Lecture 14: Boosting

Machine Learning, Summer Term 2019

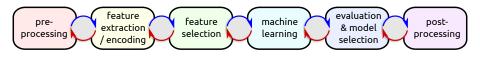
July 4, 2019

Michael Tangermann Frank Hutter Marius Lindauer

University of Freiburg



The Big Picture



- Lecture 1: overview
- Lecture 2-6: linear methods
- Lecture 7-9: algorithm-independent principles
- Lectures 10-15: nonlinear methods
 - Lecture 10-12: kernel-based methods
 - Lectures 13-14: tree-based methods and ensembles
 - Lecture 15: neural networks

Motivation for Boosting

Winning Methods of 10 Kaggle competitions in 2016 with non-image input (Competitions with images: deep neural networks dominate)

Almost all winners were large ensembles prominently using boosting:

Competition	Winners
Expedia Hotel Recommendations	1st: XGB
Santander Customer Satisfaction	3rd: XGB, RF, AdaBoost & others
Home Depot Product Search Relevance	1st and 3rd: XGB and RF
BNP Paribas Cardif Claims Management	1st and 2nd: XGB, RF & others
March Machine Learning Mania 2016	1st: RF and logarithmic regression
Telstra Network Disruptions	1st: sklearn, XGB, NN
Prudential Life Insurance Assessment	Top 3 used XGB (2nd and 3rd also others)
Airbnb New User Bookings	2nd: XGB; 3rd: XGB, NN, RF, ET
Homesite Quote Conversion	1st and 2nd: XGB & others; 3rd: others

XGB = Extreme Gradient Boosting

Places not listed: choice of method not released

Motivation for Boosting

 Similar to random forests, boosting has often been called the best off-the-shelf model (e.g., by Leo Breiman, inventor of random forests)

Motivation for Boosting

- Similar to random forests, boosting has often been called the best off-the-shelf model (e.g., by Leo Breiman, inventor of random forests)
- Similar advantages as random forests (we'll boost trees)
 - Trees: easy to interpret
 - Directly handle categorical features
 - Scalable to many data points (can be fast)
 - Scalable to many features (automated feature selectors)
 - Robust performance even for small datasets

Lecture Overview

Introduction to Boosting

2 AdaBoost

Gradient Boosting

Lecture Overview

Introduction to Boosting

2 AdaBoost

Gradient Boosting

Boosting combines weak learners

- A weak learner is a learning algorithm that does at least slightly better than random (e.g., strictly better than 50% error for binary classification)
 - E.g., email spam filter: occurrence of 'buy now' would already let us classify better than random
 - Often, these simple rules already yield reasonable classification performance

Boosting combines weak learners

- A weak learner is a learning algorithm that does at least slightly better than random (e.g., strictly better than 50% error for binary classification)
 - E.g., email spam filter: occurrence of 'buy now' would already let us classify better than random
 - Often, these simple rules already yield reasonable classification performance
- Boosting combines many weak learners into a highly accurate decision model.

Boosting combines weak learners

- A weak learner is a learning algorithm that does at least slightly better than random (e.g., strictly better than 50% error for binary classification)
 - E.g., email spam filter: occurrence of 'buy now' would already let us classify better than random
 - Often, these simple rules already yield reasonable classification performance
- Boosting combines many weak learners into a highly accurate decision model.
- In this lecture, we use decision trees as our class of weak learners (even single-level trees, 'stumps', are sometimes used)

• Like bagging, boosting is an committee / method that combines many weak learners (submodels) into a highly accurate decision model.

