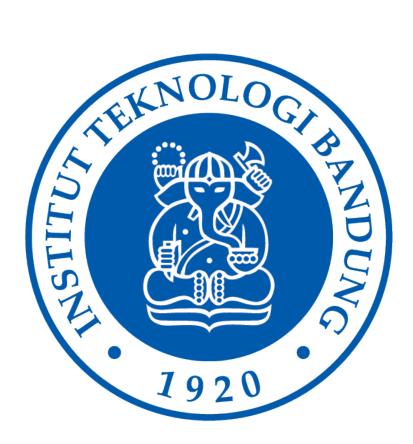
Laporan Tugas Kecil 3 IF2211 Strategi Algoritma Semester II Tahun Akademik 2021/2022

Penyelesaian Persoalan 15-Puzzle dengan Algoritma *Branch and Bound*



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A. Algoritma Branch and Bound untuk menyelesaikan 15-Puzzle

Algoritma yang digunakan untuk menyelesaikan 15-Puzzle menggunakan pendekatan branch and bound. Algoritma branch and bound pada umumnya mirip dengan algoritma breadth-first search (BFS) namun ditambah dengan ketentuan simpul berikutnya yang dicari/diekspansi adalah simpul dengan cost terkecil. Cost dari setiap simpul adalah suatu estimasi ongkos termurah lintasan. Karena cost adalah estimasi, maka nilainya dihitung secara heuristik.

Dalam perhitungan cost simpul 15-Puzzle, digunakan taksiran cost sebagai berikut,

$$\hat{c}(P) = f(P) + \hat{g}(P)$$

dengan $\hat{c}(P)$ adalah cost untuk simpul P, f(P) panjang lintasan dari simpul akar ke P, dan $\hat{g}(P)$ adalah taksiran panjang lintasan terpendek dari P ke simpul solusi dengan akar P yang diestimasikan dengan menghitung jumlah ubin tidak kosong yang tidak terdapat pada susunan akhir.

Implementasi algoritma branch and bround dilakukan dengan membuat sebuah pohon keadaan simpul yang direpresentasikan dengan sebuah kelas yang memiliki atribut konfigurasi puzzle sementara, panjang lintasan dari simpul akar, dan urutan langkahlangkah dari simpul akar. Terdapat pula metode pada kelas untuk menghitung cost dari konfigurasi puzzle dan mengubah posisi ubin kosong. Ubin kosong direpresentasikan dengan angka 0. Simpul-simpul ini kemudian dimasukkan ke sebuah priority queue bawaan dari Python dengan prioritas cost terkecil.

Pendekatan algoritma branch and bound yang digunakan dalam menyelesaikan masalah 15-Puzzle menggunakan taksiran cost seperti pada rumus di atas dan juga menerapkan beberapa teknik heuristik demi mempercepat alur kerja algoritma. Heuristik pertama yang diterapkan adalah setiap pembangkitan simpul baru mempunyai syarat bahwa konfigurasi puzzle tersebut belum pernah dicek sebelumnya. Heuristik kedua adalah dalam pemilihan simpul dengan cost terkecil, bila ada dua atau lebih simpul dengan cost terkecil maka akan dipilih simpul yang dibangkitkan paling akhir sehingga mempunyai kedalaman yang lebih dalam. Alasan diterapkannya heuristik ini agar pohon pencarian simpul tidak mencabang besar dari simpul-simpul dengan kedalaman yang lebih dangkal yang berkemungkinan membuahkan lebih banyak kemungkinan solusi yang baru. Heuristik terakhir adalah pembangkitan simpul anak-anak mempertimbangkan langkah sebelumnya yang pernah dilakukan sehingga langkah tidak mengembalikan konfigurasi puzzle kembali ke langkah sebelumnya. Misalnya bila pada langkah sebelumnya

memindahkan ubin kosong ke atas, maka pada langkah ini tidak boleh memindahkan ubin kosong ke bawah.

Karena penentuan langkah-langkah untuk satu solusi saja membutuhkan waktu yang cukup lama karena ketidakefisienan *cost* dalam menentukan simpul terbaik untuk diekspansikan, maka pencarian solusi berhenti ketika satu solusi telah dihasilkan.

