

# Introduction to Neural Networks

# About this Course (Course 1/5)

## Courses in this Specialization

- 1. Neural Networks and Deep Learning —
- 2. Improving Deep Neural Networks: Hyperparameter tuning, Regularization and Optimization
- 3. Structuring your Machine Learning project
- Convolutional Neural Networks
- 5. Natural Language Processing: Building sequence models

## Courses in this Specialization

#### 1. Neural Networks and Deep Learning

- Improving Deep Neural Networks: Hyperparameter tuning, Regularization and Optimization
- 3. Structuring your Machine Learning project
- Convolutional Neural Networks
- 5. Natural Language Processing: Building sequence models

#### Outline of this Course

Week 1: Introduction

Week 2: Basics of Neural Network programming

Week 3: One hidden layer Neural Networks

Week 4: Deep Neural Networks

#### Outline of this Course

#### Week 1: Introduction

Week 2: Basics of Neural Network programming

Week 3: One hidden layer Neural Networks

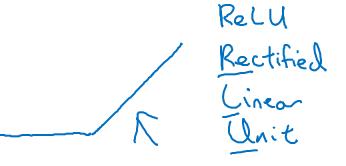
Week 4: Deep Neural Networks

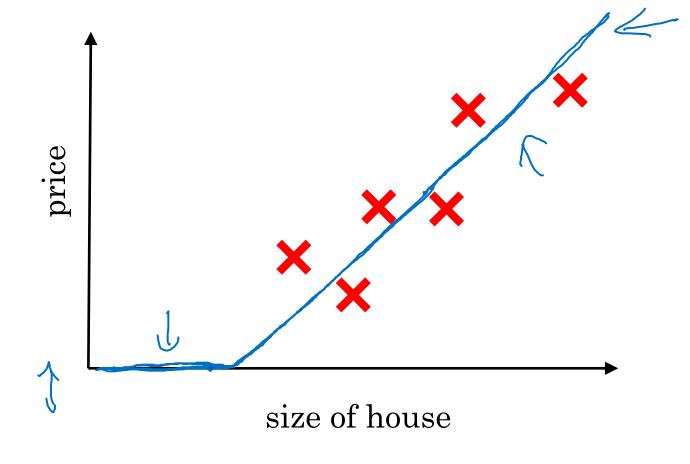


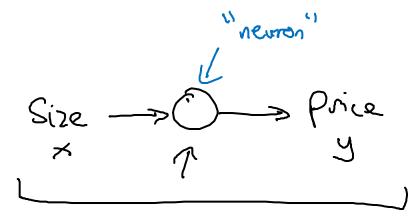
