Radix Sort in RISC-V asm

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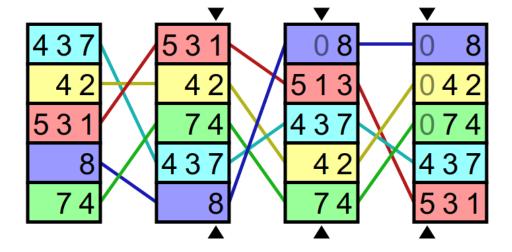


Radix Sort

Specifiche:

- Algoritmo di ordinamento non-comparativo, non è limitato al lower bound o(n log n)
- Lavora su numeri interi o naturali in una base qualsiasi, a seconda dell'implementazione
- Si appoggia a un algoritmo di ordinamento stabile, in questo caso al Counting Sort

Radix Sort (LSD)



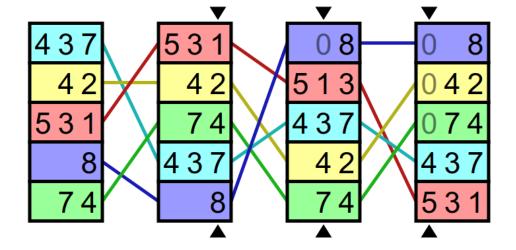


Radix Sort

Funzionamento:

- Partendo dalla cifra meno significativa ordina gli elementi prendendo in considerazione uno spazio decimale per volta
- In caso di cife identiche mantiene l'ordine (relativo) del passaggio precedente (vedi nell'ultimo passaggio <u>0</u>08, <u>0</u>42, <u>0</u>74)
- Non effettua confronti per decidere in che ordine sistemare i numeri

Radix Sort (LSD)





Algoritmi implementati

Radix Sort

- Funzione richiamata dal programma principale
- Utilizza la funzione Max per trovare il numero maggiore
- Calcola il numero di cifre del numero maggiore, ovvero il numero di passaggi da effettuare
- Per ogni passaggio richiama il Counting Sort selettivo su uno spazio decimale diverso
- Counting Sort selettivo
 - Ordina l'array che gli viene passato considerando una sola cifra decisa dal chiamante
 - Gestisce le cifre uguali mantenendo l'ordine relativo preesistente tra i due elementi

Max

• Restituisce il numero massimo contenuto dell'array passato come parametro



radixsort()

```
C++
void radixsort(int arr[], int n)
    // Find the maximum number
   // to know number of digits
                                                       loop2:
    int max = getMax(arr, n);
   // Do counting sort for every digit.
    // Note that instead of passing digit
    // number, exp is passed. exp is 10^i
    // where i is current digit number
   for (int exp = 1; max \geq exp; exp *= 10)
        countSort(arr, n, exp);
                                                        endloop2:
```

RISC-V

```
radixsort: #a2=n #a3=input array address
   addi sp,sp,-8
   sd ra,0(sp)
   jal ra,max
   ld ra, \theta(sp)
   addi sp,sp,+8
   addi sp,sp,-16
   sd s0,0(sp)
   sd s1,8(sp)
   #for (int exp = 1; max >= exp; exp *= 10)
   # countSort(arr, n, exp);
   addi s0, a0, 0 #s0 = max
   li s1,1
                   \#s1 = exp
   addi a4, s1, 0 #passing exp to countingsort
   addi sp,sp,-8
   sd ra,0(sp)
   jal ra, countingsort
   ld ra,0(sp)
   addi sp,sp,+8
   li t0,10
   mul s1,s1,t0
   bge s0,s1,loop2
   ld s0,0(sp)
   ld s1,8(sp)
   addi sp,sp,16
ret
```



countingsort() [1/3]

```
C++
void countSort(int arr[], int n, int exp)
   int output[n]; // output array
   int i, count[10] = {0};
   // Store count of occurrences in count[]
   for (i = 0; i < n; i++)-
        count[ (arr[i]/exp)%10 ]++; -
   // Change count[i] so that count[i] now contains actual
   // position of this digit in output[]
   for (i = 1; i < 10; i++)
       count[i] += count[i - 1];
   // Build the output array
   for (i = n - 1; i >= 0; i--) {
       count[ (arr[i]/exp)%10 ]--;
       output[ count[(arr[i]/exp)%10] ] = arr[i];
   // Copy the output array to arr[], so that arr[] now
   // contains sorted numbers according to current digit
   for (i = 0; i < n; i++)
        arr[i] = output[i];
```

RISC-V

```
// Store count of occurrences in count[]
     for (i = 0; i < n; i++)
         count[ (arr[i]/exp)%10 ]++;
     li t0,0 #i=0
→ loop3:
     li t1, bytes
     mul t1,t0,t1 #offset from arr[0] to arr[i]
     add t2,a3,t1 #t2 = address of arr[i]
     lw t3,0(t2) #t3 = arr[i]
     # count[ (arr[i]/exp)%10 ]++;
     div t4,t3,a4
     li t1,10
     rem t4,t4,t1 #t4 = (arr[i]/exp)%10 //index of count array
     la a5,count #a5 = count array address
     li t1,bytes
     mul t1,t4,t1 #offset from count[0] to count[t4]
     add t5,a5,t1 #t5 = address of count[t4]
     1w + 6,0(+5) + + 6 = count[+4]
     addi t6, t6, 1 \# t6 = t6 + 1
     sw t6,0(t5) \#count[t4] = count[t4] + 1
     addi t0,t0,1
                     #1++
     blt t0,a2,loop3 #i<n
 endloop3:
```



countingsort() [2/3]

arr[i] = output[i];

