Clustering and Similarity: Retrieving Documents

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Retrieving documents of interest

Document retrieval

- Currently reading article you like

Document retrieval

- Currently reading article you like
- **Goal**: Want to find similar article

Document retrieval

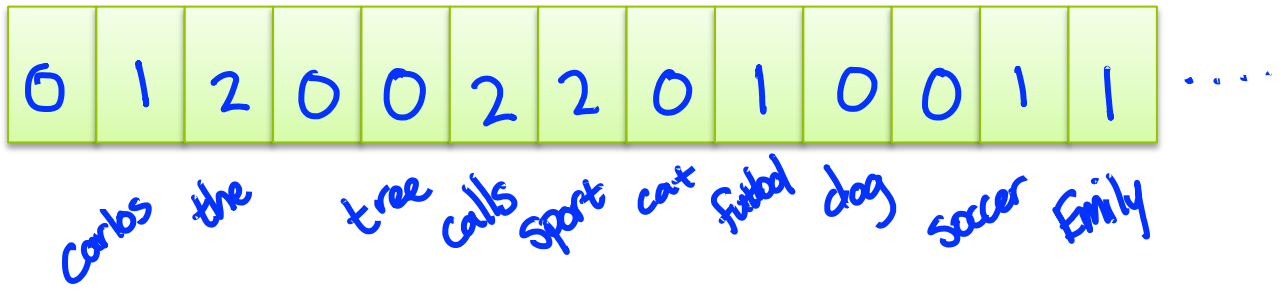
Challenges

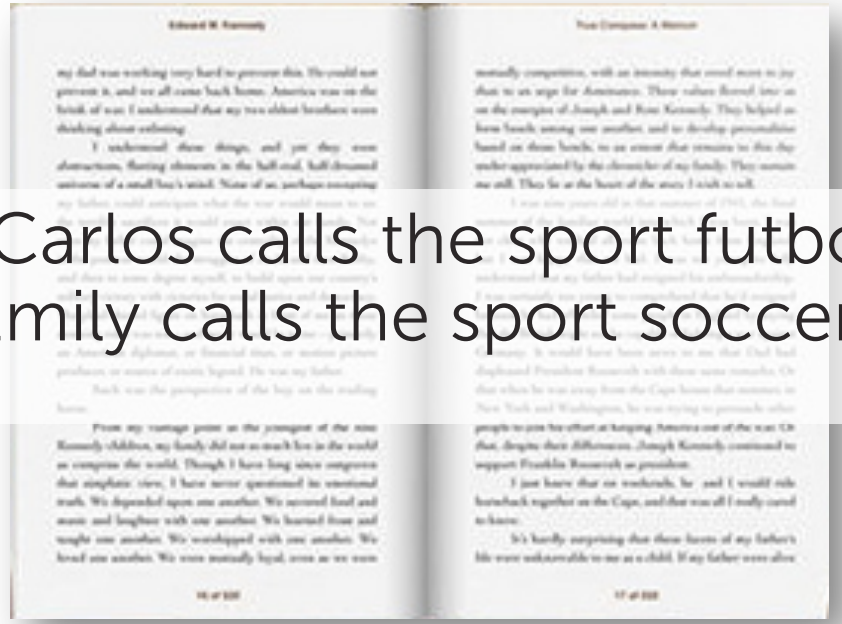
- How do we measure similarity?
- How do we search over articles?

Word count representation for measuring similarity

Word count document representation

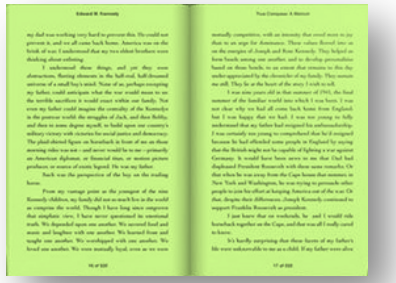
- Bag of words model
  - Ignore order of words
  - Count # of instances of each word in vocabulary





"Carlos calls the sport futbol. Emily calls the sport soccer."