# Introduction to Deep Learning

# What is a Neural Network?

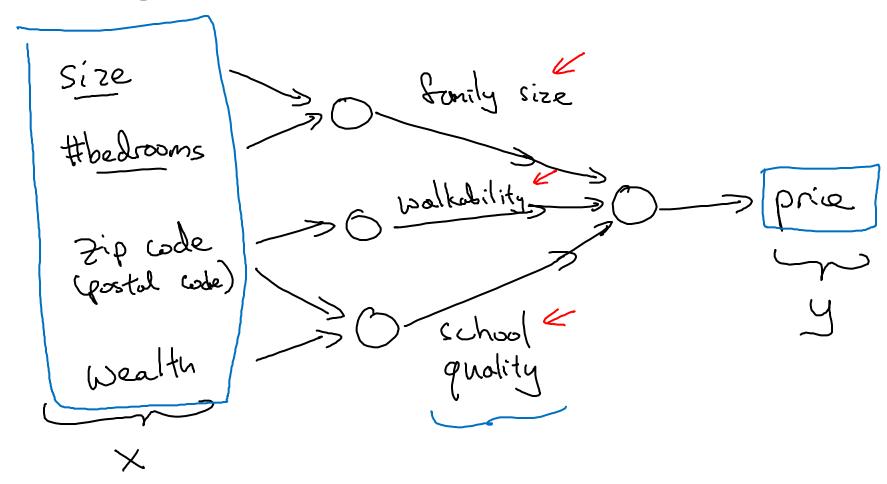
## Housing Price Prediction



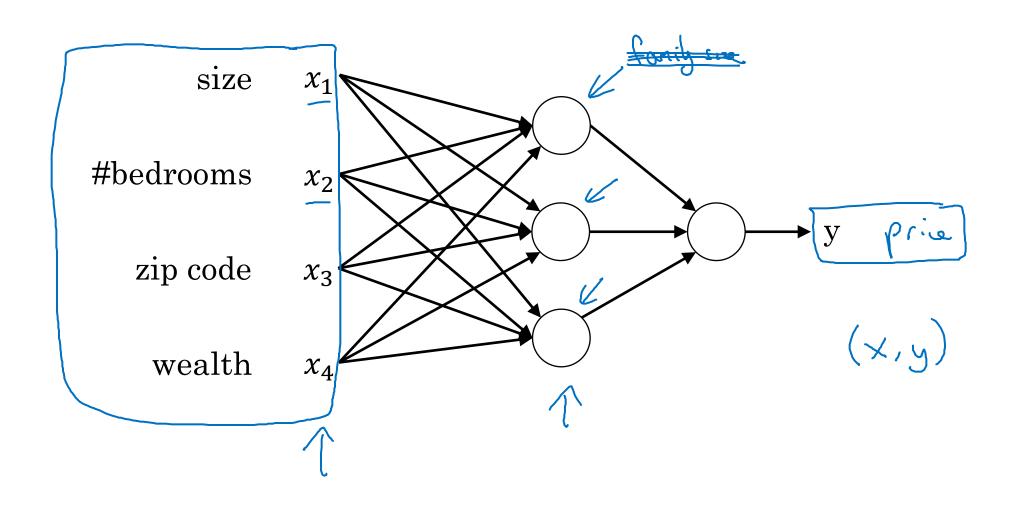




## Housing Price Prediction



## Housing Price Prediction





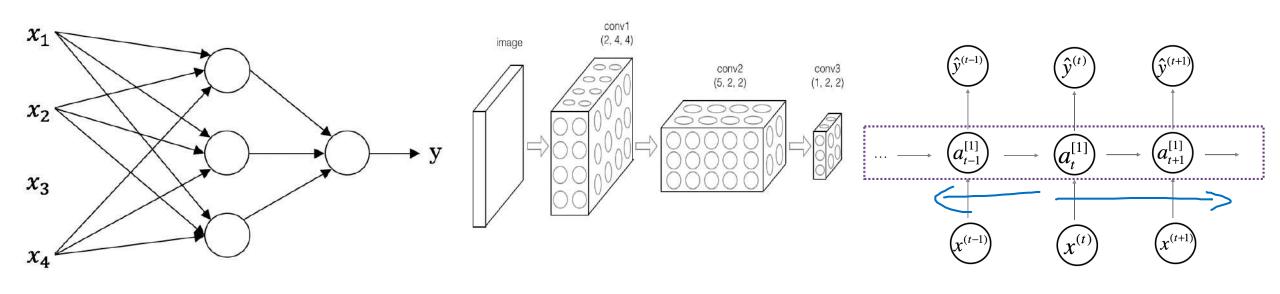
# Introduction to Deep Learning

Supervised Learning with Neural Networks

# Supervised Learning

Input(x)	Output (y)	Application
Home features	Price	Real Estate Student
Ad, user info	Click on ad? (0/1)	Online Advertising
Image	Object (1,,1000)	Photo tagging 3 CNN
Audio	Text transcript	Speech recognition } knn
English	Chinese	Machine translation
Image, Radar info	Position of other cars	Autonomous driving Tuston/

## Neural Network examples



Standard NN

Convolutional NN

**Recurrent NN** 

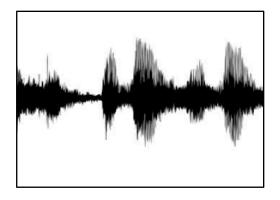
## Supervised Learning

#### Structured Data

\(\frac{1}{2}\)			
Size	#bedrooms	•••	Price (1000\$s)
2104	3		400
1600	3		330
2400	3		369
:	:		:
3000	4		540

$\underline{\hspace{1cm}}$	V	_	$\sqrt{}$
User Age	Ad Id	•••	Click
41	93242		1
80	93287		0
18	87312		1
:	:		:
27	71244		1

#### Unstructured Data





Audio

Image

Four scores and seven years ago...