RISC-V

#for (i = 1; i < 10; i++)

```
count[i] += count[i - 1];
                                                                         li t0,1 #i=1
C++
                                                                    →loop4:
                                                                         la a5,count #a5 = count array address
void countSort(int arr[], int n, int exp)
                                                                         li t1,bytes
                                                                         addi t0,t0,-1
                                                                                         #t0 = i-1
   int output[n]; // output array
                                                                         mul t1,t0,t1
                                                                                         #offset from count[0] to count[i-1]
   int i, count[10] = {0};
                                                                                         #t2 = address of count[i-1]
                                                                         add t2,a5,t1
   // Store count of occurrences in count[]
                                                                         lw t4,0(t2)
                                                                                         \#t4 = count[i-1]
   for (i = 0; i < n; i++)
                                                                         addi t0,t0,+1
                                                                                         #t0 = i
       count[ (arr[i]/exp)%10 ]++;
                                                                         li t1,bytes
   // Change count[i] so that count[i] now contains actual
                                                                         mul t1,t0,t1
                                                                                         #offset from count[0] to count[i]
   // position of this digit in output[]
                                                                                         #t2 = address of count[i]
                                                                         add t2,a5,t1
   for (i = 1; i < 10; i++)
                                                                         lw t3,0(t2)
                                                                                         #t3 = count[i]
       count[i] += count[i - 1]; -
                                                                         add t3,t3,t4
                                                                                        \#t3 = count[i] + count[i - 1];
   // Build the output array
                                                                         sw t3,0(t2)
                                                                                         \#count[i] = t3
   for (i = n - 1; i >= 0; i--) {
       count[ (arr[i]/exp)%10 ]--;
                                                                         addi t0,t0,1
       output[ count[(arr[i]/exp)%10] ] = arr[i];
                                                                         li t1,10
                                                                         blt t0,t1,loop4
   // Copy the output array to arr[], so that arr[] now
                                                                     endloop4:
   // contains sorted numbers according to current digit
   for (i = 0; i < n; i++)
```

countingsort() [3/3]

C++

```
void countSort(int arr[], int n, int exp)
   int output[n]; // output array
   int i, count[10] = {0};
   // Store count of occurrences in count[]
   for (i = 0; i < n; i++)
       count[ (arr[i]/exp)%10 ]++;
   // Change count[i] so that count[i] now contains actual
   // position of this digit in output[]
   for (i = 1; i < 10; i++)
       count[i] += count[i - 1];
   // Build the output array
   for (i = n - 1; i >= 0; i--) \{ -1 \}
       count[ (arr[i]/exp)%10 ]--;-
       output[ count[(arr[i]/exp)%10] ] = arr[i];
   // Copy the output array to arr[], so that arr[] now
   // contains sorted numbers according to current digit
   for (i = 0; i < n; i++)
       arr[i] = output[i];
```

RISC-V

```
addi t0,a2,-1 #i=n-1
▶ loop6:
     li t1,bytes
     mul t1,t0,t1 #offset from arr[0] to arr[i]
     add t2,a3,t1 #t2 = address of arr[i]
     lw t3,0(t2) #t3 = arr[i]
     # count[ (arr[i]/exp)%10 ]--;
     div t4,t3,a4
     li t1,10
     rem t4,t4,t1 #t4 = (arr[i]/exp)%10 //index of count array
     la a5,count #a5 = count array address
     li t1, bytes
     mul t1,t4,t1 #offset from count[0] to count[t4]
     add t5,a5,t1 #t5 = address of count[t4]
     1w + 6,0(+5) + + 6 = count[+4]
     addi t6,t6,-1 #t6 = t6 - 1
     sw t6,0(t5) \#count[t4] = count[t4] - 1
     #keeping t3=arr[i] and t6=count[ (arr[i]/exp)%10 ]
     #free tmp registers: t1,t2,t4,t5
     li t1,bytes
     mul t1,t6,t1 #offset from output[0] to output[t6]
     add t2,s3,t1 #t2 = address of output[t6]
     sw t3,0(t2) #output[count[ (arr[i]/exp)%10 ] ] = arr[i];
     addi t0,t0,-1 #i--
     bge t0,zero,loop6 #i>=0
 endloop6:
```

```
max()
```

```
#a2=n #a3=array address #a0=max #a1=max address
                                                                li t3,0 #i=0
                                                                lw t2,0(a3) #arr[i]
                                                                #set first element as max
                                                                addi a0,t2,0
                                                                 addi a1,a3,0
                                                                li t3,1 #i=1
C++
                                                                bge t3,a2,endloop1 #i>=n
// A utility function to get maximum value in arr[]
                                                          → loop1:
                                                                li t0,bytes
int getMax(int arr[], int n)
                                                                mul t1,t3,t0 #offset
                                                                add t0,a3,t1 #address of arr[i]
    int mx = arr[0]; -
                                                                lw t2,0(t0) #arr[i]
    for (int i = 1; i < n; i++) —
        if (arr[i] > mx) ————
                                                                bgt t2,a0,then1 #if arr[i]>max
            mx = arr[i]; ———
                                                                 j endif1 #do nothing
                                                             then1:
    return mx;
                                                                #set arr[i] as max
                                                                addi a0,t2,0
                                                                addi a1,t0,0
                                                             endif1:
                                                                 addi t3,t3,1 #i++
                                                                blt t3,a2,loop1 #i<n
                                                             endloop1:
                                                             ret
```

RISC-V

max:

