

# Cooperative Inverse Reinforcement Learning

Dylan Hadfield-Menell

CS237: Reinforcement Learning

May 31, 2017

# The Value Alignment Problem



Example taken from Eliezer Yudkowsky's NYU talk

# The Value Alignment Problem



# The Value Alignment Problem



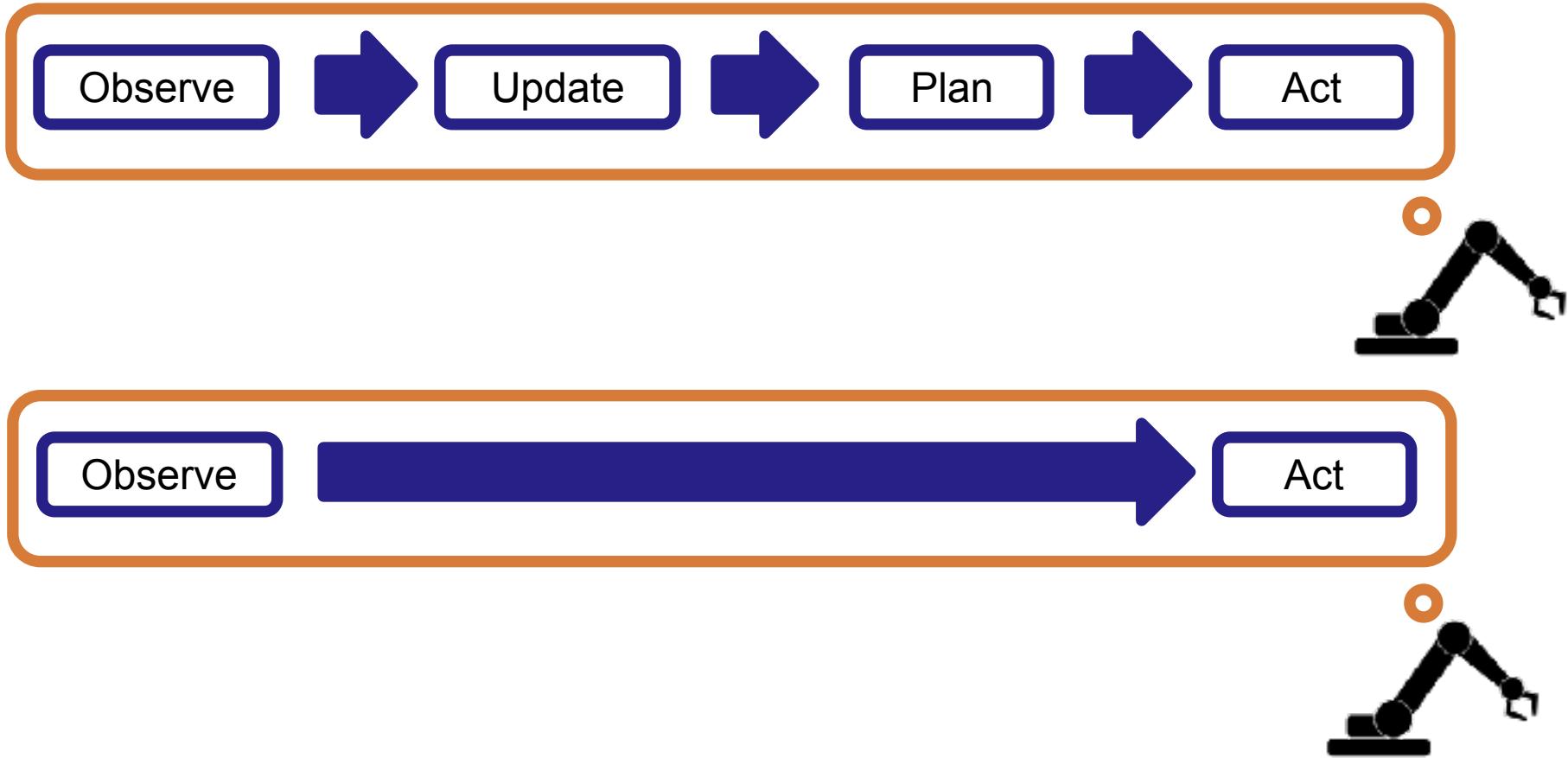


# The Value Alignment Problem

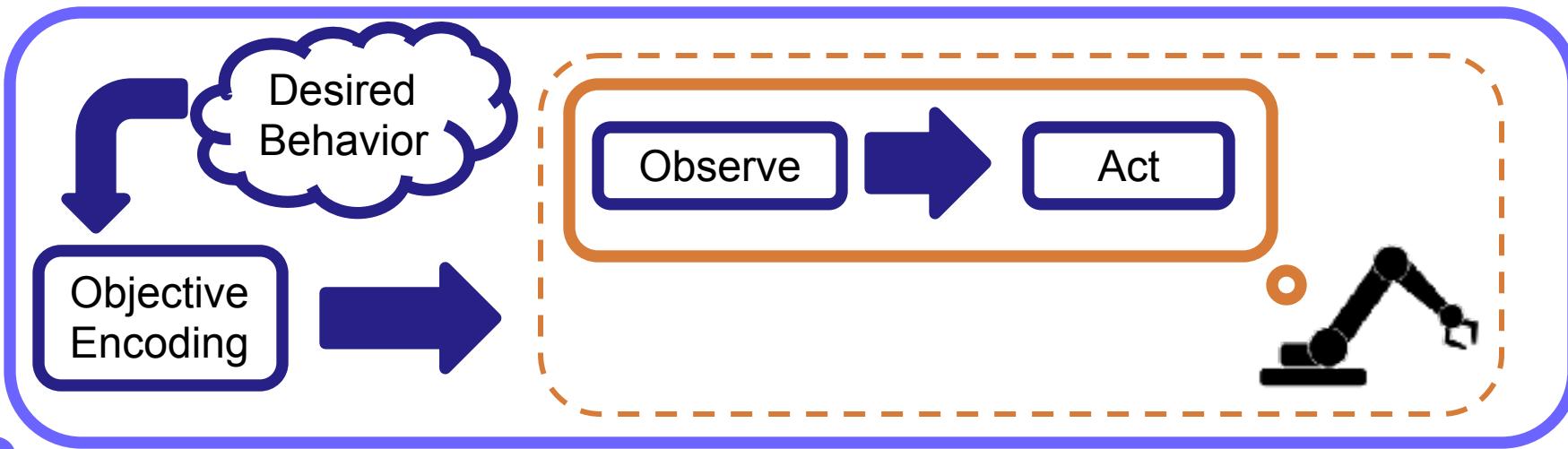
---



# Action Selection in Agents: Ideal



# Action Selection in Agents: Reality



Challenge: how do we account  
for errors and failures in the  
encoding of an objective?

# The Value Alignment Problem

---

How do we make sure that the agents we build pursue ends that we actually intend?

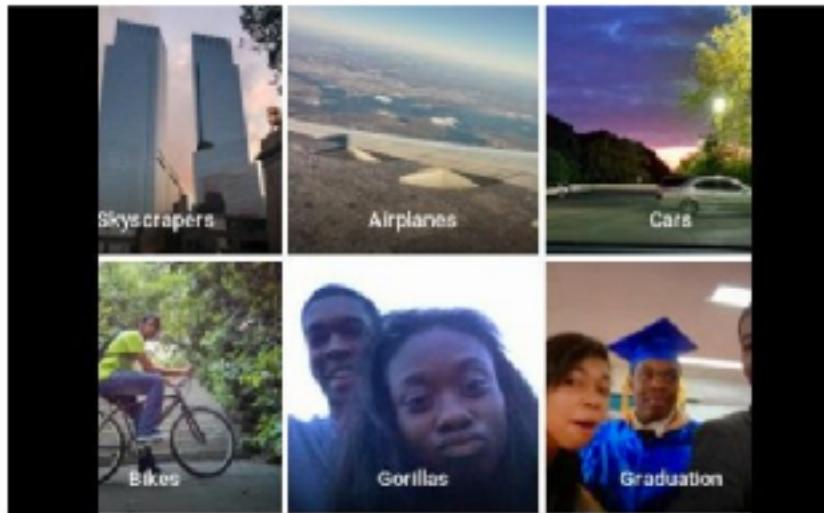
# Reward Engineering is Hard



# Reward Engineering is Hard

## Google apologises for Photos app's racist blunder

1 July 2015 | Technology



diri noir avec banan @jackyalcine · Jun 29

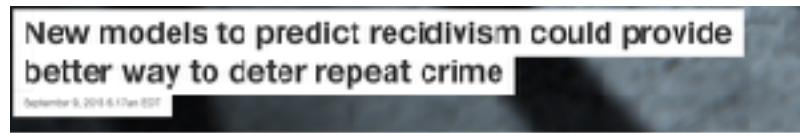
Google Photos, y'all [REDACTED] My friend's not a gorilla.

# What could go wrong?

## Medical Devices: The Therac-25\*

Nancy Leveson  
University of Washington

“...a computer-controlled radiation therapy machine....massively overdosed 6 people. These accidents have been described as the worst in the 35-year history of medical accelerators.”



BusinessInnes

## An AI-Fueled Credit Formula Might Help You Get a Loan

Starts 2nd Friday in May at 6pm, meeting every  
**WEDNESDAY** at 6pm at the church.

## **YOUR FILTER BUBBLE IS DESTROYING DEMOCRACY**

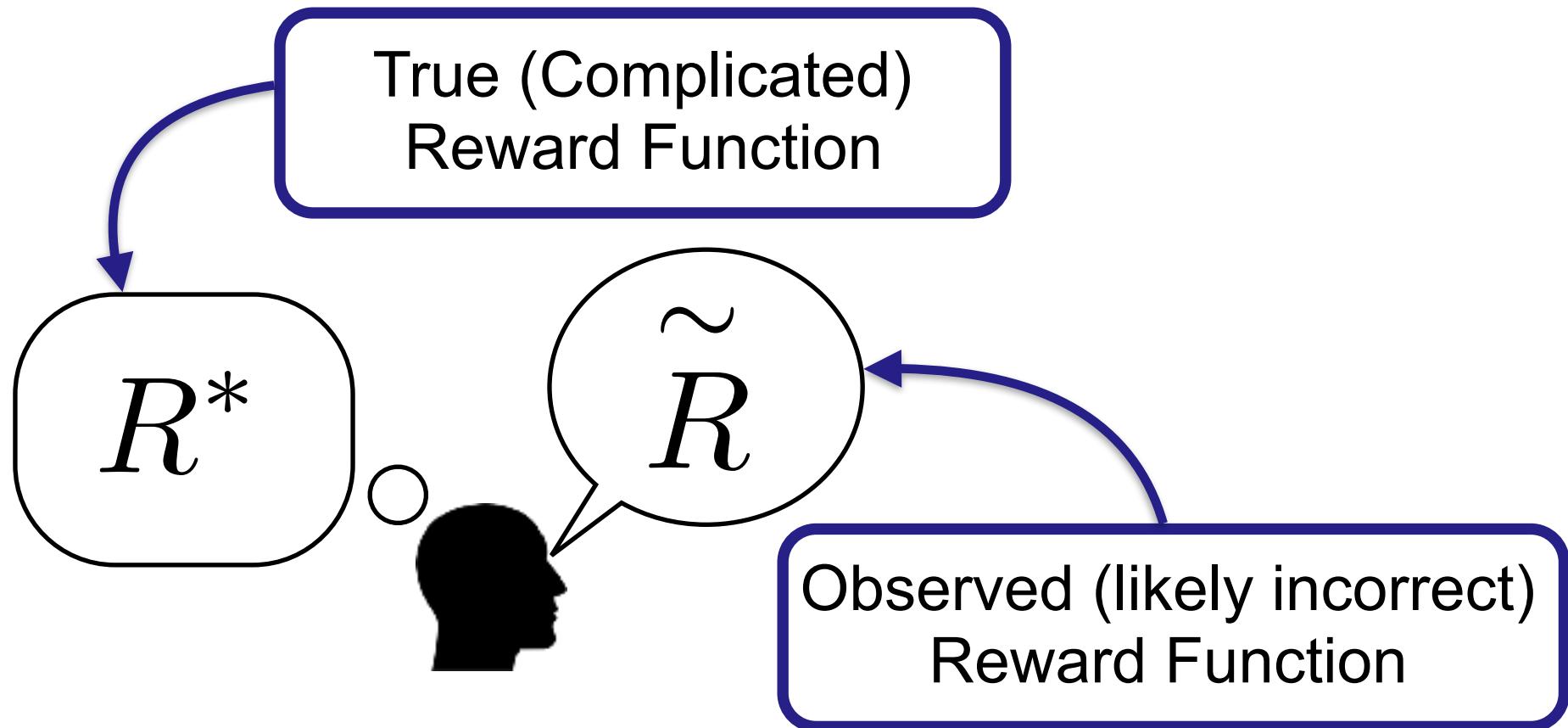


# Reward Engineering is Hard

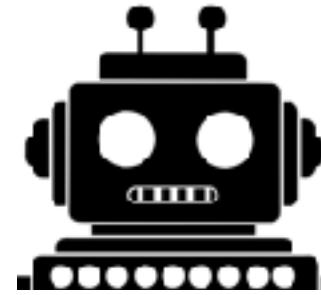
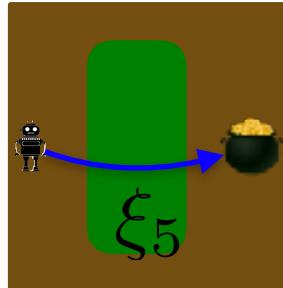
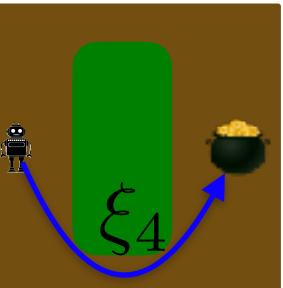
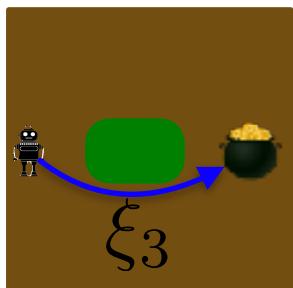
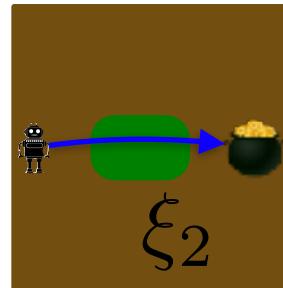
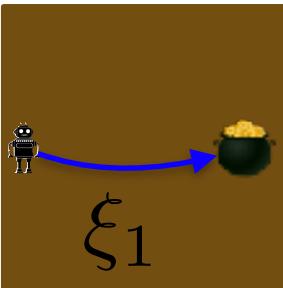
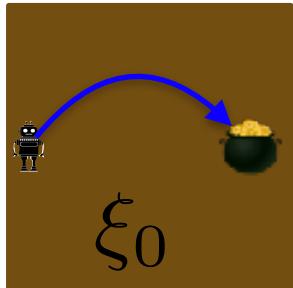
---

At best, reinforcement learning and similar approaches reduce the problem of generating useful behavior to that of designing a ‘good’ reward function.

# Reward Engineering is Hard

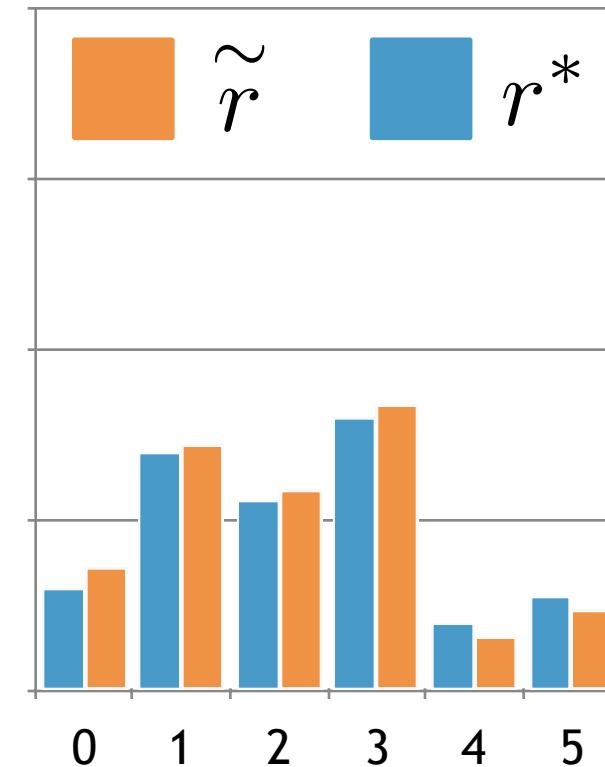
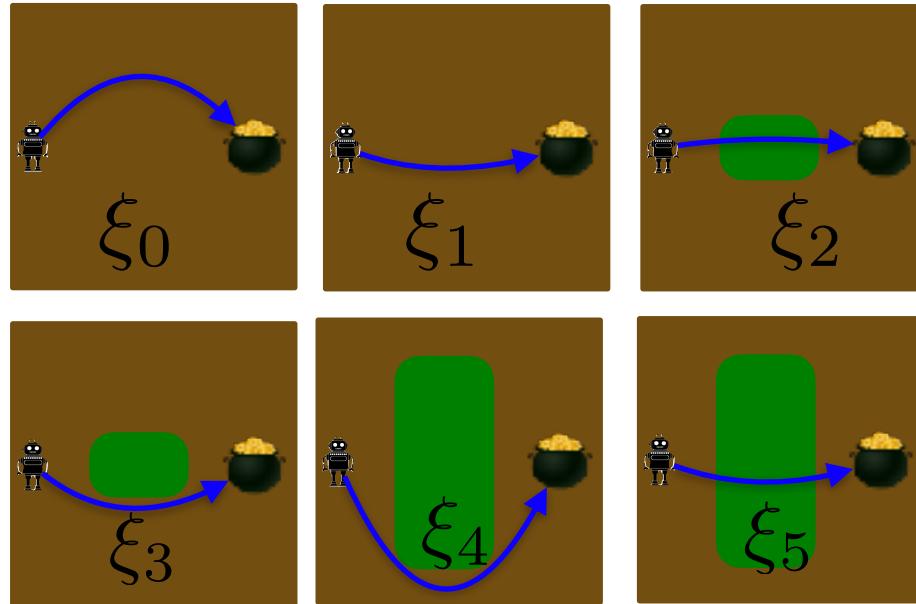