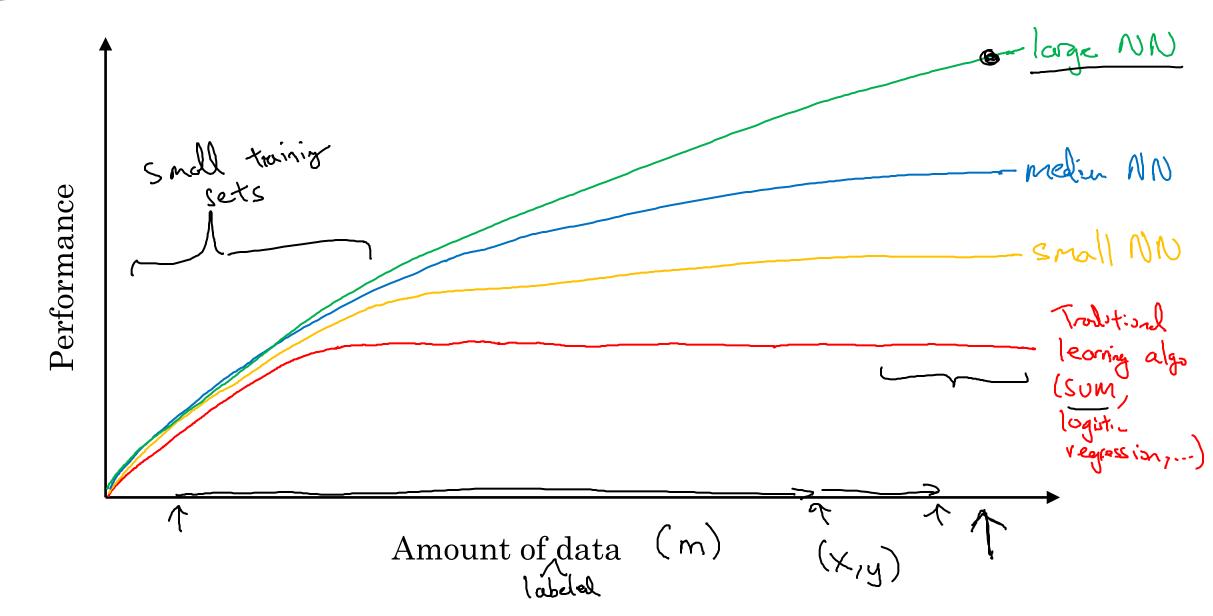
**Text** 



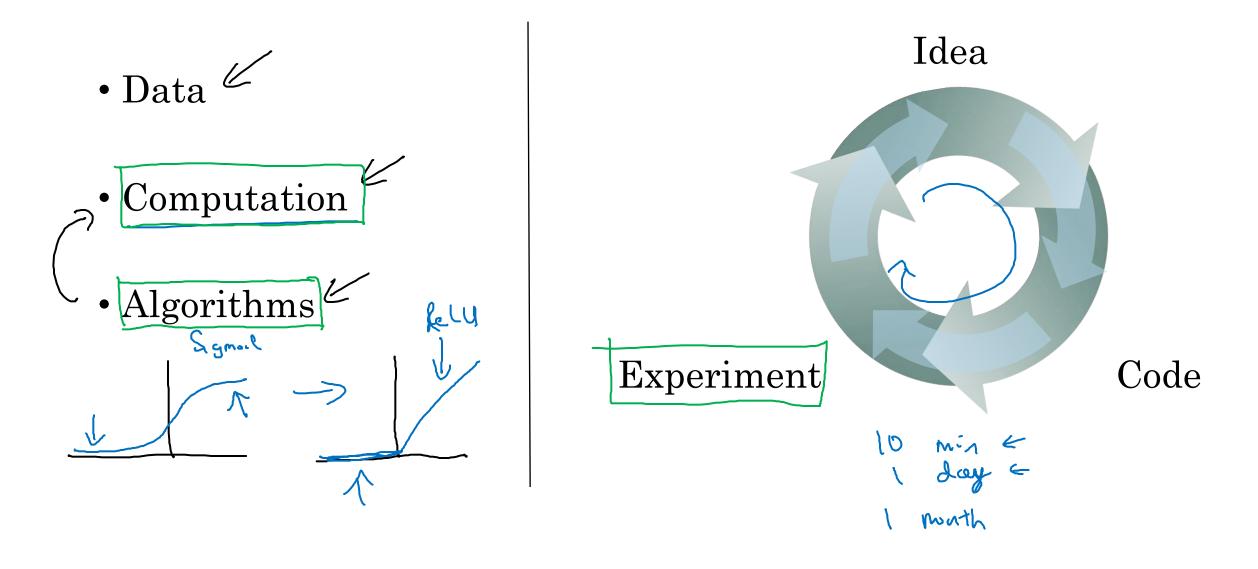
# Introduction to Neural Networks

# Why is Deep Learning taking off?

## Scale drives deep learning progress



# Scale drives deep learning progress



#### Outline of this Course

Week 1: Introduction

#### Week 2: Basics of Neural Network programming

Week 3: One hidden layer Neural Networks

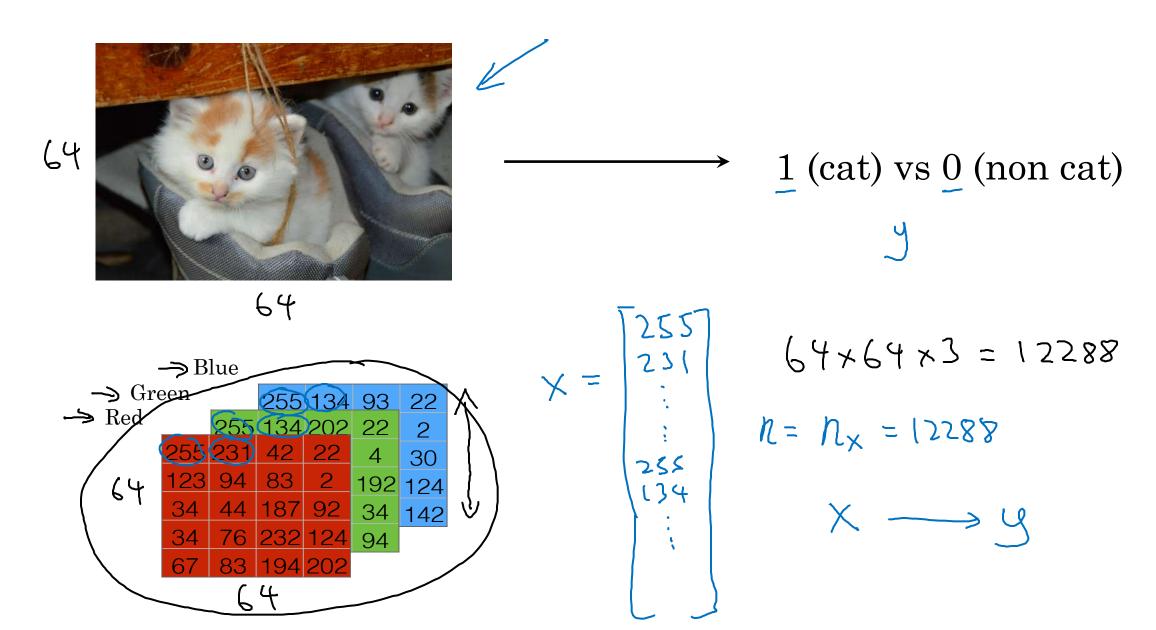
Week 4: Deep Neural Networks



# Basics of Neural Network Programming

# Binary Classification

## Binary Classification



### Notation

$$(x,y) \times \mathbb{CR}^{n_{x}}, y \in \{0,1\}$$

$$m + \text{rainiy evarples}: \{(x^{(i)}, y^{(i)}), (x^{(i)}, y^{(2i)}), \dots, (x^{(m)}, y^{(m)})\}$$

$$M = M + \text{rain} \qquad M + \text{test} = \# + \text{test} \text{ examples}.$$

$$X = \begin{bmatrix} x^{(i)} & x^{(2i)} & \dots & x^{(m)} \\ x^{(i)} & x^{(2i)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(i)} & x^{(2i)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(i)} & x^{(2i)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(m)} & x^{(m)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$



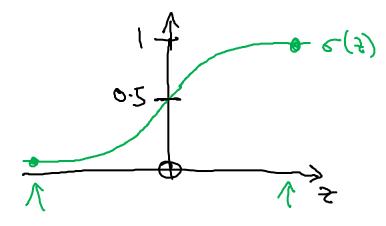
# Basics of Neural Network Programming

# Logistic Regression

Logistic Regression

Given X, want 
$$\hat{y} = P(\hat{y} = 1/X)$$
 $\times \in \mathbb{R}^{n_X}$ 

Output 
$$y = 5(w^T \times + b)$$



$$X_0 = 1, \quad x \in \mathbb{R}^{n_x + 1}$$

