
lel-ʼŋɪɸɔ-ɗɪ ɟɪ lel-ɗɪ ɟɪ jeʷle-ʼɸcʰɗɪɔ

aaaaaaaaA, the language of *Rymako*

uruwi

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aaaaaaaaaaaaaaaa

A complete grammar

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Dedicated to Isoraķatheð.

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0.1 | Introduction

1 | Phonology and orthography

1.1 | Phoneme inventory

Table 1.1: The consonants of aaaaaaaaaA.

	Bilabial	Alveolar	Palatal	Velar	Glottal
Nasal	m	n	ɲ	ŋ	
Plosive	p b	t d	c ɟ	k ɡ	ʔ
Fricative	f	s	ʃ	x	
(coarticulated)	θ x	ɸ x		ɸʃ	
Affricate		ts	tʃ		
Lateral fricative		ɬ			
Approximant		ɹ	j	w	
Lateral approximant		l			
Trill		r			

Table 1.2: The vowels of aaaaaaaaaA.

Spread	Half-rounded	Rounded
i	ɤ	y
u	ʊ	u
ɛ		œ
ʌ		ɔ
ä		

In addition to consonants and vowels, aaaaaaaaaA has rod signals, represented by numbers. Rod A is blue and held by one's dominant hand and B is red and held by one's non-dominant hand.

1. Rod A is raised to one's chest, while B is pointed down.
2. Rods A and B are crossed in the front.
3. Rod B is raised upwards in front of the nondominant arm, while rod A is lowered.

4. Rod A is pointed sideways near one's nondominant arm, while rod B is lowered.
5. Rods A and B are extended to the sides.
6. Rods A and B are extended, facing forward.
7. Rod A is raised forward, while B is pointed to the side.
8. Rod B is raised forward, while A is pointed to the side.

Lowering both rods is interpreted as an absence of a rod signal.

If the use of rods are unavailable, the numerals of the positions may be pronounced.

1.2 | Hacmisation

aaaaaaaaA uses the hacm script with superscript letters to indicate phonemes not found in Arka. The transcriptions can be found in Tables 1.3 and 1.4.

Table 1.3: The consonants of aaaaaaaaaA.

	Bilabial	Alveolar	Palatal	Velar	Glottal
Nasal	ɒ	n	n ^ɥ	n ^ɣ	
Plosive	d b	f ɳ	f ^ɥ ɳ ^ɥ	ɭ ɸ	.
Fricative	ɑ	ʃ	l	h	
(coarticulated)	j ^h	ɑ ^h		ɑ ^l	
Affricate		ʃʃ	ʎ		
Lateral fricative		s			
Approximant		ɹ	ɥ	o	
Lateral approximant		l			
Trill		r			

Table 1.4: The vowels of aaaaaaaaaA.

Spread	Half-rounded	Rounded
ɕ	ɕ ^ə	ɕ ^ɔ
ə ^ɕ	ə	ə ^ɔ
e		e ^ɔ
ɔ ^e		ɔ
ɪ		

Rod signs are represented by the hacm digits <1 ʃ ʈ ʂ ʑ ɳ Δ> attached to the end of the verbs they encompass. Proper words are preceded by a backslash <\>.

Vowels that are inferrable from context are sometimes omitted. For example, /æ-fan/ (to speak) is written <ʎeɑn>, but /æ-fin/ (to spread), which is less common, is written <ʎeɑcn>, with the second vowel. Most of this grammar will leave all vowels written.

1.3 | Phonotactics

An onset consists of one of the following:

- any single consonant other than /l/ (the exceptions are <le> [lek] and related words),
- any obstruent followed by an approximant other than /l/,
- or any plosive followed by /r/,
- or any nasal followed by /j/ or /w/.

A nucleus consists of one vowel.

A coda consists of one of the following:

- nothing,
- a nasal,
- a voiceless plosive (excluding /ʔ/),
- /ɹ/, /s/ or /l/

1.4 | Stress

Stress falls on the last syllable with a coda, or otherwise the second-to-last syllable.

See table 1.5 for examples.

Table 1.5: Examples of stress locations.

Orthography	Location of stress (# from last)
Dɪʃ	2
nɪ.cn	1
.əʔfələ	2
lɪjnedc ^a	3

1.5 | Vowel harmony

For the purposes of vowel harmony, vowels are divided into front and back vowels. /a/ is neutral. A root with neither front nor back vowels acts as if it has front vowels.

2 | Syntax

2.1 | Basic word order

The basic word order is VSO. Descriptors follow what they modify.

2.2 | Questions

Binary questions have the interrogative polarity marker and no change to syntax.

In wh-questions, the wh-word is pulled to the front (i. e. before the verb). This requires case marking for the wh-word:

flen peac^əjhi nc^ʔɕ
who-ACC speak-FAR.PAST-Q PR.FAR.SG
Whom did you speak to?

This applies only to questions, not interrogative-mood clauses that act as relative clauses:

peac^əjhi nc^ʔ flel, qif mu.
speak-FAR.PAST-Q PR.FAR.SG who, see-NEAR.PAST PR.ANAPH_OBJ.INT
I saw the person whom you talked to.

2.3 | Multiple clauses

A sentence might have multiple clauses. Each clause in a sentence follows the basic VSO order, and clauses are separated with commas.

3 | Nouns

Nouns are declined for number, case and definiteness.

3.1 | Number

aaaaaaaaA has many grammatical numbers:

Table 3.1: The discrete grammatical numbers of aaaaaaaaaA.

Number	Constraint on $x \in \mathbb{Z}$
Integral	none
Nullary	$x = 0$
Singular	$ x = 1$
Dual	$ x = 2$

Table 3.2: The continuous grammatical numbers of aaaaaaaaaA.

Number	Constraint on $x \in \mathbb{R}$
Nullary	$x = 0$
Subsingular	$ x < 1$
Supersingular	$1 \leq x < 2$
Plural	$ x \geq 2$ or x is unknown

3.2 | Case

In a clause with both the subject and object directly expressed in that order, both the subject and object are declined in the nominative case (and their roles are inferred through word order). In a clause where only one is present, or where both are expressed in the opposite order, the subject will receive the nominative case and the object will receive the accusative case.

3.3 | Noun classes

There are three overarching groups of noun classes.

3.3.1 | Countable

Nouns in these classes are declined for a discrete number.

1. Sentient – such as humans, AIs, deities.
2. Animate – nonsentient animals.
3. Inanimate – anything else.

3.3.2 | Measurable

Nouns in this class are declined for a continuous number.

4. Measure – all measurable nouns, especially units of measurement.

3.3.3 | Uncountable

Nouns in these classes are not declined for number, and require compounding with a countable or measurable noun in order to be quantified.

5. Fluid – liquids and gases.
6. Edible – edible (to humans) non-fluids.
7. Inedible – inedible (to humans) non-fluids.
8. Abstract – abstract ideas.

3.4 | Definiteness

The definite form of a noun is formed regularly by reduplicating the first syllable (without the coda): <𐤃𐤓𐤕> “a person” becomes <𐤃𐤓𐤃𐤓𐤕> “the person”.

3.5 | Declension table

3.5.1 | Countable classes

Note that noun declensions respect vowel harmony. For nouns with back vowels, replace the front vowels with the back vowels of the same height and rounding, and vice versa.

Table 3.3: Declensions for countable nouns.

	Integral	Nullary	Singular	Dual
--	----------	---------	----------	------

	Integral	Nullary	Singular	Dual
Sentient: <ɖɪɪ> “person”				
Nominative	ɖɪɪ	ɖɪɪle	ɖɪɪ	ɖɪɪl
Accusative	ɖɪɪn	ɖɪɪnʰle	ɖɪɪncɟ	ɖɪɪnɪl
Sentient: <ɟʰi.en> “magician”				
Nominative	ɟʰi.en	ɟʰi.eʃe	ɟʰi.eɟ	ɟʰi.el
Accusative	ɟʰi.eɲcn	ɟʰi.enʰle	ɟʰi.eɲcɟ	ɟʰi.eɲcl
(Note that the final consonant is preserved only in the integral nominative form.)				
Animate: <ɖənʰɔ> “rabbit”				
Nominative	ɖənʰɔ	ɖənʰɔɔʰe	ɖənʰɔɟ	ɖənʰɔ.əʰc
Accusative	ɖənʰɔn	ɖənʰɔnʰe	ɖənʰɔn	ɖənʰɔnəʰc
Animate: <ɟcʰɪ> “fox”				
Nominative	ɟcʰɪ	ɟcʰe	ɟcʰɟ	ɟcʰ.c
Accusative	ɟcʰɲcn	ɟcʰnʰle	ɟcʰɲcɟ	ɟcʰɲc
Inanimate: <ɰɪɽəʰ> “statue”				
Nominative	ɰɪɽəʰ	ɰɪɽəʰɔʰe	ɰɪɽəʰɟ	ɰɪɽəʰɟ
Accusative	ɰɪɽəʰɔ	ɰɪɽəʰɔɔʰe	ɰɪɽəʰɔɟ	ɰɪɽəʰəʰc
Inanimate: <.cɖen> “house”				
Nominative	.cɖen	.cɖeʃe	.cɖel	.cɖeɟ
Accusative	.cɖeɲcn	.cɖeɲcɔʰe	.cɖeɲcɟ	.cɖeɲcac

3.5.2 | Measurable classes

Table 3.4: Declensions for measurable nouns.