- Like bagging, boosting is an committee / method that combines many weak learners (submodels) into a highly accurate decision model.
- ullet Boosting trains submodels sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels

- Like bagging, boosting is an committee / method that combines many weak learners (submodels) into a highly accurate decision model.
- ullet Boosting trains submodels sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels
 - ★ This is exactly like bagging
 - ★ This is different to bagging

- Like bagging, boosting is an committee / method that combines many weak learners (submodels) into a highly accurate decision model.
- ullet Boosting trains submodels sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels
 - ★ This is exactly like bagging
 - ★ This is different to bagging
- Boosting can optionally give different weights to its submodels

- Like bagging, boosting is an committee / method that combines many weak learners (submodels) into a highly accurate decision model.
- ullet Boosting trains submodels sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels
 - ★ This is exactly like bagging
 - ★ This is different to bagging
- Boosting can optionally give different weights to its submodels
 - This is exactly like bagging
 - ★ This is different to bagging

- Like bagging, boosting is an committee / method that combines many weak learners (submodels) into a highly accurate decision model.
- ullet Boosting trains submodels sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels
 - ★ This is exactly like bagging
 - ★ This is different to bagging
- Boosting can optionally give different weights to its submodels
 - This is exactly like bagging
 - ★ This is different to bagging
- Boosting can optionally bootstrap samples and use random feature subsets

- Like bagging, boosting is an committee / method that combines many weak learners (submodels) into a highly accurate decision model.
- ullet Boosting trains submodels sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels
 - ★ This is exactly like bagging
 - ★ This is different to bagging
- Boosting can optionally give different weights to its submodels
 - This is exactly like bagging
 - ★ This is different to bagging
- Boosting can optionally bootstrap samples and use random feature subsets
 - This is exactly like bagging
 - ★ This is different to bagging

Two approaches to boosting

Boosting: Submodels are trained sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels

In this lecture, we will consider two algorithms that implement boosting:

Two approaches to boosting

Boosting: Submodels are trained sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels

In this lecture, we will consider two algorithms that implement boosting:

- Adaboost, where mistakes are identified by weightings on more "difficult" data points
 - Each submodel also gets a different weight, based on how "good" it is

Two approaches to boosting

Boosting: Submodels are trained sequentially, with the m-th submodel trained to fix the mistakes of the first m-1 submodels

In this lecture, we will consider two algorithms that implement boosting:

Adaboost, where mistakes are identified by weightings on more

- "difficult" data points
 - Each submodel also gets a different weight, based on how "good" it is
- Gradient Boosting, where mistakes are identified by the gradient of our loss function
 - Each submodel gets the same weight

Lecture Overview

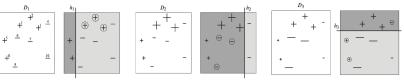
Introduction to Boosting

2 AdaBoost

Gradient Boosting

Basic idea: iteratively construct submodels G_m that fix previous errors

- ullet We'll have a weight w_i for each data point i
 - w_i measures how hard data point x_i is to predict
 - Start with uniform weights $w_i^{(1)}$, adapt across iterations m: $w_i^{(m)}$
 - In each iteration m, exponentially increase weights of data points x_i misclassified by G_m :



from [Schapire and Freund, 2012]

Figure

Basic idea: iteratively construct submodels G_m that fix previous errors

- ullet We'll have a weight w_i for each data point i
 - w_i measures how hard data point x_i is to predict
 - Start with uniform weights $w_i^{(1)}$, adapt across iterations m: $w_i^{(m)}$
 - In each iteration m, exponentially increase weights of data points x_i misclassified by G_m :

$$w_i^{(m+1)} := \left\{ egin{array}{ll} w_i^{(m)} imes \exp(lpha_m) &, & \mbox{if } y_i
eq G_m(x_i) \\ w_i^{(m)} &, & \mbox{otherwise} \end{array}
ight.$$

Basic idea: iteratively construct submodels G_m that fix previous errors

- ullet We'll have a weight w_i for each data point i
 - w_i measures how hard data point x_i is to predict
 - Start with uniform weights $w_i^{(1)}$, adapt across iterations m: $w_i^{(m)}$
 - In each iteration m, exponentially increase weights of data points x_i misclassified by G_m :

$$w_i^{(m+1)} := \begin{cases} w_i^{(m)} imes \exp(lpha_m) &, & \text{if } y_i
eq G_m(x_i) \\ w_i^{(m)} &, & \text{otherwise} \end{cases}$$
 $= w_i^{(m)} \exp(lpha_m \mathbb{I}(y_i
eq G_m(x_i))$