$$Y = 6 (0^{T}x)$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_2 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \\ 0_1 \end{bmatrix}$$

$$S = \begin{bmatrix} 0_0 \\ 0_1 \end{bmatrix}$$



# Basics of Neural Network Programming

# Logistic Regression cost function

Given 
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want  $\hat{y}^{(i)} \approx y^{(i)}$ .

Loss (error) function:  $\int (\hat{y}, y) = \frac{1}{2}(\hat{y} - y)^2$ 

If  $y = 1$ :  $\int (\hat{y}, y) = -\log \hat{y} \in \text{Mont log} \hat{y} | \log e$ , wat  $\hat{y} | \log e$ .

If  $y = 0$ :  $\int (\hat{y}, y) = -\log \hat{y} \in \text{Mont log} | \log e$ , wat  $\hat{y} | \log e$ .

If  $y = 0$ :  $\int (\hat{y}, y) = -\log (1 - \hat{y}) \in \text{Mont log} | \log e$ , wat  $\hat{y} | \log e$ .

If  $y = 0$ :  $\int (\hat{y}, y) = -\log (1 - \hat{y}) \in \text{Mont log} | \log e$ , wat  $\hat{y} | \log e$ .

Cost function:  $\int (\omega, b) = \frac{1}{m} \sum_{i=1}^{m} f(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} g(\hat{y}^{(i)} \log y^{(i)} + (1 - y^{(i)}) \log (1 - \hat{y}^{(i)})$ 



# Basics of Neural Network Programming

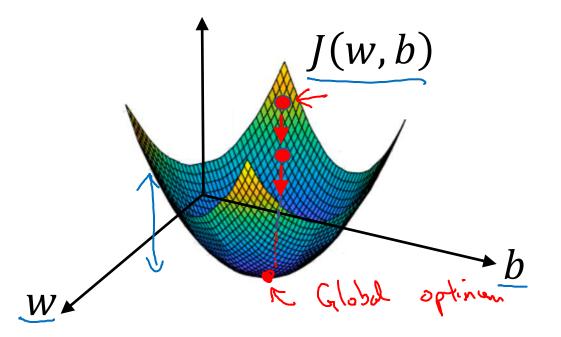
### **Gradient Descent**

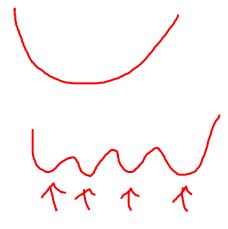
### Gradient Descent

Recap: 
$$\hat{y} = \sigma(w^T x + b)$$
,  $\sigma(z) = \frac{1}{1 + e^{-z}}$ 

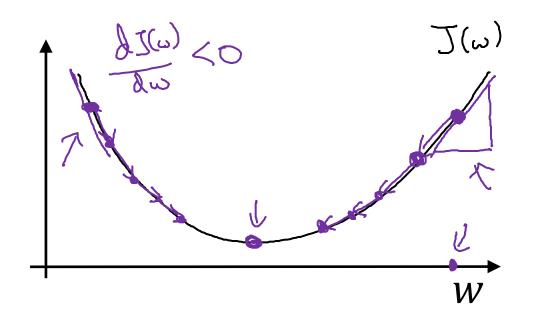
$$\underline{J(w,b)} = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