	Plural	Nullary	Subingular	Supersingular
Measure: <ɲəɖəʰ> “day (continuous)”				
Nominative	ɲəɖəʰ	ɲəɖəʰɲəʰ	ɲəɖəʰɪ	ɲəɖəʰn
Accusative	ɲəɖəʰn	ɲəɖəʰɲəʰn	ɲəɖəʰnʰe	ɲəɖəʰnəʰn
Measure: <ɖel> “volume” (in expressions such as <ɖel-ɲəɟəʰ> “cupful”)				
Nominative	ɖel	ɖeɲcʰ	ɖeɲcɪ	ɖeɲcn
Accusative	ɖeɲcn	ɖeɲcʰn	ɖeɲcnʰe	ɖeɲcnɲcn
(Note that the final consonant is preserved only in the plural nominative form.)				

3.5.3 | Uncountable classes

Notably, uncountable-class noun declensions do not respect vowel harmony.

Table 3.5: Declensions for measurable nouns.

	Mass
Fluid: <ɑʰəɲəʰ> “water”	
Nominative	ɑʰəɲəʰ
Accusative	ɑʰəɲəʰn
Fluid: <neled> “nitrogen”	

In wh-questions, the wh-word assumes the second position and the other argument becomes the first.

If a clause has no explicit arguments, the first argument is understood to be the subject.

Table 3.7: Personal pronouns. <-n>, <-en> or <-ɔ̃n> is suffixed for the accusative case.

(continuous) (discrete)	Pl. / Sub. / Sup. Integral	Nullary Nullary	Singular	Dual
Near	fi	lefi	de	acɥc
Far	dɔ	ɔ̃dɔ	nə ^c	bɥi
Other	nc	lenc	sc ^{ɔ̃}	liɥc
Anaph. Sub.	ɥi	leɥi	.cd	n ^{ɔ̃} cɥc
Anaph. Obj.	ɥɔ	ɔ̃ɥɔ	.ə ^c ɔ̃	n ^{ɔ̃} ə ^c ɥɔ
Generic	.ə ^{ɔ̃}			

(For the observant readers: notice the similarity to Kavinan's system.)

3.6.1 | Last-clause pronouns

The anaphoric pronoun <bej> (accusative: <bejen>) is grammatically an other pronoun, and it refers to the previous clause said. Likewise, <bedcɥ> (accusative: <bedcn>) refers to the clause before the previous one.

3.7 | Compounding

Nouns can be compounded together in a head-initial manner. When that happens, only the leftmost noun is the one to be declined.

ɔ̃el-ɥəɔ̃-ə^ləɥə^{ɔ̃}-ɥcɥ
 volume-cup-water-five
 five cupfuls of water

Note that integral pronouns can modify other nouns, in which personal possession is indicated:

ɔ̃el-ɥəɔ̃-ə^ləɥə^{ɔ̃}-ɥcɥ-fi
 volume-cup-water-five-PR.NEAR.INTEGRAL
 (arg1)'s five cupfuls of water

Descriptors can also compound on nouns. This compounding is productive in aaaaaaaaA.

ɔ̃ɥi-lə^{ɔ̃}fi
 person-old

old people

(Compare to ႁႏ ႏႃႉ “person old-SENTIENT”.)

3.8 | Possession

“X’s Y” is translated as <Y=ႁႏ ႏႃ X>. The possessive construction is also used to create appositives.

Observe that possession marks the head, and <=ႁႏ> is a clitic, not an affix, as in the following example:

ႁႃႁႃႏႃႉ-ႃႉႃႉ-ႁႏ ႏႃ ႏႃႉ.

DEF~rabbit-SING-water=GEN POS magician-SING

the magician’s water rabbit

In more casual speech, <ႏႃ> may be dropped.

4 | Verbs

Verbs are conjugated for person of the subject, tense, polarity and tellicity, in two paradigms. Conjugation respects vowel harmony.

Table 4.1: Person-tense conjugations for verbs, using <ḍilɪn> “(S) eats (O)”.

	Nonpast	Past
Near	ḍilɪn	ḍilɪf
Far	ḍilɪn	ḍilc ^a j
Other	ḍilɪ	ḍilc ^a
Anaph. Sub.	ḍile	ḍilel
Anaph. Obj.	ḍilc.e	ḍilc.el
Generic	ḍilc ^ɔ	ḍilc ^ɔ

Table 4.2: Person-tense conjugations for verbs, using <peacn> “(S) spreads (O)”.

	Nonpast	Past
Near	peacn	peacf
Far	peaɪn	peac ^a j
Other	peaɪ	peac ^a
Anaph. Sub.	peae	peael
Anaph. Obj.	peac.e	peac.el
Generic	peac ^a	peac ^a

to which a suffix is added:

Table 4.3: Polarity-tellicity suffixes for verbs. The interrogative affix can also follow a negative affix.

	Positive	Negative	Interrogative
Telic	–	–le / –ɔ ^e	–hɪ
Atelic	–ɔc / –ɔc ^c	–ɪ	–lc ^a / –lə

Notes:

- “Negative atelic” means something akin to “unsuccessfully tried to avoid doing X”.
- The interrogative polarity, in addition to marking questions, is used to mark clauses that may or may not be true but are referred to later in the sentence.

Some examples:

ḏḏḏḏ ḏḏḏḏ ḏḏḏḏ.
eat-NEAR.NONPAST fish flower
Fish eat flowers.

ḏḏḏḏ ḏḏḏḏ ḏḏḏḏ, ḏḏḏḏ ḏḏḏḏ ḏḏḏḏ.
eat-NEAR.NONPAST fish flower, eat-NEAR.NONPAST cat PR.ANAPH_SUB
Fish eat flowers, and cats eat fish.

ḏḏḏḏ ḏḏḏḏ ḏḏḏḏ, ḏḏḏḏ ḏḏḏḏḏḏ.
eat-NEAR.NONPAST fish flower, eat-ANAPH_SUB.NONPAST grass-ACC
Fish eat flowers, and they eat grass.
(Grass is inedible to humans, but edible to fish.)

ḏḏḏḏḏḏ ḏḏḏḏ ḏḏḏḏ.
eat-NEAR.NONPAST-NEG flower fish
Flowers don’t eat fish.

ḏḏḏḏ ḏḏḏḏ ḏḏḏḏḏḏḏ, ḏḏḏḏ ḏḏḏḏ.
carry-OTHER.NONPAST PR.OTHER.SG DEF~book-SG, worry-NEAR.NONPAST PR.NEAR.INT
PR.LAST_CLAUSE
He has the book; that worries me.
or: That he has the book worries me.

ḏḏḏḏḏ ḏḏḏḏ ḏḏḏḏḏḏḏ, ḏḏḏḏ ḏḏḏḏ.
carry-OTHER.NONPAST-INTERROGATIVE PR.OTHER.SG DEF~book-SG, worry-NEAR.NONPAST
PR.NEAR.INT PR.LAST_CLAUSE
He might have the book; that worries me.
or: That he might have the book worries me.

4.1 | Aspect

Verbs can also be marked for aspect, either using a rod sign directly on the verb, or a particle with a rod sign, placed anywhere between the verb it modifies and the next verb.

Table 4.4: Aspect markers. Those with hyphens are attached to verb. Those without hyphens are placed as separate particles anywhere after the verb.

Aspect name	Marking	Meaning
Imperfect	–1	An action that is currently going on. Also used to distinguish static actions as opposed to dynamic (e. g. <i>wear</i> as opposed to <i>put on</i>).
Interrupted	1c11	An action that was interrupted.
Perfect	–1	An action that has already finished. Changes present tense to immediate past. Also used to distinguish dynamic actions as opposed to static (e. g. <i>put on</i> as opposed to <i>wear</i>).
Gnomic	–ʔ	A general truth or aphorism, or an action done habitually.
Gnomic dubitative	1c1ʔ	A general truth or aphorism that the speaker considers to be false.
Deontic necessity	–᳚	An action that the speaker insists on happening.
Epistemic necessity	1əᵘᵈ᳚	An action that the speaker infers that is happening.
Deontic potential	–᳚	An action that the speaker permits to occur.
Epistemic potential	1əᵘᵈ᳚	An action that the speaker infers that might happen.
Unexpected	–ɿ	An action that is unexpected (akin to using “but”).
Comparative	deɿ	Indicates an action of greater intensity than what was described in the previous clause.
Nonexclusive subject	1c1	Indicates that the subject comprises not only of what is explicitly mentioned, but also other things.
Nonexclusive object	1cʔ	Indicates that the object comprises not only of what is explicitly mentioned, but also other things.
Nonexclusive argument	1c᳚	Combination of both nonexclusive subject and nonexclusive object.