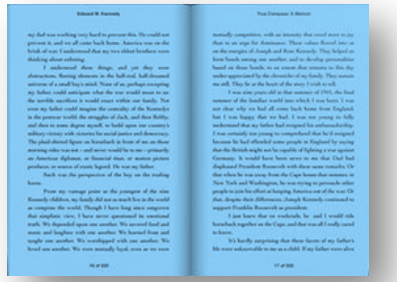
Measuring similarity



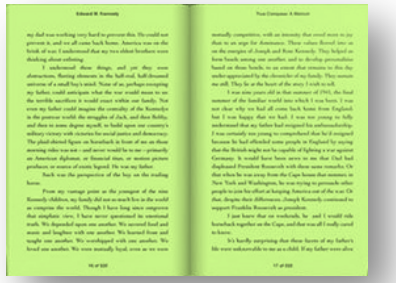
1	0	0	0	5	3	0	0	1	0	0	0	0

1*3
+
5*2
= 13

3	0	0	0	2	0	0	1	0	1	0	0	0



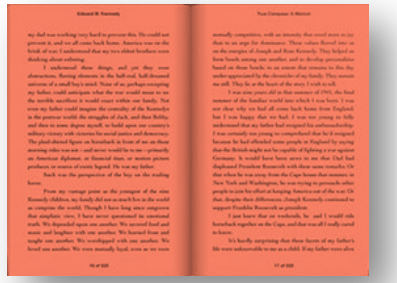
Measuring similarity



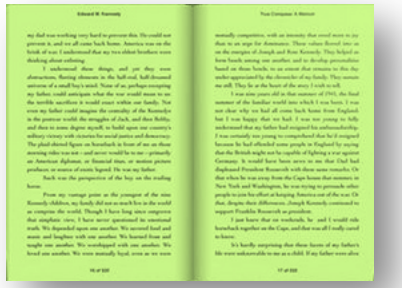
1	0	0	0	5	3	0	0	1	0	0	0	0

→ **0**

0	0	1	0	0	0	9	0	0	6	0	4	0



Issues with word counts – Doc length



1	0	0	0	5	3	0	0	1	0	0	0	0

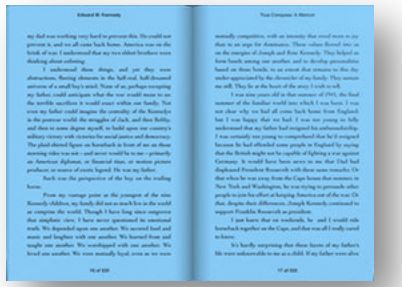
2	0	0	0	10	6	0	0	2	0	0	0	0

3	0	0	0	2	0	0	1	0	1	0	0	0

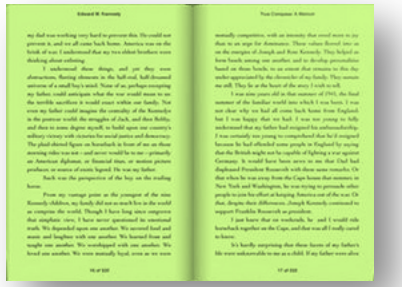
Similarity = 13

6	0	0	0	4	0	0	2	0	2	0	0	0

Similarity = 52



Solution = normalize



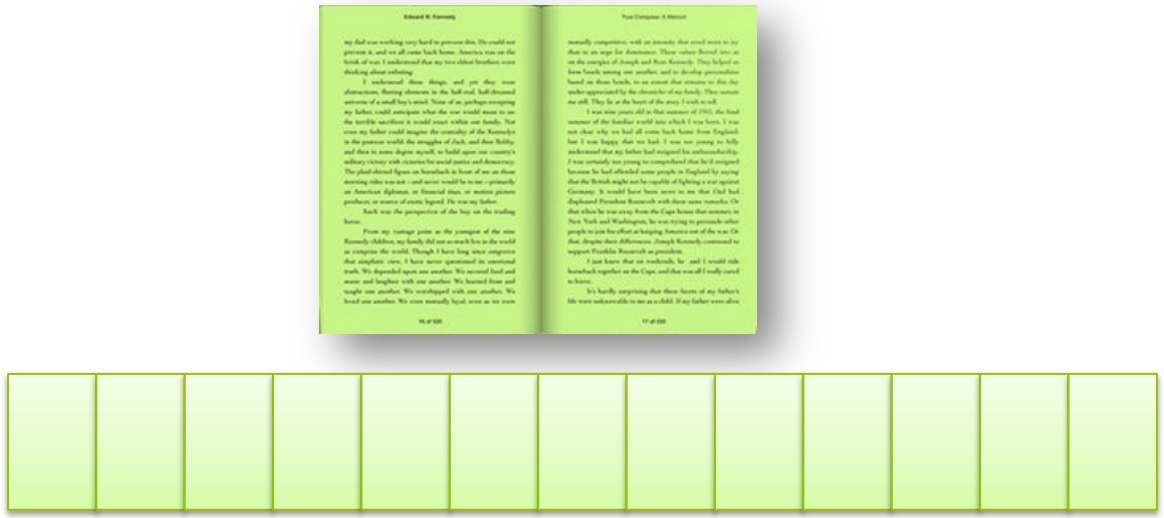
1	0	0	0	5	3	0	0	1	0	0	0	0

$$\sqrt{(1^2 + 5^2 + 3^2 + 1^2)}$$

1/6	0	0	0	5/6	3/6	0	0	1/6	0	0	0	0

Prioritizing important words with tf-idf

Issues with word counts – Rare words



Common words in doc: “the”, “player”, “field”, “goal”

Dominate rare words like: “futbol”, “Messi”

Document frequency

- What characterizes a rare word?
  - Appears infrequently in the corpus

- Emphasize words appearing in few docs
  - Equivalently, discount word *w* based on
    # of docs containing *w* in corpus

Important words

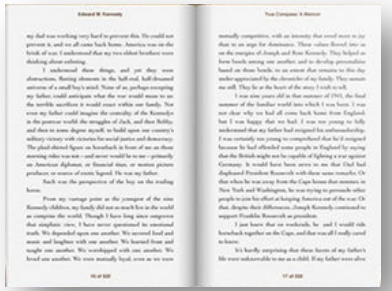
- Do we want only rare words to dominate???

- What characterizes an important word?
  - Appears frequently in document (common locally)
  - Appears rarely in corpus (rare globally)

- Trade off between local frequency and global rarity

TF-IDF document representation

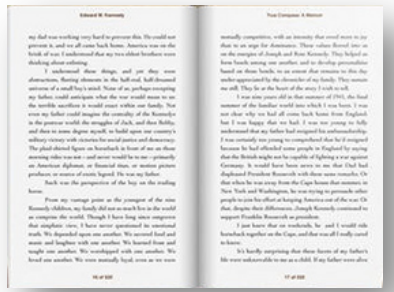
- Term frequency – inverse document frequency (tf-idf)