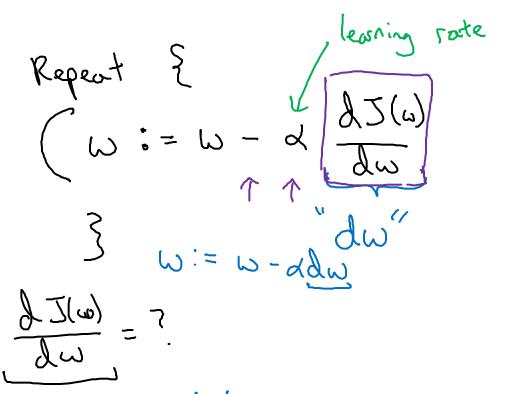
Want to find w, b that minimize J(w, b)

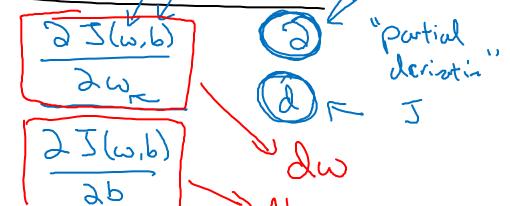




### Gradient Descent





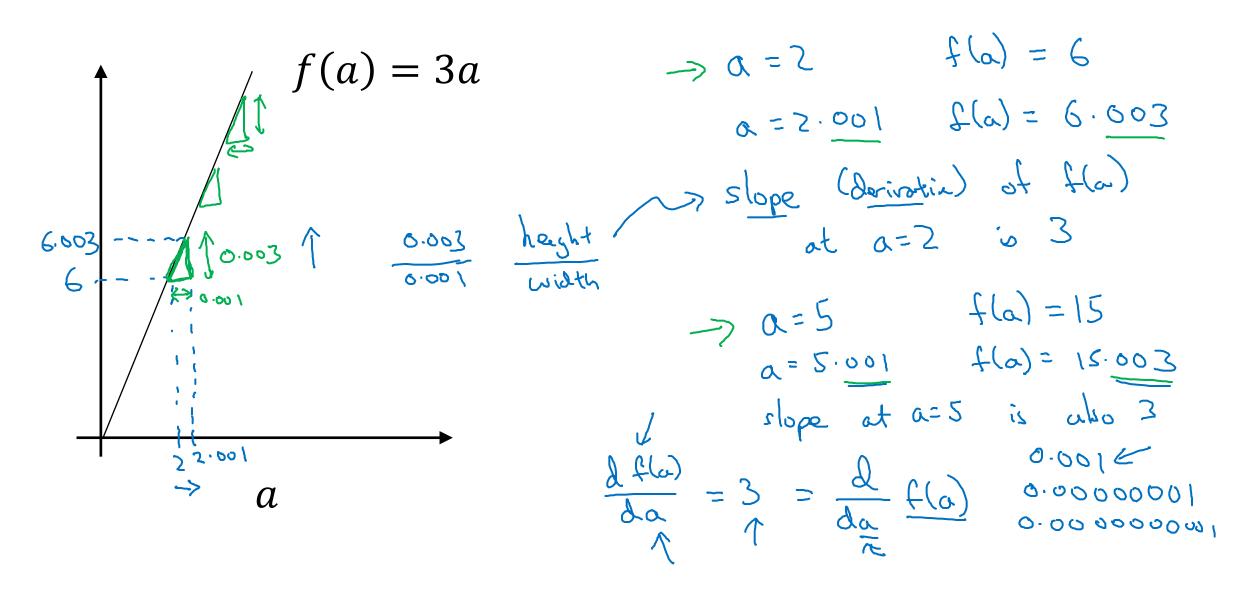




# Basics of Neural Network Programming

### Derivatives

### Intuition about derivatives



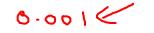


# Basics of Neural Network Programming

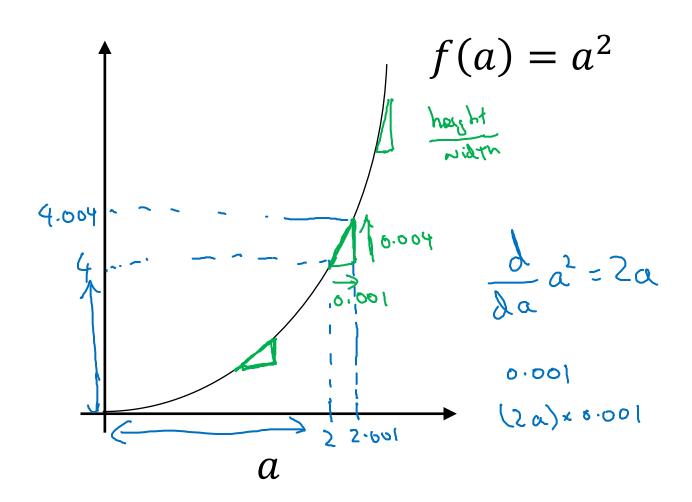
deeplearning.ai

# More derivatives examples

### Intuition about derivatives



6.00000....01K



$$R = 2$$
 $a = 2.001$ 
 $f(a) = 4$ 
 $(4.004004)$ 
 $slope$  (derivative) of  $f(a)$  at