An example:

11111c1 de nc, 1cnc.ɛ1ʃ dənʔidoᵘ–ɲ.
 fight-NEAR.PAST-ATELIC-IMPERFECT PR.NEAR.SG PR.OTHER.INT, shoot-ANAPH_OBJ.PAST-
 UNEXPECTED knee-SG.ACC-PR.ANAPH_SUB.INT
 I tried to fight them, but they shot my knee.

4.2 | Obliques

aaaaaaaaA lacks oblique arguments. Instead, equivalent expressions employ serial verb constructions. For instance, “he ate soup with a spoon” would be reduced to “he held a spoon and ate soup”:

dɿc^a sc^o aɔ^oɿɔ^ol, ɒilɛl sɪdʒɒn.
 INST-OTHER.PAST PR.OTHER.SG spoon-SG, eat-ANAPH_SUB.PAST soup-ACC
 He held a spoon and ate soup.
 or: He ate soup with a spoon.

Likewise:

nɪ.ɪ nc jəjəl-hɪ.ɪp, ncɒɛ hɪhɪɾə^odɔ^o.
 TEMPORAL-OTHER PR.OTHER.INT DEF~day-SG-spring, dance-ANAPH_SUB DEF~statue-SG.ACC
 They will wait until the spring equinox and dance around the statue.
 or: They will dance around the statue on the spring equinox.

A similar construction can be used for the negation of obliques:

dɿc^ale sc^o aɔ^oɿɔ^ol, ɒilɛl sɪdʒɒn.
 INST-OTHER.PAST-NEG PR.OTHER.SG spoon-SG, eat-ANAPH_SUB.PAST-UNEXPECTED soup-ACC
 He did not hold a spoon, but ate soup.
 or: He ate soup without a spoon.

4.3 | Conjunctions

Conjunctions such as “and” are treated like obliques. For instance, “and” is represented by the verb <acn>, and precedes the clause in which the two are used:

ac^a \ɿc^aje \ɿpəl, ɒilɛl fɛp.c^on.
 and-OTHER.PAST Ryse Tarul, eat-ANAPH_SUB.PAST beef-ACC
 Ryse and Tarul ate beef.

Sufficiently complex nesting may be unrepresentable using only anaphoric referents. The easiest way to resolve this issue is to use definite nouns in place of anaphoric referents.

ac^a \ɿc^aje \ɿpəl, ac^a fɛp.c^o sɪdʒɒ, ɒɪlc^a ɒɪɒɪɪl ɱɪ.
 and-OTHER.PAST Ryuse Tarul, and-OTHER.PAST beef soup, eat-OTHER.PAST DEF~person-DU PR.ANAPH_SUB.CONT
 [They,] Ryse and Tarul ate beef and soup.

4.4 | Subordinate clauses

Ideas such as “if” or “because” are also expressed with verbs. For example, $\langle \text{ni.cn} \rangle$ “wait, when” is also used for “if”:

feɣilehi, ni.cn fi bej, æhcn.
rain-OTHER-NEG-Q, wait-NEAR PR.NEAR.INT ANAPH_CLAUSE, play-NEAR
If it doesn't rain, we will play.

Note the clausal argument to $\langle \text{ni.cn} \rangle$, since our condition is an entire clause instead of a noun.

4.4.1 | Conditions

Conditional ideas whose English translations contain “if” can also be expressed in a more concise way, but this usage can sometimes sound colloquial:

feɣilehi, æhcn.
rain-OTHER-NEG-Q, play-NEAR
If it doesn't rain, we will play.

4.5 | Comparatives

The comparative is a function $\text{cmp} : A \times A \times (A \rightarrow \mathbb{R}) \times (A \times A \rightarrow \{0, 1\}) \rightarrow \{0, 1\}$, where $\text{cmp}(a, b, f, \sqsupset) = f(a) \sqsupset f(b)$.

Consider the following sentences:

Fish eat flowers more than cats.
More fish eat flowers than cats.

Semantically, they can be translated to:

$$\text{cmp}(\text{fish}, \text{cats}, a \mapsto (\# \text{ of flowers eaten by } a), >) \quad (4.1)$$

$$\text{cmp}(\text{fish}, \text{cats}, a \mapsto (\# \text{ of } a \text{ that eat flowers}), >) \quad (4.2)$$

The heart of comparatives in aaaaaaaaA is the quadrivalent verb $\langle \text{ɔɰɔɰ} \ a \ b \ f \ \sqsupset \rangle$. Thus:

ɔɰɔɰhi ɭɔɰɔɰ-jʰcn, ɔɰɔɰ siɖe nɣɰɰ ɰɔ nef.
eat-GENERIC-Q flower-ACC.INT-how_many, CMP-NEAR fish cat PR.ANAPH_OBJ.INT >
Fish eat more flowers than cats.

ɔɰɔɰhi .əʔ-jʰcn ɭɔɰɔɰ, ɔɰɔɰ siɖe nɣɰɰ ɰɰ nef.
eat-GENERIC-Q PR.GENERIC-how_many flower, CMP-NEAR fish cat PR.ANAPH_SUB.INT
>

More fish eat flowers than cats.

Note that we place a clause whose argument is the generic pronoun before the comparative clause. From the *doran*-clause, we refer to the function using the anaphoric pronoun referring to the position of the return value.

Table 4.5: Comparators in aaaaaaaaaA.

□	Comparator
>	nef
<	ac ^ə
=	fe ^ə n ^ə
≥	f ^u il
≤	dcj
≠	.c ^ə
≈	pej
≫	a ^h e
≪	din

4.6 | Ditransitive-like constructions

In English, some verbs such as *give* take two objects: the item being given and the recipient of the item. Since clauses in aaaaaaaaaA can take only one object, translating such verbs requires multiple clauses:

fɪpɪf de hɪpɪpɪcɔen, nebel \pɪc^əjen.
 lose-NEAR.PAST PR.NEAR.SG DEF~book, give_to-ANAPH.SUB.PAST Ri^use-ACC
 I gave the book to Ryse.

4.7 | Transitivity

Verbs that are intransitively (i. e. have no object passed at this time) can be turned into a causative form with the prefix <ɸC->:

fɪlɪɪɪf aɪpɪpɪn^ue.
 fall-NEAR.PAST DEF~coin
 The coins fell.

de ɸɪlɪɪɪɪf aɪpɪpɪn^ue
 PR.NEAR.SG TRANS-fall-OTHER.PAST DEF~coin
 I dropped the coins.

Note that the word order changes to SVO. In addition, the verb is conjugated for its object, rather than the subject as expected. If the following clause uses an anaphoric

subject, it refers to the object of the current clause.

Moreover, the verb does not need to be one that can never take an object. In the above example, <fclrcn> means “(S) falls on (O)”. However, if the verb in question is taking an object, it cannot be transitivised directly and a more roundabout way is required:

fclrcf aqeaqen^{4e} pıfı.
fall-NEAR.PAST DEF~coin grass
The coins fell on the grass.

de ƣfclrc^ə aqeaqen^{4e}, fclrcel pıfıbe.
PR.NEAR.SG TRANS-fall-OTHER.PAST DEF~coin, fall-ANAPH.SUB.PAST grass-ACC
I dropped the coins; they fell on grass.
or: I dropped the coins on grass.

4.8 | Clauses with nullary arguments

A clause with one or more arguments that are nullary or modified by nullary-number nouns (either through compounding or possession) will have a negative verb as well:

dəfınle dıjıle.
recall-NEAR-NEG person=NULL
No one knows.

fjclfınle de jıfıdı jcl j^hı.ele.
want-NEAR-NEG PR.NEAR.SG ring=GEN POS magician=NULL
I don't want the rings of any magician.

4.9 | The copula

The copula <jcn> can take a noun as an object, in which case it can mean identity or membership. (Location is expressed with <lıcn> “be at”.) With no object at all, it is used to denote existence.

It can also accept a descriptor, in which case the descriptor is attached before <jcn> in the dictionary form.

5 | Descriptors

Descriptors act as adjectives or adverbs. They follow what they modify, and are inflected for the noun class or verbal person of their antecedents.