Basic idea: iteratively construct submodels G_m that fix previous errors

- ullet We'll have a weight w_i for each data point i
 - w_i measures how hard data point x_i is to predict
 - Start with uniform weights $w_i^{(1)}$, adapt across iterations m: $w_i^{(m)}$
 - In each iteration m, exponentially increase weights of data points x_i misclassified by G_m :

$$w_i^{(m+1)} := \begin{cases} w_i^{(m)} imes \exp(lpha_m) &, & ext{if } y_i
eq G_m(x_i) \\ w_i^{(m)} &, & ext{otherwise} \end{cases}$$
 $= w_i^{(m)} \exp(lpha_m \mathbb{I}(y_i
eq G_m(x_i))$

- We'll also compute a weight α_m for each submodel G_m
 - This depends on how good the model is
 - We'll use these weights α_m for a weighted majority vote in the end

ullet Binary classification problem; class labels +1 and -1

- ullet Binary classification problem; class labels +1 and -1
- Final model G(x) combines individual submodels G_1, \ldots, G_M through a weighted majority vote with weights $\alpha_1, \ldots, \alpha_M$:

$$G(x) = \operatorname{sign}\left(\sum_{m=1}^{M} \alpha_m G_m(x)\right)$$

- ullet Binary classification problem; class labels +1 and -1
- Final model G(x) combines individual submodels G_1, \ldots, G_M through a weighted majority vote with weights $\alpha_1, \ldots, \alpha_M$:

$$G(x) = \operatorname{sign}\left(\sum_{m=1}^{M} \alpha_m G_m(x)\right)$$

• Submodels G_m are weighted depending on their error err_m :

$$\alpha_m := \log \frac{1 - err_m}{err_m}$$

- E.g., $err_m = 0.1 \to \alpha_m = 2.197$
- E.g., $err_m = 0.4 \to \alpha_m = 0.41$
- E.g., $err_m = 0.5 \rightarrow \alpha_m = 0$

- ullet Binary classification problem; class labels +1 and -1
- Final model G(x) combines individual submodels G_1, \ldots, G_M through a weighted majority vote with weights $\alpha_1, \ldots, \alpha_M$:

$$G(x) = \operatorname{sign}\left(\sum_{m=1}^{M} \alpha_m G_m(x)\right)$$

• Submodels G_m are weighted depending on their error err_m :

$$\alpha_m := \log \frac{1 - err_m}{err_m}$$

- E.g., $err_m = 0.1 \to \alpha_m = 2.197$
- E.g., $err_m = 0.4 \to \alpha_m = 0.41$
- E.g., $err_m = 0.5 \rightarrow \alpha_m = 0$
- This choice of α_m can be shown to minimize an upper bound of the final hypothesis error (see [Schapire, 2003] for details)

ullet The (unweighted) training error rate of a submodel G_m is

$$\overline{err} = \frac{1}{N} \sum_{i=1}^{N} \mathbb{I}(y_i \neq G_m(x_i)).$$

ullet The (unweighted) training error rate of a submodel G_m is

$$\overline{err} = \frac{1}{N} \sum_{i=1}^{N} \mathbb{I}(y_i \neq G_m(x_i)).$$

ullet The weighted training error rate of submodel G_m is

$$err_m = \frac{\sum_{i=1}^{N} w_i \mathbb{I}(y_i \neq G_m(x_i))}{\sum_{i=1}^{N} w_i}$$

ullet The (unweighted) training error rate of a submodel G_m is

$$\overline{err} = \frac{1}{N} \sum_{i=1}^{N} \mathbb{I}(y_i \neq G_m(x_i)).$$

ullet The weighted training error rate of submodel G_m is

$$err_m = \frac{\sum_{i=1}^{N} w_i \mathbb{I}(y_i \neq G_m(x_i))}{\sum_{i=1}^{N} w_i}$$