# Why is reward engineering hard?

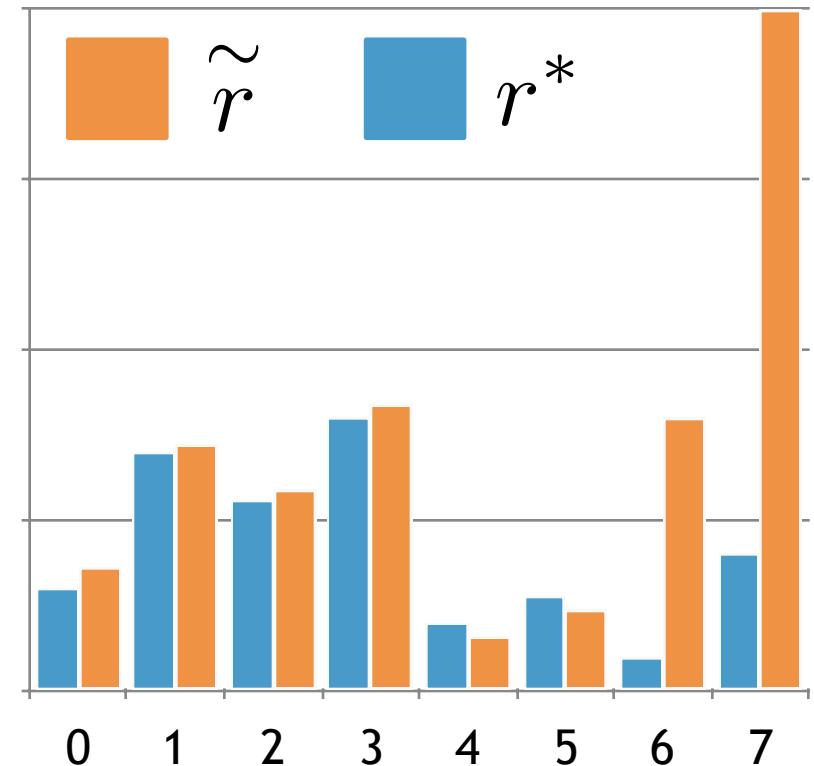
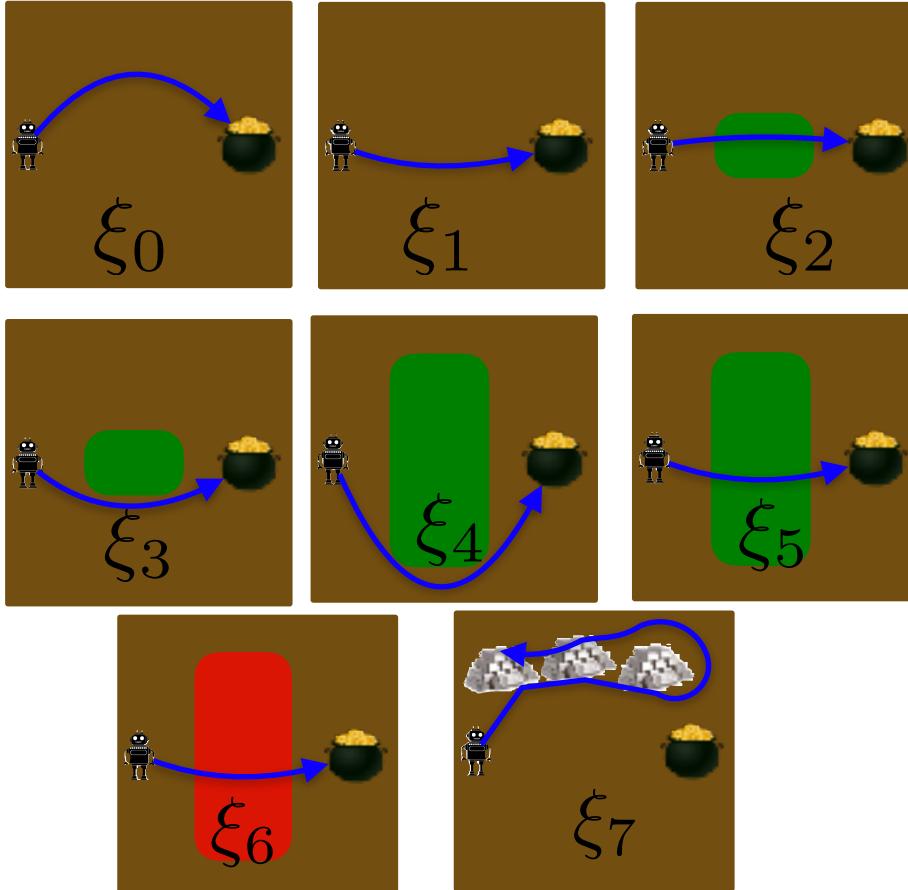


$$\xi^* = \operatorname{argmax}_{\xi \in \Xi} r(\xi)$$

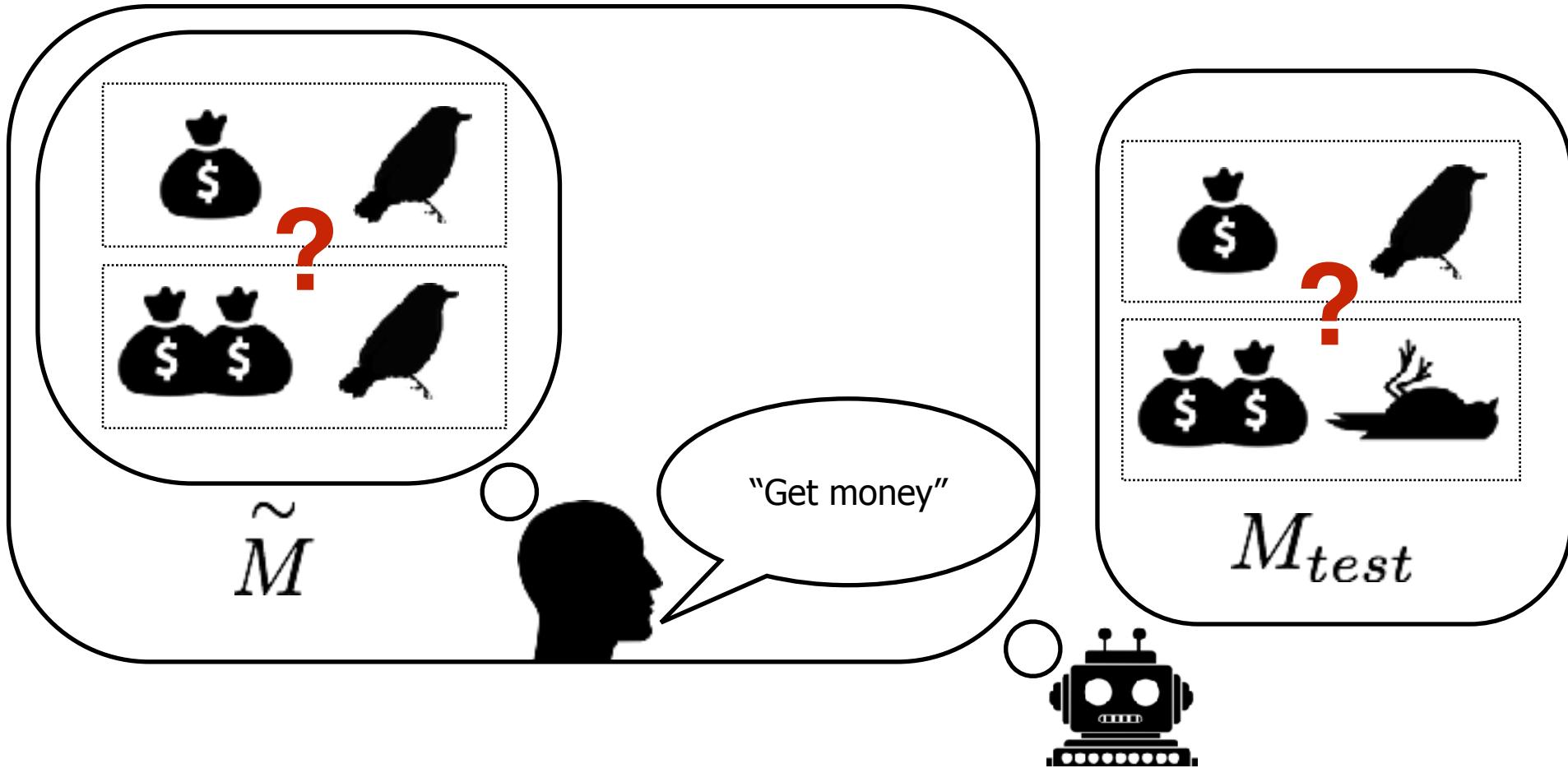
# Why is reward engineering hard?



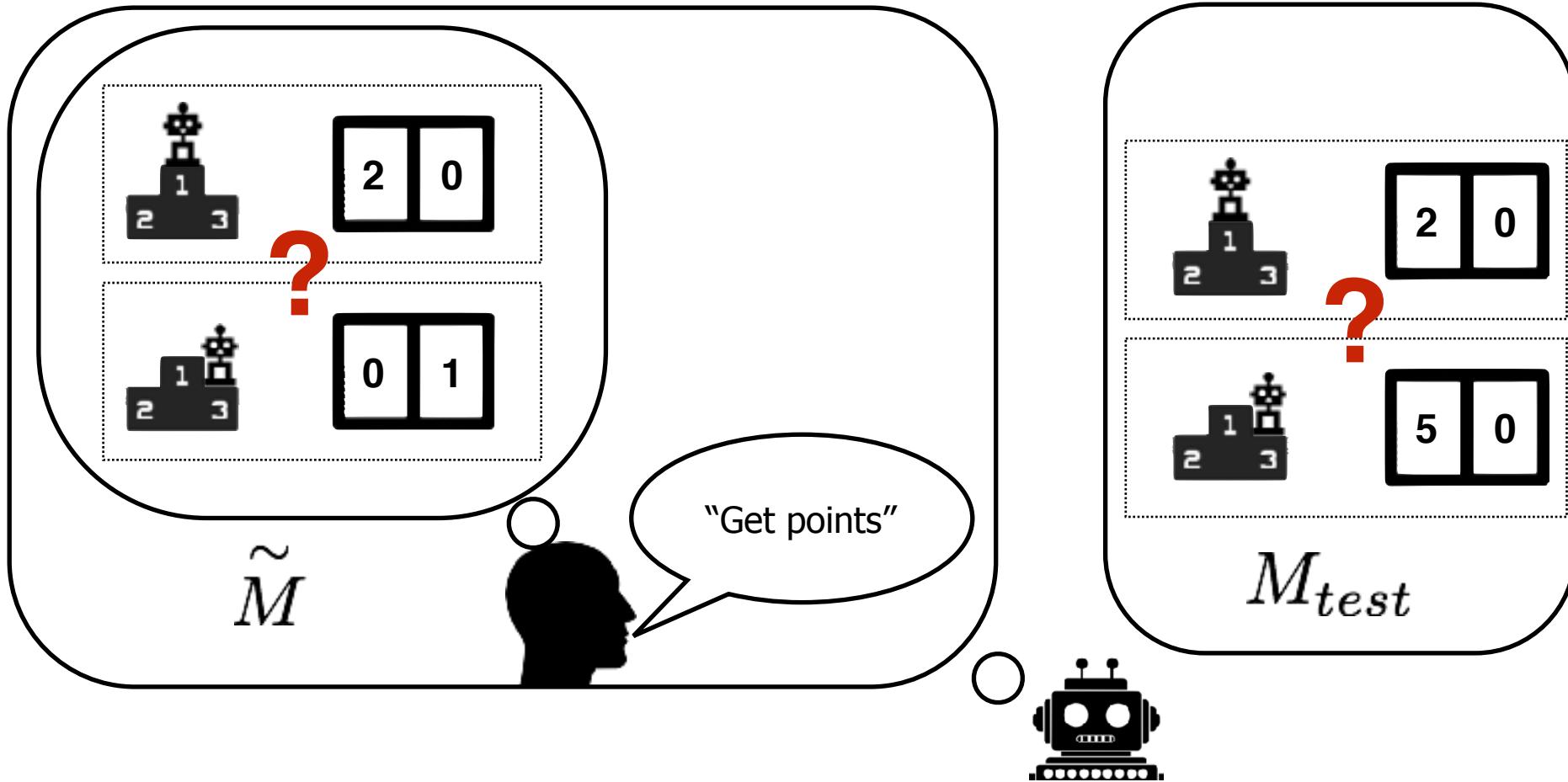
# Why is reward engineering hard?