Table 5.1: Descriptor declensions, using the descriptors <hedfi> “large” and <leʔfi> “old”.

Class or person	Declined form	
Sentient	hedfi	leʔfi
Animate	hedfi	leʔfi
Inanimate	hedfe	leʔfə ^e
Measure	hedfiy	leʔfiy
Fluid	hedfej	leʔfə ^e j
Edible	hedfc	leʔfə ^c
Inedible	hedfeʔ	leʔfə
Abstract	hedfc ^a	leʔfə
Near	hedfiy	leʔfiy
Far	hedfiy	leʔfiy
Other	hedfey	leʔfey
Anaph. Sub.	hedfiy	leʔfiy
Anaph. Obj.	hedfey	leʔfey
Generic	hedfc ^y	leʔfə ^y

5.1 | Conversion

A noun can be converted to a descriptor by appending <-i>.

A descriptor can be converted to an abstract noun meaning “the nature of being ~” by replacing the final <-i> with <-cnel>.

6 | Tree mode

As mentioned in section 4.3, anaphoric referents in a linked-list sentence are sometimes insufficient for expressing even simple sentence structures. While the easiest method of resolving this issue is using definite nouns, aaaaaaaaaA also provides a mode where sentences are not linked lists of clauses, but rather (binary) trees.

6.1 | Activation

Tree mode is enabled automatically when the treeing particle <ᵿᵿ> is used, and disabled at the end of a sentence.

6.2 | Branch-switching

The aforementioned particle <ᵿᵿ> marks the beginning of the right branch of the tree. The right branch is ended by the particle <ᵿᵿΔ>, which causes the next clause to join the left and right branches.

(N. B. <ᵿᵿ> and <ᵿᵿΔ> can occur only between clauses. If the particles are represented by left and right brackets, respectively, then the brackets should match.)

6.3 | Anaphoric pronouns in joiner clauses

In clauses that join two branches, anaphoric pronouns require marking whether the antecedent occurs in the left predecessor <ᵿᵿ> or the right predecessor <ᵿᵿΔ>. This is done by marking the pronoun with <-ᵿ> or <-Δ>.

Likewise, verbs can be modified with <-ᵿ> or <-Δ> to indicate which branch the subject came from.

6.4 | Errors

The following are ungrammatical:

- Using the particle <ᵿᵿΔ> or the branched anaphoric pronouns when tree mode is disabled

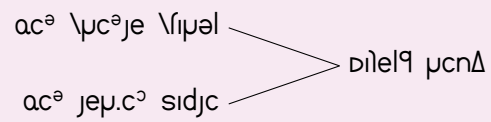
- Using the particle $\langle n^4\Delta \rangle$ other than to close a corresponding $\langle n^4\eta \rangle$
- Using the unbranched anaphoric pronouns in clauses with two predecessors
- Using the branched anaphoric pronouns in clauses with one predecessor
- Starting a new branch with $\langle n^4\eta \rangle$ when the current branch is empty

6.5 | Example

The second example in section 4.3 can be expressed as follows:

$ac^a \setminus \mu c^a \eta \setminus \eta \mu \theta$, $n^4\eta \ ac^a \ \eta \mu.c^o \ \text{sidjc}$, $n^4\Delta \ \text{d}\eta \text{el}\eta \ \mu c n \Delta$.

The resulting tree is shown below:



7 | Numerals

aaaaaaaaA uses a mixed-base system for its numerals. Numerals are abstract nouns. A Perl 6 program to convert numerals can be found in Section A.3.

7.1 | Single-digit numerals

Here are the numerals for $n < 17$:

Table 7.1: The cardinal numbers from 0 – 16.

base 10	base v	word
0	0	μəɒ
1	1	ac ^ə l
2	2	ʃɪj
3	ʔ	ɔ ^h e ^ə n
4	ŋ	ɑ ^h ɪμ
5	ʔ	ʔcɪ
6	ʃ	ɒɪe
7	ɣ	ʃɪcɪ
8	Δ	də ^ə n
9	L	hed
10	F	bən ^ə
11	7	nə ^c
12	£	le ^ə
13	‡	j ^h cd
14	A	ɪɪn
15	V	lel
16	ψ	.ɪμ

Note that digits above 9 use capital hacm letters.

7.2 | Numerals up to $19 \cdot 17$

These are represented by two digits. The multiples of 17 are shown below:

Table 7.2: Multiples of 17, up to $18 \cdot 17$.

base 10	base v	word
17	10	selc ^a
34	J0	ɔilc ^a
51	ʔ0	ɔ ⁴ e ³ lc ^a
68	00	ʃɔlc ^a
85	ʔ0	ʔcʃlc ^a
102	ʃ0	ɔ ⁴ elc ^a
119	90	ʃcʃlc ^a
136	Δ0	də ³ nə
153	L0	helc ^a
170	F0	bən ⁴ ə
187	70	nə ^c lə
204	£0	le ³ lc ^a
221	‡0	j ^h cdlc ^a
238	A0	ɥinc ^a
255	∇0	lelyc ^a
272	ψ0	.ilyc ^a
289	Ð0	jɪlsc ^a
306	℥0	heddc ^a

Thus $y \cdot 17 + x$ is written $\langle x-y \rangle$.

7.3 | Numerals up to $13 \cdot 19 \cdot 17 = 4199$

These are represented by three digits. The multiples of $19 \cdot 17$ are listed below:

Table 7.3: Multiples of $19 \cdot 17$, up to $12 \cdot 19 \cdot 17$.

base 10	base v	word
323	100	hɪjɪn
646	J00	ʃɪjɪn
969	ʔ00	ɔ ⁴ e ³ jɪn
1292	000	ɔ ⁴ ɪjɪn
1615	ʔ00	ʔcɪjɪn
1938	ʃ00	ɔ ⁴ eɪjɪn
2261	900	ʃcɪjɪn
2584	Δ00	də ³ nɪn
2907	L00	heɪjɪn
3230	F00	bən ⁴ ɪjɪn

base 10	base v	word
3553	700	nə ^c jɪɪn
3876	£00	le ³ jɪɪn

Thus $(z \cdot 19 \cdot 17) + (y \cdot 17) + x$ is written $\langle z-x-y \rangle$.

7.4 | Numerals up to and including $4199 \cdot (4199 + 1)/2 = 8817900$

The numeral for 4199 is $\langle \text{ə.ɔlə}^c \rangle$, written as $\langle 1:000 \rangle$.

Likewise, two $\langle \text{ə.ɔlə}^c \rangle$ is written as $\langle \text{J}:000 \rangle$ and pronounced $\langle \text{ə.ɔlə}^c\text{-fɪj} \rangle$, but the second $\langle \text{ə.ɔlə}^c \rangle$ is one smaller than the first. In other words, $\langle \text{J}:000 \rangle = 4199 + (4199 - 1) = 8397$.

Table 7.4: “Multiples” of $\langle \text{ə.ɔlə}^c \rangle$.

“Multiple”	Difference from last	Total
(0)		0
1:000	4199	4199
J:000	4198	8397
ʔ:000	4197	12594
0:000	4196	16790
ʔ:000	4195	20985
...		
£.ʔV:000	3	8817897
£.ʔW:000	2	8817899
1::000:000	1	8817900

Thus the n th “multiple” differs from the $(n-1)$ th multiple by $(4199 + 1 - n)$ (given $1 \leq n \leq 4199$), and the sum of the first n “multiples” is

$$\begin{aligned}
 y(n) &= \sum_{i=1}^n (4200 - i) \\
 &= \frac{1}{2} \cdot (8399 \cdot n - n^2)
 \end{aligned} \tag{7.1}$$

And likewise, for some given y , the largest “multiple” of $\langle \text{ə.ɔlə}^c \rangle$ not smaller than y has the index

$$N(y) = \left\lfloor \frac{1}{2} \cdot (8399 - \sqrt{70543201 - 8 \cdot y}) \right\rfloor \tag{7.2}$$

In other words, for any numeral $\langle n_1:n_2 \rangle$, $n_1 + n_2$ must be less than 4199.

7.5 | Higher numerals

The bases of higher numerals b_i can be derived from the recurrence relation

$$b_i = \begin{cases} 4199 & \text{if } i = 1 \\ \frac{b_{i-1} \cdot (b_{i-1} + 1)}{2} & \text{otherwise} \end{cases} \quad (7.3)$$

Then b_i acts as a new triangular base. Equations 7.1 and 7.2 can be generalised to the following:

$$y(n, b_i) = \sum_{i=1}^n (b_i + 1 - n) \quad (7.4)$$

$$= \frac{1}{2} \cdot (n \cdot (2 \cdot b_i + 1 - n)) \quad (7.5)$$

$$N(y, b_i) = \left\lfloor \frac{1}{2} \cdot \left(2 \cdot b_i - \sqrt{4 \cdot b_i^2 + 4 \cdot b_i + 1 - 8 \cdot y} \right) \right\rfloor \quad (7.6)$$

It follows that $y(n_1, b_i) + n_2$ is represented as $\langle n_1 :^i n_2 \rangle$ (i colons), and such a numeral must satisfy $n_1 + n_2 < b_i$.

