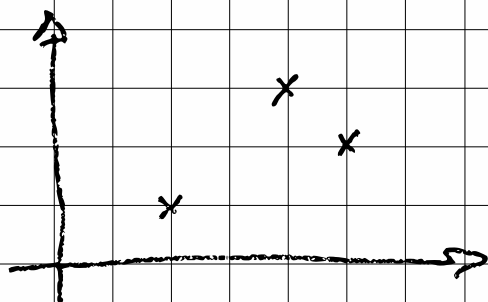


①



$$\frac{1}{N} \sum_{i=1}^n (y_i - (ax_i + b))^2 \quad (\text{Error}(a, b))$$

$$\frac{\partial \text{Error}}{\partial a} = \frac{1}{N} \sum_{i=1}^n 2(y_i - ax_i - b)(-x_i) = 0$$

$$\frac{\sum_{i=1}^n x_i y_i - \sum_{i=1}^n b x_i}{\sum_{i=1}^n x_i^2} = a$$

$$\frac{\partial F}{\partial b} \frac{1}{N} \sum_{i=1}^n (y_i - ax_i - b)^2 = \frac{1}{N} \sum_{i=1}^n 2(y_i - ax_i - b)(-1) = 0$$

$$= \frac{\sum_{i=1}^n (-y_i + ax_i + b)}{N}$$

$$= \frac{\sum_{i=1}^n y_i}{N} + \frac{\sum_{i=1}^n x_i y_i - \sum_{i=1}^n b x_i}{\sum_{i=1}^n x_i^2} x_i + nb = 0$$

$$\frac{\sum_{i=1}^n x_i y_i - \sum_{i=1}^n b x_i}{\sum_{i=1}^n x_i^2} x_i + nb = \sum_{i=1}^n y_i$$

$$\frac{\partial}{\partial b} \left[\frac{1}{N} \sum (y_i - (ax_i + b))^2 \right] = 0$$

$$\frac{1}{N} \sum 2(y_i - ax_i - b)(-1) = 0$$

$$\sum -\frac{2}{N} (y_i - ax_i - b) = 0$$

$$\sum -\frac{2}{N} y_i + \frac{2}{N} ax_i + \frac{2}{N} b = 0$$

$$a \sum x_i + \sum b = \sum y_i$$

$$\frac{\sum x_i \sum x_i y_i}{\sum x_i^2} - \frac{b(\sum x_i)^2}{\sum x_i^2} + bn = \sum y_i$$

$$\frac{1}{\sum x_i^2} (\sum x_i \sum x_i y_i - b(\sum x_i)^2 + bn \sum x_i^2) = \sum y_i$$

$$\sum x_i \sum x_i y_i - b((\sum x_i)^2 - n \sum x_i^2) = \sum y_i \sum x_i^2$$

$$-b((\sum x_i)^2 - n \sum x_i^2) = \sum y_i \sum x_i^2 - \sum x_i \sum x_i y_i$$

$$-b = \frac{\sum y_i \sum x_i^2 - \sum x_i \sum x_i y_i}{(\sum x_i)^2 - n \sum x_i^2}$$

$$b = \frac{\sum x_i \sum x_i y_i - \sum y_i \sum x_i^2}{(\sum x_i)^2 - n \sum x_i^2} \quad (b)$$

back substitution

$$a = \frac{\sum x_i y_i}{\sum x_i^2} - \frac{(\sum x_i)^2 \sum x_i y_i - \sum x_i \sum y_i \sum x_i^2}{(\sum x_i)^2 \sum x_i^2 - n \sum x_i^2 \sum x_i^2}$$

$$a = \frac{\sum x_i y_i}{\sum x_i^2} -$$

$$\frac{\sum x_i y_i}{\sum x_i^2} - \frac{(\sum x_i \sum x_i y_i - \sum y_i \sum x_i^2) \sum x_i}{((\sum x_i)^2 - n \sum x_i^2) \sum x_i^2}$$

$$\frac{\sum x_i y_i ((\sum x_i)^2 - n \sum x_i^2) - (\sum x_i \sum x_i y_i - \sum y_i \sum x_i^2) \sum x_i}{((\sum x_i)^2 - n \sum x_i^2) \sum x_i^2}$$

$$\frac{(\sum x_i)^2 \sum x_i y_i - \sum x_i y_i \sum x_i^2 \cdot n - (\sum x_i)^2 \sum x_i y_i + \sum x_i \sum y_i \sum x_i^2}{\sum x_i^2 ((\sum x_i)^2 - n \sum x_i^2)}$$

$$\frac{\sum x_i^2 (\sum x_i \sum y_i - \sum x_i y_i \cdot n)}{\sum x_i^2 ((\sum x_i)^2 - n \cdot \sum x_i^2)} = \frac{\sum x_i \sum y_i - n \sum x_i y_i}{(\sum x_i)^2 - n \sum x_i^2}$$

(a)