 $a = 2$ 
 $a = 3$ 
 $a = 4$ 
 $a = 4$ 
 $a = 5$ 
 $a = 5.001$ 
 $a = 5$ 
 $a = 5.001$ 
 $a = 5$ 
 $a = 5$ 

## More derivative examples

$$f(a) = a^2$$

$$f(a) = a^3$$

$$\frac{d}{da}(a) = 3a^{2}$$
 $3x2^{3} = 12$ 

$$\frac{d}{da}f(a) = \frac{1}{a}$$

$$\frac{1}{20.0005}$$

$$\frac{d}{da}(a) = \frac{1}{2}$$

$$\frac{d}{da}(a) = \frac{1}{2}$$

$$a = 5.001$$
  $f(a) = 8$   
 $a = 5.001$   $f(a) = 8$ 

$$Q = 2.001 \quad f(w) \approx 0.69365$$

$$0.0005 \quad 0.0005$$



# Basics of Neural Network Programming

# Computation Graph

## Computation Graph

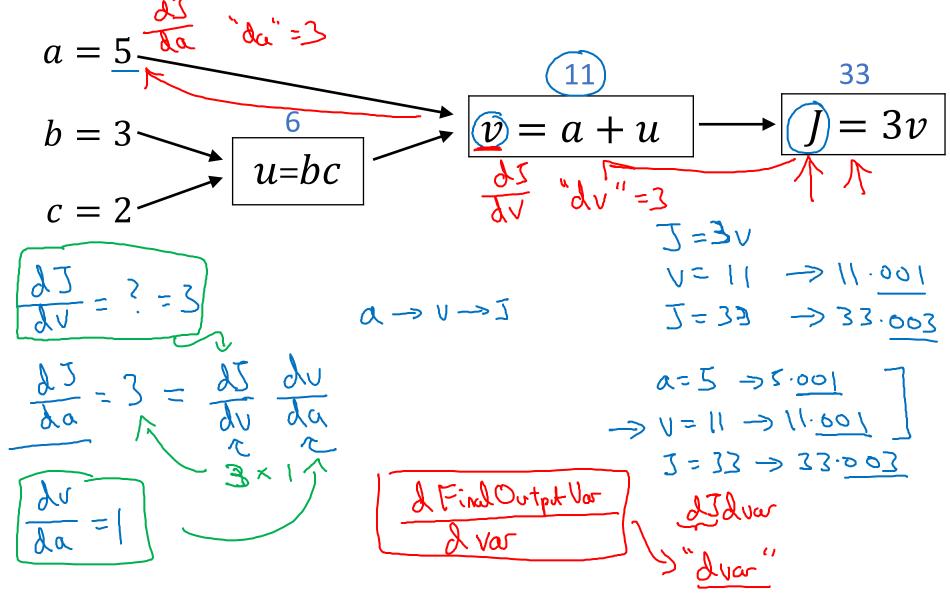
$$J(a,b,c) = 3(a+bc) = 3(5+3n^2) = 33$$
 $U = bc$ 
 $J = 3v$ 
 $0 = 3$ 



# Basics of Neural Network Programming

Derivatives with a Computation Graph

# Computing derivatives



$$f(a) = 3a$$

$$df(w) = df$$

$$da = 3$$

$$dJ = 3$$

$$dJ = 3$$

## Computing derivatives

$$\begin{array}{c}
a = 5 \\
b = 3 \\
b = 3
\end{array}$$

$$\begin{array}{c}
b = 3 \\
b = 6
\end{array}$$

$$\begin{array}{c}
c = 2 \\
\hline
du = 3
\end{array}$$

$$\begin{array}{c}
du = 3 \\
\hline
du = 3
\end{array}$$

$$\begin{array}{c}
du = 3 \\
\hline
du = 3
\end{array}$$

$$\begin{array}{c}
du = 3 \\
\hline
du = 3
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 3 \\
\hline
du = 3
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 3 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 3 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 3 \\
\hline
du = 3 \\
\hline
du = 3 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 3 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 3 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
\hline
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6$$