Here are the names of the bases themselves:

Table 7.5: Names of higher bases.

Base	base v	word
b_1	1:000	ṽə.ṽlə ^c
b_2	1::000:000	ḁəp ^c ṽi
b_3	1:::000:000::000:000	ṽiṽə ^c
b_4		ṽəncəi

7.6 | Cardinal and ordinal numerals

Cardinal numerals compound to their antecedents; ordinal numerals use the possessive $\langle -\text{D}_1 \text{ jcl} \rangle$ construction:

ḁḁai–ṽə^cn
 child-three
 three children

ḁḁaiḁi jcl ṽə^cn
 child-SG=GEN POS three
 the third child

8 | Derivational morphology

The following methods are used to derive related terms from existing ones.

8.1 | Abstraction

Abstraction is a derivation that takes a non-abstract noun and returns the abstract noun representing the concept of the argument. This formation appends $\langle -ne \rangle$ or $\langle -n\omega^e \rangle$ to the noun.

Examples:

- $\langle h\mu c\alpha en \rangle$ *book* \rightarrow $\langle h\mu c\alpha ene \rangle$ *literature*
- $\langle h\omega l \rangle$ *cart* \rightarrow $\langle h\omega l n\omega^e \rangle$ *transportation*

Note that any double letters collapse into a single.

8.2 | Dematuration

Dematuration is a derivation that takes a noun and returns a noun of the same class that represents an immature form of the argument (not necessarily a diminutive). $\langle f\epsilon - \rangle$ or $\langle f\epsilon^c - \rangle$ are prepended to nouns that begin in $\langle j \rangle$ or $\langle l \rangle$, or $\langle j\epsilon - \rangle$ or $\langle j\epsilon^c - \rangle$ otherwise.

Examples:

- $\langle \mathfrak{D}l\mathfrak{j} \rangle$ *person* \rightarrow $\langle j\epsilon \mathfrak{D}l\mathfrak{j} \rangle$ *child*
- $\langle f\mathfrak{j}\omega\mu\epsilon^{\mathfrak{o}} \rangle$ *fruit* \rightarrow $\langle j\epsilon^c f\mathfrak{j}\omega\mu\epsilon^{\mathfrak{o}} \rangle$ *unripe fruit*
- $\langle j\epsilon r\mathfrak{l}l\mathfrak{c}n \rangle$ *essay* \rightarrow $\langle f\epsilon j\epsilon r\mathfrak{l}l\mathfrak{c}n \rangle$ *draft*

8.3 | Verb-to-noun conversions

Verb-to-noun conversions involve an operation called *inversion*; this operation swaps certain phonemes of a word:

- front vowels ↔ back vowels
- voiceless plosives ↔ voiced plosives
- ɑ ↔ j^h
- j ↔ ɑ^h (in any position other than in a coda)
- h ↔ ɑ^l
- ɸ ↔ ɽ (in any position other than after a fricative in an onset)
- s ↔ l (in any position other than in a coda)
- ɥ ↔ o

For instance, ⟨ɸi.ɕiŋ⟩ would be inverted to ⟨ɽi.ə^oŋiŋ⟩.

All other phonemes are unchanged.

Since all of the conversions below are straightforward, only their names will be mentioned.

Table 8.1: Verb-to-noun conversions, from the inversion of the verb stem.

Name	Affix
Agent	–e ^o n ^o / –ɔn ^o
Patient	–e ^o d / –ɔd
Location	–e ^o ɸ / –ɔɸ
Instrument	–iɽi

Table 8.2: An example with ⟨nə^obɪŋ⟩ to *steal*.

Name	Derivation	Meaning
Agent	nc ^o de ^o n ^o	thief
Patient	nc ^o de ^o d	stolen goods
Location	nc ^o de ^o ɸ	site of theft
Instrument	nc ^o dɽiɽi	tool used for theft

9 | Names

Names fall into two grammatical categories:

- *Nominal names* act as nouns. They are usually single words.
- *Clausal names* are entire clauses. These names usually refer to places, although a few people have clausal names. In extreme cases, such a name can span multiple clauses.

9.1 | Nominal names

These names act as nouns, and they are preceded by a backslash <\>. If the name spans multiple words (as common in foreign names), spaces are escaped by backslashes. No distinction is made between native and foreign names.

Only personal names can stand on their own, and even then, only given or full names. Other names must modify a common noun describing the nature of what is named, in the integral number without definiteness.

Table 9.1: Some examples of nominal names.

Name	Type
\pɕ ^ə je	Personal (native)
\ɸɪpəl	Personal (native)
\pɛɓcn	Personal (foreign)
dpe ^ɔ ɓe-\oɪɪ.c	Place (foreign)

Native names will usually respect vowel harmony. Children of parents who work in professions demanding physical labour (e. g. bricklaying) will usually have names with back vowels. In contrast, those born to parents of professions that do not demand physical strength (e. g. computer programming) will usually bear names with front vowels.

These names comprise of one or more clauses. Due to the nature of clausal names, they are all considered native. Most of these names refer to places; personal clausal names are almost always nicknames or such. Orthographically, they are put into square brackets <[]>.

We call the *referent* the subject, the object or the verb of the last clause, respectively depending on the type of anaphoric pronoun used to refer to the name. If the referent is a noun, it must be declined in the integral number without definiteness.

Table 9.2: Some examples of clausal names.

Name	Type	Literal meaning
[AEʰʰe³ dʰiŋi ɕaɔ]	Place	The trees covered the ground
[dʰəli ʰʰe³ðe ɕe³]-\lenɕe³]	Place	The city remembers the Šedrý star
[ac⁰ ɲiʱə-Di jɕ jəp jʰi.en-Di jɕ ɲoɕ³, ʰoejɕ.el ʰʰe³ðeð]	Place	The city was founded by the warrior of the sun and the wizard of the moon
[deji ʌʂɛTF³ jɕe³]-selc⁰]	Personal	<i>Gulto</i> takes care of 17 foxes

ni.ɪ biːnən-bəj, [bəʃi dpeʔbe ɲəʔ]-\lenɲəʔ, ʃʰi diːdiɲ .CD.
wait-OTHER year-future, (name), go-OTHER DEF~person-SG PR.ANAPH.SUB.SG
He will go to Muta Pröme Ryk-Šedry̆ next year.

10 | Calendar

Domain II, which contains *Rymako*, has a day that is 26.99410 hours long. Other figures are given in terms of local days:

Table 10.1: Astronomical measures for Domain II.

Period	Length in local days
Local (synodic) day	1.00000
Sidereal day	0.99699
Tropical year (l_y)	301.94714
Sidereal year	302.03719
Synodic month (l_m)	30.80152
Sidereal month	27.95032

10.1 | Tides

In Domain II, the offset of the sea level due to the tide can be modeled by the following equations:

$$y = y_s + y_m \quad (10.1)$$

$$y_s = A_s \cdot (1 + A_{sa} \cdot \cos(\tau \cdot t)) \cdot \cos(2 \cdot \tau \cdot t) \quad (10.2)$$

$$y_m = A_m \cdot \left(1 + A_{ma} \cdot \cos\left(\frac{\tau \cdot t}{l_m}\right)\right) \cdot \cos\left(\frac{2 \cdot \tau \cdot (1 - l_m) \cdot t}{l_m}\right) \quad (10.3)$$

where:

$$\begin{aligned}
\tau &= 2 \cdot \pi \\
A_s &\approx 0.675 \\
A_{sa} &\approx 0.0532 \\
A_m &\approx 1.267 \\
A_{ma} &\approx 0.176 \\
y &= \text{offset of sea level in metres} \\
t &= \text{time since HAT in local synodic days}
\end{aligned}$$

An exact solution to $dy/dt = 0$ is not known to exist. However, the solutions to this equation can be found numerically. Consult Section A.1 for a Sage program to do so.

As the calendar used by aaaaaaaaaA uses the high and low tides to count time, it is not synchronised even with days. The basic unit of time in the calendar is the *tidal day* $\langle \mu\theta\delta\theta^c \rangle$ (l_t) – the amount of time between a high tide and the second high tide thereafter, which is, on average, 1.03356 local synodic days, but can vary considerably. Thus:

$$l_m/l_t \approx 29.80148 \quad (10.4)$$

$$\approx 4053/136 \quad (10.5)$$

$$l_y/l_m \approx 9.80299 \quad (10.6)$$

$$\approx 7215/736 \quad (10.7)$$

This suggests that:

1. most months will have 30 days, but every 136 months, 27 months will have only 29.
2. most years will have 10 months, but every 736 years, 145 years will have only 9.