 As mentioned, these weighted training error rates are used for computing the model weights:

$$\alpha_m := \log \frac{1 - err_m}{err_m}$$

FINAL CLASSIFIER

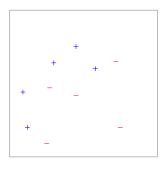


Training Sample $\cdots \bullet G_1(x)$

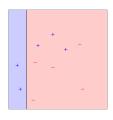
from [Hastie, Tibshirani and Friedman]

AdaBoost Example (step m = 1)

Example taken from [Schapire, 2003] Model class: simple axis-aligned splits (decision stumps)



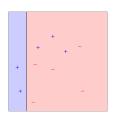
AdaBoost Example (step m = 1)



How large is the error err_1 of this first model?

 \star 0.3 \star 0.2 \star 0.5 \star 0.7

AdaBoost Example (step m = 1)



How large is the error err_1 of this first model?

★ 0.3 ★ 0.2 ★ 0.5 ★ 0.7

AdaBoost Example (step m = 1 details)

Model error and model weight:

$$err_1 = \sum_{i=1}^{N} w_i^{(1)} \mathbb{I}(G_1(x_i) \neq y_i) = \frac{1}{10} \times 3 = 0.3$$

 $\alpha_1 = \log \frac{1 - err_1}{err_1} = \log \frac{1 - 0.3}{0.3} \approx 0.847$

AdaBoost Example (step m = 1 details)

• Model error and model weight:

$$err_1 = \sum_{i=1}^{N} w_i^{(1)} \mathbb{I}(G_1(x_i) \neq y_i) = \frac{1}{10} \times 3 = 0.3$$

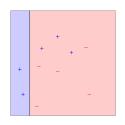
$$\alpha_1 = \log \frac{1 - err_1}{err_1} = \log \frac{1 - 0.3}{0.3} \approx 0.847$$

• Weight adaptation for data points:

$$w_i^{(m+1)} = w_i^{(m)} \exp(\alpha_m \mathbb{I}(y_i \neq G_m(x_i)))$$

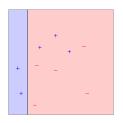
- Misclassified data point: $w_i^{(2)} \leftarrow w_i^{(1)} \exp(\alpha_1) \approx 0.1 \exp(0.847) \approx 0.233$
- Correctly classified data points: $w_i^{(2)} \leftarrow w_i^{(1)} = 0.1$

AdaBoost Example (step m=2)



$$err_2 = \frac{\sum_{i=1}^{N} w_i^{(2)} \mathbb{I}(G_m(x_i) \neq y_i)}{\sum_{i=1}^{N} w_i^{(2)}} \approx \frac{0.1 + 0.1 + 0.1}{1.4} \approx 0.21$$
$$\alpha_2 = \log \frac{1 - err_2}{err_2} \approx \log \frac{1 - 0.21}{0.21} \approx 1.3$$

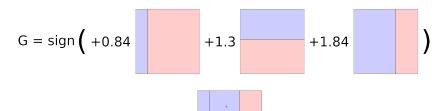
AdaBoost Example (step m = 3)



$$err_3 \approx 0.14, \alpha_3 \approx 1.84$$

AdaBoost Example

Final classifier:



AdaBoost - Complete Algorithm

Algorithm 10.1 AdaBoost.M1.