Secara garis besar, langkah algoritma yang diimplementasikan adalah sebagai berikut:

- 1. Masukkan simpul akar ke antrean *priority queue*. Bila simpul akar adalah solusi (matriks terurut 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, ubin kosong), berhenti.
- 2. Jika *priority queue* kosong, berhenti.
- 3. Jika *priority queue* tidak kosong, pilih simpul *i* dengan *cost* terkecil. Bila terdapat beberapa simpul dengan *cost* terkecil, pilih simpul yang dibangkitkan paling akhir.
- 4. Jika simpul *i* adalah solusi, berhenti.
- 5. Jika simpul *i* bukan simpul solusi, bangkitkan semua anak-anak untuk langkah atas, bawah, kiri, dan kanan dengan syarat heuristik konfigurasi puzzle belum pernah dicek dan langkah tidak kebalikan dari langkah sebelumnya, dan juga letak ubin kosong memperbolehkan dilakukannya langkah tersebut. Bila simpul *i* tidak mempunyai anak, kembali ke langkah 2.
- 6. Untuk setiap anak *i*, hitung *cost*-nya dan masukkan anak-anak tersebut ke *priority queue* dengan mencatat *cost* dan urutan dibangkitkannya.

B. Checklist Keberjalanan Program

Poin	Ya	Tidak
1. Program berhasil dikompilasi	V	
2. Program berhasil <i>running</i>	V	
3. Program dapat menerima input dan menuliskan output	V	
4. Luaran sudah benar untuk semua data uji	V	
5. Bonus dibuat		V

C. Kode Program dalam Python

Program ditulis pada bahasa Python secara modular, terdiri atas lima modul serta satu file *main.py* pada folder *src*.

1. Algorithm.py

Berisi fungsi algoritma *branch and bound* 15-Puzzle yang membuat sebuah *priority queue* dari konfigurasi puzzle awal yang sudah dibangkitkan secara acak atau melalui file. Fungsi algoritma tersebut mengembalikan simpul solusi yang berisi langkah-langkah penyelesaian dan banyaknya simpul yang dibangkitkan pada algoritma.

```
import numpy as np
from queue import PriorityQueue
from PuzzleNode import *
def Algorithm(Puzzle):
   checkedMatrics = {}
    # Add root puzzle config to checkedMatrics
   checkedMatrics[Puzzle.tobytes()] = True
   # counter to prioritize innermost node
   priority = 0
   q = PriorityQueue()
    rootNode = PuzzleNode(Puzzle, 0, [0])
   q.put((rootNode.getCost(), priority, rootNode))
    raisedNodes = 1
    # Initialize matrix to check for solution
    solutionMatrix = np.matrix([[1,2,3,4], [5,6,7,8], [9,10,11,12],
[13,14,15,0]])
    foundSolution = False
   while not q.empty() and not foundSolution:
        # Get innermost node with lowest cost
       currentNode = q.get()[2]
       lastMove = currentNode.getLastMove()
       # Check if node puzzle is solution
        if (currentNode.comparePuzzle(solutionMatrix)):
            foundSolution = True
```

```
# MOVE ENUMERATION
            # 0 NONE
                       (note. placeholder for first move)
                       // NEXT MOVE DOWN
            # 2 LEFT
            # 3 DOWN
                       // NEXT MOVE UP
            # NEXT MOVE DOWN
            if lastMove != 1 and currentNode.getRowNull() < 3:</pre>
                newPuzzle = currentNode.getPuzzle().copy()
                newNode = PuzzleNode(newPuzzle, currentNode.getDistance()+1,
currentNode.getMoves().copy())
                newNode.moveDown()
                newNode.addMove(3)
                # Add node if puzzle config has not been checked
                if newNode.getPuzzle().tobytes() not in checkedMatrics:
                    checkedMatrics[newNode.getPuzzle().tobytes()] = True
                    raisedNodes += 1
                    priority -= 1
                    q.put((newNode.getCost(), priority, newNode))
            # NEXT MOVE RIGHT
            if lastMove != 2 and currentNode.getColNull() < 3:</pre>
                newPuzzle = currentNode.getPuzzle().copy()
                newNode = PuzzleNode(newPuzzle, currentNode.getDistance()+1,
currentNode.getMoves().copy())
                newNode.moveRight()
                newNode.addMove(4)
                if newNode.getPuzzle().tobytes() not in checkedMatrics:
                    checkedMatrics[newNode.getPuzzle().tobytes()] = True
                    raisedNodes += 1
                    priority -= 1
                    q.put((newNode.getCost(), priority, newNode))
            # NEXT MOVE UP
            if lastMove != 3 and currentNode.getRowNull() > 0:
                newPuzzle = currentNode.getPuzzle().copy()
                newNode = PuzzleNode(newPuzzle, currentNode.getDistance()+1,
currentNode.getMoves().copy())
                newNode.moveUp()
                newNode.addMove(1)
                if newNode.getPuzzle().tobytes() not in checkedMatrics:
```

```
checkedMatrics[newNode.getPuzzle().tobytes()] = True
                    raisedNodes += 1
                    priority -= 1
                    q.put((newNode.getCost(), priority, newNode))
            # NEXT MOVE LEFT
           if lastMove != 4 and currentNode.getColNull() > 0:
               newPuzzle = currentNode.getPuzzle().copy()
                newNode = PuzzleNode(newPuzzle, currentNode.getDistance()+1,
currentNode.getMoves().copy())
               newNode.moveLeft()
                newNode.addMove(2)
                if newNode.getPuzzle().tobytes() not in checkedMatrics:
                    checkedMatrics[newNode.getPuzzle().tobytes()] = True
                    raisedNodes += 1
                    priority -= 1
                    q.put((newNode.getCost(), priority, newNode))
    currentNode.setMoves(currentNode.getMoves()[1::])
    return currentNode, raisedNodes
```

