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Divide b.s by $y^{\frac{1}{2}}$, we get

$$\frac{dy}{dx} + y = y^{-\frac{1}{2}} \dots \textcircled{i}$$

$$h = -\frac{1}{2}$$

$$v = y^{1-x}$$

$$v = y^{1-\left(-\frac{1}{2}\right)}$$

$$v = y^{1+\frac{1}{2}}$$

$$v = y^{\frac{3}{2}}$$

$$\cancel{y} \quad y = v^{\frac{2}{3}}$$

$$\frac{dy}{dx} = \frac{2}{3} v^{\frac{1}{3}} \frac{dv}{dx}$$

put in \textcircled{i}

$$\frac{2}{3} v^{\frac{1}{3}} \frac{dv}{dx} + v^{\frac{2}{3}} = \left(v^{\frac{2}{3}}\right)^{-\frac{1}{2}}$$

$$\frac{2}{3} v^{\frac{1}{3}} \frac{dv}{dx} + v^{\frac{2}{3}} = v^{\frac{1}{3}}$$

$$\text{Mult by } \frac{3}{2} v^{\frac{1}{3}}$$

$$\left(\frac{2}{3} v^{\frac{1}{3}} \frac{dv}{dx}\right) \left(\frac{3}{2} v^{\frac{1}{3}}\right) + \left(v^{\frac{2}{3}}\right) \left(\frac{3}{2} v^{\frac{1}{3}}\right) = \left(v^{\frac{1}{3}}\right) \left(\frac{3}{2} v^{\frac{1}{3}}\right)$$

$$\frac{dv}{dx} + \frac{3v}{2} = \frac{3}{2}$$

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$$1 - v = \frac{1}{e^{\frac{3}{4}x^2}}$$

$$v = 1 + \frac{1}{e^{\frac{3}{4}x^2}}$$

put $v = y^{\frac{8}{3}}$ we get

$$y^{\frac{8}{3}} = 1 + \frac{1}{e^{\frac{3}{4}x^2}}$$

$$y = \left(1 + \frac{1}{e^{\frac{3}{4}x^2}} \right)^{\frac{3}{8}}$$

$$y(0) = 4$$

$$4 = \left(1 + \frac{1}{e^{\frac{3}{4}(0)^2}} \right)^{\frac{3}{8}}$$

$$4 = \left(1 + \frac{1}{C} \right)^{\frac{3}{8}}$$

$$(4)^{\frac{8}{3}} = 1 + \frac{1}{C}$$

$$8 = 1 + \frac{1}{C}$$

$$8 - 1 = \frac{1}{C}$$

$$7 = \frac{1}{C}$$

$$C = \frac{1}{7}$$

Solution to given

IVP is $y = \left(1 + \frac{1}{\frac{1}{7}e^{\frac{3}{4}x^2}} \right)^{\frac{3}{8}}$