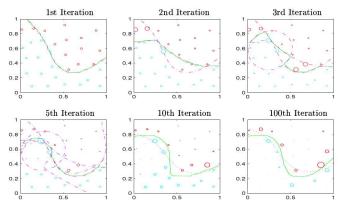
- 1. Initialize the observation weights $w_i = 1/N, i = 1, 2, \dots, N$.
- 2. For m = 1 to M:
 - (a) Fit a classifier $G_m(x)$ to the training data using weights w_i .
 - (b) Compute

$$err_m = \frac{\sum_{i=1}^{N} w_i I(y_i \neq G_m(x_i))}{\sum_{i=1}^{N} w_i}.$$

- (c) Compute $\alpha_m = \log((1 \operatorname{err}_m)/\operatorname{err}_m)$.
- (d) Set $w_i \leftarrow w_i \cdot \exp[\alpha_m \cdot I(y_i \neq G_m(x_i))], i = 1, 2, \dots, N.$
- 3. Output $G(x) = \operatorname{sign} \left[\sum_{m=1}^{M} \alpha_m G_m(x) \right]$.

from [Hastie, Tibshirani and Friedman]

AdaBoost: Focus on Hardest Data Points



Taken from [Meir, Raetsch, 2003]: AdaBoost on a 2D toy data set: color indicates the label, diameter is proportional to the weight of the example. Purple dashed lines: decision boundaries of the single classifiers (up to 5th iteration). Solid green line: decision boundary of the combined classifier. In the last two plots the decision line of Bagging is plotted for a comparison.

Main problem of AdaBoost: if the data is very noisy, it can overfit badly / it it very sensitive to outliers

Lecture Overview

Introduction to Boosting

2 AdaBoost

Gradient Boosting

Break: Teaching evaluations

- Teaching evaluations are running
 - Evaluations are our only formal reward
 - We redesigned much of the course, so feedback is very valuable
- Let's take a 10-minute break to do the evaluation right now

ullet With AdaBoost, we took the sign of a weighted majority vote of M submodels, for binary classification:

$$G(x) = \operatorname{sign}\left(\sum_{m=1}^{M} \alpha_m \, G_m(x)\right)$$

 Let's now generalise to a real-valued prediction, and remove the weights on each submodel:

$$G(x) = \sum_{m=1}^{M} G_m(x)$$

ullet Again, we will fit these M submodels sequentially.

Suppose that M-1 submodels have already been fitted, and our task is to fit the $M{\rm th}$ submodel.

$$G(x) = \sum_{m=1}^{M-1} G_m(x) + G_M(x)$$

Suppose that M-1 submodels have already been fitted, and our task is to fit the $M{\rm th}$ submodel.

$$G(x) = \sum_{m=1}^{M-1} G_m(x) + G_M(x)$$

As always, our objective is to minimise the loss over all data points:

$$\sum_{i=1}^{N} L(y_i, \sum_{m=1}^{M-1} G_m(x_i) + G_M(x_i))$$

Suppose that M-1 submodels have already been fitted, and our task is to fit the Mth submodel.

$$G(x) = \sum_{m=1}^{M-1} G_m(x) + G_M(x)$$

As always, our objective is to minimise the loss over all data points:

$$\sum_{i=1}^{N} L(y_i, \sum_{m=1}^{M-1} G_m(x_i) + G_M(x_i))$$

Question: What method have we seen for iteratively minimising the loss of a model's predictions?

- ★ PCA ★ ICA ★ Talking to domain experts ★ Gradient descent

Gradient Boosting: Idea

• We can use **any** differentiable loss function L, and find the gradient g_i of our model's predictions (with M submodels) with respect to our predictions for each data point i:

$$g_i = \frac{\partial L(y_i, G(x_i))}{\partial G(x_i)}$$

Gradient Boosting: Idea

• We can use **any** differentiable loss function L, and find the gradient g_i of our model's predictions (with M submodels) with respect to our predictions for each data point i:

$$g_i = \frac{\partial L(y_i, G(x_i))}{\partial G(x_i)}$$

- We then fit our new weak learner G_{M+1} with parameters θ_{M+1} using a gradient descent step $-\nu \cdot g$ as our target variable y.
 - ν is our gradient descent step size, or learning rate. In the context of gradient boosting, ν is also known as shrinkage.

$$\theta_{M+1} = \underset{\theta}{\operatorname{arg\,min}} \sum_{i=1}^{N} L(-\nu \cdot g_i, G(x_i; \theta))$$

Gradient Boosting Algorithm (Simplified)

- 1. Initialize G = best constant prediction for y.
- 2. For m=1 to M
 - (a) For i=1 to N: $g_i=\frac{\partial L(y_i,G(x_i))}{\partial G(x_i)}$
 - (b) Fit weak learner G_m to data $\langle x_i, -\nu \cdot g_i \rangle_{i=1}^N$
 - (c) Update $G(x) \leftarrow G(x) + G_m(x)$
- 3. Output final prediction G(x)

Gradient Boosting: Plugging in decision trees

- 1. Initialize G = best constant prediction for y.
- 2. For m=1 to M
 - (a) For i=1 to N: $g_i=\frac{\partial L(y_i,G(x_i))}{\partial G(x_i)}$
 - (b) Fit decision tree G_m to data $\langle x_i, -\nu \cdot g_i \rangle_{i=1}^N$
 - (c) Update $G(x) \leftarrow G(x) + G_m(x)$
- 3. Output final prediction G(x)

Each of these lines is basically one line in Python (using a tree building library)

Gradient Boosting: Plugging in Squared Error Loss

 Plugging in squared error loss to our gradient function, we get a familiar result:

$$g_i = \frac{\partial L(y_i, G(x_i))}{\partial G(x_i)}$$
$$= \frac{\partial \frac{1}{2}(y_i - G(x_i))^2}{\partial G(x_i)}$$
$$= -(y_i - G(x_i))$$

Gradient Boosting: Plugging in Squared Error Loss

 Plugging in squared error loss to our gradient function, we get a familiar result:

$$g_i = \frac{\partial L(y_i, G(x_i))}{\partial G(x_i)}$$
$$= \frac{\partial \frac{1}{2}(y_i - G(x_i))^2}{\partial G(x_i)}$$
$$= -(y_i - G(x_i))$$

- ightarrow Doing a step w.r.t. the negative gradient: Fit a submodel with the previous model's residuals $y_i-G(x_i)$ as targets.
 - Review: why do we use the *negative* gradient?



Gradient Tree Boosting with L2 Error

- 1. Initialize G = best constant prediction for y.
- 2. For m=1 to M
 - (a) For i = 1 to N: $r_i = y_i G(x_i)$
 - (b) Fit decision tree G_m to data $\langle x_i, -\nu \cdot r_i \rangle_{i=1}^N$
 - (c) Update $G(x) \leftarrow G(x) + G_m(x)$
- 3. Output final prediction G(x)
 - Computationally very simple!
- This is related to forward stagewise additive modelling, which fits an additive model by greedily fitting one component at a time

Gradient Boosting: Plugging in Absolute Error

 Plugging in absolute error loss to our gradient function, we get another effective algorithm:

$$g_i = \frac{\partial L(y_i, G(x_i))}{\partial G(x_i)}$$

$$= \frac{\partial |y_i - G(x_i)|}{\partial G(x_i)}$$

$$= \operatorname{sign}(y_i - G(x_i))$$

Gradient Boosting: Plugging in Absolute Error

 Plugging in absolute error loss to our gradient function, we get another effective algorithm:

$$\begin{array}{lcl} g_i & = & \dfrac{\partial L\left(y_i,G(x_i)\right)}{\partial G(x_i)} \\ & = & \dfrac{\partial |y_i - G(x_i)|}{\partial G(x_i)} \\ & = & \mathrm{sign}(y_i - G(x_i)) \end{array}$$

Review: when would you expect this to perform better than squared

The link between Gradient Boosting and Adaboost

• What if we plug in the exponential loss function $L(y_i, G(x_i)) = \exp(-y_i \times G(x_i))$?

The link between Gradient Boosting and Adaboost

- What if we plug in the exponential loss function $L(y_i, G(x_i)) = \exp(-y_i \times G(x_i))$?
- It turns out that we recover the Adaboost algorithm!
 - The optimal G_m minimizes weighted error:

$$G_m = \arg\min_{G} \sum_{i=1}^{N} w_i^{(m)} \mathbb{I}(y_i \neq G(x_i))$$

• Reintroduce a model weight α_m as in Adaboost:

$$\alpha_m = \log \frac{1 - err_m}{err_m}$$

The weight update rule is as in Adaboost:

$$w_i^{(m+1)} \propto w_i^{(m)} \cdot \exp(\alpha_m \mathbb{I}(y_i \neq G_m(x_i)))$$

• (More info on ILIAS; these details will not be examinable)

• Recall our formal definition of a tree $G(x_i; \theta)$, where:

$$\theta = \langle \underbrace{\{R_1, \dots, R_J\}}_{\text{leaf regions}}, \underbrace{\{w_1, \dots, w_J\}}_{\text{leaf scores}} \rangle$$

• Recall our formal definition of a tree $G(x_i; \theta)$, where:

$$\theta = \langle \underbrace{\{R_1, \dots, R_J\}}_{\text{leaf regions}}, \underbrace{\{w_1, \dots, w_J\}}_{\text{leaf scores}} \rangle$$

- ullet We can impose a complexity penalty Ω on each submodel G_m
 - hyperparameters γ and λ penalise tree complexity J and leaf score magnitude $\|\mathbf{w}_m\|$ respectively:

$$\Omega(G_m) = \gamma J_m + \frac{1}{2} \lambda \|\mathbf{w}_m\|_2^2$$

• Recall our formal definition of a tree $G(x_i; \theta)$, where:

$$\theta = \langle \underbrace{\{R_1, \dots, R_J\}}_{\text{leaf regions}}, \underbrace{\{w_1, \dots, w_J\}}_{\text{leaf scores}} \rangle$$

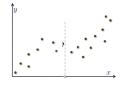
- ullet We can impose a complexity penalty Ω on each submodel G_m
 - hyperparameters γ and λ penalise tree complexity J and leaf score magnitude $\|\mathbf{w}_m\|$ respectively:

$$\Omega(G_m) = \gamma J_m + \frac{1}{2} \lambda \|\mathbf{w}_m\|_2^2$$

• Our method for fitting each submodel then becomes:

$$\theta_m = \underset{\theta}{\operatorname{arg min}} \left[\sum_{i=1}^{N} L(-\nu \cdot g_i, G(x_i; \theta)) + \Omega(G_m) \right]$$

- Suppose we have a prior belief that:
 - there should be few divisions along the axes of our input space . . .
 - ... but that these divisions should separate highly different samples



- Suppose we have a prior belief that:
 - there should be few divisions along the axes of our input space . . .
 - ... but that these divisions should separate highly different samples



• What would be an appropriate hyperparameter setting?

$$\Omega(G_m) = \gamma J_m + \frac{1}{2} \lambda \|\mathbf{w}_m\|_2^2$$

- \bigstar High γ , High λ \bigstar High γ , Low λ \bigstar Low γ , Low λ
- Tangermann, Hutter & Lindauer

Summary by learning goals

Having heard this lecture, you can now . . .

- explain the principles of boosting, and how it differs from bagging
- describe the steps of the AdaBoost algorithm
- describe the steps of the gradient boosting approach
- Explain the relationship between gradient boosting, gradient descent, and Adaboost
- Describe the role of shrinkage and regularisation in gradient boosting

Further Reading

- Main source: Hastie, Tibshirani and Friedman
 - Chapter 10: Boosting and Additive Trees
- Wikipedia article on boosting
- Specialized literature
 - Schapire: A boosting tutorial www.cs.princeton.edu/~schapire
 - Meir and Raetsch, 2003: An introduction to boosting
 - Raetsch: Tutorial at MLSS 2003



Preview of Assignment 9

In the $9^{\rm th}$ assignment, you will

- Implement the AdaBoost algorithm
- Implement the gradient boosting algorithm