2. PuzzleNode.py

Berisi kelas PuzzleNode untuk merepresentasikan setiap simpul pada pencarian solusi algoritma. Setiap simpul memegang atribut konfigurasi puzzle, jarak dari root, dan langkah-langkah sebelumnya. Kelas mempunyai metode getter/setter yang diperlukan, penghitung cost dari ubin yang tidak di posisi benar, penggerak atas/bawah/kiri/kanan ubin kosong, pembanding konfigurasi puzzle, dan metode pendukung lainnya.

```
import numpy as np
from PuzzleGeneration import *

class PuzzleNode:
    """Class to represent a node in tree.
    A node contains the puzzle configuraton,
    distance from root, and list of moves"""

def __init__(self, puzzle, distance, moves):
    """User-defined constructor for PuzzleNode class"""
    self.puzzle = puzzle
    self.distance = distance
    self.moves = moves

def getPuzzle(self):
```

```
"""Getter for puzzle"""
    return self.puzzle
def getDistance(self):
    """Getter for distance from root"""
   return self.distance
def getMoves(self):
   """Getter for list of moves"""
   return self.moves
def setMoves(self, newMove):
    """Set for list of moves"""
   self.moves = newMove
def getLastMove(self):
    """Getter for last move"""
   return (self.moves)[-1]
def getCost(self):
    """Returns cost of a node using c(i) = f(i) + g(i)
   where c(i) is cost of node i, f(i) is cost to reach
   node i from root, and g(i) is total of non-empty tile
   that is in wrong place"""
   cost = self.distance
    for i in range(4):
        for j in range(4):
            if i*4+j+1 != self.puzzle[i, j] and self.puzzle[i, j] != 0:
                cost += 1
    return cost
def getRowNull(self):
    """Getter for row of empty tile"""
   row0, col0 = np.where(self.puzzle == 0)
    return row0
def getColNull(self):
    """Getter for column of empty tile"""
    row0, col0 = np.where(self.puzzle == 0)
    return col0
def addMove(self, lastMove):
    """Add move to list of moves"""
   self.moves.append(lastMove)
def moveDown(self):
    """Method to move empty tile down"""
   row = self.getRowNull()
```

```
col = self.getColNull()
    self.puzzle[row, col] = self.puzzle[row+1, col]
    self.puzzle[row+1, col] = 0
def moveRight(self):
    """Method to move empty tile right"""
   row = self.getRowNull()
   col = self.getColNull()
   self.puzzle[row, col] = self.puzzle[row, col+1]
    self.puzzle[row, col+1] = 0
def moveUp(self):
   """Method to move empty tile up"""
   row = self.getRowNull()
   col = self.getColNull()
   self.puzzle[row, col] = self.puzzle[row-1, col]
   self.puzzle[row-1, col] = 0
def moveLeft(self):
   """Method to move empty tile left"""
   row = self.getRowNull()
   col = self.getColNull()
   self.puzzle[row, col] = self.puzzle[row, col-1]
    self.puzzle[row, col-1] = 0
def comparePuzzle(self, matrix):
    """Method to check if puzzle config is the same as matrix
   using binary comparison"""
   return self.puzzle.tobytes() == matrix.tobytes()
def printNode(self):
   print("Puzzle:")
   PrintPuzzle(self.puzzle)
   print(f"Cost: {self.getCost()}")
    print(f"Distance: {self.distance}")
    print(f"Row: {self.getRowNull()} Col: {self.getColNull()}")
    print(f"Moves: {self.moves}")
   print()
```