Figure 10.1: Table of year lengths in a cycle.

0123456789		0123456789		0123456789		0123456789
0 XXXXX9XXXX		19 XX9XXXX9XX		38 9XXXX9XXXX		57 XX9XXXX9X
1 9XXXX9XXXX		20 XXX9XXXX9X		39 9XXXX9XXXX		58 XXX9XXXX9X
2 9XXXX9XXXX		21 XXX9XXXX9X		40 9XXXX9XXXX		59 XXX9XXXX9X
3 9XXXX9XXXX		22 XXX9XXXX9X		41 X9XXXX9XXX		60 XXX9XXXX9
4 9XXXX9XXXX		23 XXX9XXXX9X		42 X9XXXX9XXX		61 XXX9XXXX9
5 9XXXX9XXXX		24 XXX9XXXX9X		43 X9XXXX9XXX		62 XXX9XXXX9
6 9XXXX9XXXX		25 XXX9XXXX9X		44 X9XXXX9XXX		63 XXX9XXXX9
7 X9XXXX9XXX		26 XXX9XXXX9		45 X9XXXX9XXX		64 XXX9XXXX9
8 X9XXXX9XXX		27 XXX9XXXX9		46 X9XXXX9XXX		65 XXX9XXXX9
9 X9XXXX9XXX		28 XXX9XXXX9		47 XX9XXXX9XX		66 XXX9XXXXX
10 X9XXXX9XXX		29 XXX9XXXX9		48 XX9XXXX9XX		67 9XXXX9XXXX
11 X9XXXX9XXX		30 XXX9XXXX9		49 XX9XXXX9XX		68 9XXXX9XXXX
12 X9XXXX9XXX		31 XXX9XXXX9		50 XX9XXXX9XX		69 9XXXX9XXXX
13 X9XXXX9XX		32 XXX9XXXX9		51 XX9XXXX9XX		70 9XXXX9XXXX
14 XX9XXXX9XX		33 XXX9XXXXX		52 XX9XXXX9XX		71 9XXXX9XXXX
15 XX9XXXX9XX		34 9XXXX9XXXX		53 XX9XXXX9X		72 9XXXX9XXXX
16 XX9XXXX9XX		35 9XXXX9XXXX		54 XXX9XXXX9X		73 9XXXX9
17 XX9XXXX9XX		36 9XXXX9XXXX		55 XXX9XXXX9X		
18 XX9XXXX9XX		37 9XXXX9XXXX		56 XXX9XXXX9X		

9: 9 months

X: 10 months

10.5 | Subdivisions of the day

Lek-Tsaro has two systems for subdividing the day.

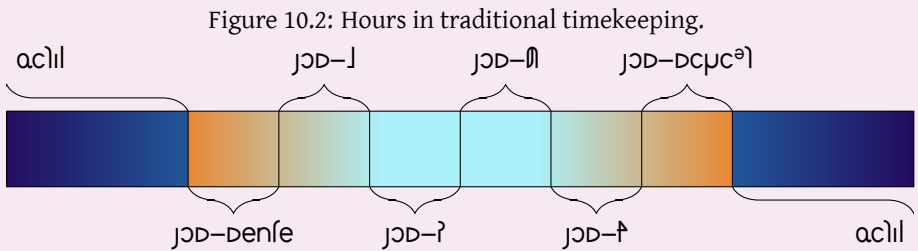
10.5.1 | Traditional timekeeping

The traditional system of timekeeping relies on subdivisions of the solar day. As shown in Figure 10.2, the period between sunrise and sunset are divided into six equally-sized parts <ᵛᵛ>, and the night is considered a separate category. This implies that the length of the “hours” depends on the seasons.

The traditional timekeeping system is vague – typically, the most precise interval used is a quarter or eighth of an “hour”.

10.5.2 | Modern timekeeping

The need for precise schedules necessitated another standard for subdividing the day. The modern system is based on the tidal day, rather than the solar day. In theory, each



tidal day is divided into 23 equal parts $\langle \text{ליל} \rangle$, each of which is divided into 80 equal parts $\langle \text{זאָנע} \rangle$, which are each divided into 40 equal parts $\langle \text{זאָנעל} \rangle$.

Of course, having 23 $\langle \text{ליל} \rangle$ per tidal day requires predicting the next two high tides. For that reason, each day's $\langle \text{ליל} \rangle$ are based on the length of the *previous* tidal day, such that each day might have more or less than 23 $\langle \text{ליל} \rangle$.

A | Listings of programs

A.1 | workfiles/7/tides.sage

```
1 # How many values to output
2
3 limit = int(sys.argv[1]) if len(sys.argv) > 1 else 1000
4
5 # :P
6
7 tau = 2 * pi
8
9 t = var("t")
10
11 # Constants
12
13 A_s = 0.675; A_sa = 0.0532; A_m = 1.267; A_ma = 0.176; l_m = 30.80152
14
15 # Solar component
16 y_s2 = A_s * (1 + A_sa * cos(tau * t)) * cos(2 * tau * t)
17 # Lunar component
18 y_m2 = A_m * (1 + A_ma * cos(tau * t / l_m)) * cos(2 * tau * t / l_m -
19     2 * tau * t)
20 y = y_s2 + y_m2
21 yp = diff(y, t)
22
23 # High and low tides occur at values of t where dy/dt = 0.
24
25 i = 0
26 time = 0
27 print(0)
28 while i < limit:
29     try:
30         time2 = find_root(yp == 0, time + 0.000000001, time + 0.35)
31         print(time2)
32         time = time2
33         i += 1
34     except:
35         time += 0.01
```

workfiles/7/tides.sage

A.2 | workfiles/7/bins.pl6

```

1  # CONSTANTS
2
3  constant \MONTHS_PER_YEAR_CYCLE = 7215;
4  constant \YEARS_PER_YEAR_CYCLE = 736;
5  constant \AVG_MONTHS_PER_YEAR = MONTHS_PER_YEAR_CYCLE /
    YEARS_PER_YEAR_CYCLE;
6
7  # COMPUTATION
8  # For each year, take as many months as are needed
9  # in order to cycle to the next.
10
11 my $c = 0;
12 my @k;
13
14 for 0 ..^ YEARS_PER_YEAR_CYCLE -> $i {
15     my $need = 1 - ($c - floor($c));
16     my $objs = ceiling($need * AVG_MONTHS_PER_YEAR);
17     @k[$i] = $objs;
18     $c += $objs / AVG_MONTHS_PER_YEAR;
19 }
20
21 # DISPLAY
22
23 my \cols = 4;
24 my $len = @k.elems;
25
26 say ("    0123456789" xx cols).join(" | ");
27
28 my \total-rows = ceiling($len / 10);
29 my \rows = ceiling(total-rows / cols);
30
31 for 0 ..^ rows -> $j {
32     for 0 ..^ cols -> $p {
33         print(" | ") if $p != 0;
34         my $q = $j + rows * $p;
35         next if $q >= total-rows;
36         printf("%3d ", $q);
37         for 0 ..^ 10 {
38             my $i = 10 * $q + $_;
39             if $i >= $len { print " "; }
40             else {
41                 print "0123456789XE".substr(@k[$i], 1);
42             }
43         }
44     }
45     say "";
46 }

```

workfiles/7/bins.pl6

A.3 | workfiles/7/conno.pl6

```

1 my $digits-str = "0123456789TKXSNVFM";
2 my @digits = $digits-str.comb;
3
4 sub convert-small-fwd($n, $pad = False) {
5     die "$n must be < 4199" if $n >= 4199;
6     my $a = $n div (19 * 17);
7     my $b = ($n div 17) % 19;
8     my $c = $n % 17;
9     return
10         (!$pad && $a == 0 ?? "" !! @digits[$a]) ~
11         (!$pad && $b == 0 && $a == 0 ?? "" !! @digits[$b]) ~
12         @digits[$c];
13 }
14
15 sub convert-small-back($s) {
16     die "$s must be 3 chars or fewer" if $s.chars > 3;
17     my $c = $digits-str.index($s.substr(* - 1, 1) // "0");
18     my $b = $digits-str.index($s.substr(* - 2, 1) // "0");
19     my $a = $digits-str.index($s.substr(* - 3, 1) // "0");
20     return $c + 17 * ($b + 19 * $a);
21 }
22
23 sub triangle($n, $p) {
24     return ($n * (2 * $p + 1 - $n)) div 2;
25 }
26
27 sub sqrt-floor($y) {
28     die "$y is negative" if $y < 0;
29     return $y if $y < 2;
30     my $small = sqrt-floor($y +> 2) +< 1;
31     my $large = $small + 1;
32     return $small if $large * $large > $y;
33     return $large;
34 }
35
36 sub sqrt-ceil($y) {
37     my $n = sqrt-floor($y);
38     return $n if $n * $n == $y;
39     return $n + 1;
40 }
41
42 sub untriangle($y, $p) {
43     return (2 * $p + 1 - sqrt-ceil(4 * $p * $p + 4 * $p - 8 * $y + 1))
44         div 2;
45 }
46
47 my @powers = (4199);
48
49 for 0 .. 10 {
50     my $p = @powers[* - 1];
51     @powers.push: $p * ($p + 1) div 2;
52 }
53
54 sub convert-large-fwd-h($n, $i, $pad = False) {