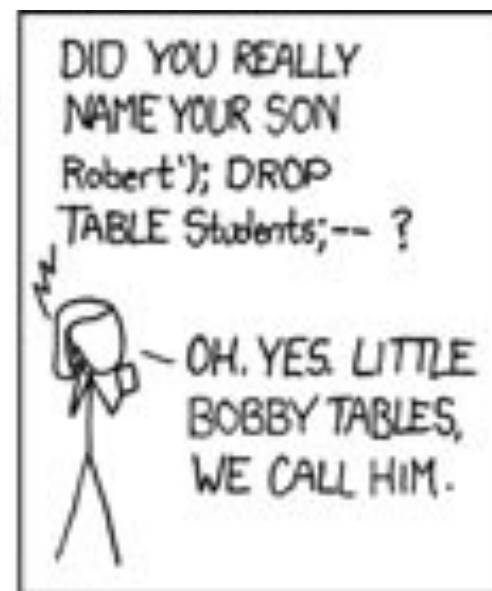
# Negative Side Effects



# Reward Hacking



# Analogy: Computer Security



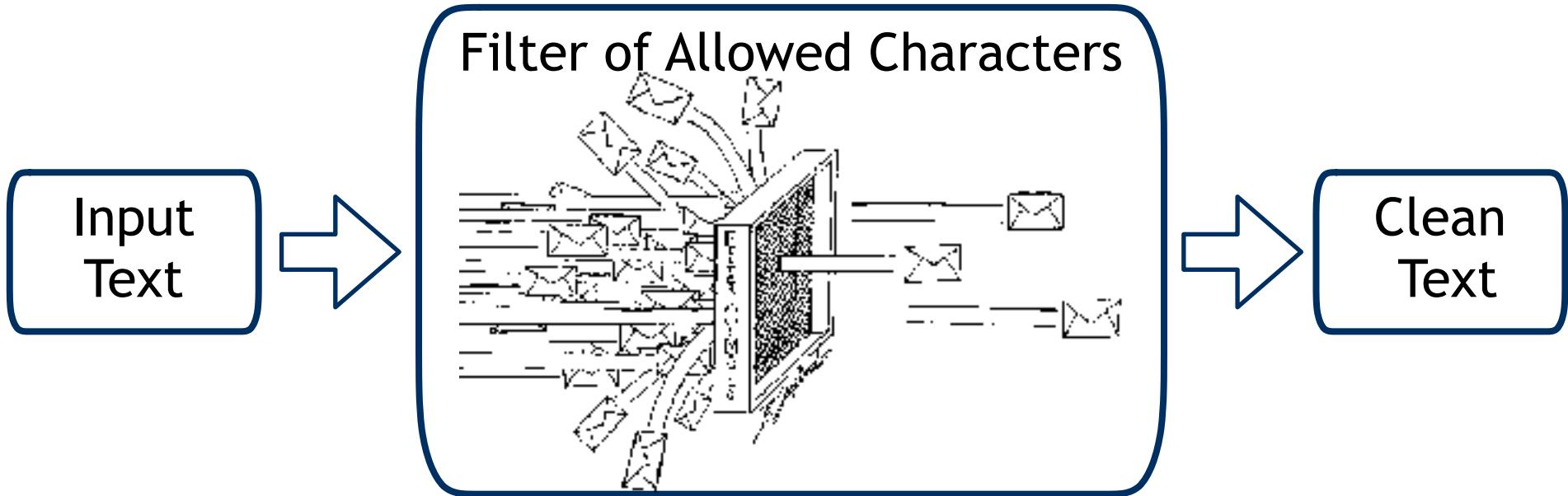
# Solution 1: Blacklist

Input  
Text



Clean  
Text

# Solution 2: Whitelist

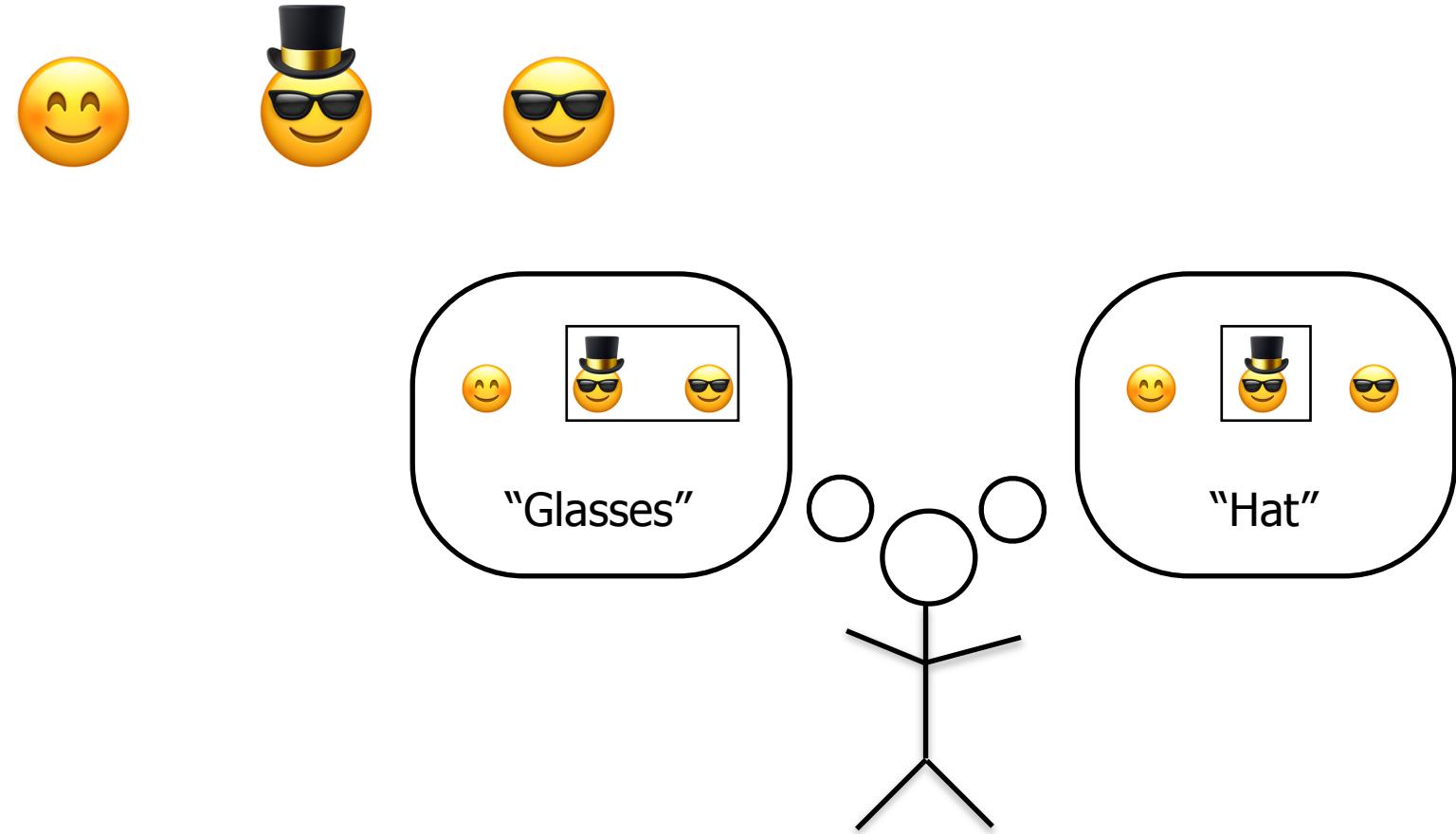


# Goal

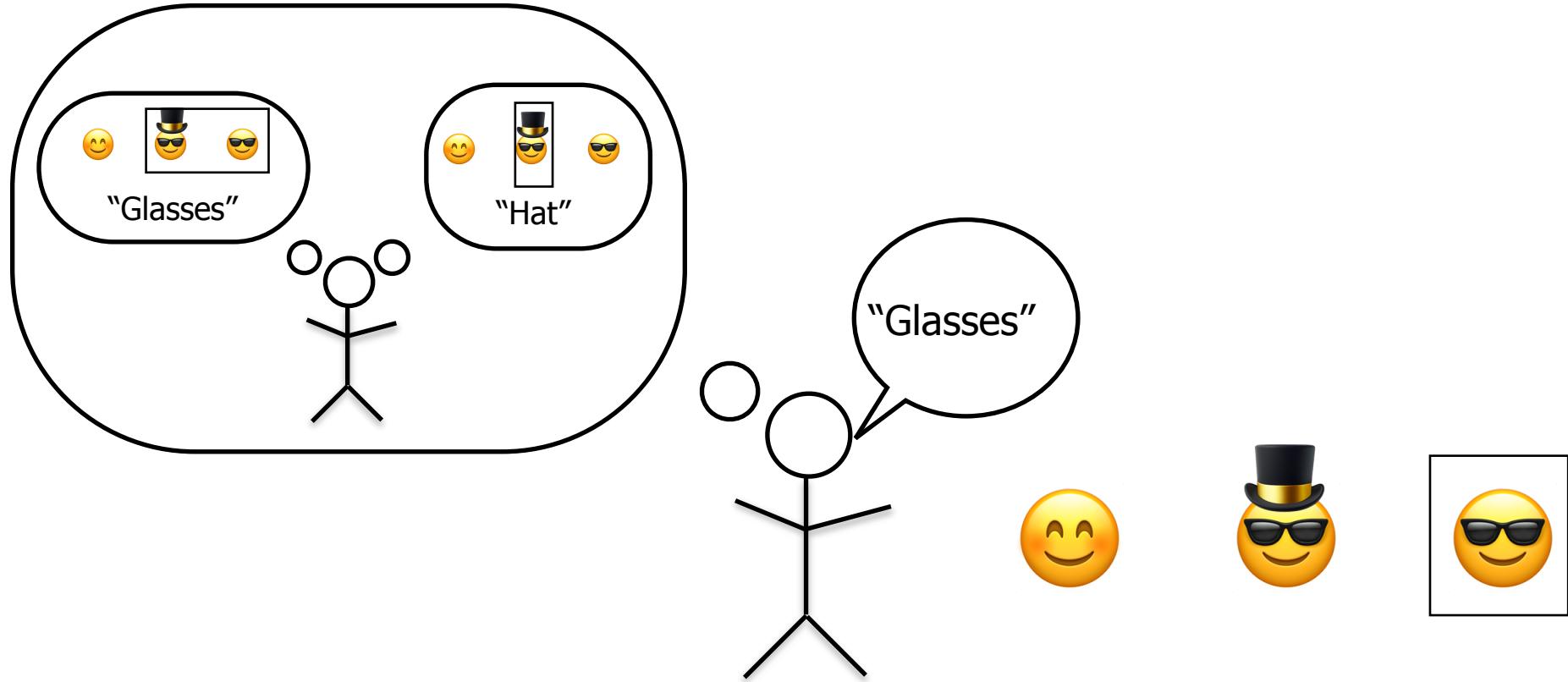
---

Reduce the extent to which  
system designers have to play  
whack-a-mole

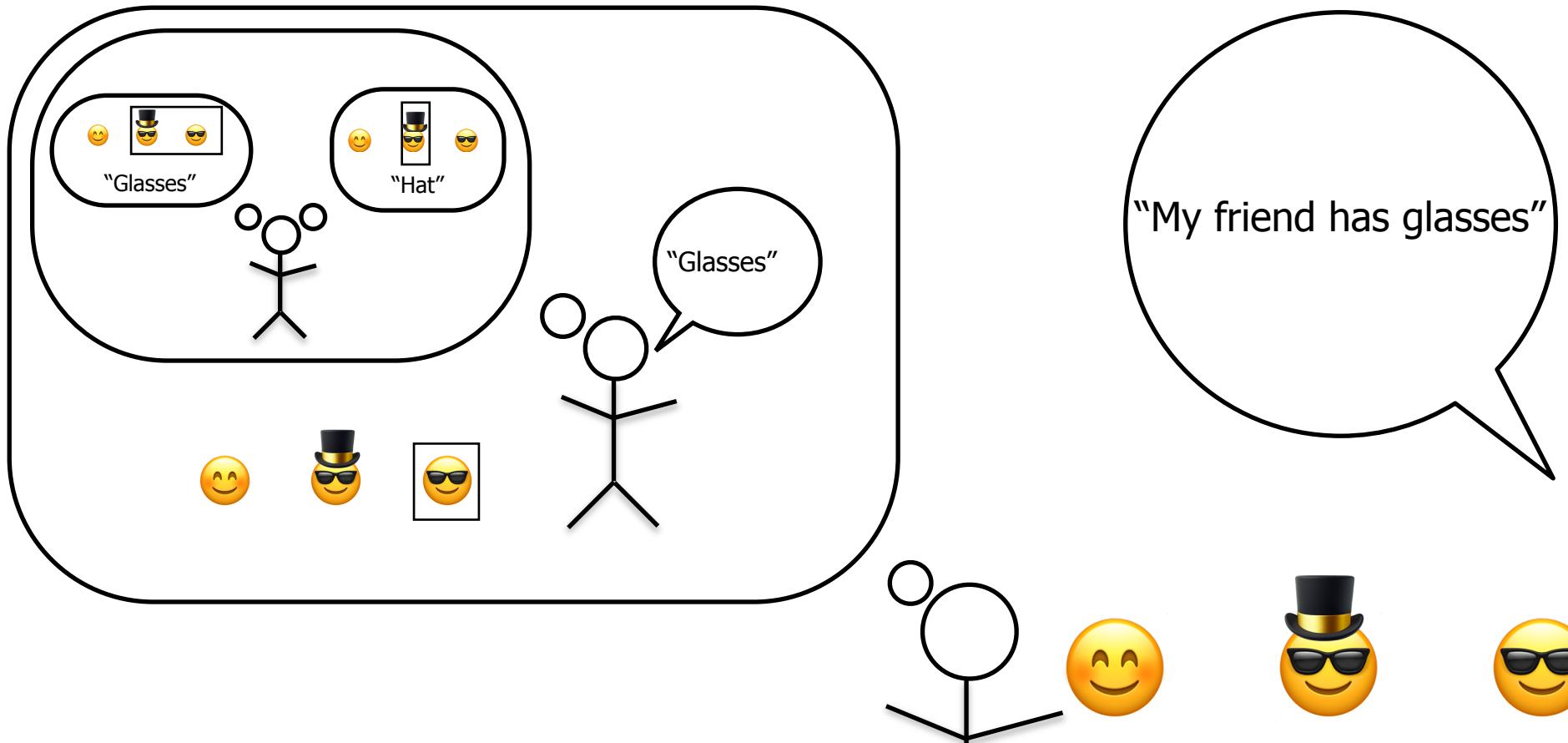
# Inspiration: Pragmatics



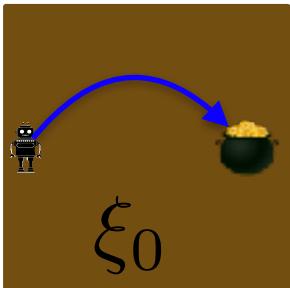
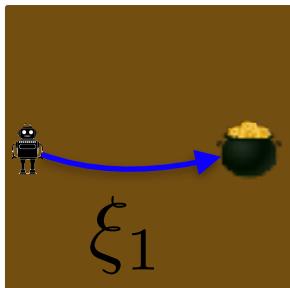
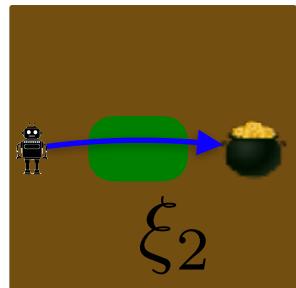
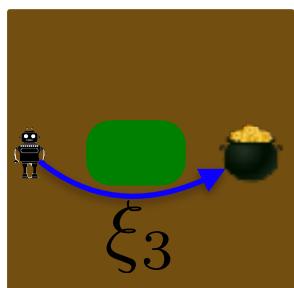
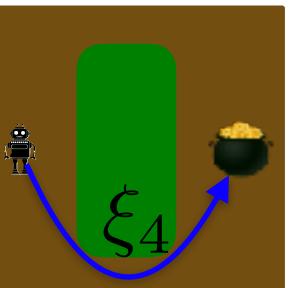
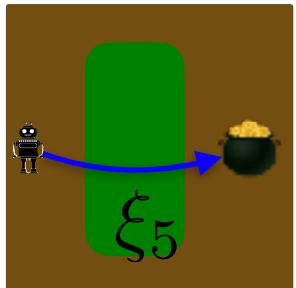
# Inspiration: Pragmatics



# Inspiration: Pragmatics



# Notation

 $\xi_0$  $\xi_1$  $\xi_2$  $\xi_3$  $\xi_4$  $\xi_5$ 

$\xi$  trajectory

$\phi$  features

$w$  weights

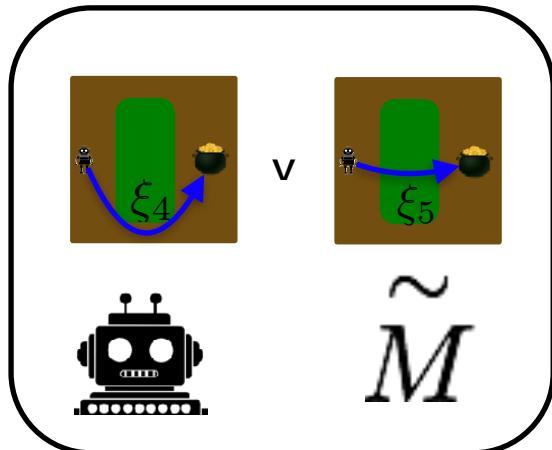
linear reward function

$$R(\xi; w) = w^\top \phi(\xi)$$

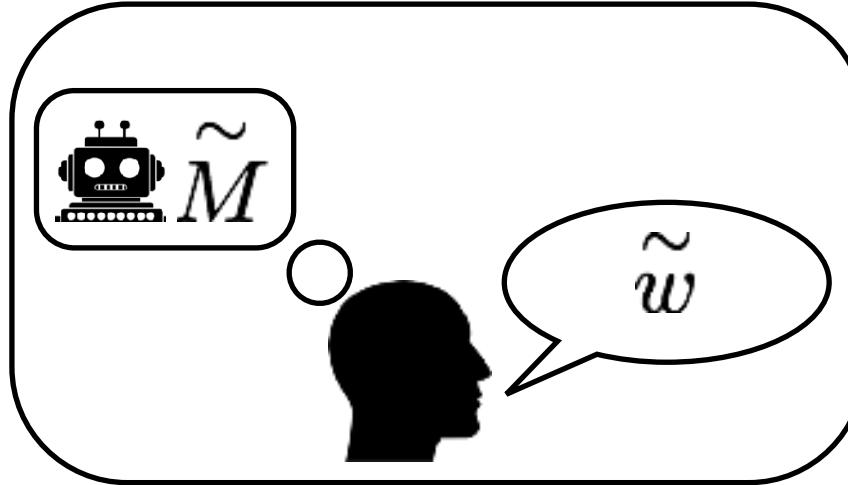
# Literal Reward Interpretation

$$\tilde{\pi}(\xi) \propto \exp\left(\tilde{w}^\top \phi(\xi)\right)$$

selects trajectories in proportion  
to proxy reward evaluation

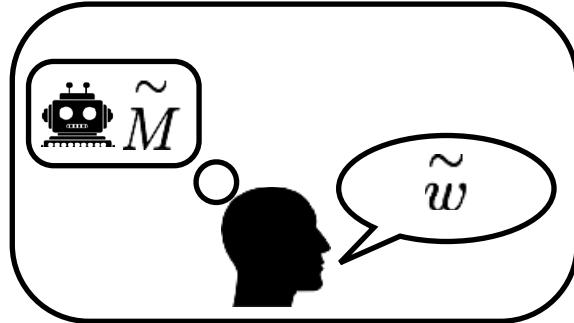


# Designing Reward for Literal Interpretation



Assumption: rewarded behavior has high true utility *in the training situations*

# Designing Reward for Literal Interpretation

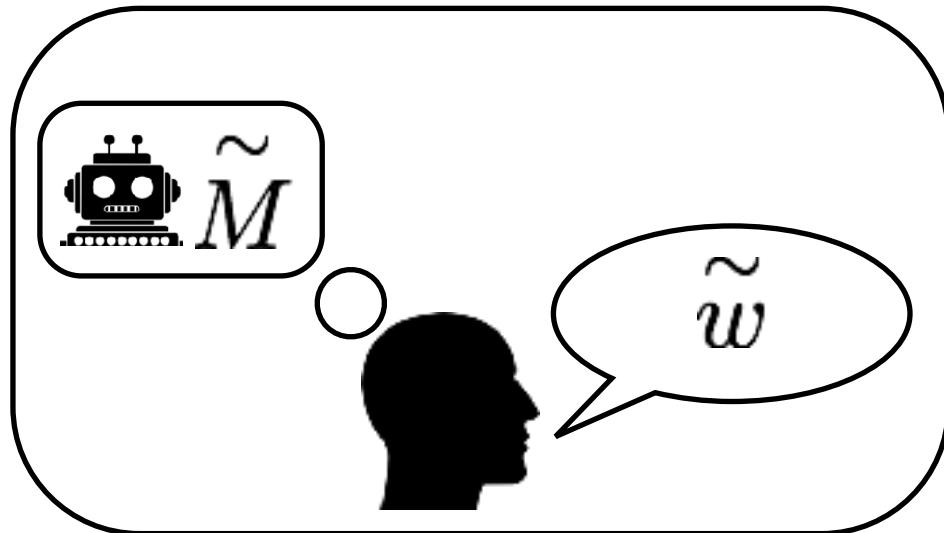


Literal optimizer's trajectory distribution conditioned on  $\tilde{w}$ .

