and $\|\cdot\|_1$ stands for the l_1 -norm. Of note, $\mathbf{1}^{\top}\mathbf{y} = \mathbf{1}^{\top}f(\mathbf{x}) = 1$, $\mathbf{1} \in \{1\}^K$ being an all-ones vector. In addition, the MAE loss can be rewritten for softmax outputs, yielding:

$$MAE(\mathbf{y}, f(\mathbf{x})) = 2(1 - \mathbf{1}^{\mathsf{T}}(\mathbf{y} \odot f(\mathbf{x})))$$
(4-3)

- where \odot stands for the element-wise product.
- The CE is characterized by the following properties:
- It is unbounded from above.
- It heavily penalizes confident but wrong predictions.
- It is more sensitive to noisy labels.

- On the other hand, the MAE is characterized by the following properties:
- It is bounded and more robust to outliers.
- It assigns equal weights to all mistakes regardless of confidence.
- It is symmetric in softmax based representations.
- It is more robust to noisy labels but slower to train.
- The GCE loss function is defined by the authors in [Zhang and Sabuncu, 2018] as:

$$GCE(\mathbf{y}, f(\mathbf{x})) = 2 \frac{1 - (\mathbf{1}^{\top}(\mathbf{y} \odot f(\mathbf{x})))^q}{q},$$
(4-4)

with $q \in (0,1]$. Remarkably, the limiting case for $q \to 0$ in GCE is equivalent to the GE expression, and when q=1, it equals the MAE loss. In addition, the GCE holds the following gradient with regard to θ :

$$\frac{\partial GCE(\mathbf{y}, f(\mathbf{x}; \theta)|k)}{\partial \theta} = -f_k(\mathbf{x}; \theta)^{q-1} \nabla_{\theta} f_k(\mathbf{x}; \theta). \tag{4-5}$$

- 669 The GCE loss exhibits several desirable properties:
- It is more robust to label noise compared to standard cross-entropy
- The truncation parameter q allows for controlling the sensitivity to outliers
- It preserves the convexity property for optimization

4.1.2 Extension to Multiple Annotators

In the context of multiple annotators, we need to consider the varying reliability of each annotator across different regions of the image. Let's consider a k-class multiple annotators segmentation problem with the following data representation:

$$\mathbf{X} \in \mathbb{R}^{W \times H}, \{\mathbf{Y}_r \in \{0, 1\}^{W \times H \times K}\}_{r=1}^R; \ \mathbf{\hat{Y}} \in [0, 1]^{W \times H \times K} = f(\mathbf{X})$$
 (4-6)

where the segmentation mask function maps the input to output as:

$$f: \mathbb{R}^{W \times H} \to [0, 1]^{W \times H \times K} \tag{4-7}$$

The segmentation masks \mathbf{Y}_r satisfy the following condition for being a softmax-like representation:

$$\mathbf{Y}_r[w, h, :] \mathbf{1}_k^{\top} = 1; \ w \in W, h \in H$$
 (4-8)

4.1.3 Reliability Maps and Truncated GCE

The key innovation in our approach is the introduction of reliability maps Λ_r for each annotator:

$$\left\{ \Lambda_r(\mathbf{X}; \theta) \in [0, 1]^{W \times H} \right\}_{r=1}^R \tag{4-9}$$

These reliability maps estimate the confidence of each annotator at every spatial location (w,h) in the image. The maps are learned jointly with the segmentation model, allowing the network to:

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- Weight the contribution of each annotator differently across the image
- Adapt to varying levels of expertise in different regions
- Handle cases where annotators might be more reliable in certain areas than
 others
- The proposed Truncated Generalized Cross Entropy for Semantic Segmentation (TGCE $_{SS}$) combines the robustness of GCE with the flexibility of reliability maps:

$$TGCE_{SS}(\mathbf{Y}_{r}, f(\mathbf{X}; \theta)|_{r}(\mathbf{X}; \theta)) = \mathbb{E}_{r} \left\{ \mathbb{E}_{w,h} \left\{ \Lambda_{r}(\mathbf{X}; \theta) \circ \mathbb{E}_{k} \left\{ \mathbf{Y}_{r} \circ \left(\frac{\mathbf{1}_{W \times H \times K} - f(\mathbf{X}; \theta)^{\circ q}}{q} \right); k \in K \right\} + \left(\mathbf{1}_{W \times H} - \Lambda_{r}(\mathbf{X}; \theta) \right) \circ \left(\frac{\mathbf{1}_{W \times H} - \left(\frac{1}{k} \mathbf{1}_{W \times H} \right)^{\circ q}}{q} \right); w \in W, h \in H \right\}; r \in R \right\}$$

$$(4-10)$$

where $q \in (0,1)$ controls the truncation level. The loss function consists of two main components:

- The first term weighted by Λ_r represents the GCE loss for regions where the annotator is considered reliable
- The second term weighted by $(1-\Lambda_r)$ provides a uniform prior for regions where the annotator is considered unreliable
- For a batch containing N samples, the total loss is computed as:

$$\mathscr{L}(\mathbf{Y}_r[n], f(\mathbf{X}[n]; \theta)|_r(\mathbf{X}[n]; \theta)) = \frac{1}{N} \sum_{n=1}^{N} TGCE_{SS}(\mathbf{Y}_r[n], f(\mathbf{X}[n]; \theta)|_r(\mathbf{X}[n]; \theta))$$
(4-11)

999 4.2 Proposed Model

Our proposed model architecture combines the strengths of UNET with a ResNet34 backbone, specifically designed to work with the TGCE $_{SS}$ loss function. The
architecture is illustrated in Figure ??.

4.2.1 Backbone Architecture

- The model uses a pre-trained ResNet-34 as its encoder backbone. ResNet-34's deep residual learning framework provides several advantages:
- Efficient feature extraction through residual connections
- Pre-trained weights that capture rich visual representations
- Stable gradient flow during training
- The ResNet-34 backbone is modified to serve as the encoder in our UNET architecture. We remove the final fully connected layer and use the feature maps from different stages of the network for skip connections.

4.2.2 UNET Architecture

- The UNET architecture consists of an encoder-decoder structure with skip connections. The encoder path follows the ResNet-34 structure, while the decoder path uses transposed convolutions for upsampling. The architecture includes:
- Four downsampling stages in the encoder (ResNet-34 blocks)
- Four upsampling stages in the decoder
- Skip connections between corresponding encoder and decoder stages
- Batch normalization and ReLU activation after each convolution

20 4.2.3 Reliability Map Branch

- A key innovation in our architecture is the addition of a parallel branch for estimating reliability maps. This branch:
- Takes the same encoder features as input
- Uses a series of 1×1 convolutions to reduce channel dimensions
- Produces R reliability maps Λ_r for each annotator
- Applies a sigmoid activation to ensure values in [0,1]

\mathbf{z}_{T} 4.2.4 Integration with TGCE $_{SS}$ Loss

- 728 The model outputs two components:
- Segmentation masks $\mathbf{\hat{Y}} = f(\mathbf{X}; \theta)$
- Reliability maps $\{\Lambda_r(\mathbf{X}; \theta)\}_{r=1}^R$
- These outputs are used to compute the $TGCE_{SS}$ loss as described in Section ??. The
- 132 loss function guides the learning of both the segmentation masks and reliability
- maps simultaneously.

4.2.5 Training Process

- 735 The training process involves:
- Initializing the ResNet-34 backbone with pre-trained weights
- Training the entire network end-to-end
- Using the Adam optimizer with a learning rate of 10^{-4}
- Applying the $TGCE_{SS}$ loss to update both the segmentation and reliability branches
- The model's architecture allows it to:
- Learn robust segmentation features through the ResNet-34 backbone
- Capture fine-grained details through UNET's skip connections
- Adapt to annotator reliability through the parallel reliability branch
- Handle multiple annotators' inputs effectively

4.3 Experiments

747 **4.3.1** Dataset

4.3.2 Metrics

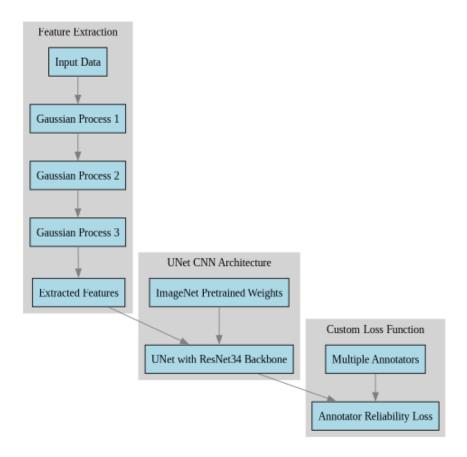


Figure **4-1** Solution Architecture (mockup)

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