

Optimisation and Statistical Data Analysis

Exercise Set 8 (Categorical distribution)

Problem 1

3% of the bottles produced in a factory are defective. Before the bottles are shipped, an inspector grades them “pass” or “fail”. The inspector fails 90% of bottles that are defective and fails 20% of bottles that are ok.

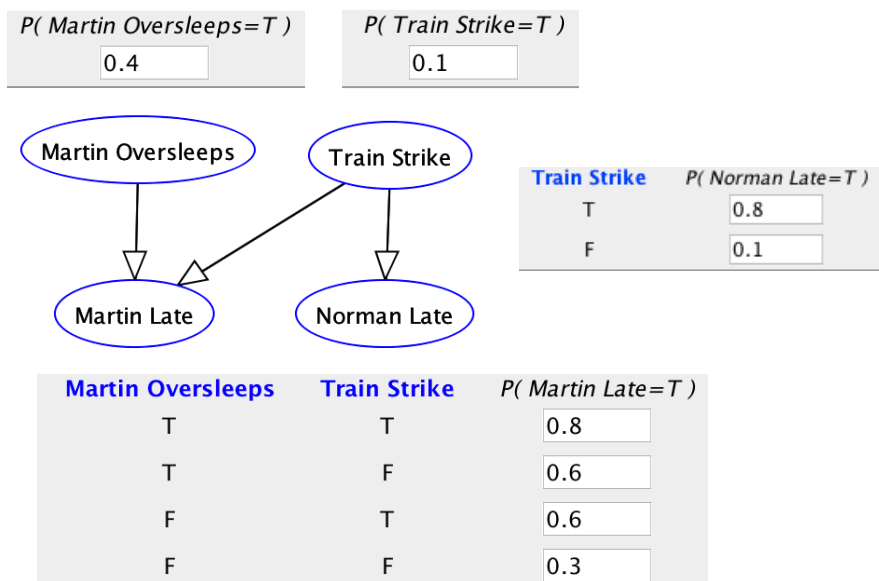
- (a) Use a frequency diagram for 1000 bottles to determine the probability that a failed bottle is defective and the probability that a passed bottle is defective.



- (b) Use Bayes' formula to find the probabilities in (a).
- (c) Suppose that a bottle is shipped if and only if it is passed by two independent inspectors. Using the answer from (b), find the probability that a shipped bottle is defective

Problem 2

Build the following belief network using the *Belief and decision network tool* from aispace.org/downloads.shtml/



- (a) You observe that Martin is late today. Which is the more probable cause of Martin's lateness, oversleeping or train strike?

- (b) You discover that Norman is also late. Now which is the most probable cause of Martin's lateness?
- (c) What is the probability that both Martin and Norman are late?

Extra problems

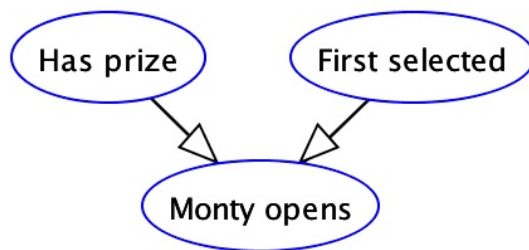
- (a) Solve problem 1 using the *Belief and decision network tool*.
- (b) Solve problem 2 using Bayes' formula.
- (c) Solve the Monty Hall problem (i.e. show that it is better to switch than not to switch) using a belief network with three nodes:

First selected: the door is first selected by the contestant;

Monty opens: the door is then opened by Monty Hall;

Has prize: the door has the prize.

Every node has three states: *door #1*, *door #2*, *door #3*.



Answers 1. (a) 12.22%, 0.39% (c) 0.05%
 2. (a) oversleeping (b) train strike (c) 9.22%