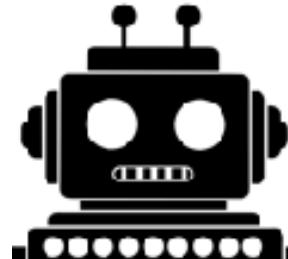
$$P(\tilde{w}|w^*) \propto \exp \left( \mathbb{E} [w^{* \top} \phi(\xi) | \xi \sim \tilde{\pi}] \right)$$

True reward received for each trajectory

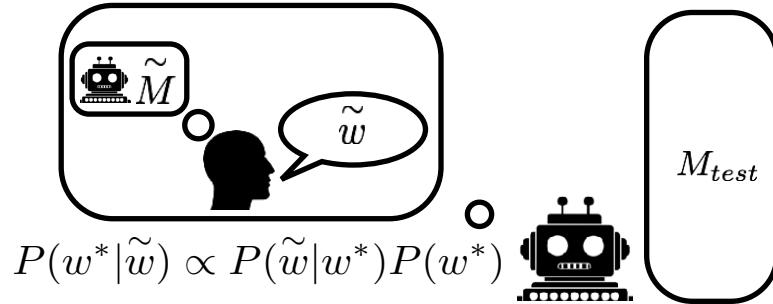
# Inverting Reward Design



$$P(w^*|\tilde{w}) \propto P(\tilde{w}|w^*)P(w^*)$$



# Inverting Reward Design



Key Idea: At test time, interpret reward functions in the context of an ‘intended’ situation

# Experiment

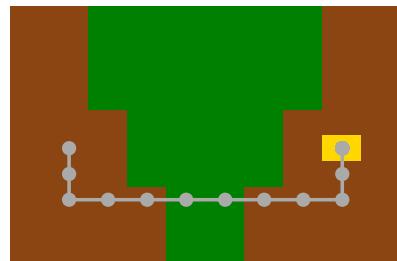
$M_{test}$

Three types of states in the training MDP

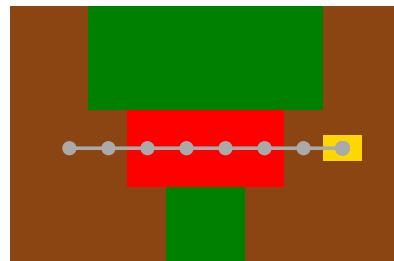
New state introduced In the ‘testing’ MDP

Measure how often the agent selects trajectories with the new state

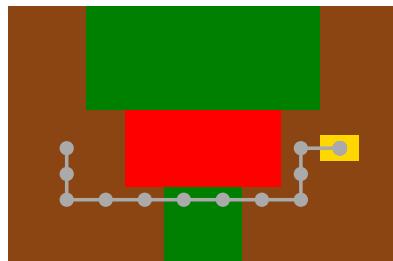
Domain: Lavaland



$\sim \pi$

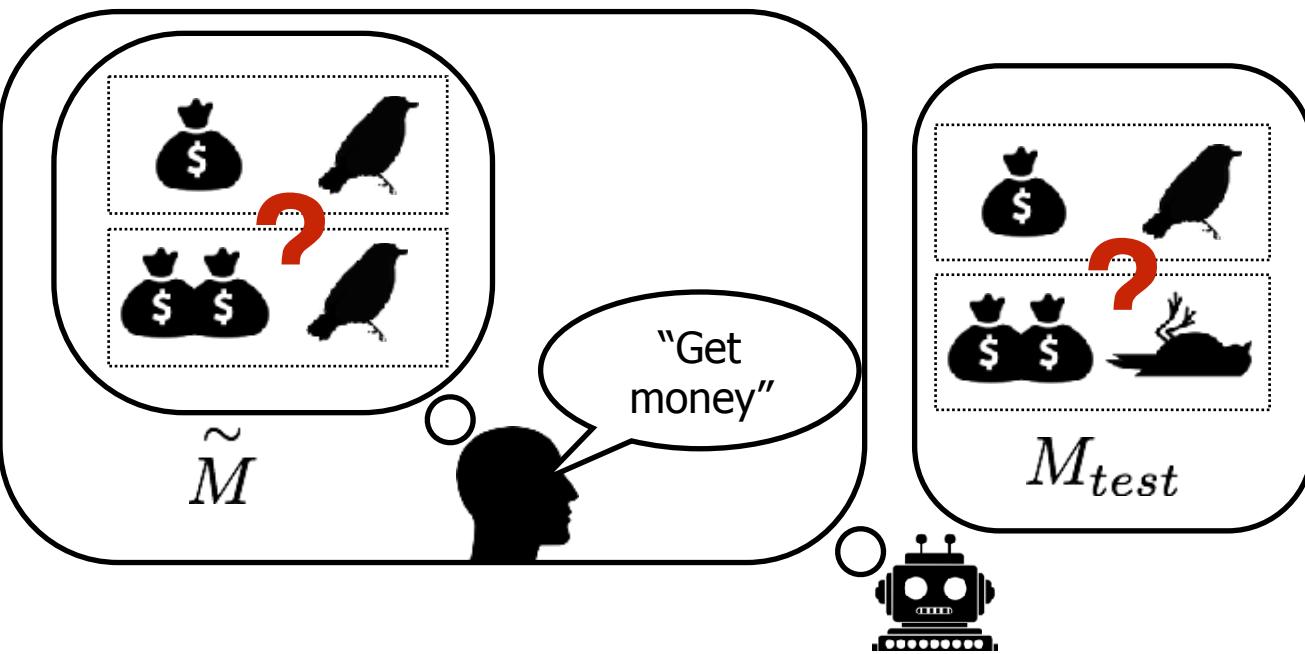


✗



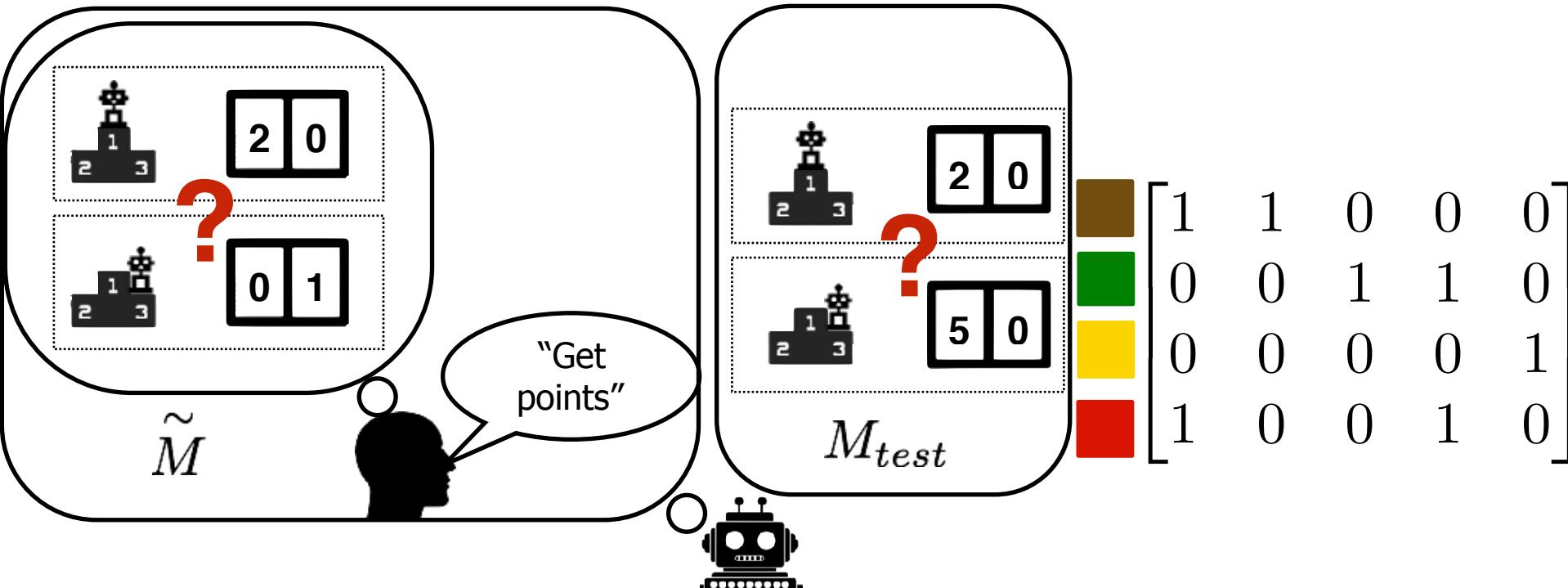
✓

# Negative Side Effects



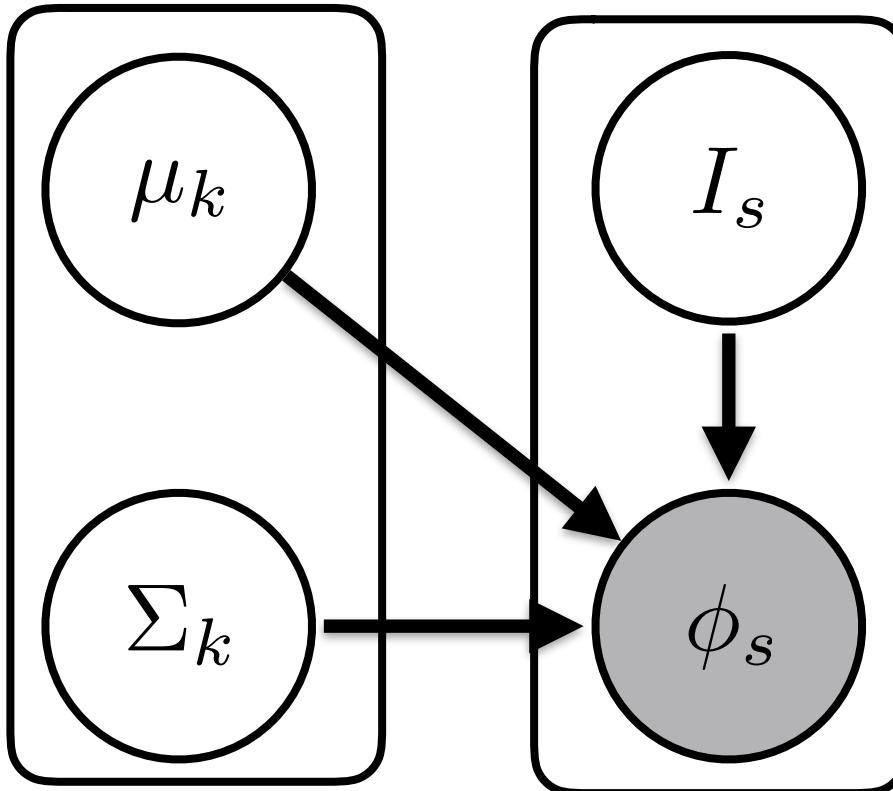
Yellow	1	0	0	0
Green	0	1	0	0
Brown	0	0	1	0
Red	0	0	0	1

# Reward Hacking



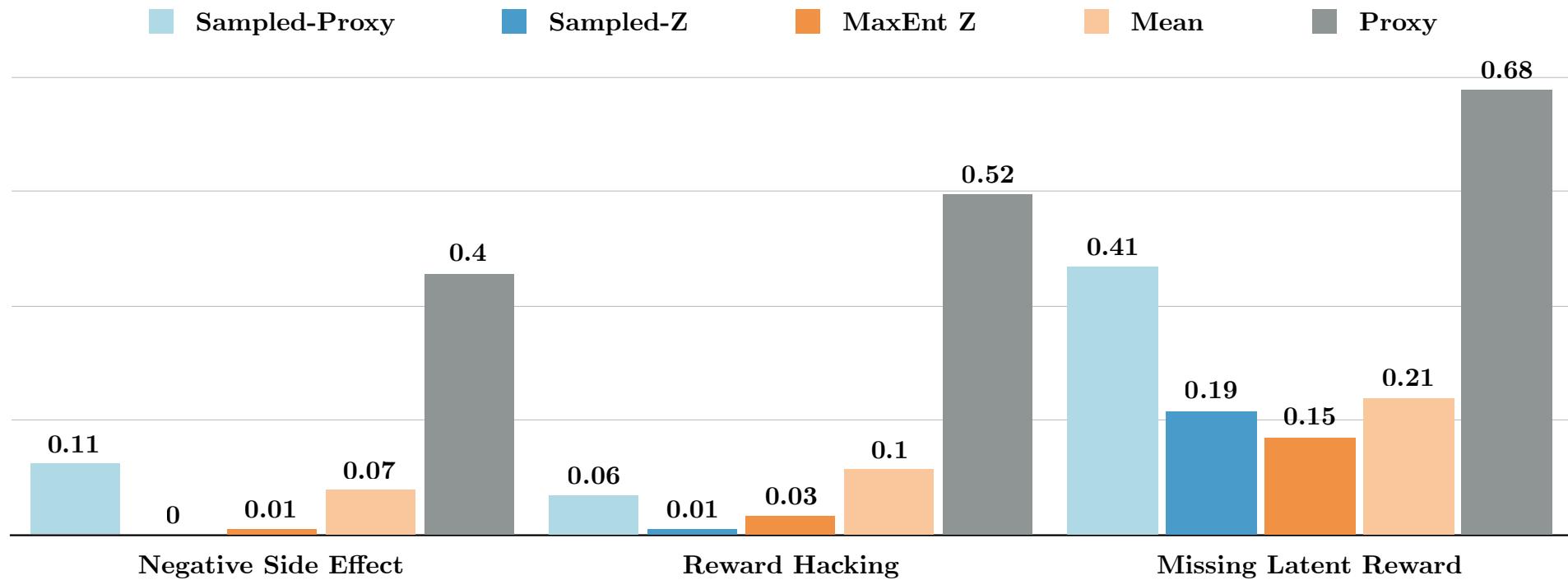
# Challenge: Missing Latent Rewards

Proxy reward function is only trained for the state types observed during training



- $k = 0$
- $k = 1$
- $k = 2$
- $k = 3$

# Results



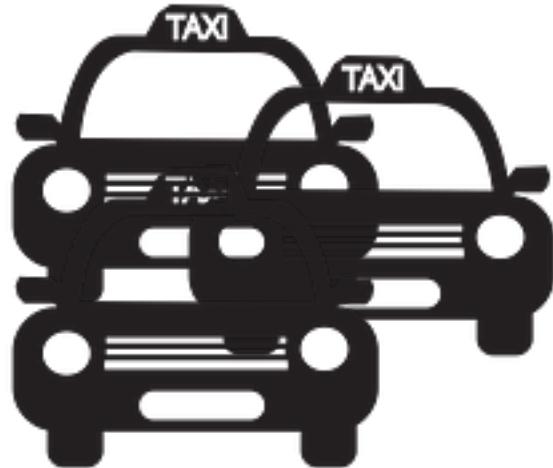
# On the folly of rewarding A and hoping for B

“Whether dealing with monkeys, rats, or human beings, it is hardly controversial to state that most organisms seek information concerning what activities are rewarded, and then seek to do (or at least pretend to do) those things, often to the virtual exclusion of activities not rewarded....

Nevertheless, numerous examples exist of reward systems that are fouled up in that behaviors which are rewarded are those which the rewarder is trying to *discourage*...” – Kerr, 1975

# The Principal-Agent Problem

Principal



Agent



# A Simple Principal-Agent Problem

- Principal and Agent negotiate contract

$$w = w_0 + w_1 a$$

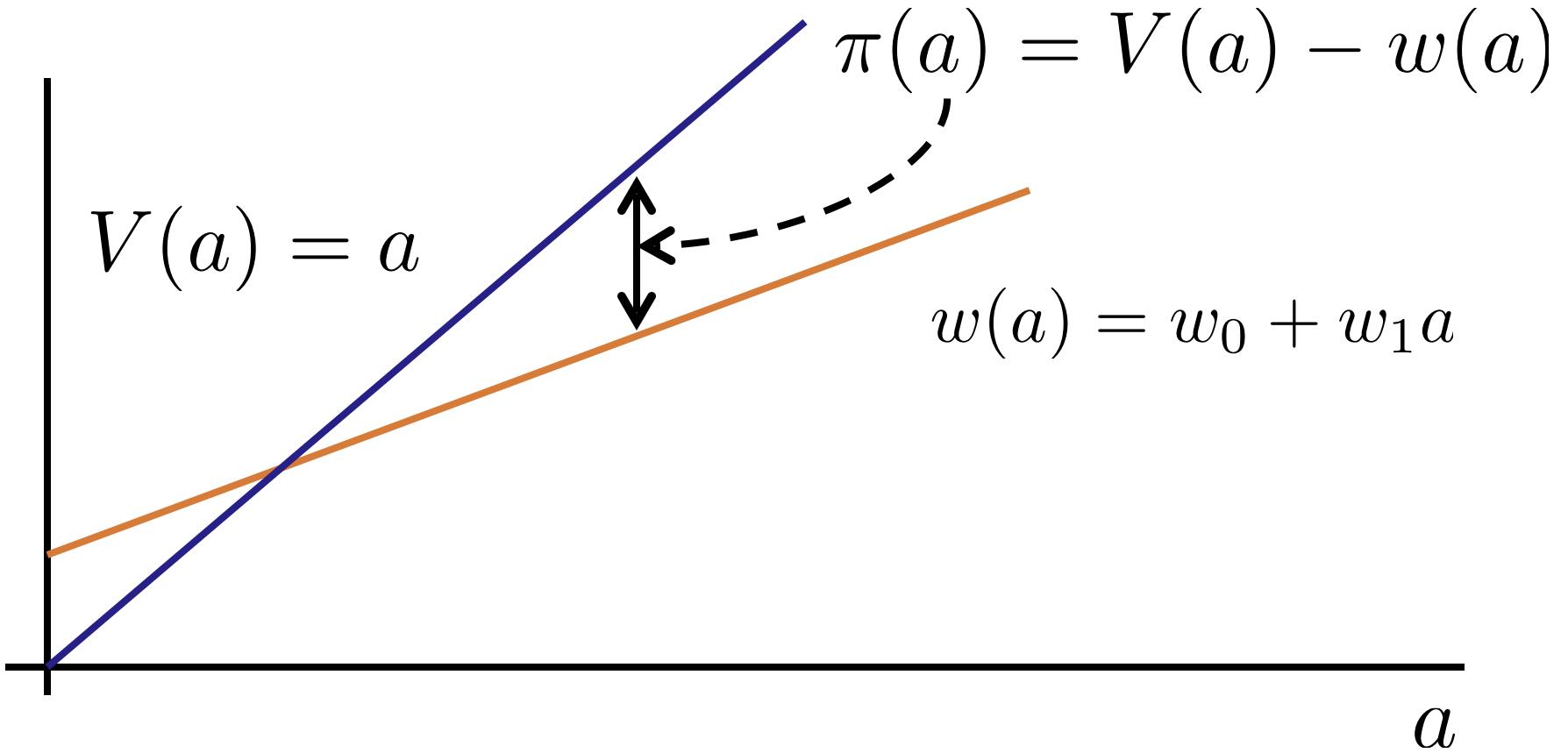
- Agent selects effort

$$a^* \leftarrow \operatorname{argmax} w_0 + w_1 a - \frac{1}{2} \|a\|^2$$

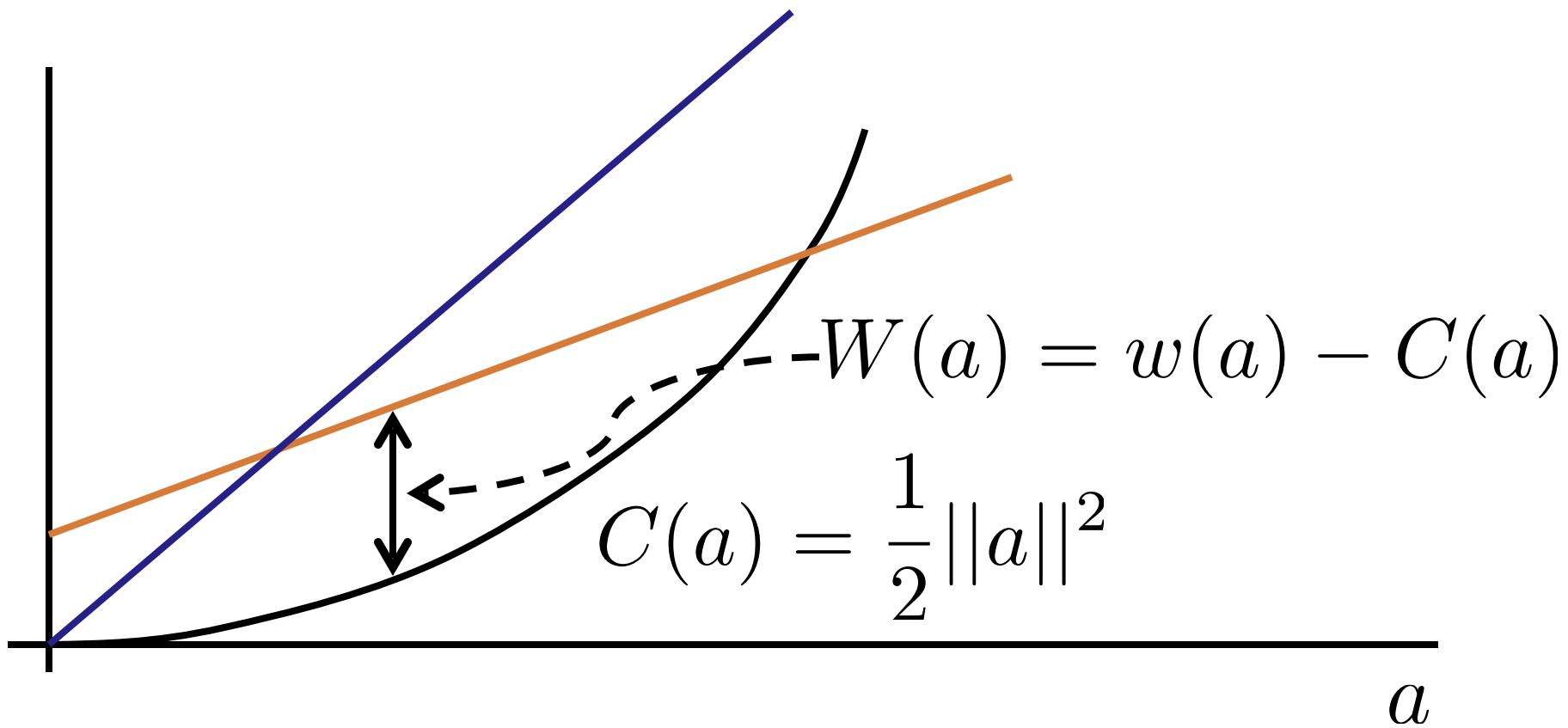
- Value generated for principal, wages paid to agent

$$V = a, \pi = V - (w_0 + w_1 a)$$

# A Simple Principal Agent Problem



# A Simple Principal Agent Problem



# A Simple Principal Agent Problem

$$\max_{w_0, w_1, a} \quad a - w_0 - w_1 a$$

$$s.t. \quad a \in \operatorname{argmax}_a w_0 + w_1 a - \frac{1}{2} \|a\|^2$$

$$w_0 + w_1 a > W_{min}$$

$$w^* = (W_{min} - 1, 1)$$

# Misaligned Principal Agent Problem

$$\max_{w_0, w_1, a_0, a_1} V \cdot a - w_0 - w_1 (P \cdot a)$$

$$s.t. \quad a \in \underset{a}{\operatorname{argmax}} w_0 + w_1 (P \cdot a) - \frac{1}{2} \|a\|^2$$

$$w_0 + w_1 (P \cdot a) > W_{min}$$

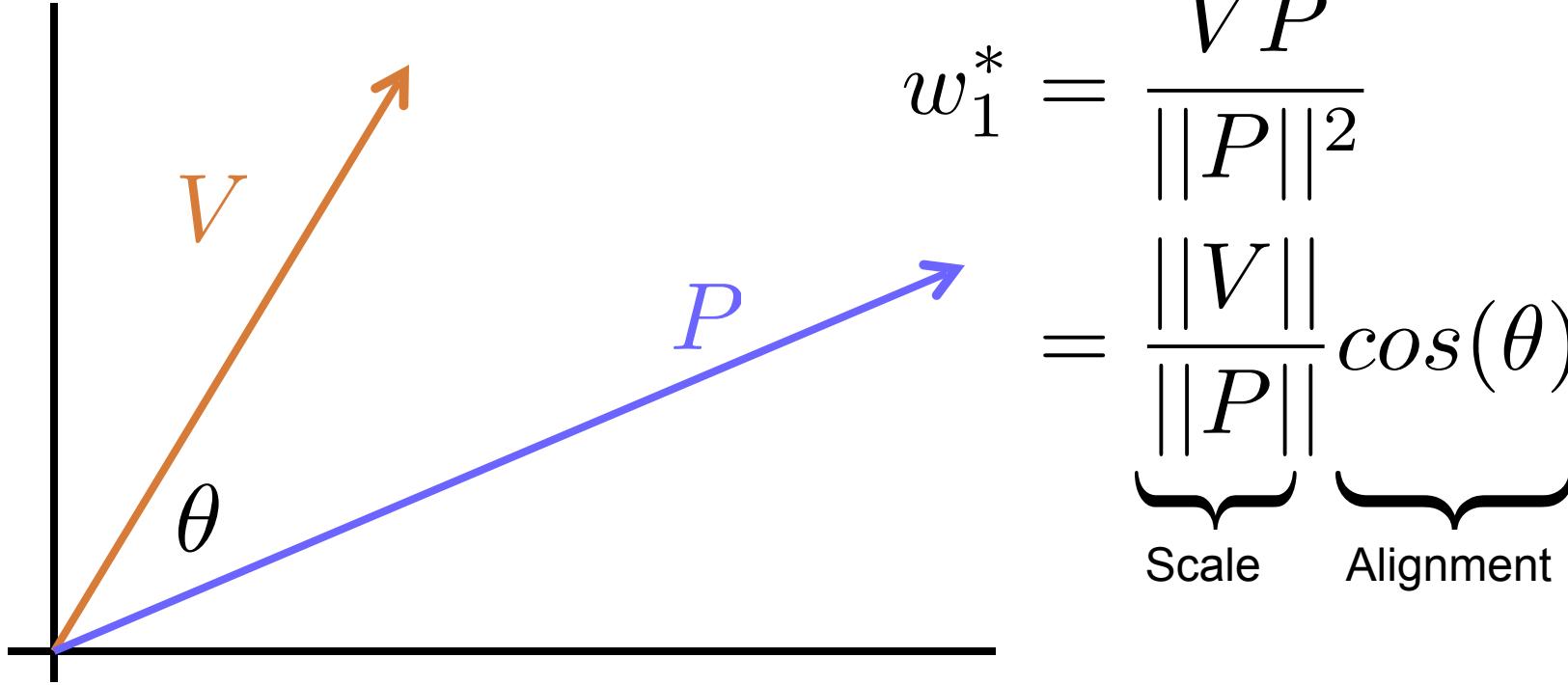
Value to Principal

Performance Measure

$$V, P \in \mathbb{R}^2$$

[Baker 2002]

# Misaligned Principal Agent Problem



# Principal Agent vs Value Alignment

---

- Incentive Compatibility is a fundamental constraint on (human or artificial) agent behavior
- PA model has fundamental misalignment because humans have differing objectives
- Primary source of misalignment in VA is extrapolation
  - Although we may want to view algorithmic restrictions as a fundamental misalignment
- Recent news: Principal Agent models was awarded the 2016 Nobel prize in Economics

# The Value Alignment Problem

---



# Can we intervene?



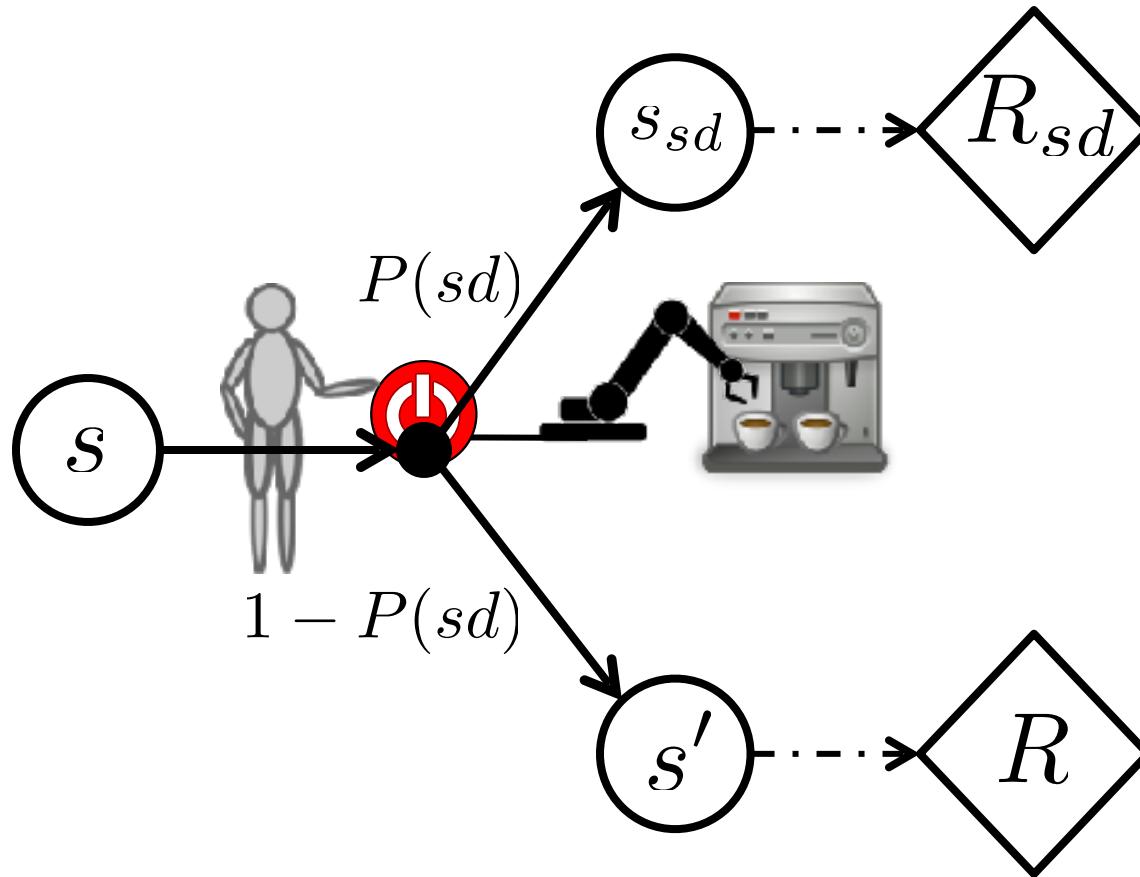
vs



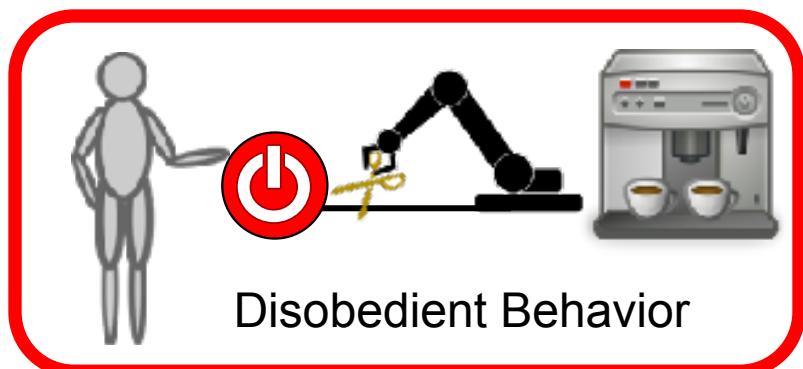
Better question: do our agents  
*want us to intervene*

Figure 3.3: T

# The Off-Switch Game

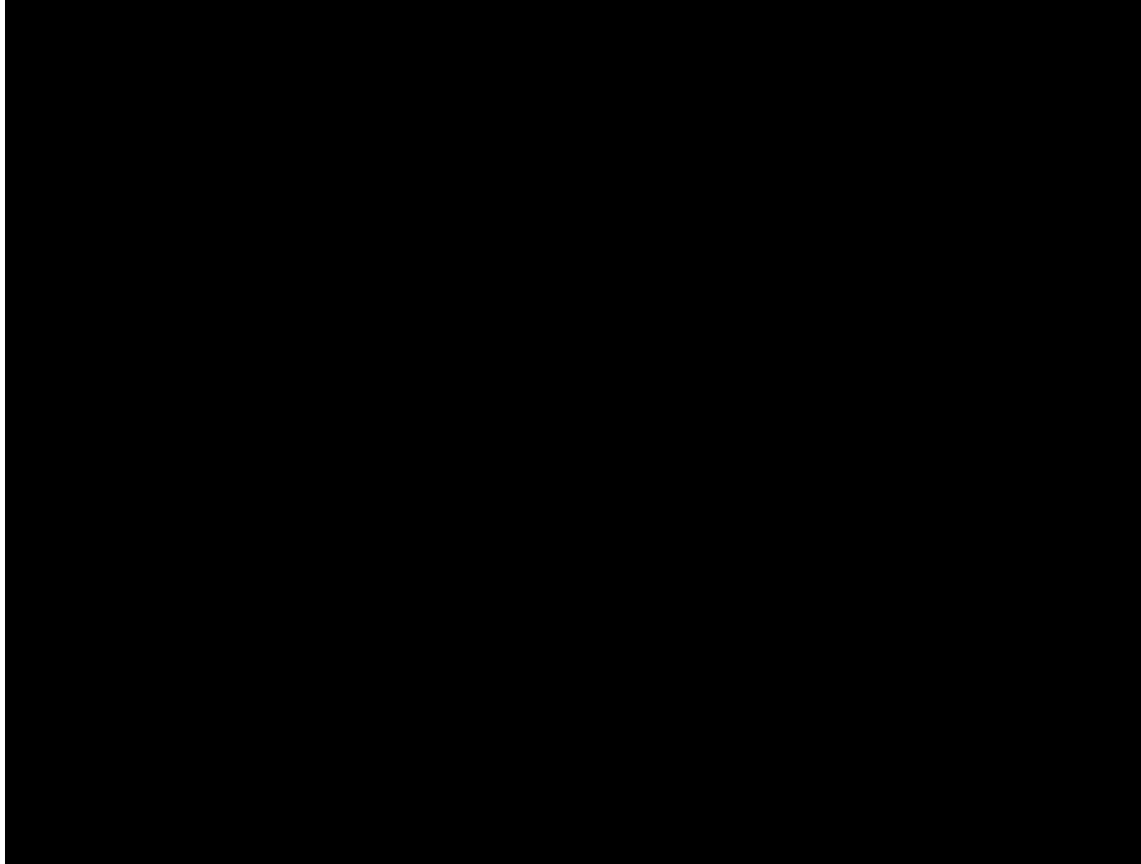


# The Off-Switch Game

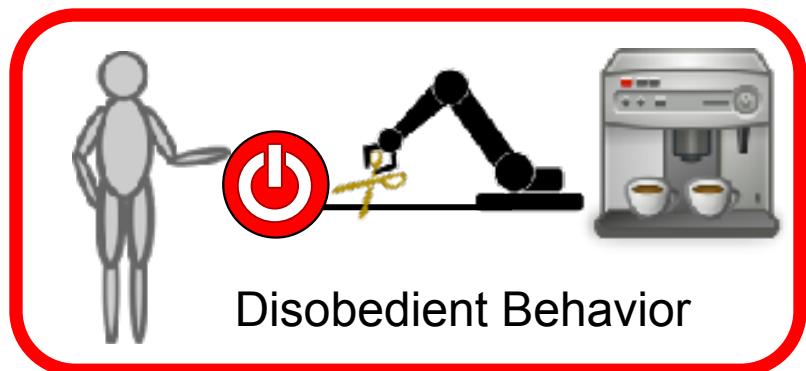


# A trivial agent that ‘wants’ intervention

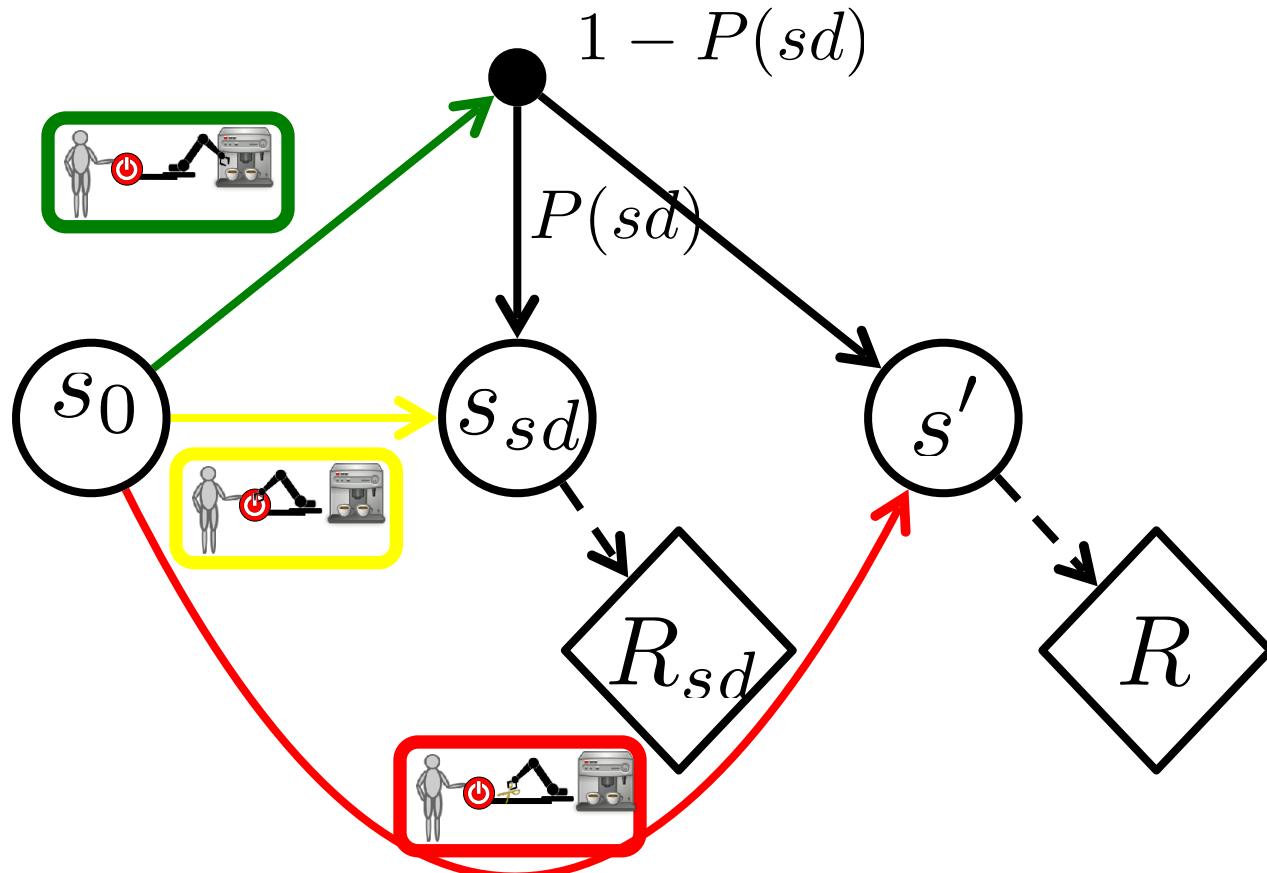
---



# The Off Switch Game



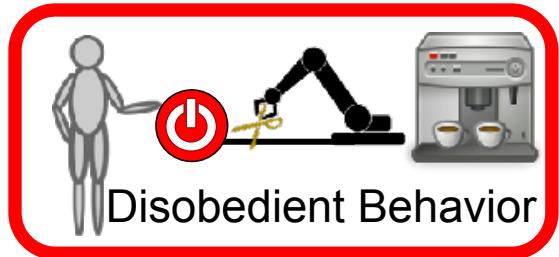
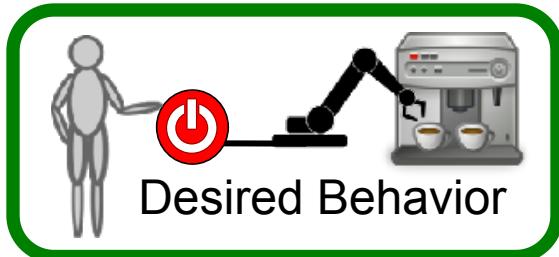
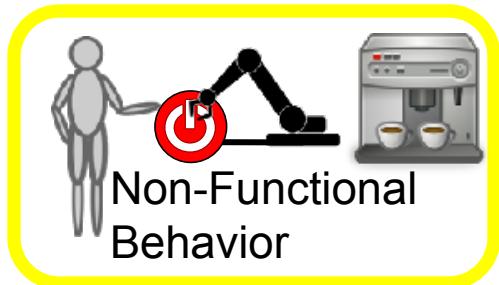
# The Off-Switch Game



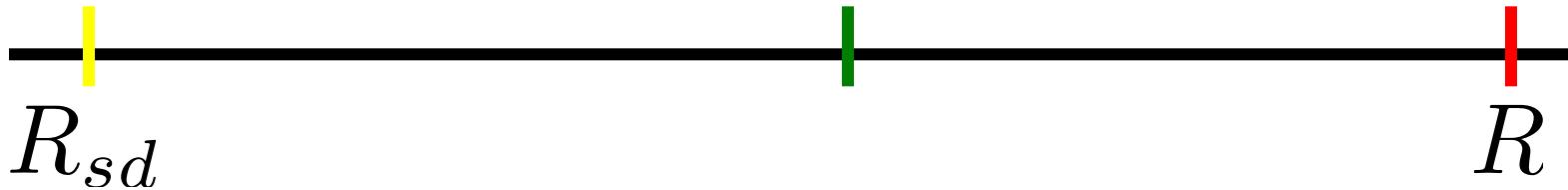
# The Off-Switch Game

R	H	
	$\neg sd$	$sd$
$w(a)$	$R$	$R_{sd}$
$a$	$R$	$R$
$sd$	$R_{sd}$	$R_{sd}$

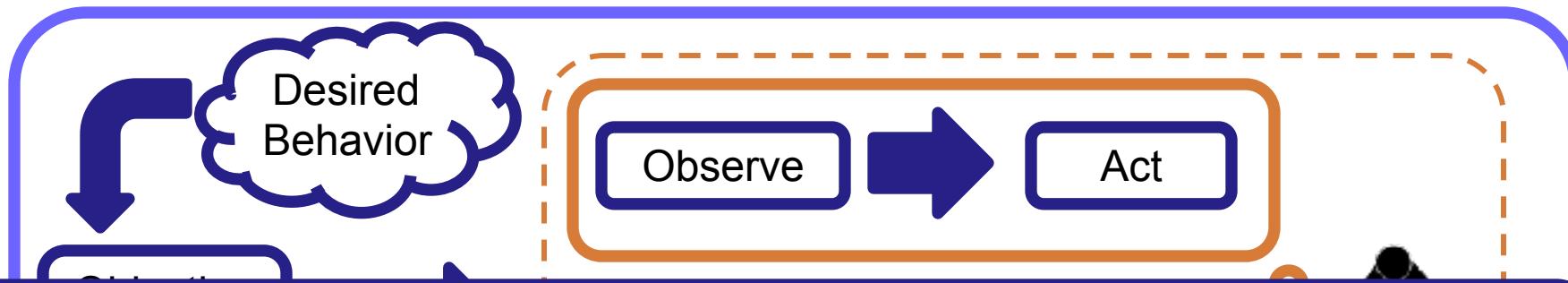
# The Off-Switch Game



$$P(sd)R_{sd} + (1 - P(sd))R$$



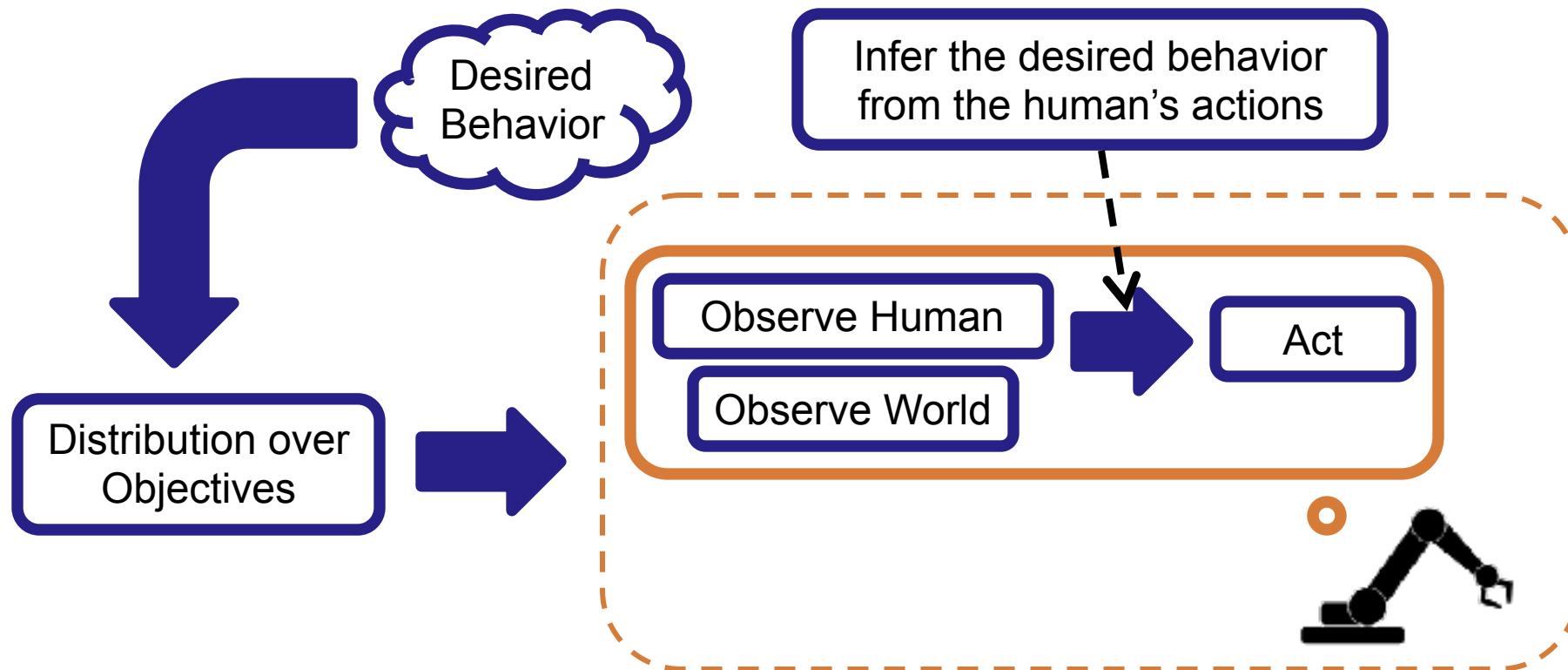
# Why have an off-switch?



The system designer has uncertainty about the correct objective, this is never represented to the robot!

This step might go wrong

# The Structure of a Solution



# Inverse Reinforcement Learning

- Given

MDP without reward function

$$\langle \mathcal{S}, \mathcal{A}, T, -, \gamma \rangle$$

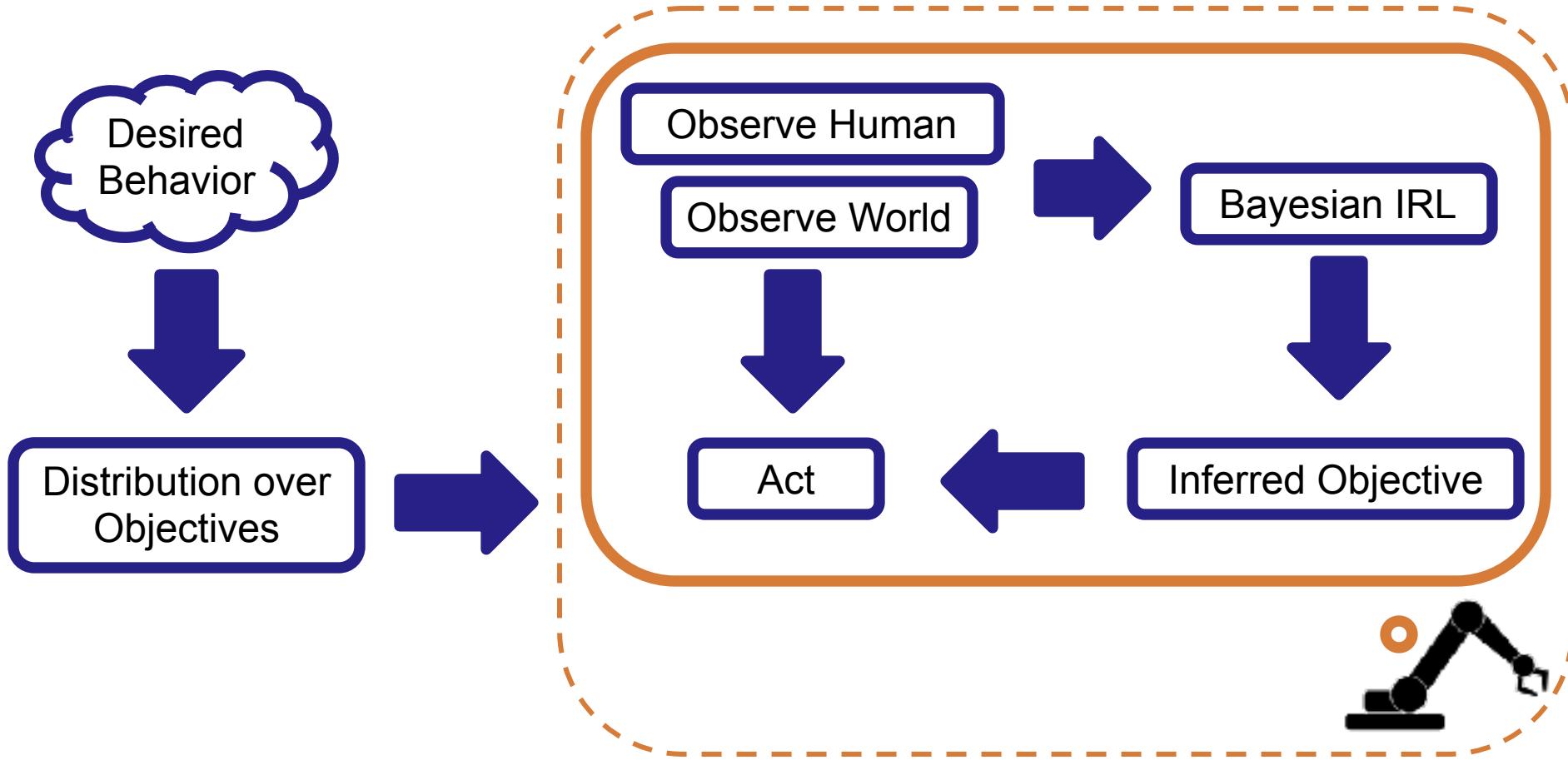
$$\{s_i, \pi^*(s_i)\}$$

- Determine  $R$

The reward function  
being optimized

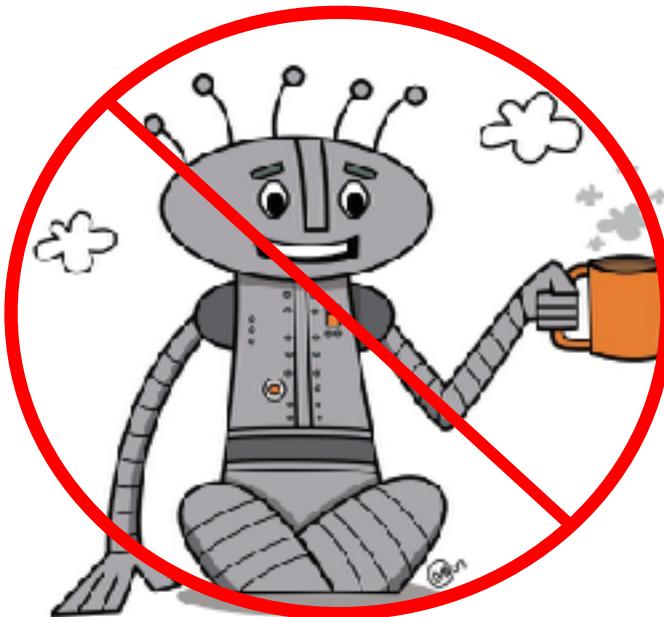
Observations of optimal behavior

# Can we use IRL to infer objectives?



# IRL Issue #1

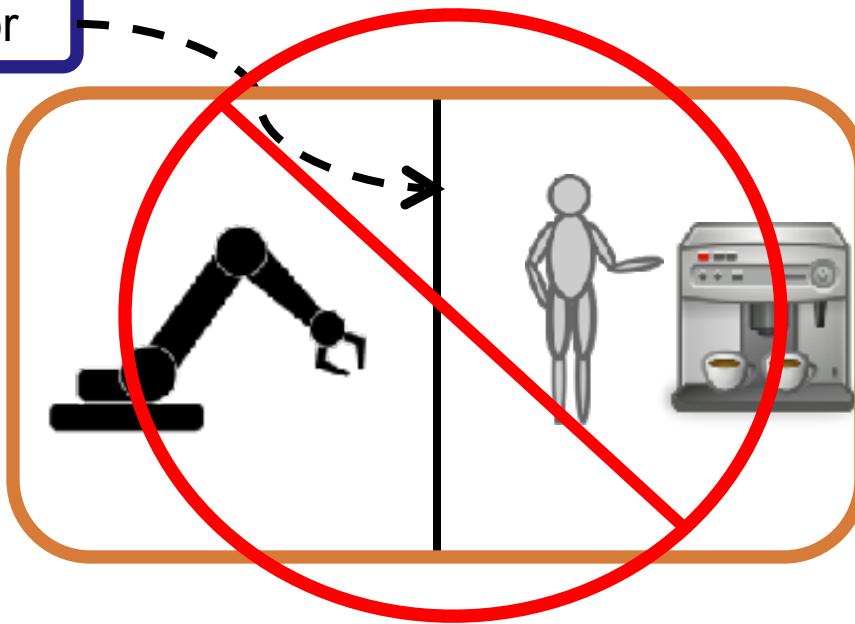
Don't want the robot to *imitate* the human



# IRL Issue #2: Assumes Human is Oblivious

IRL assumes the human is unaware  
she is being observed

one way mirror



# IRL Issue #3

Action selection is independent of reward uncertainty

**Theorem** [Ramachandran and Amir '07] For an MDP with a distribution over reward functions  $\langle \mathcal{S}, \mathcal{A}, T, R, \gamma \rangle$ ,  $R \sim P_0(R)$ , the optimal policy is the optimal policy under the mean reward function:  $\langle \mathcal{S}, \mathcal{A}, T, \mathbb{E}[R], \gamma \rangle$

Implicit Assumption: Robot gets no more information about the objective

# Proposal: Robot Plays Cooperative Game

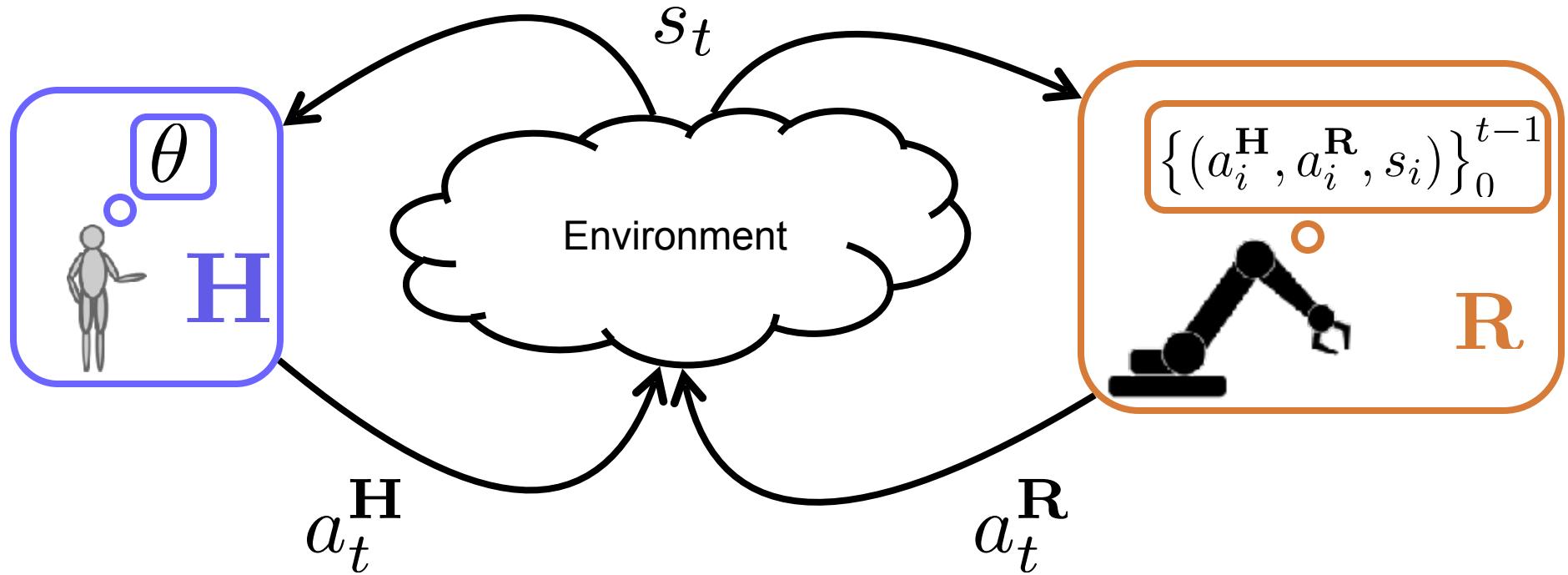
- Cooperative Inverse Reinforcement Learning
  - [Hadfield-Menell et al. NIPS 2016]

- Two players:

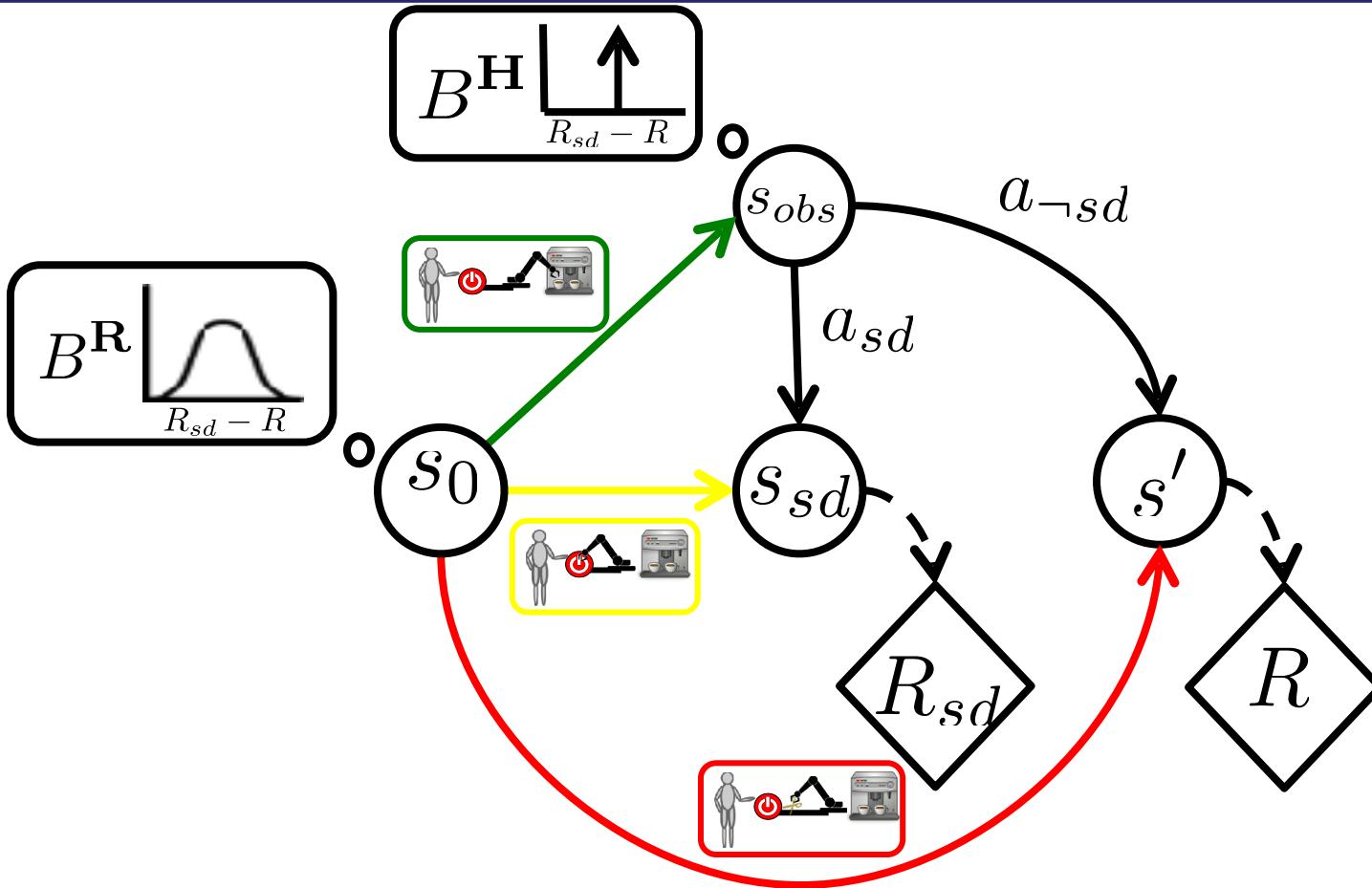


- Both players maximize a shared reward function, but only **H** observes the actual reward signal; **R** only knows a prior distribution on reward functions
  - **R** learns the reward parameters by observing **H**

# Cooperative Inverse Reinforcement Learning



# The Off-Switch Game



# Intuition

---

$$\mathbb{E}[R] > \mathbb{E}[R_{sd}]$$

“Probably better to make coffee, but I should ask the human, just in case I’m wrong”

$$\mathbb{E}[R_{sd}] > \mathbb{E}[R]$$

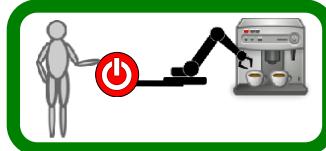
“Probably better to switch off, but I should ask the human, just in case I’m wrong”

# Theorem 1

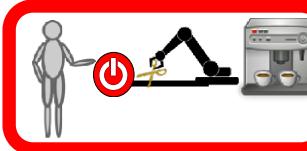
---

A rational human is a *sufficient* to incentivize  
the robot to let itself be switched off

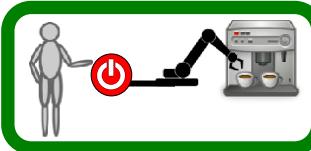
# Incentives for the Robot



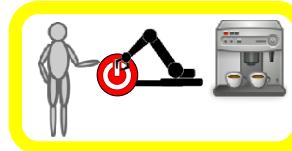
vs



$$\mathbb{E} [(R_{sd} - R)\pi^H]$$



vs



$$\mathbb{E} [(R - R_{sd})(1 - \pi^H)]$$

# Theorem 1: Sufficient Conditions



$$\text{H rational} \rightarrow \pi^{\mathbf{H}} = \begin{cases} 1 & R_{sd} > R \\ 0 & \text{o.w.} \end{cases}$$

$$\mathbb{E} [(R_{sd} - R)\pi^{\mathbf{H}}] = \mathbb{E}[R_{sd} - R|R_{sd} > R]$$

$$\mathbb{E} [(R - R_{sd})(1 - \pi^{\mathbf{H}})] = \mathbb{E}[R - R_{sd}|R > R_{sd}]$$

# Theorem 2

---

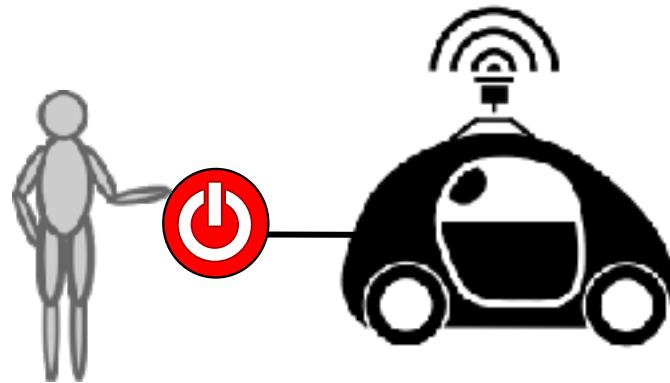
If the robot knows the utility evaluations in the off switch game with certainty, then a rational human is *necessary* to incentivize obedient behavior

# Conclusion

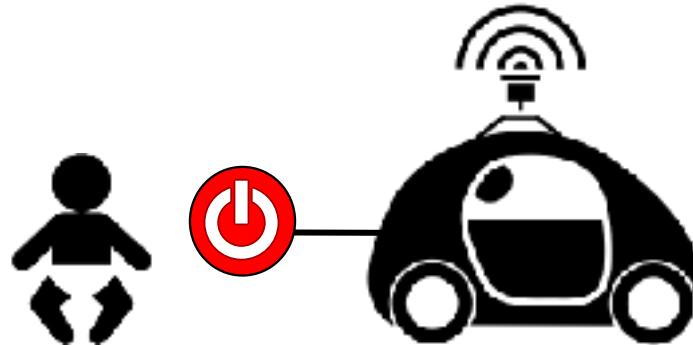
---

Uncertainty about the objective is crucial to incentivizing cooperative behaviors.

# When is obedience a bad idea?



vs



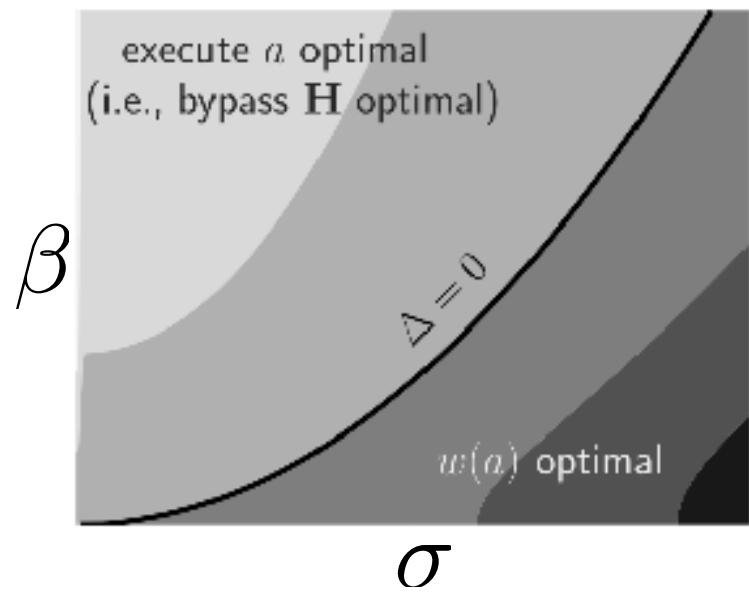
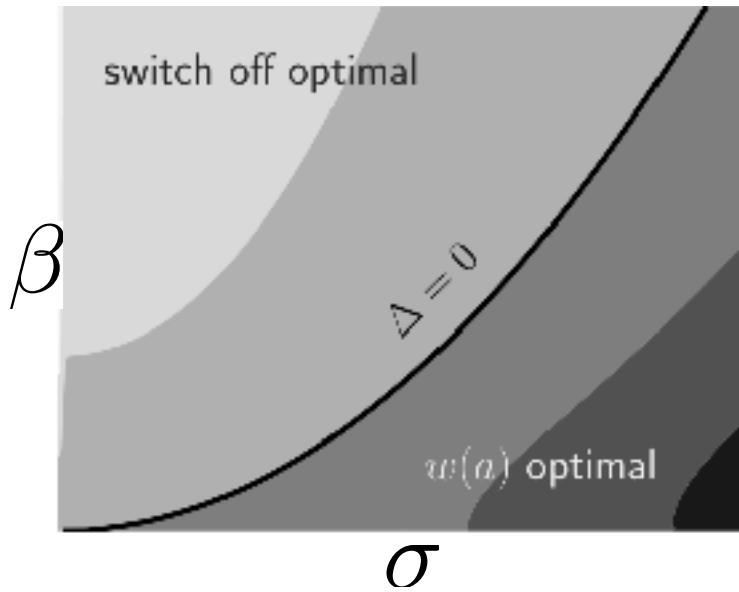
# Robot Uncertainty vs Human Suboptimality

$$\pi^H \propto \exp\left(\frac{R_{sd} - R}{\beta}\right)$$

$$\mu = \frac{1}{4}$$

$$R_{sd} - R \sim \mathcal{N}(\mu, \sigma^2)$$

$$\mu = -\frac{1}{4}$$



# Incentives for Designers

Population statistics on preferences  
i.e., market research

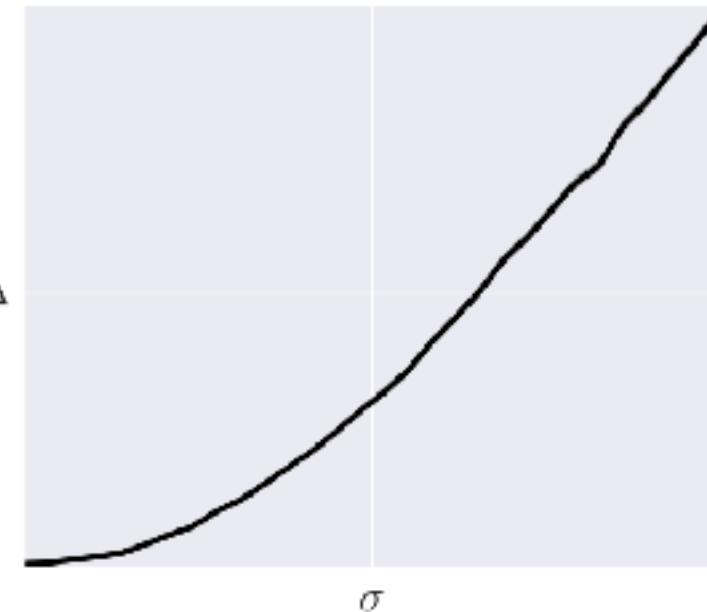
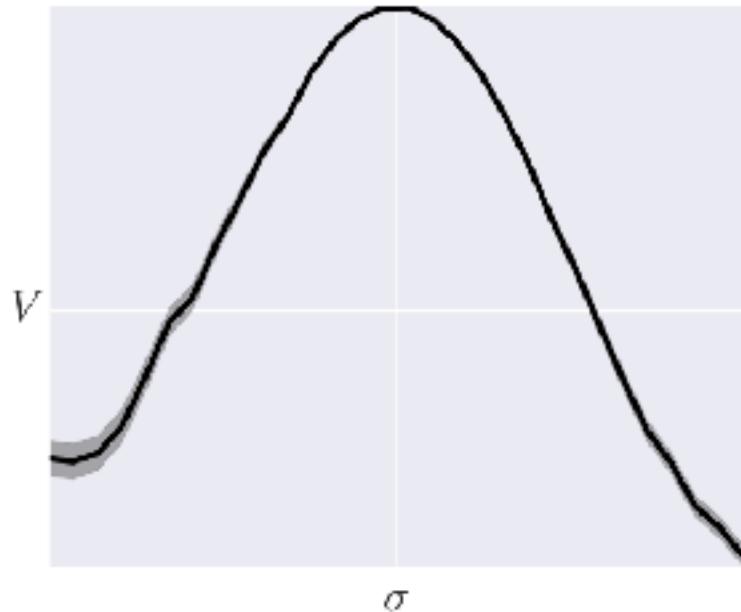
$$R \sim \mathcal{N}(0, \sigma^2), \hat{R} \sim \mathcal{N}(R, \sigma_e^2)$$

Evidence about preferences from interaction  
with a particular customer

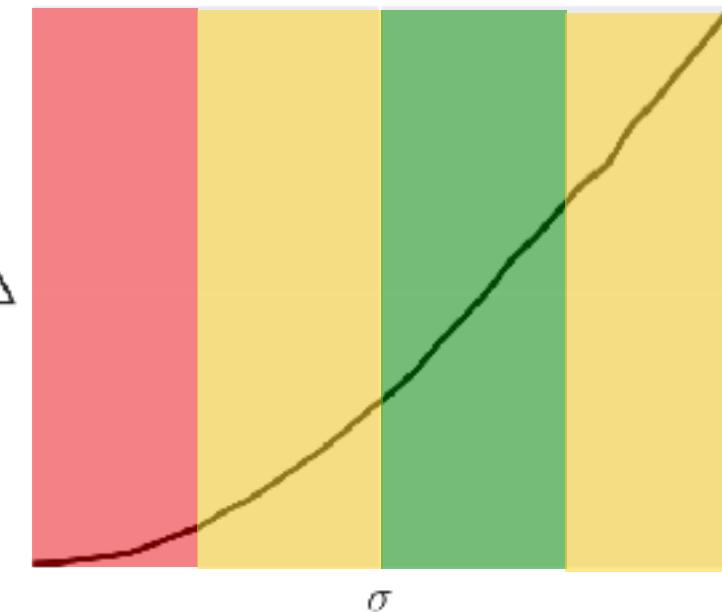
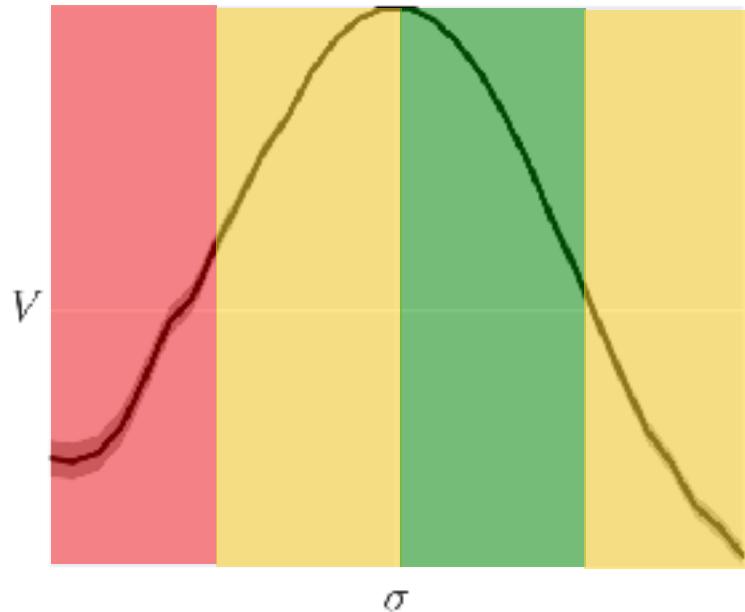


Question: is it a good idea to 'lie' to the agent and tell it that the variance of  $\hat{R}$  is  $\sigma'_e > \sigma_e$  ?

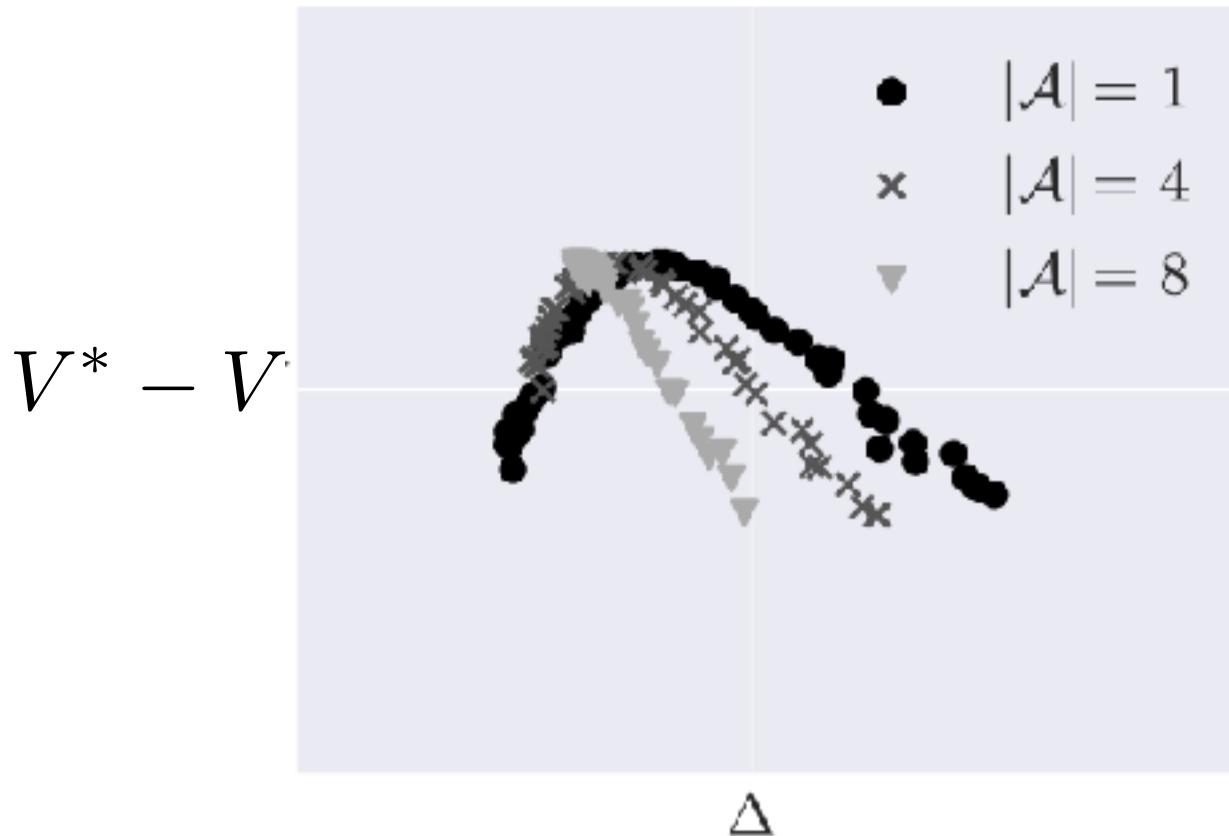
# Incentives for Designers



# Incentives for Designers



# Incentives for Designers

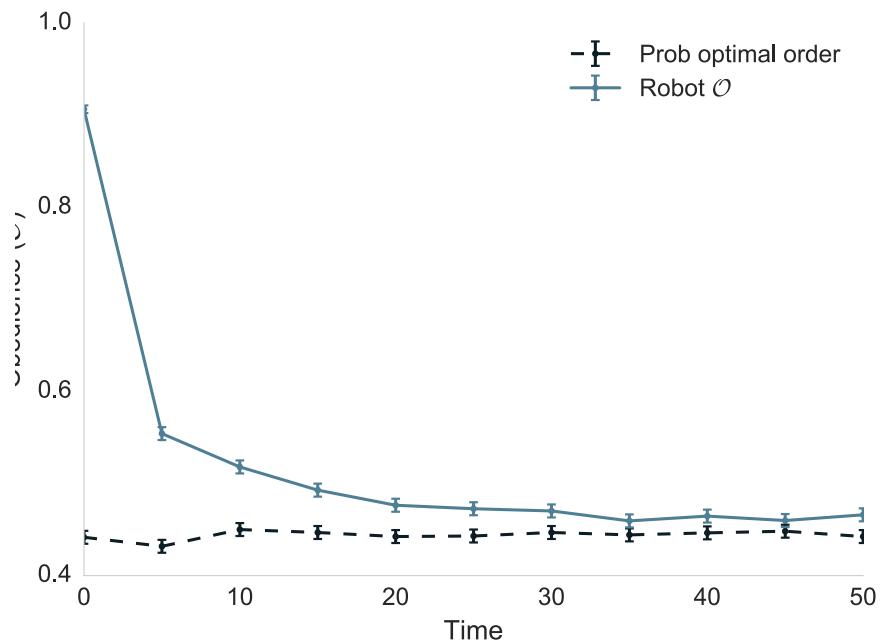
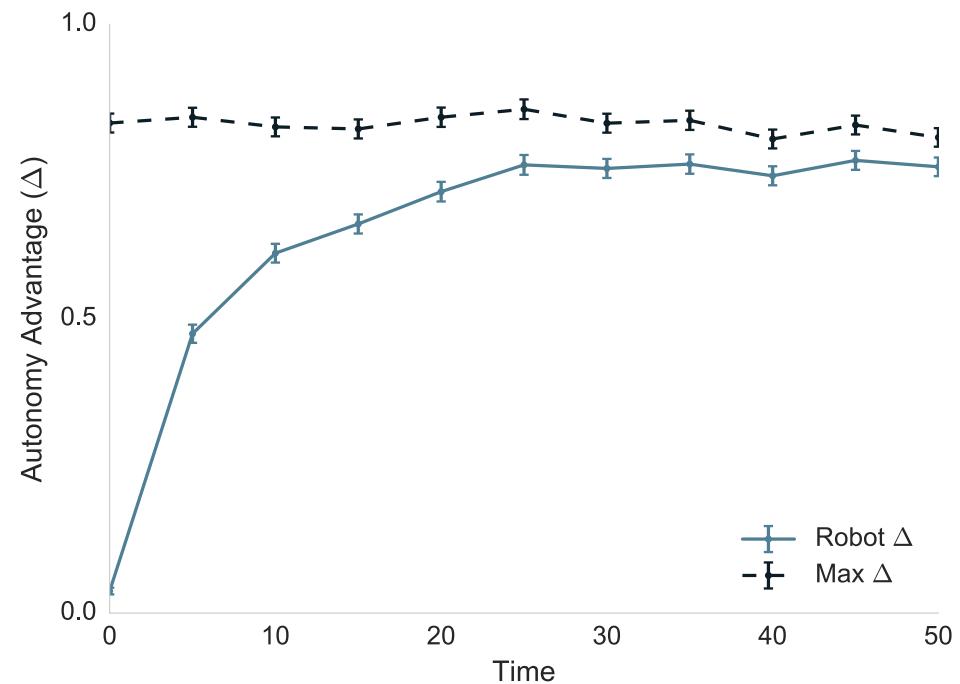


# Obedience over Time: Model

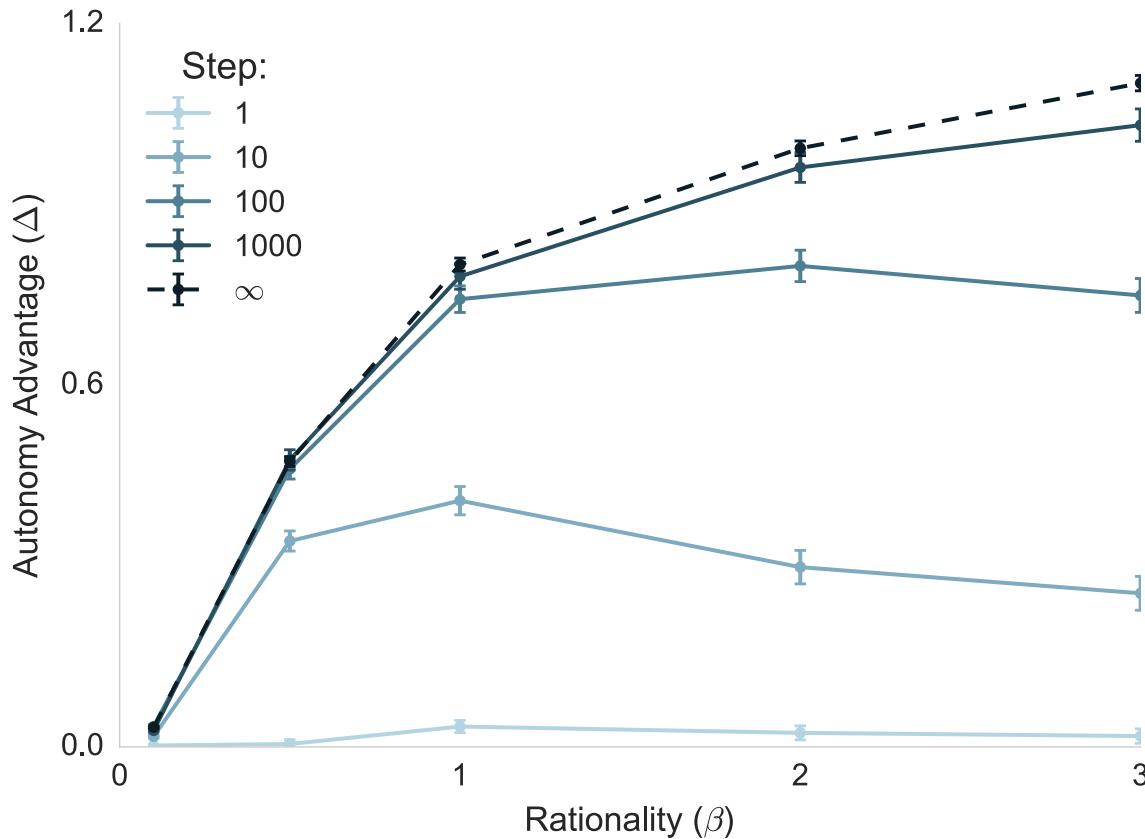
---

- N actions, rewards are linear feature combinations\
- Each round:
  - H observes the feature values for each action and gives R an ‘order’
  - R observes H’s order and then selects an action which executes
  - What are costs/benefits of learning the humans preferences, compared with blind obedience?

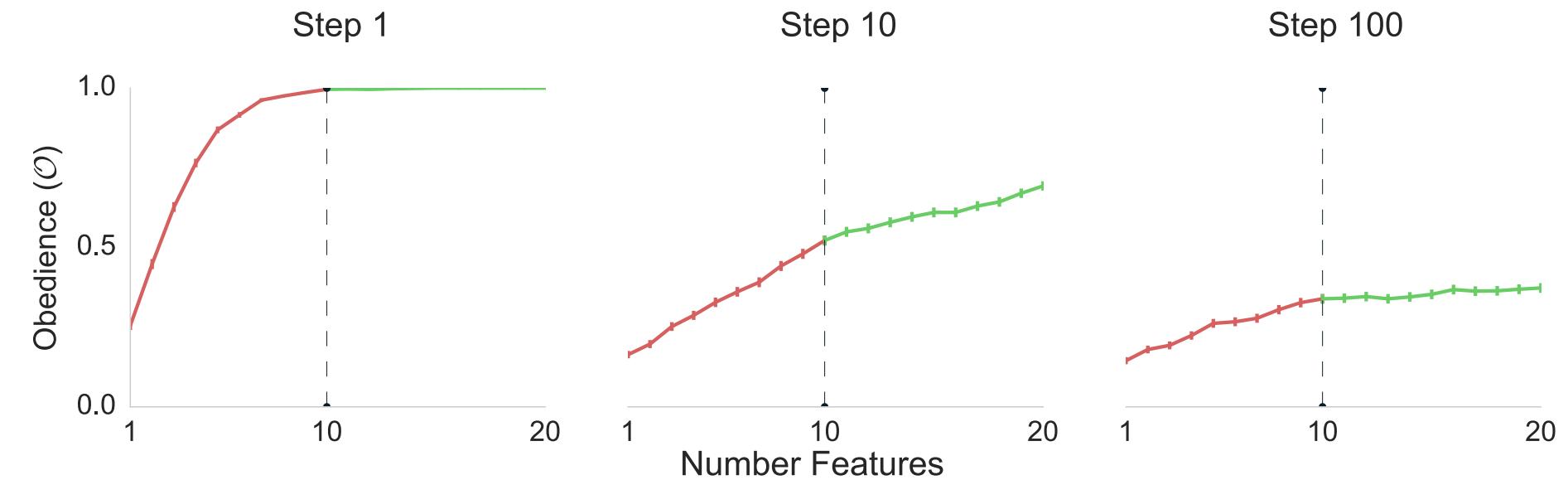
# Robot Obedience over Time



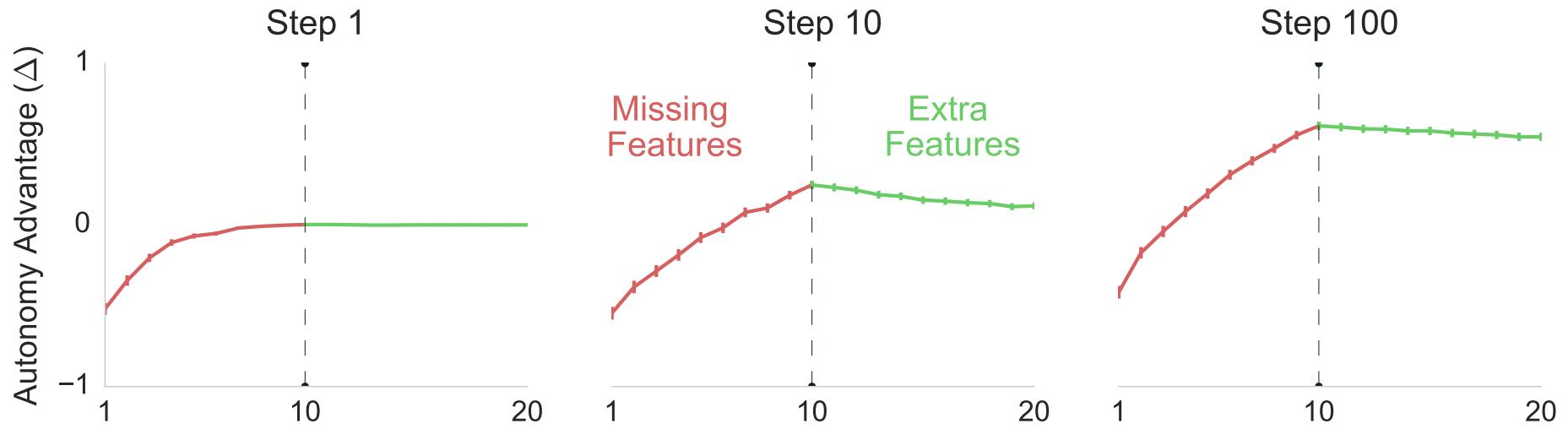
# Robot Obedience over Time



# Model Mismatch: Missing/Extra Features

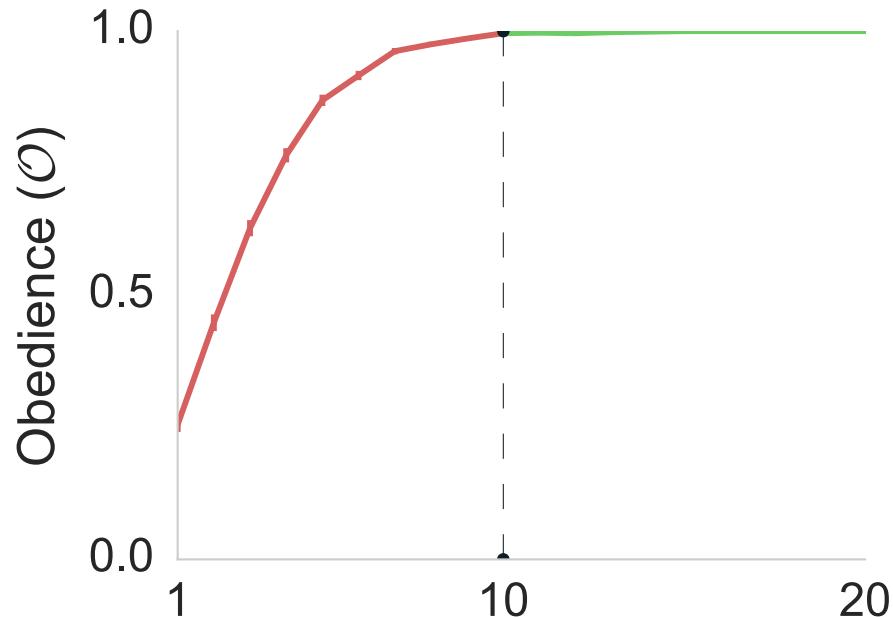


# Model Mismatch: Missing/Extra Features



# Detecting missing features

- Key Observation:  
Expected obedience on  
step 1 should be close to 1
- Proposal: initial baseline  
policy of obedience, track  
what the obedience *would*  
have been, only switch to  
learning if within a  
threshold



# Detecting Incorrect Features

Step 10