3. Prerequisites.pv

Berisi fungsi-fungsi yang menghitung Kurang(i) untuk setiap ubin i pada posisi awal, mencetak Kurang(i) untuk setiap ubin i tersebut, dan menghitung $\sum Kurang(i) + X$.

```
import numpy as np

def ArrayKurangI(puzzle):
```

```
"""Returns an array of index 0-15 to calculate Kurang(i)
    FlattenedPuzzle = (np.asarray(puzzle)).flatten()
    lengthFlattened = len(FlattenedPuzzle)
    KurangI = [0 for i in range(lengthFlattened)]
    # calculte sum of Kurang(i) for each i
    for i in range(lengthFlattened):
        # if i = 0, assume all next elements add up to Kurang(0)
        if FlattenedPuzzle[i] == 0:
            KurangI[FlattenedPuzzle[i]] += lengthFlattened - (i + 1)
        for j in range(i+1, lengthFlattened):
            if FlattenedPuzzle[j] < FlattenedPuzzle[i] and FlattenedPuzzle[j]</pre>
!= 0:
                KurangI[FlattenedPuzzle[i]] += 1
    return KurangI
def PrintTileKurangI(arr):
    """Print Kurang(i) for each i tile"""
    for i in range(1, len(arr)):
        print(f"Tile {i}: {arr[i]}")
    print(f"Empty tile: {arr[0]}")
def KurangIX(puzzle, arrKurangI):
    """calculate X based on 0 position"""
    if (np.where(puzzle == 0)[0] + np.where(puzzle == 0)[1]) % 2 == 1:
        return 1
    else:
        return 0
```

4. PuzzleGeneration.py

Berisi fungsi untuk membuat posisi awal puzzle dari acak atau dari file dan juga prosedur untuk mengecek apakah puzzle valid formatnya dan mencetak puzzle. Pengecek kevalidan puzzle akan *raise* error bila ada ketidakvalidan yang akan di*catch* oleh program utama.

```
import random
from Exception import *

def CheckValidPuzzle(puzzle):
    """Check if a puzzle is considered valid"""

# Check if rows of puzzle are 4
    if len(puzzle) != 4:
```

```
raise Shape44Error
    # Check if length of each row is 4
    for i in range(4):
        if len(puzzle[i]) != 4:
            raise Shape44Error
    # Check if length of unique elements is 16
    if len(list(set(i for j in puzzle for i in j))) != 16:
        raise Shape44Error
    for i in range(4):
        for j in range(4):
            if not 0 <= puzzle[i][j] <= 15:</pre>
                raise Shape44Error
def GeneratePuzzle():
    """Generate a random puzzle"""
    Puzzle = [[0 for j in range(4)] for i in range(4)]
    Elements = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15]
    for i in range(4):
        for j in range(4):
            Puzzle[i][j] = random.choice(Elements)
            Elements.remove(Puzzle[i][j])
    return Puzzle
def OpenPuzzle(mainpath, filename):
    """Open a puzzle from a file in test folder"""
    with open(mainpath + filename, 'r') as f:
            Puzzle = [[int(num) for num in line.split()] for line in f]
    return Puzzle
def PrintPuzzle(puzzle):
    """Print puzzle with padding for 1 or 2 digits"""
    print("======")
    for i in range(4):
        for j in range(4):
            if puzzle[i, j] == 0:
                print(" - ", end="")
            elif puzzle[i, j] < 10:</pre>
                print(f" {puzzle[i, j]} ", end="")
                print(f"{puzzle[i, j]} ", end="")
        print()
    print("=======")
```

5. Exception.py

Berisi kelas-kelas turunan *exception* untuk mencetak pesan bila terjadi error. Kelas-kelas tersebut digunakan untuk mengatasi error-error yang terdapat terutama pada pembangkitan puzzle dan juga pada input pengguna.

```
class Error(Exception):
    """Base class for other exceptions"""
    pass

class SelectionError(Error):
    """Raised when the user selects an invalid option"""
    pass

class Shape44Error(Error):
    """Raised when the puzzle is not a 4x4 matrix"""
    pass

class NotReachableError(Error):
    """Raised when the puzzle solution is not reachable"""
    pass
```

6. Main.py

File utama pada program memiliki urutan prosedur:

- 1. Membangkitkan puzzle sesuai pilihan pengguna secara acak atau input dari file
- 2. Menampilkan posisi awal puzzle
- 3. Menghitung nilai dari Kurang(i) setiap ubin i dan $\sum Kurang(i) + X$, mencetaknya, dan menentukan apakah puzzle dapat diselesaikan.
- 4. Menerapkan algoritma branch and bound untuk posisi awal puzzle
- 5. Menghitung waktu yang dibutuhkan untuk menjalankan algoritma
- 6. Mencetak langkah-langkah solusi, waktu yang dibutuhkan, dan jumlah simpul yang dibangkitkan.

```
import time
import numpy as np
from os.path import dirname, abspath

from Exception import *
from Prerequisites import *
from PuzzleGeneration import *
from PuzzleNode import *
from Algorithm import *
```

```
WELCOME TO AFAN'S 15-PUZZLE SOLVER!")
    print("
    print("========"")
    print("Made by: 13520023 - Ahmad Alfani Handoyo")
    print("Assume: Empty tile is represented with a 0\n")
   print("Generate starting puzzle position:\n1. Randomly generated puzzle\n2.
Input from file")
    choose = int(input("Choose 1 or 2: "))
   # Generate a random puzzle
   if choose == 1:
       Puzzle = GeneratePuzzle()
   elif choose == 2:
       filename = input("\nInput filename of puzzle: ")
       testPath = dirname((dirname(abspath(__file__)))) + "/test/"
       Puzzle = OpenPuzzle(testPath, filename)
       CheckValidPuzzle(Puzzle)
       raise SelectionError
    Puzzle = np.matrix(Puzzle)
    startingPuzzle = Puzzle.copy()
   print("\nSTARTING PUZZLE CONFIGURATION:")
    PrintPuzzle(Puzzle)
    # Calculate Kurang(i) for each i tile
    startTime = time.time()
   print("\nKurang(i):")
    KurangArr = ArrayKurangI(Puzzle)
    PrintTileKurangI(KurangArr)
   print("\nSum of Kurang(i) + X: ")
    Reachability = np.sum(KurangArr) + KurangIX(Puzzle, KurangArr)
   print(Reachability)
   # Reachable if sum of kurang(i) + x is even
    if Reachability % 2 != 0:
       raise NotReachableError
   print("\nPUZZLE SOLUTION IS REACHABLE!")
    print("Calculating solution...\n")
    solutionNode, raisedNodes = Algorithm(Puzzle)
    timeTaken = time.time() - startTime
    solutionMoves = solutionNode.getMoves()
```

```
print(f"SOLUTION FOUND IN {len(solutionMoves)} STEPS!\n")
print("Show steps to reach solution?")
print("1. Show all steps at once")
print("2. Show every 10 steps")
print("3. Show every 5 steps")
print("4. Show every step")
print("5. Don't show")
choose = int(input("Choose 1, 2, 3, 4 or 5: "))
if 1 <= choose <= 4:
   if choose == 1:
        steps = len(solutionMoves)
    elif choose == 2:
        steps = 10
    elif choose == 3:
        steps = 5
   elif choose == 4:
        steps = 1
   print("\n=======")
   print(" SOLUTION")
    print("=======")
   SolutionPrint = PuzzleNode(startingPuzzle,0,[0])
   moveEnum = ["NONE", "UP", "LEFT", "DOWN", "RIGHT"]
    print("\nSTART")
   PrintPuzzle(SolutionPrint.getPuzzle())
    for i in range(len(solutionMoves)):
        if i % steps == 0 and i != 0:
            input("\nPress enter to continue...")
        currentMove = solutionMoves[i]
        if currentMove == 1:
            SolutionPrint.moveUp()
        elif currentMove == 2:
            SolutionPrint.moveLeft()
        elif currentMove == 3:
            SolutionPrint.moveDown()
        elif currentMove == 4:
            SolutionPrint.moveRight()
        print(f"\nSTEP {i+1}")
        PrintPuzzle(SolutionPrint.getPuzzle())
        print(f"MOVE: {moveEnum[currentMove]}")
elif choose == 5:
   raise SelectionError
```

```
print(f"\nAlgorithm runtime: {timeTaken} seconds")
   print(f"Raised nodes: {raisedNodes}")
except ValueError:
   print("\nPlease input a number!")
except SelectionError:
   print("\nPlease input an allowed selection!")
except Shape44Error:
   print("\nPlease input a unique 4x4 puzzle with values 0-15!")
except FileNotFoundError:
   print("\nPuzzle file not found!")
except KeyboardInterrupt:
   print(f"Keyboard Interrupt!")
except NotReachableError:
    print("\nPUZZLE SOLUTION IS NOT REACHABLE!")
   print(f"Algorithm runtime: {time.time() - startTime} seconds")
print("\n==========")
print(" THANK YOU FOR USING AFAN'S 15-PUZZLE SOLVER!")
print("========="")
```

D. Berkas Teks Contoh Instansiasi 5 Buah Persoalan 15-Puzzle

Pembangkitan konfigurasi awal puzzle dapat secara acak atau melalui input file. Bila melalui input file, maka konfigurasi awal puzzle dituliskan pada file berformat .txt dan dimasukkan ke folder *test*. Ubin kosong direpresentasikan dengan angka 0.

Dalam menguji coba program terdapat 5 *test case*. Berikut isi teks 5 *test case* tersebut sebagai contoh cara instansiasi input persoalan 15-Puzzle.

1. unsolvable1.txt

2. unsolvable2.txt

8 4 10 11
9 7 15 13
2613
12 14 0 5

3. solvable1_15.txt

4. solvable2 20.txt

5. solvable3 25.txt

E. Screenshot Input dan Output Program

Program dijalankan dengan menjalankan *Main.py* pada folder *src*. Berikut merupakan input dan output pengujian 5 *test case* yang terdapat di atas.

1. Kasus tidak dapat diselesaikan 1 (unsolvable1.txt)

```
### Tile 9: 3

### WELCOME TO AFAN'S 15-PUZZLE SOLVER!

### Build 9

### Tile 10: 9

### Tile 10: 9

### Tile 10: 9

### Tile 11: 3

### Made by: 13520023 - Ahmad Alfani Handoyo

### Assume: Empty tile is represented with a 0

### Assume: Empty tile is represented with a 0

### Assume: Empty tile is represented with a 0

### Assume: Empty tile is represented with a 0

### Tile 12: 1

### Tile 13: 1

### Tile 14: 7

### Generate starting puzzle position:

### Kurang(i):

### Tile 15: 5

### Empty tile: 5

### Line 1: 0

### Choose 1 or 2: 2

### Tile 3: 2

### Tile 4: 2

### Tile 5: 0

### Tile 6: 1

### PUZZLE SOLUTION IS NOT REACHABLE!

### STARTING PUZZLE CONFIGURATION:

### Tile 8: 4
```

```
THANK YOU FOR USING AFAN'S 15-PUZZLE SOLVER!
```

2. Kasus tidak dapat diselesaikan 2 (unsolvable2.txt)

```
STARTING PUZZLE CONFIGURATION:
                                                                                                  Tile 5: 0
                                                 8 4 10 11
                                                                                                  Tile 7: 5
                                                 9 7 15 13
                                                                                                  Tile 8: 7
                                                 2 6 1 3
Assume: Empty tile is represented with a 0
                                                                                                 Tile 9: 6
                                                12 14 - 5
                                                                                                 Tile 10: 7
Generate starting puzzle position:
                                                                                                 Tile 11: 7
1. Randomly generated puzzle
                                                                                                 Tile 12: 1
                                                Kurang(i):
2. Input from file
                                                                                                 Tile 13: 6
                                                Tile 1: 0
Choose 1 or 2: 2
                                                                                                 Tile 14: 1
                                                Tile 2: 1
                                                                                                 Tile 15: 8
                                                 Tile 3: 0
Input filename of puzzle: unsolvable2.txt
```

Sum of Kurang(i) + X:

57

PUZZLE SOLUTION IS NOT REACHABLE!
Algorithm runtime: 0.005002021789550781 seconds

THANK YOU FOR USING AFAN'S 15-PUZZLE SOLVER!

3. Kasus dapat diselesaikan, 15 langkah (solvable1 15.txt)

```
Empty tile: 1

Sum of Kurang(i) + X:

2. Show every 10 steps
3. Show every 5 steps
4. Show every step
5. Don't show
Calculating solution...

Choose 1, 2, 3, 4 or 5: 1

SOLUTION FOUND IN 15 STEPS!

Show steps to reach solution?

1. Show all steps at once
```

START	STEP 2	STEP 4
		=======
	5 1 7 3	5 1 7 3
5 1 7 3	9 2 6 4	9 2 6 4
9 2 6 4	10 11 8 -	10 - 11 8
10 11 8 12	13 14 15 12	13 14 15 12
13 14 - 15		
	MOVE: UP	MOVE: LEFT
STEP 1	STEP 3	STEP 5
	========	
5 1 7 3	5 1 7 3	5 1 7 3
9 2 6 4	9 2 6 4	9 2 6 4
10 11 8 12	10 11 - 8	- 10 11 8
13 14 15 -	13 14 15 12	13 14 15 12
========		
MOVE: RIGHT	MOVE: LEFT	MOVE: LEFT
STEP 6		CTC 40
	STEP 8	STEP 10
5 1 7 3	1 - 7 3	1 2 7 3
- 2 6 4	5 2 6 4	5 6 - 4
9 10 11 8	9 10 11 8	9 10 11 8
13 14 15 12	13 14 15 12	13 14 15 12
=======	========	=======
MOVE: UP	MOVE: RIGHT	MOVE: RIGHT
CTCD 7		
STEP 7	STEP 9	STEP 11
	========	
- 1 7 3 5 2 6 4	1 2 7 3	1 2 - 3
	5 - 6 4	5 6 7 4
9 10 11 8	9 10 11 8	9 10 11 8
13 14 15 12	13 14 15 12	13 14 15 12
	========	=======
MOVE: UP	MOVE: DOWN	MOVE: UP
STEP 12	STEP 14	
=========		
1 2 3 -	1 2 3 4	
5 6 7 4	5 6 7 8	
9 10 11 8	9 10 11 -	
13 14 15 12	13 14 15 12	
========	=========	
MOVE: RIGHT	MOVE: DOWN	
STEP 13	STEP 15	
========	========	
1 2 3 4	1 2 3 4	Algorithm runtime: 0.011993885040283203 seconds
5 6 7 -	5 6 7 8	Algorithm runtime: 0.011993885040283203 seconds Raised nodes: 117
9 10 11 8	9 10 11 12	Naisea Houes. 117
13 14 15 12	13 14 15 -	
=========	=========	THANK YOU FOR HETHE AFAN'S 15 DITTIE COLVERY
		THANK YOU FOR USING AFAN'S 15-PUZZLE SOLVER!
MOVE: DOWN	MOVE: DOWN	