```

```

53 # base case
54 if $i == 0 {
55     return convert-small-fwd($n, $pad);
56 }
57 # recursive
58 my $super = untriangle($n, @powers[$i - 1]);
59 my $infra = $n - triangle($super, @powers[$i - 1]);
60 if $super == 0 && !$pad {
61     return convert-large-fwd-h($infra, $i - 1, False);
62 }
63 return
64     convert-large-fwd-h($super, $i - 1, $pad) ~
65     (":" x $i) ~
66     convert-large-fwd-h($infra, $i - 1, True);
67 }
68
69 sub convert-large-fwd($n, $pad = False) {
70     my $i = 0;
71     ++$i while @powers[$i] <= $n;
72     convert-large-fwd-h($n, $i, $pad);
73 }
74
75 sub convert-large-back($s) {
76     # Find the longest run of colons
77     my @matches = ($s =~ m:g/":+"/); #/"
78     if (!@matches) {
79         return convert-small-back($s);
80     }
81     my $longest-match = @matches.max(*.chars);
82     my $i = (~$longest-match).chars;
83     my $left = $s.substr(0, $longest-match.from);
84     my $right = $s.substr($longest-match.to);
85     my $sup = convert-large-back($left);
86     my $inf = convert-large-back($right);
87     return triangle($sup, @powers[$i - 1]) + $inf;
88 }
89
90 multi MAIN(Int :$fwd) {
91     say convert-large-fwd($fwd);
92 }
93 multi MAIN(Str :$back) {
94     say convert-large-back($back);
95 }

```

workfiles/7/conno.pl6

A.4 | workfiles/7/count-days.pl6

```

1 # Count the number of days between 1/0/0 and D/M/Y, inclusive.
2
3 # CONSTANTS
4
5 constant \MONTHS_PER_YEAR_CYCLE = 7215;
6 constant \YEARS_PER_YEAR_CYCLE = 736;

```



```

7 constant \AVG_MONTHS_PER_YEAR = MONTHS_PER_YEAR_CYCLE /
  YEARS_PER_YEAR_CYCLE;
8 constant \MONTHS_PER_MONTH_CYCLE = 136;
9 constant \DAYS_PER_MONTH_CYCLE = 4053;
10
11 # COMPUTATION
12 # For each year, take as many months as are needed
13 # in order to cycle to the next.
14
15 my $c = 0;
16 my @k = (0);
17
18 for 0 ..^ YEARS_PER_YEAR_CYCLE -> $i {
19   my $need = 1 - ($c - floor($c));
20   my $objs = ceiling($need * AVG_MONTHS_PER_YEAR);
21   @k[$i + 1] = $objs;
22   $c += $objs / AVG_MONTHS_PER_YEAR;
23 }
24
25 my @cumk = [\+] @k;
26
27 sub months-before-year($year) {
28   my $whole-cycles = $year div YEARS_PER_YEAR_CYCLE;
29   my $remainder = $year % YEARS_PER_YEAR_CYCLE;
30   return $whole-cycles * MONTHS_PER_YEAR_CYCLE + @cumk[$remainder];
31 }
32
33 my @m = (0);
34
35 for 0 ..^ MONTHS_PER_MONTH_CYCLE -> $i {
36   @m.push: ($i % 5 == 2) ?? 29 !! 30;
37 }
38
39 my @cumm = [\+] @m;
40
41 sub days-before-month($month) {
42   my $whole-cycles = $month div MONTHS_PER_MONTH_CYCLE;
43   my $remainder = $month % MONTHS_PER_MONTH_CYCLE;
44   return $whole-cycles * DAYS_PER_MONTH_CYCLE + @cumm[$remainder];
45 }
46
47 sub days-before-date($d2, $m, $y) {
48   my $d = $d2 - 1; # d is 0-indexed
49   my $bm = months-before-year($y) + $m;
50   return days-before-month($bm) + $d;
51 }
52
53 sub MAIN($d2, $m, $y) {
54   say days-before-date($d2, $m, $y);
55 }

```

workfiles/7/count-days.pl6

B | Arithmetic in base v

This chapter describes algorithms for performing arithmetic operations in Lek-Tsaro's number system.

B.1 | Operations on small numbers

B.1.1 | Additions

If both addends are smaller than 4199, then it is sufficient to use mixed-base addition:

$$\begin{array}{r}
 1 \\
 0 F L \\
 9 ? A \\
 \hline
 F A ? \\
 \\
 1 1 \\
 J ? \uparrow \\
 \mathfrak{L} \psi ? \\
 \hline
 1 J 0 \Delta
 \end{array}$$

B.1.2 | Subtraction

If both of the operands are smaller than 4199, then it is sufficient to use mixed-base subtraction.

$$\begin{array}{r}
 ? 1? \\
 \mathfrak{J} ? A \\
 0 F L \\
 \hline
 J \mathfrak{L} \uparrow
 \end{array}$$

B.1.3 | Determining parity

A number less than 4199 is even iff the sum of its digits in base v is even – that is, either none of its digits are odd, or if exactly two are.

B.1.4 | Dividing by two

If a number's base- v representation contains only even digits, then divide each digit by two.

If the representation has two odd digits, then take advantage of the identities

$$11_v/2 = 9_v$$

$$101_v/2 = 99_v$$

$$110_v/2 = T0_v$$

This operation is written as $\langle D \rangle$, short for $\langle D \psi ne \rangle$ “one half”. Thus, in hacm:

- $D11 = L$
- $D101 = LL$
- $D110 = F0$

B.1.5 | Multiplication

With the previous two operations, it is now possible to use peasant multiplication to multiply small numbers.

B.2 | Operations on larger numbers

B.2.1 | Addition

For some $i \in \mathbb{N}$, and two numbers number $a = x_a :^i y_a$ and $b = x_b :^i y_b$, we take advantage of the fact that

$$x_a :^i y_a + x_b :^i y_b = (x_a + 1) :^i y_a + (x_b - 1) :^i y_b + (x_a - x_b + 1) \quad (B.1)$$

$$x_a :^i y_a + x_b :^i y_b = (x_a + x_b) :^i y_a + 0 :^i y_b + x_a \cdot x_b \quad (B.2)$$

$$= (x_a + x_b) :^i (y_a + y_b) + x_a \cdot x_b \quad (B.3)$$

Romanisation

In this text, the romanisation is used only to transcribe names into English. Whenever possible, the hacmisation should be used.

Table B.1: The consonants of aaaaaaaaaA.

	Bilabial	Alveolar	Palatal	Velar	Glottal
Nasal	m	n	ɲ	ŋ	
Plosive	p b	t d	tʃ dʃ	k g	ʔ
Fricative	f	s	ʃ	h	
(coarticulated)	ɸh	fh		fʃ	
Affricate		ts	tʃ		
Lateral fricative		ɬ			
Approximant		r	j	w	
Lateral approximant		l			
Trill		ʀ			

Table B.2: The vowels of aaaaaaaaaA.

Spread	Half-rounded	Rounded
i	y	ɥ
ĩ	u	ũ
e		ö
ë		o
a		

Rod signs are represented by the Arabic digits <1 2 3 4 5 6 7 8> attached to the end of the verbs they encompass. Proper words are preceded by a backslash <\>.

<ɲ> should be capitalised as <N> only if one can depend on the majuscule glyph appearing like an N with a hook. Otherwise, it should be spelled <Ng>.