$$\begin{array}{c}
du = 6 \\
du = 6
\end{array}$$

$$\begin{array}{c}
du = 6 \\
du = 6$$

$$\begin{array}{c}
du$$



## Basics of Neural Network Programming

Logistic Regression Gradient descent

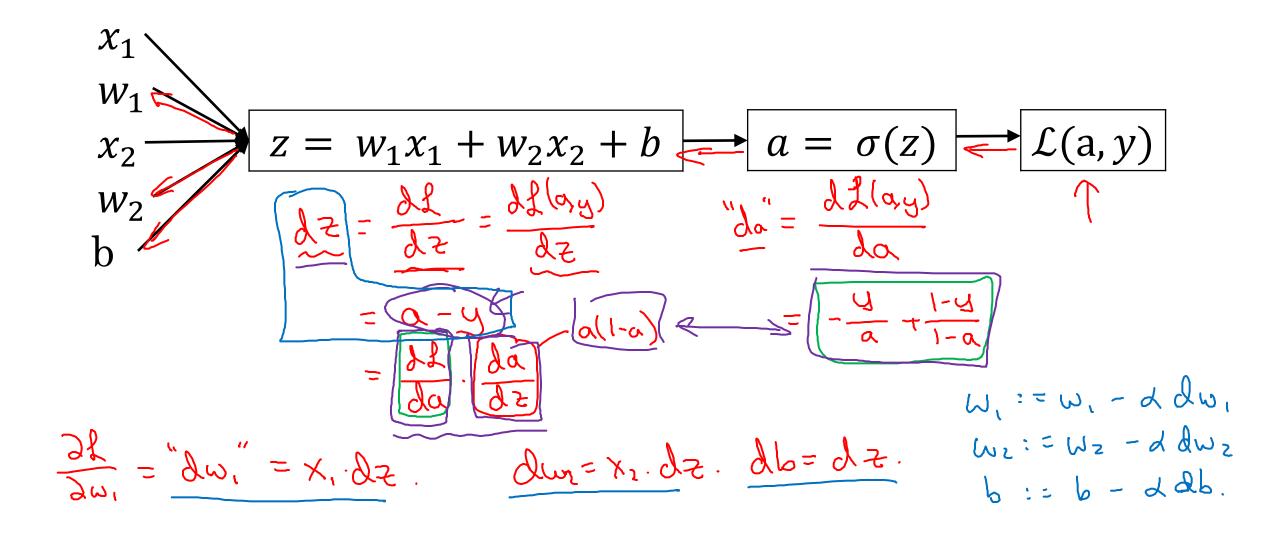
## Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

## Logistic regression derivatives





## Basics of Neural Network Programming

Gradient descent on m examples

### Logistic regression on m examples

$$\frac{J(\omega,b)}{J(\omega,b)} = \frac{1}{m} \sum_{i=1}^{m} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

## Logistic regression on m examples

$$J=0$$
;  $dw_{i}=0$ ;  $dw_{i}=0$ ;  $db=0$ 
 $Z^{(i)}=w^{T}x^{(i)}+b$ 
 $Z^{(i)}=(z^{(i)})$ 
 $Z^{(i$ 

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$

Vectorization



## Basics of Neural Network Programming

Logistic Regression Gradient descent

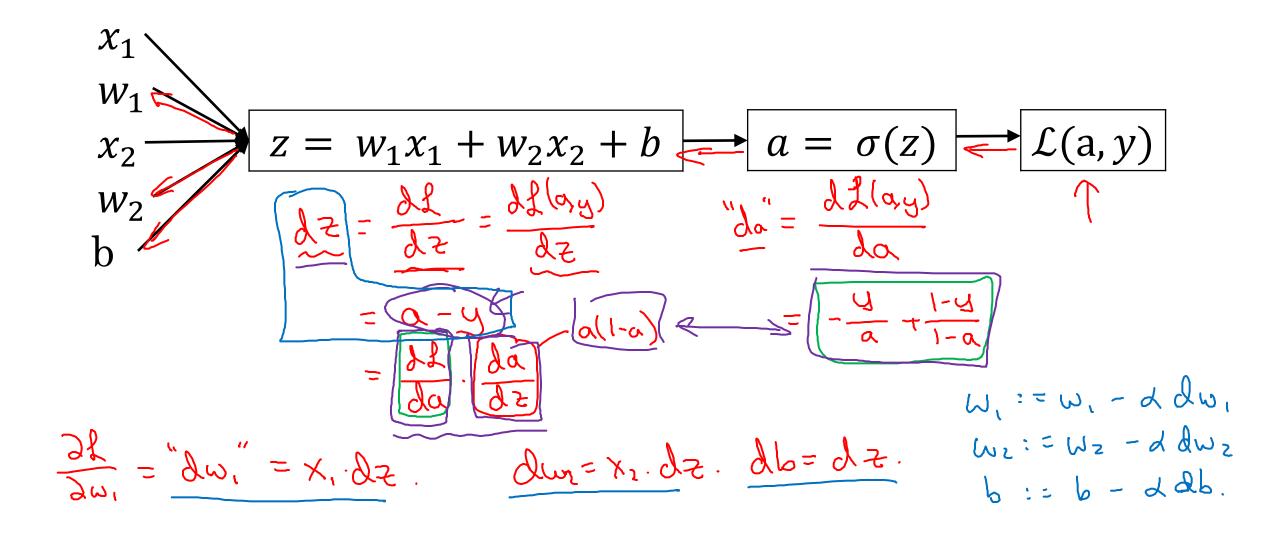
## Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