4. Kasus dapat diselesaikan, 20 langkah (solvable2_20.txt)

	STARTING PUZZLE CONFIGURATION:	Tile 4: 1
WELCOME TO AFAN'S 15-PUZZLE SOLVER!		Tile 5: 0
	3 2 4 8	Tile 6: 0
Made by: 13520023 - Ahmad Alfani Handoyo	1 - 7 12	Tile 7: 2
Assume: Empty tile is represented with a 0	5 10 6 15	Tile 8: 4
	9 13 11 14	Tile 9: 0
Generate starting puzzle position:		Tile 10: 2
1. Randomly generated puzzle		Tile 11: 0
2. Input from file	Kurang(i):	Tile 12: 5
Choose 1 or 2: 2	Tile 1: 0	Tile 13: 1
	Tile 2: 1	Tile 14: 0
Input filename of puzzle: solvable2_20.txt	Tile 3: 2	Tile 15: 4
Empty tile: 10		
Sum of Kurang(i) + X:	2. Show every 10 steps	
32	3. Show every 5 steps	
	4. Show every step	
PUZZLE SOLUTION IS REACHABLE!	5. Don't show	
Calculating solution	Choose 1, 2, 3, 4 or 5: 1	
SOLUTION FOUND IN 20 STEPS!	==========	
SULUTION FOUND IN 20 STEPS!		
SOUNTION FOUND IN SO SIERS!	SOLUTION	
Show steps to reach solution?		
	SOLUTION	
Show steps to reach solution? 1. Show all steps at once	SOLUTION	STEP 4
Show steps to reach solution?	SOLUTION STEP 2	STEP 4
Show steps to reach solution? 1. Show all steps at once	SOLUTION ===================================	========
Show steps to reach solution? 1. Show all steps at once START ==================================	STEP 2	1 3 4 8
Show steps to reach solution? 1. Show all steps at once START ==================================	STEP 2	1 3 4 8 5 2 7 12
Show steps to reach solution? 1. Show all steps at once START 3 2 4 8 1 - 7 12 5 10 6 15	SOLUTION	1 3 4 8 5 2 7 12 - 10 6 15
Show steps to reach solution? 1. Show all steps at once START	SOLUTION	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START 3 2 4 8 1 - 7 12 5 10 6 15	SOLUTION ===================================	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START	SOLUTION	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START	STEP 2	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START	STEP 2	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START	STEP 2	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START 3 2 4 8 1 - 7 12 5 10 6 15 9 13 11 14 STEP 1 STEP 1	SOLUTION	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START 3 2 4 8 1 - 7 12 5 10 6 15 9 13 11 14 STEP 1 3 - 4 8	SOLUTION	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14 MOVE: DOWN STEP 5 1 3 4 8 5 2 7 12
Show steps to reach solution? 1. Show all steps at once START 3 2 4 8 1 - 7 12 5 10 6 15 9 13 11 14 STEP 1 3 - 4 8 1 2 7 12	SOLUTION	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14 MOVE: DOWN STEP 5 1 3 4 8 5 2 7 12 10 - 6 15
Show steps to reach solution? 1. Show all steps at once START 3 2 4 8 1 - 7 12 5 10 6 15 9 13 11 14 STEP 1 3 - 4 8 1 2 7 12 5 10 6 15	STEP 2	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14
Show steps to reach solution? 1. Show all steps at once START	SOLUTION	1 3 4 8 5 2 7 12 - 10 6 15 9 13 11 14 MOVE: DOWN STEP 5 1 3 4 8 5 2 7 12 10 - 6 15