C | Dictionary

1

.cɒn *ninanim* house
.əʔfəɒ *nabst* sadness, grief

r

flɪpɕ *ninanim* river
 flɪlɪn v (S) fights (O)
 flɔɾɔn v (S) falls on (O)
 flɔɕ *ninanim* flower
 flɔ^edi *desc* sufficient, wanted,
 wished-for
 flɛlɪ *desc* complete, full, mature
 flɛl *nsent* who?
 flɔɔ *nabst* power, magic, motivation
 flɔɕɔn v (S) stabs, stings (O)
 flɔɕlɪn v (S) wants (O), benefactive
 flɔɕɔ^ə *ninanim* fruit
 flɔɕɔn v (S) answers to (O)
 flɔɪn v (S) loses, frees (O); (O) escapes
 flɔɪpɪ *desc* heavy
 flɔɔ *ninanim* tree
 flɔɔ *nined* wood
 fedɔn v (S) buys (O)
 feɪ.ɕ^ə *nedib* beef
 feɪn v rain (S = other)

ʃəllɪ *nsent* coward, knave
 ʃəʔɥɔ *nined* blood vessels

ר

𐤀𐤏𐤔𐤁^o *nsent* warrior
 𐤏𐤗𐤀𐤋 *desc* potent, powerful not
 in a physical sense
 𐤋𐤏𐤁𐤔 *nabst* south
 𐤏𐤗𐤀 *v* (S) makes a loud noise
 𐤏𐤗𐤁𐤏𐤁^o *ninanim* mirror
 𐤏𐤗 *v* (S) is at (O), locational verb
 𐤏𐤗𐤁𐤏 *nmeas* subdivision of the day
 cf Grammar / Calendar / Subdivisions of
 the day / Modern timekeeping
 𐤏𐤗𐤏𐤁^o *ninanim* moon
 𐤏𐤗𐤏 *ninanim* era
 𐤏𐤗𐤏𐤁 *nined* stone
 𐤏𐤗𐤀 *desc* all, every
 𐤏𐤗𐤀 *desc* whole, entire
 𐤏𐤗^o .𐤏𐤗 *v* (S) needs (O)
 𐤏𐤗𐤀𐤋 *desc* old

1.

lpe³ncn v (S) hunts for (O)
 lcnin v (S) shoots an arrow to (O)
 lcl *nabst* nature, disposition

J

jɿɿɿ *ninanim* ring
 jcn v (S) is (O)
 jcncn v (S) attaches to, loves (O)
 jcne *nmeas* subdivision of the day
 cf Grammar / Calendar / Subdivisions of
 the day / Modern timekeeping
 jc^əl *nanim* fox
 jɔɔ *nmeas* subdivision of the day
 cf Grammar / Calendar / Subdivisions of
 the day / Traditional timekeeping
 jɔ^əɿɿ *ninanim* table
 je.in v (S) knows (O) answers (last
 clause)
 jenin v (S) is worried by (O)
 jea^lc *nabst* daytime
 jedilcn *ninanim* essay
 je^əle *ninanim* land, country
 jəf *desc* many, again
 jəɿ *ninanim* day, sun

j^h

j^h.en *nsent* magician
 j^hin v (S) goes toward (O)
 j^hɿɿcn v (S) creates (O)
 j^hcn *nabst* how many?
 j^he^əncn v (S) befriends (O)

n

nɿɿɿ *nanim* cat
 ni.cn v (S) waits for/until (O), tem-
 poral verb, if
 ni.eɿcn v (S) covers, spans (O)
 ncɔcn v (S) dances around (O)
 nchel *ninanim* group, organisation,
 order
 nc^ə *ninanim* point nc^ə-ɔɿine
 halfway point
 nelcn v (S) swims in (O)
 neɔ *desc* male
 neɿn v (S) gives something to (O)

nepacn v (S) hides from (O)
 nepɿɿ *desc* sudden
 nel *nabst* nature, temperament,
 disposition
 neldɿ *nsent* mind, brain
 nə^ənɿn v (S) kills (O), (O) dies
 nə^əɿn v (S) steals from (O)
 nə^əɿɿɔ^ən *nsent* thief

n^ə

n^əɔɿn v (S) thinks, ponders about (O)

u

u^əɿɿ *nfluid* poison

a

aɿen^ue *ninanim* coin
 acjcn v (S) obeys (O)
 acn v (S) joins (O), and
 acnɿ *desc* early
 acɿcn v touch
 acɿe *nabst* what
 ac^əl *desc* female
 aɔ^əɿɿ *ninanim* spoon
 aehcn v (S) plays with (O)
 aə^ə *ninanim* event, occurrence

a^l

a^lɿe *nabst* quote, words, speech
 a^le *ninanim* what
 a^ləɿə^ə *nfluid* water

a^h

a^hə^əɔɔ *nabst* empathy

D

- ɒɥine *nabst* one half
 ɒilɪn v (S) eats (O)
 ɒijɪ *nsent* person
 ɒɪn *nedib* rice
 ɒɔɪ *nsent* child (offspring)
 ɒɔɥɒe^ɔ *nanim* tongue
 ɒɔɥɔe^ɔ *nabst* evening
 ɒɔɪɪn v (S) produces (O)
 ɒɔɪɪn v (S) is destroyed to make, for
 (O)
 ɒɔe^ɔɥɒɒ *nanim* scorpion
 ɒelɔɪn v (S) gives birth to (O), (O) is
 born (S) is not necessarily the mother;
 this can be either parent
 ɒejɔɪn v (S) raises, takes care of,
 tends to (O)
 ɒenfe *nabst* morning
 ɒeaɥɪn v (S) stands on, is on (O)
 ɒeɔɪn v (S) drowns in (O), (O) fills
 (S)
 ɒedi *desc* in return
 ɒedɔɪn v (S) succeeds at (O), (S)
 does something to (O)
 ɒeɥɔe^ɔ *nanim* opposite side
 ɒel *nmeas* volume in expressions
 such as ɒel-ɥəjɔe^ɔ “cupful”
 ɒelli *desc* similar
 ɒelɔɪn v (S) imitates (O)
 ɒəɪɪn v (S) recalls (O)
 ɒən^ɔɔ *nanim* rabbit

ɒ

- ɒɪɪɪn v (S) is inside (O)
 ɒɪɔɔ *ninanim* back (body part)
 ɒɪɒə *nabst* life, existence
 ɒeleɒ *nfluid* nitrogen
 ɒeɒɪn v (S) sleeps
 ɒə^ɔɥɔ *ninanim* pathway

ɸ

- ɸɥə^ɔnɪn v (S) laughs at (O)

- ɸoejɪn v (S) founds (O)
 ɸɔɪɪ *desc* well (not sick)
 ɸɔɪ *nabst* five

d

- dɪɪɪɪ *nabst* ground, floor
 dɪɪen *nanim* owl
 dɥɔɪn v hold, carry, instrumental
 verb
 dɥe^ɔɒe *ninanim* city
 dɪɪɪɪn v (S) sits at (O)
 dɪɪɪn v (S) dislikes, objects to, disap-
 proves of (O)
 dɪɪe *ninanim* landmass, domain
 dɪɪɪn v (S) wears, experiences (O)
 dɪɪe^ɔ *nedib* noodles
 də.ɔɪn *nanim* large animal
 dən^ɔɪ *ninanim* knee

b

- bɪe *ninanim* year
 bɪɪəɪ *nmeas* subdivision of the day
 cf Grammar / Calendar / Subdivisions of
 the day / Modern timekeeping
 bɔɪɪn v (S) walks to (O)
 bəɪ *nabst* future, next (time period)
 bə^ɔn^ɔɪn v (S) succumbs to their im-
 pulses

h

- hɥɔɪen *ninanim* book
 hɪ.ɪɥ *nabst* spring (season)
 hɪjɔɔ *ninanim* nose
 hɪjɔe *ninanim* leaf
 hɪɪə^ɔ *ninanim* statue
 hɔɪn v (S) claims that (O)
 hɔɥɔɪn v (S) is named (O)
 hɔe^ɔɒɪ *nedib* food
 hɔɪɪ *ninanim* cart
 heɔɪn v (S) asks for, requests (O)
 heɒɪ *desc* large
 hə^ɔɒɪ *desc* evil, malicious

| ɥ

ɥin v (S) sees (O), because
ɥin[ɔ=jəp] (“see the sun”) = “wish”

| ɳ

ɳin v discipline, punish, constrain
ɳcn v (S) allows (O)

| ɸ

ɸi.cin v (S) is beside (O)
ɸifi nined grass
ɸifibi ninanim blade of grass
ɸilin v (S) climbs, rises in (O)
ɸcʰ ninanim star
ɸeain v (S) speaks to (O), (S) asks
(O)
ɸeacn v (S) spreads (O)
ɸeli ninanim place
ɸeʰi desc friendly, kind, consider-
ate, nice

ɸəli desc late
ɸəlcʰ nabst nighttime
ɸəlcʰ ninanim cup
ɸəbəʰ nmeas tidal day
ɸəʰc nined gold

| s

sɪɟc nfluid soup
sɪle nanim fish
seɳin v (S) perceives (O) non-
visually

| o

oelje nined forest

| l

lel nabst language
lelebi ninanim a language