TF-IDF document representation

- Term frequency – inverse document frequency (tf-idf)
- Term frequency

- Same as word counts

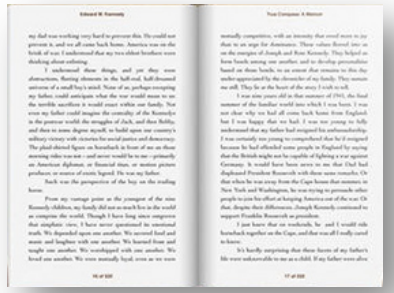


TF-IDF document representation

- Term frequency – inverse document frequency (tf-idf)
- Term frequency

- Inverse document frequency

$$\log \frac{\#\text{ docs}}{1 + \#\text{ docs using word}}$$



TF-IDF document representation

- Term frequency – inverse document frequency (tf-idf)
- Term frequency

- Inverse document frequency

$$\log \frac{\#\text{ docs}}{1 + \#\text{ docs using word}}$$

$\log \frac{\text{large \#}}{1+\text{large \#}} \approx \log 1 = 0$

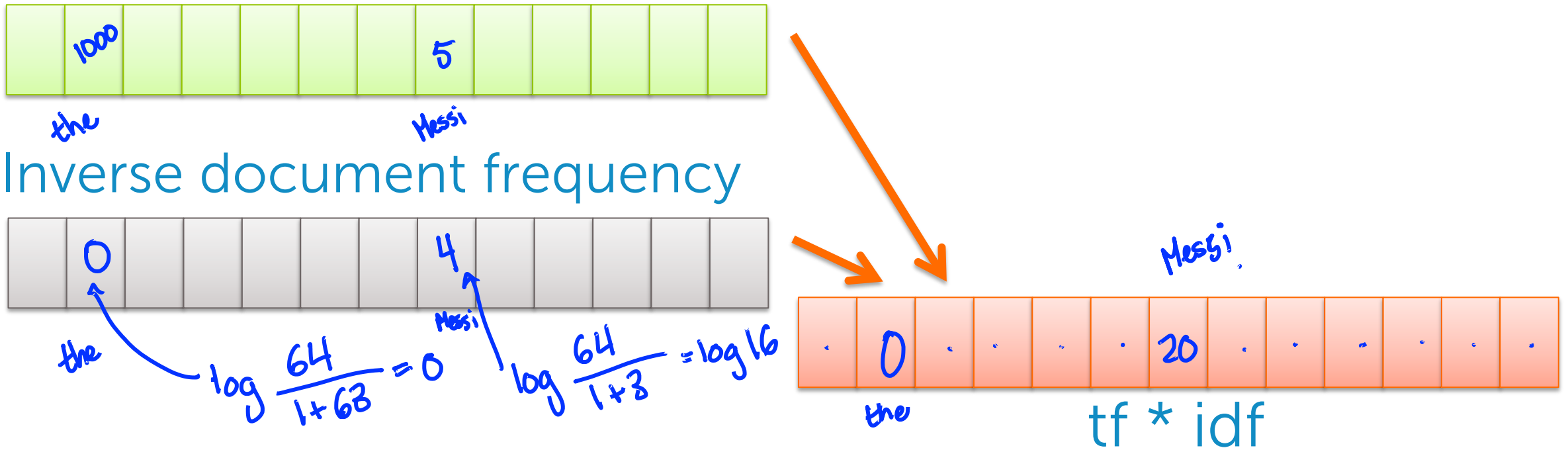
word in many docs

rare word

$\log \frac{\text{large \#}}{1+\text{small \#}} \rightarrow$ large #

TF-IDF document representation

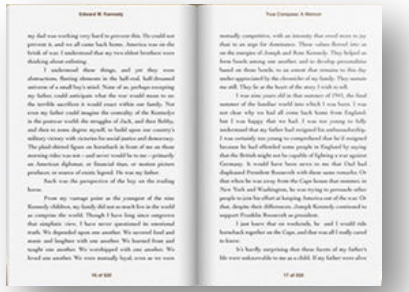
- Term frequency – inverse document frequency (tf-idf)
- Term frequency
- Inverse document frequency



Retrieving similar documents

Nearest neighbor search

- Query article:



- Corpus:

- **Specify:** Distance metric
- **Output:** Set of most similar articles

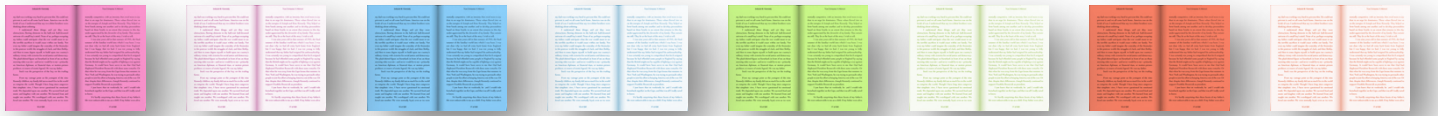
1 – Nearest neighbor

- **Input:** Query article 
- **Output:** *Most* similar article

- Algorithm:
  - Search over each article  in corpus
    - Compute **s = similarity(**  **,**  **)**
    - If **s > Best_s**, record  **=**  and set **Best_s = s**
  - Return 

k – Nearest neighbor

- **Input:** Query article 
- **Output:** *List of k* similar articles



Clustering documents

Structure documents by topic

- Discover groups (*clusters*) of related articles

SPORTS

WORLD NEWS

What if some of the labels are known?

- Training set of labeled docs

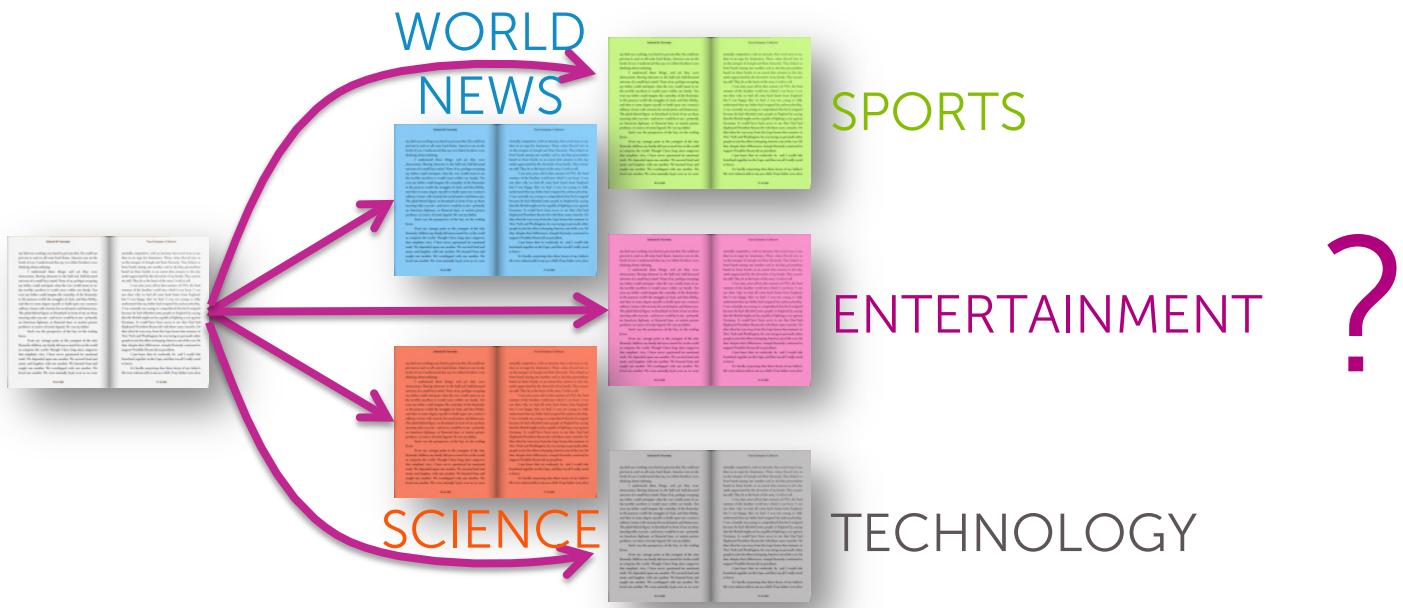
SPORTS

WORLD NEWS

ENTERTAINMENT

SCIENCE

Multiclass classification problem

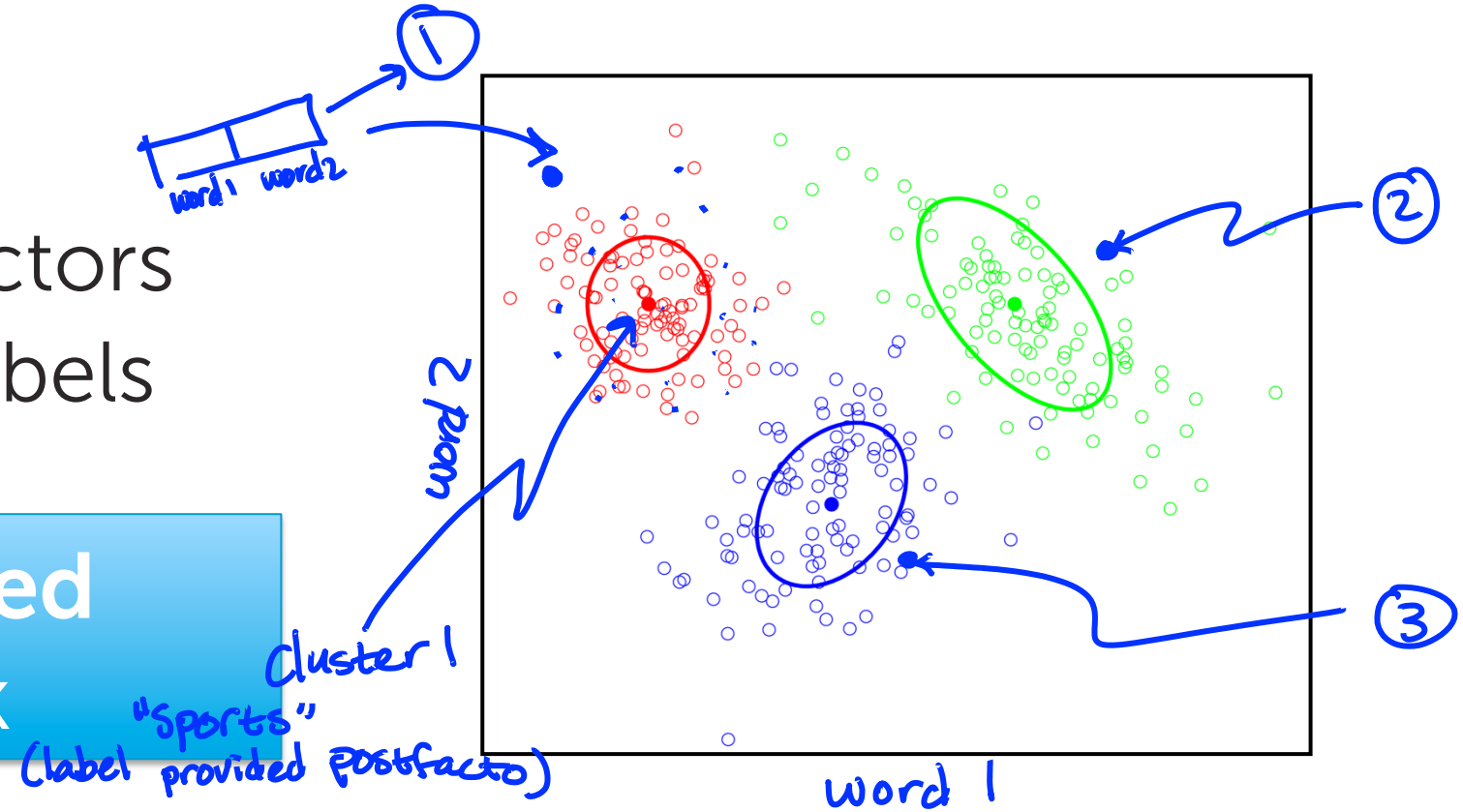


Example of
supervised learning

Clustering

- No labels provided
- Want to uncover cluster structure

- **Input:** docs as vectors
- **Output:** cluster labels

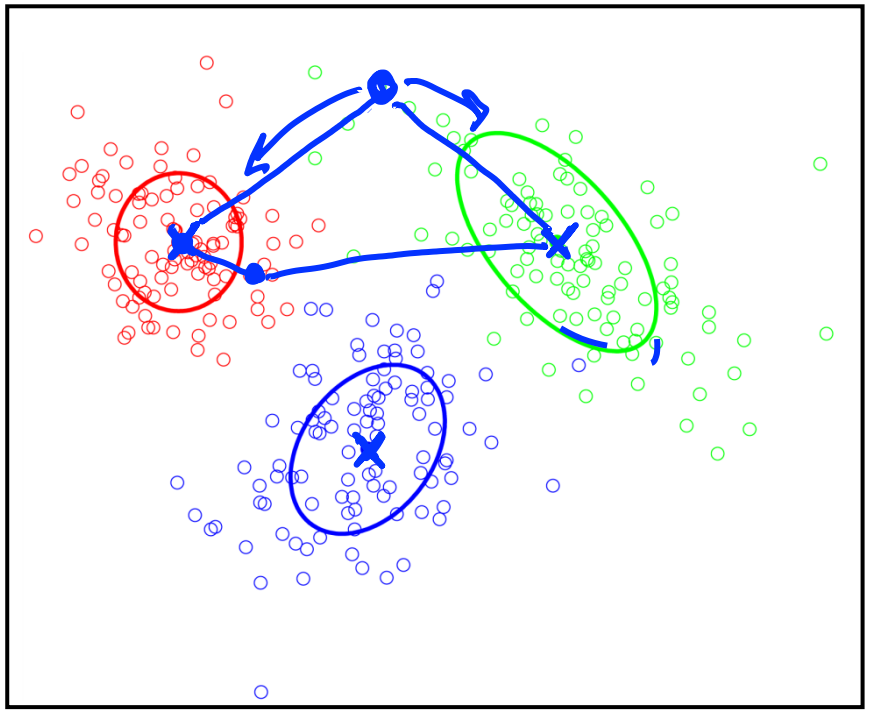


An **unsupervised learning** task

What defines a cluster?

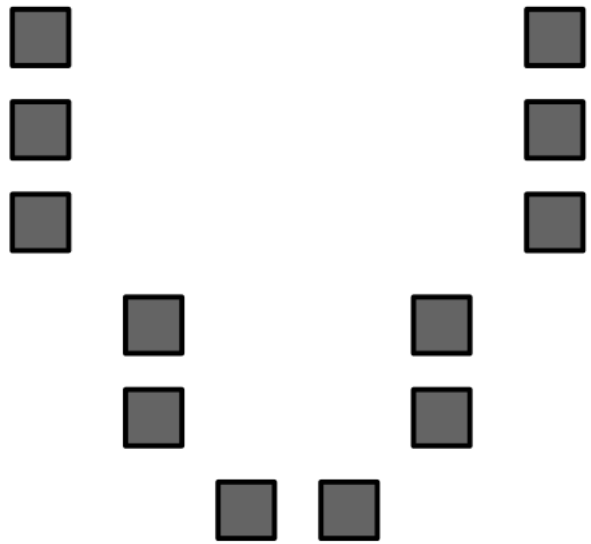
- Cluster defined by center & shape/spread

- Assign observation (doc) to cluster (topic label)
  - Score under cluster is higher than others
  - Often, just more similar to assigned cluster center than other cluster centers



k-means

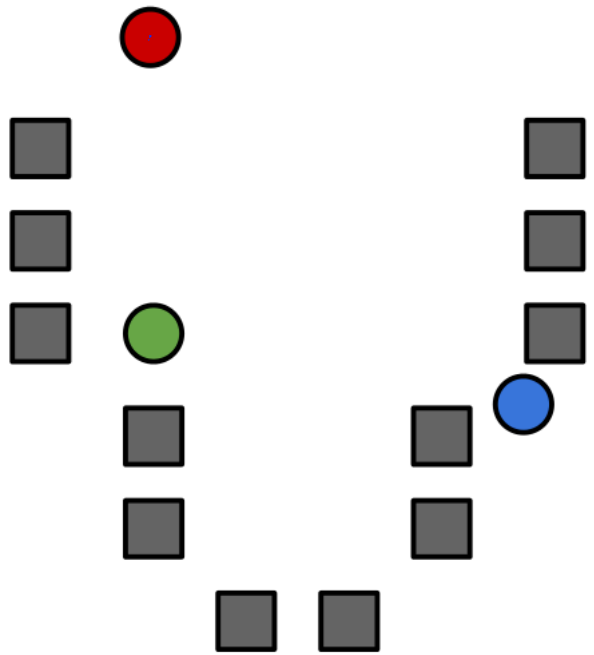
- Assume
  - Similarity metric = distance to cluster center (smaller better)



DATA to CLUSTER

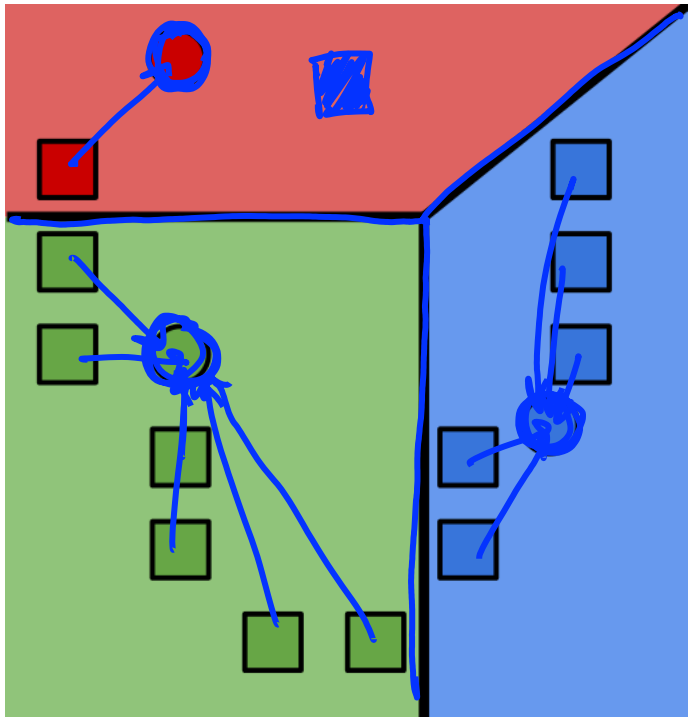
k-means algorithm

0. Initialize cluster centers



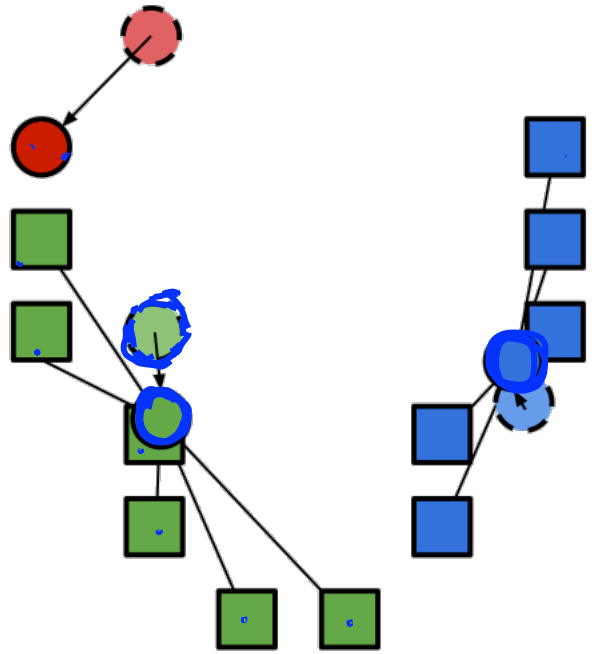
k-means algorithm

0. Initialize cluster centers
1. Assign observations to closest cluster center



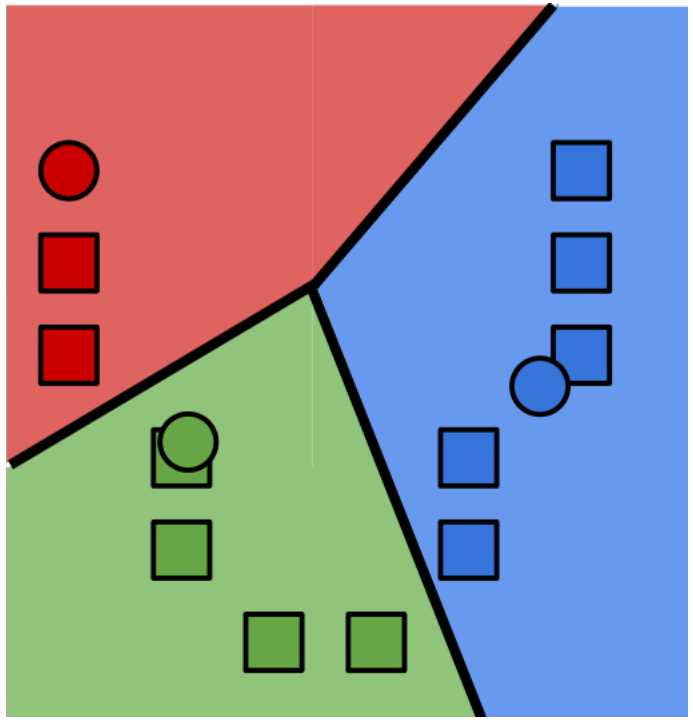
k-means algorithm

0. Initialize cluster centers
1. Assign observations to closest cluster center
2. Revise cluster centers as mean of assigned observations



k-means algorithm

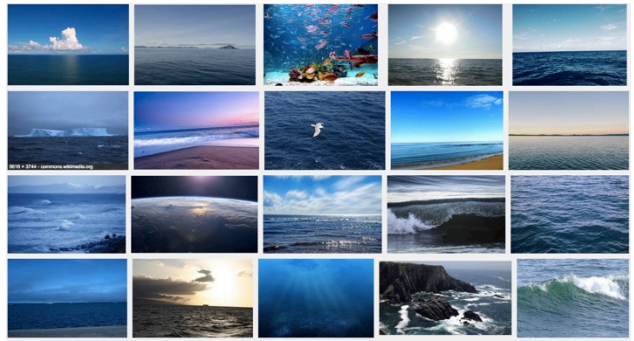
0. Initialize cluster centers
1. Assign observations to closest cluster center
2. Revise cluster centers as mean of assigned observations
3. Repeat 1.+2. until convergence

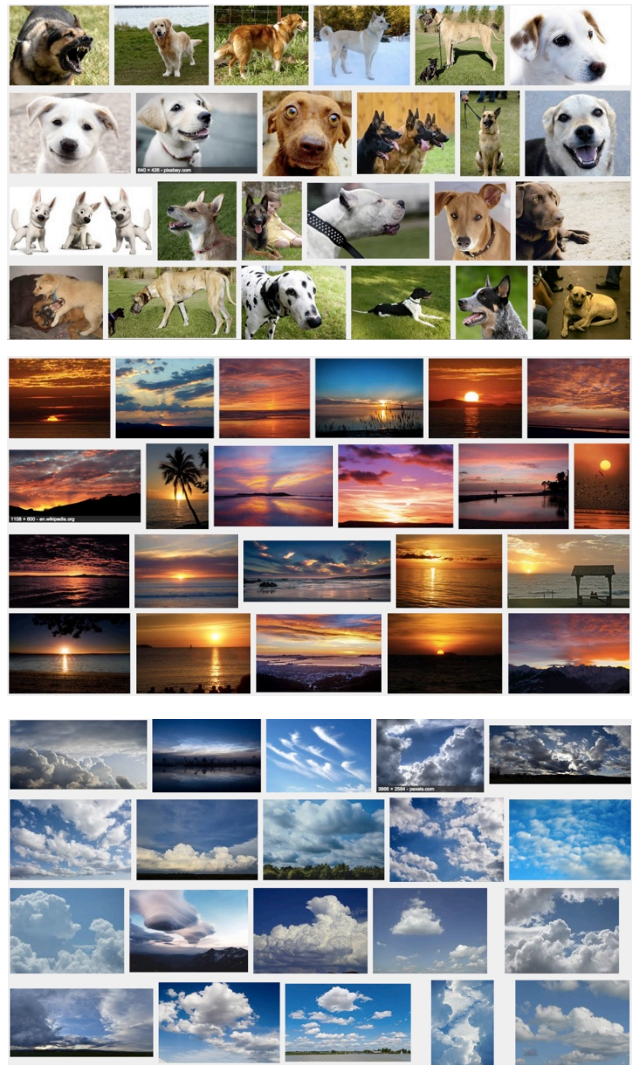


Other examples

Clustering images

- For search, group as:
  - Ocean
  - Pink flower
  - Dog
  - Sunset
  - Clouds
  - …

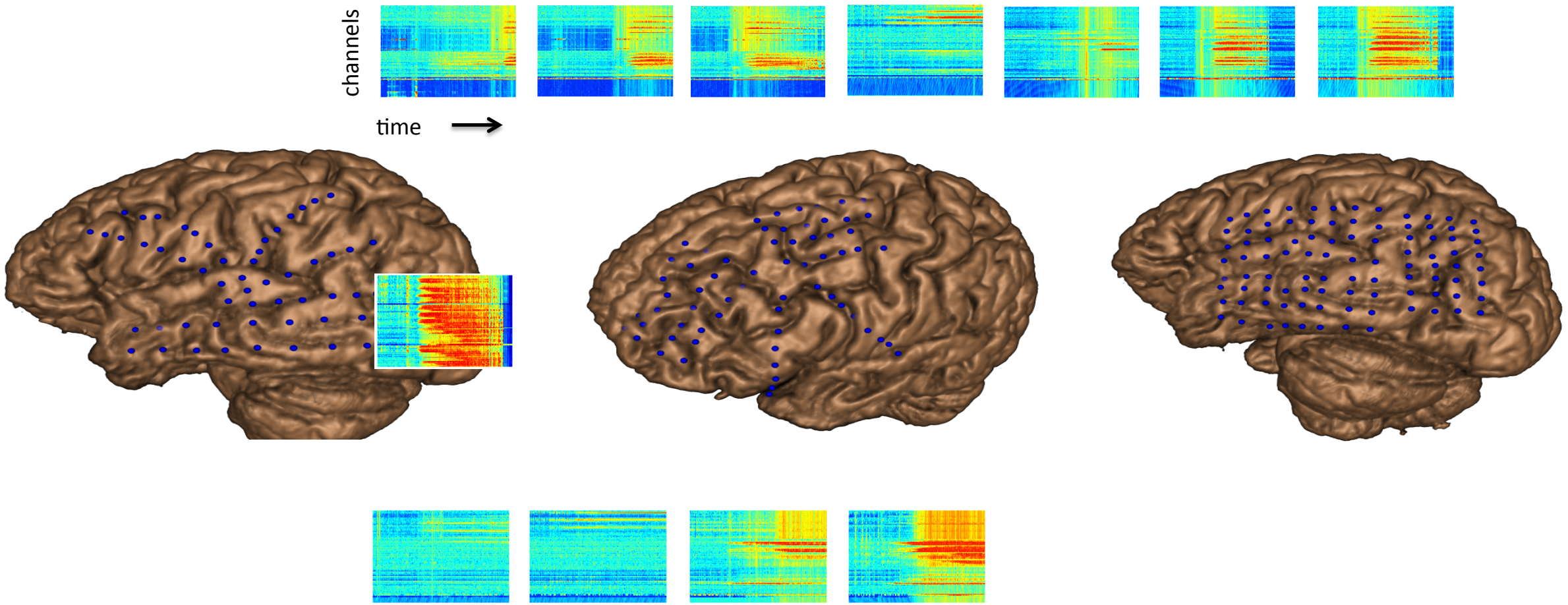




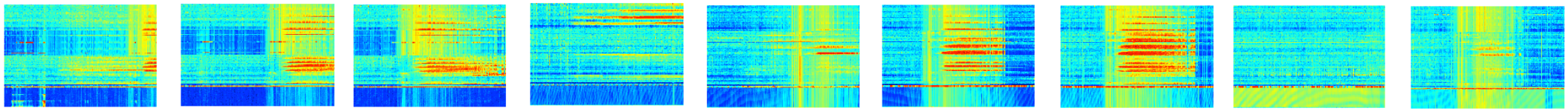
Grouping patients by medical condition

- Better characterize subpopulations and diseases

Example: Patients and seizures are diverse



Cluster seizures by observed time courses



Products on Amazon

- Discover product categories from purchase histories

~~"furniture"~~

"baby"

- Or discovering groups of **users**

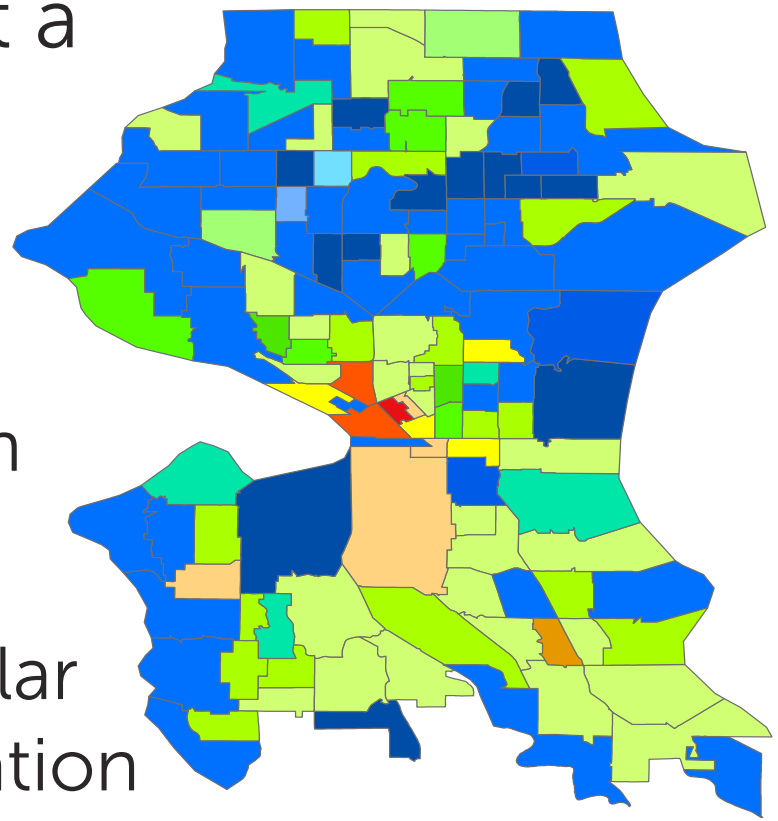
Structuring web search results

- Search terms can have multiple meanings
- Example: "cardinal"

- Use clustering to structure output

Discovering similar neighborhoods

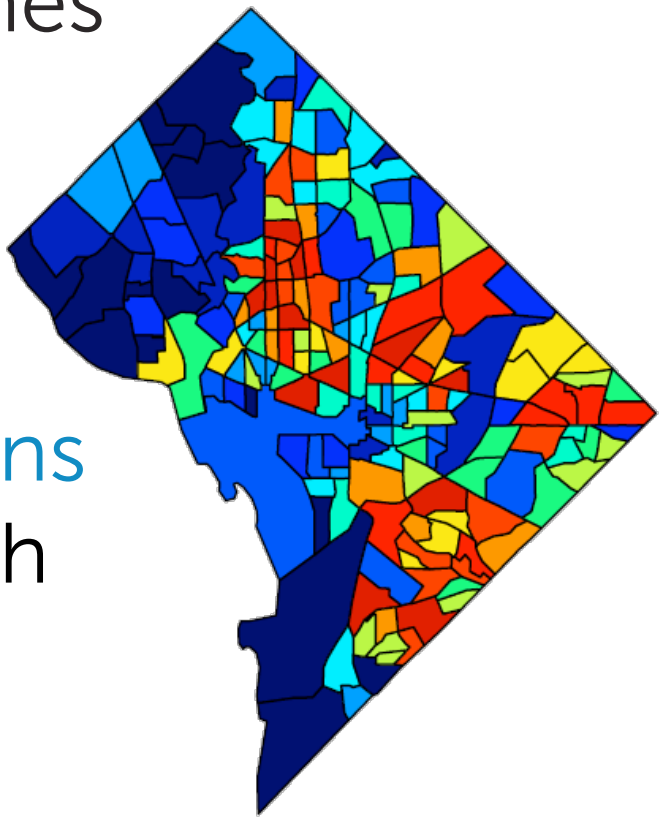
- **Task 1:** Estimate price at a small regional level
- Challenge:
  - Only a few (or no!) sales in each region per month
- Solution:
  - Cluster regions with similar trends and share information within a cluster



City of Seattle

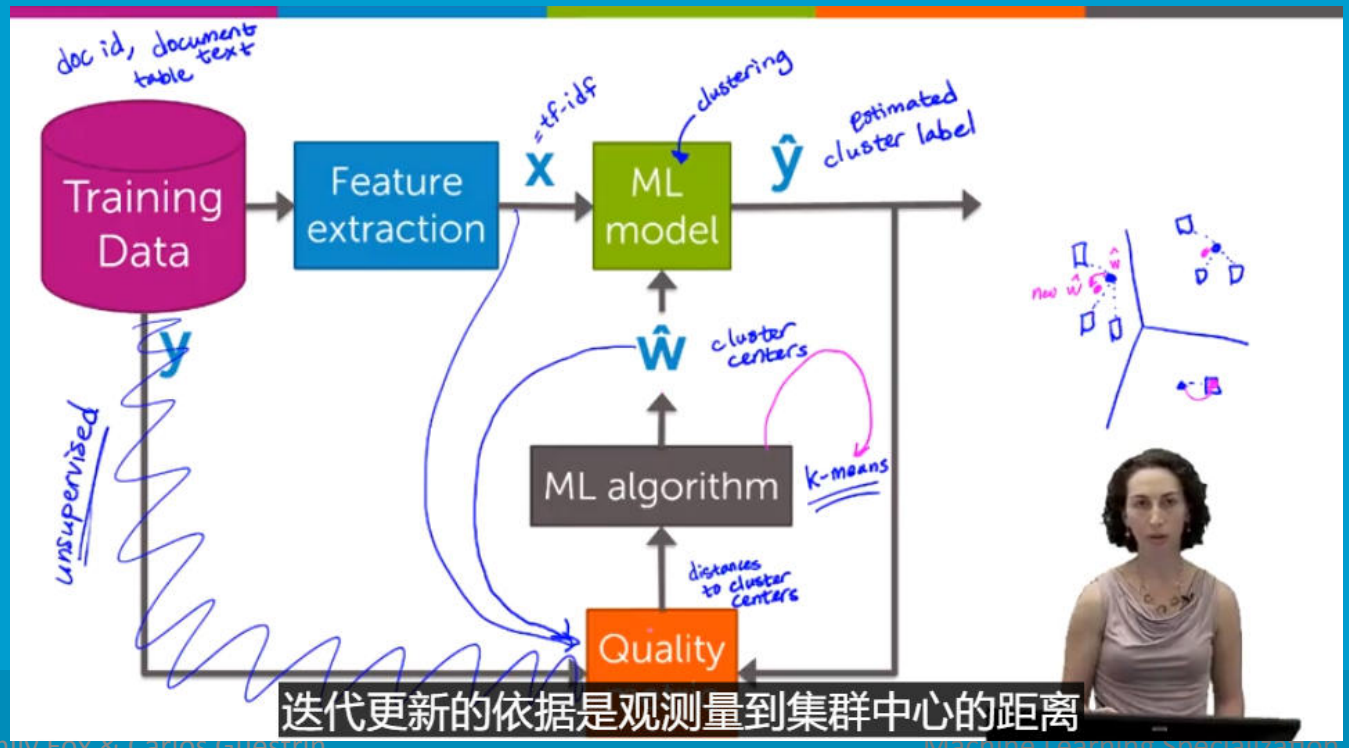
Discovering similar neighborhoods

- **Task 2:** Forecast violent crimes to better task police
- Again, cluster regions and share information!
- Leads to improved predictions compared to examining each region independently



Washington, DC

Summary for clustering and similarity



What you can do now...

- Describe ways to represent a document (e.g., raw word counts, tf-idf,...)
- Measure the similarity between two documents
- Discuss issues related to using raw word counts
  - Normalize counts to adjust for document length
  - Emphasize important words using tf-idf
- Implement a nearest neighbor search for document retrieval
- Describe the input (unlabeled observations) and output (labels) of a clustering algorithm
- Determine whether a task is supervised or unsupervised
- Cluster documents using k-means (algorithmic details to come...)
- Describe other applications of clustering