STEP 6	STEP 8	STEP 10
1 3 4 8	1 3 4 8	1 3 4 8
5 2 7 12	5 2 7 12	5 2 7 -
10 6 - 15	10 6 11 15	10 6 11 12
9 13 11 14	9 13 14 -	9 13 14 15
	=======	
MOVE: RIGHT	MOVE: RIGHT	MOVE: UP
STEP 7	STEP 9	STEP 11
	========	
1 3 4 8 5 2 7 12	1 3 4 8	1 3 4 -
10 6 11 15	5 2 7 12	5 2 7 8
9 13 - 14	10 6 11 -	10 6 11 12
9 13 - 14	9 13 14 15	9 13 14 15
MOVE: DOWN	NOVE - UP	======== MOVE: UP
	MOVE: UP	
STEP 12 ========	STEP 14	STEP 16
1 3 - 4		
5 2 7 8	1 2 3 4	1 2 3 4
10 6 11 12	5 - 7 8	5 6 7 8
9 13 14 15	10 6 11 12	- 10 11 12
=========	9 13 14 15	9 13 14 15
MOVE: LEFT		
	MOVE: DOWN	MOVE: LEFT
STEP 13	STEP 15	STEP 17
========	========	========
1 - 3 4	1 2 3 4	1 2 3 4
5 2 7 8	5 6 7 8	5 6 7 8
10 6 11 12	10 - 11 12	9 10 11 12
9 13 14 15	9 13 14 15	- 13 14 15
MOVE: LEFT	MOVE: DOWN	MOVE: DOWN
STEP 18		
1 2 3 4	STEP 20	
5 6 7 8	========	
9 10 11 12	1 2 3 4	
13 - 14 15	5 6 7 8	
	9 10 11 12	
MOVE: RIGHT	13 14 15 -	
STEP 19	MOVE: RIGHT	
1 2 3 4	Algorithm runtime: 0.1179959774017334 seconds	
5 6 7 8	Raised nodes: 1933	
9 10 11 12		
13 14 - 15		
	THANK YOU FOR USING AFAN'S 15-PUZZLE SOLVER!	
MOVE: RIGHT		

5. Kasus dapat diselesaikan, 25 langkah (solvable3 25.txt)

```
STARTING PUZZLE CONFIGURATION:
                                                                                                    Tile 5: 4
     WELCOME TO AFAN'S 15-PUZZLE SOLVER!
                                                                                                    Tile 6: 5
Made by: 13520023 - Ahmad Alfani Handoyo
Assume: Empty tile is represented with a 0
                                                  2 9 14 11
                                                 13 15 10 12
1. Randomly generated puzzle
2. Input from file
                                                 Kurang(i):
                                                 Tile 1: 0
Choose 1 or 2: 2
                                                 Tile 2: 0
Input filename of puzzle: solvable3_25.txt
                                                  5. Don't show
                                                  Choose 1, 2, 3, 4 or 5: 1
PUZZLE SOLUTION IS REACHABLE!
Calculating solution...
SOLUTION FOUND IN 25 STEPS!
Show steps to reach solution?
2. Show every 10 steps
3. Show every 5 steps
STEP 1
                                                 MOVE: DOWN
                                                 STEP 4
                                                                                                   STEP 6
 2 9 14 11
                                                 13 15 10 12
13 15 10 12
                                                                                                   13 15 10 12
MOVE: RIGHT
                                                                                                   MOVE: RIGHT
```

STEP 7	STEP 9	STEP 11
	========	
5 1 3 8	5 1 3 8	5 1 3 8
2 6 4 7	2 6 4 7	2 - 4 7
9 14 - 11	9 14 10 11	9 6 10 11
13 15 10 12	13 - 15 12	13 14 15 12
	=======	
MOVE: RIGHT	MOVE: LEFT	MOVE: UP
STEP 8	STEP 10	STEP 12
	========	
5 1 3 8	5 1 3 8	5 1 3 8
2 6 4 7	2 6 4 7	- 2 4 7
9 14 10 11	9 - 10 11	9 6 10 11
13 15 - 12	13 14 15 12	13 14 15 12
MOVE: DOWN	MOVE: UP	MOVE: LEFT
STEP 13	STEP 15	STEP 17
		========
- 1 3 8	1 3 - 8	1 3 4 8
5 2 4 7	5 2 4 7	5 2 7 -
9 6 10 11	9 6 10 11	9 6 10 11
13 14 15 12	13 14 15 12	13 14 15 12
MOVE: UP	MOVE: RIGHT	MOVE: RIGHT
STEP 14	STEP 16	STEP 18
1 - 3 8	1 3 4 8	1 3 4 -
5 2 4 7	5 2 - 7	5 2 7 8
9 6 10 11	9 6 10 11	9 6 10 11
13 14 15 12	13 14 15 12	13 14 15 12
MOVE: RIGHT	MOVE: DOWN	MOVE: UP
STEP 19	STEP 21	STEP 23
	1 2 3 4	1 2 3 4
	1 2 3 4 5 - 7 8	1 2 3 4 5 6 7 8
1 3 - 4	1 2 3 4 5 - 7 8 9 6 10 11	1 2 3 4
1 3 - 4 5 2 7 8	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8
1 3 - 4 5 2 7 8 9 6 10 11	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12 MOVE: RIGHT STEP 24
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12 MOVE: RIGHT STEP 24 1 2 3 4 5 6 7 8 9 10 11 - 13 14 15 12
1 3 - 4 5 2 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 - 7 8 9 6 10 11 13 14 15 12	1 2 3 4 5 6 7 8 9 10 - 11 13 14 15 12

F. Alamat GitHub Program

Program dapat diunduh pada repository berikut:

 $\underline{https://github.com/blueguy42/15-Puzzle-Algorithm}$