## Logistic regression derivatives





## Basics of Neural Network Programming

Gradient descent on m examples

### Logistic regression on m examples

$$\frac{J(\omega,b)}{J(\omega,b)} = \frac{1}{m} \sum_{i=1}^{m} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} J(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} f(\alpha^{(i)}, y^{(i)})$$

## Logistic regression on m examples

$$J=0$$
;  $dw_{i}=0$ ;  $dw_{i}=0$ ;  $db=0$ 
 $Z^{(i)}=w^{T}x^{(i)}+b$ 
 $Z^{(i)}=(z^{(i)})$ 
 $Z^{(i$ 

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$

Vectorization



## Basics of Neural Network Programming

Vectorizing Logistic Regression

## Vectorizing Logistic Regression

$$Z^{(1)} = w^{T}x^{(1)} + b$$

$$Z^{(2)} = w^{T}x^{(2)} + b$$

$$Z^{(3)} = w^{T}x^{(3)} + b$$

$$Z^{(3)} = \sigma(z^{(3)})$$

$$Z^$$



## Basics of Neural Network Programming

Vectorizing Logistic Regression's Gradient Computation

## Vectorizing Logistic Regression

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} = \frac{dz^{(2)} - y^{(2)}}{dz^{(2)}} - \frac{dz^{(2)}}{dz^{(2)}} - \frac$$

$$db = \frac{1}{m} \sum_{i=1}^{n} dz^{(i)}$$

$$= \frac{1}{m} \left[ x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[ x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[ x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[ x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

Implementing Logistic Regression.

J = 0, 
$$dw_1 = 0$$
,  $dw_2 = 0$ ,  $db = 0$ 

for i = 1 to m:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)}) \checkmark$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)} \checkmark$$

$$dw_1 += x_1^{(i)} dz^{(i)} dz^{(i)}$$

$$dw_2 += x_2^{(i)} dz^{(i)}$$

$$db += dz^{(i)}$$

$$J = J/m, dw_1 = dw_1/m, dw_2 = dw_2/m$$

$$db = db/m$$

$$Z = \omega^{T} X + b$$
 $Z = \omega^{T} X + b$ 
 $Z = \omega^{T} X$ 

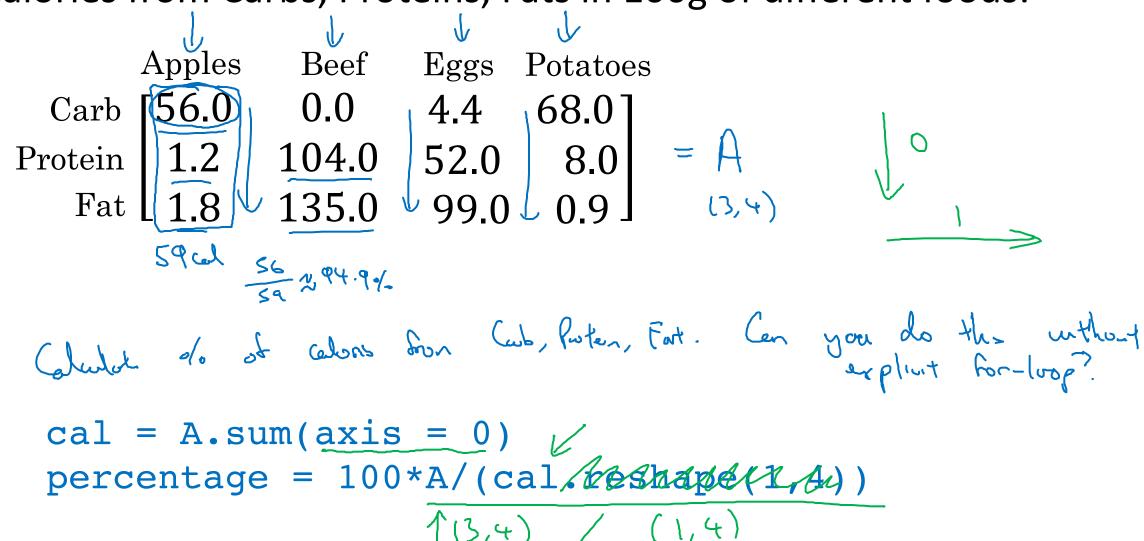


## Basics of Neural Network Programming

# Broadcasting in Python

### Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:



### Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix}$$

$$(m,n) (2)3)$$

$$\begin{bmatrix}
1 & 2 & 3 \\
4 & 5 & 6
\end{bmatrix} + 
\begin{bmatrix}
100 & 60 & 60 \\
200 & 60 & 60
\end{bmatrix} = 
\begin{bmatrix}
(m,n) & 6 & 6
\end{bmatrix}$$

### General Principle

$$(M, n) \qquad + \qquad (N, n) \qquad motics \qquad + \qquad (M, n) \qquad models \qquad + \qquad (M, n) \qquad + \qquad R \qquad = \qquad \begin{bmatrix} 101 \\ 12 \\ 1 \end{bmatrix} \qquad + \qquad 100 \qquad = \qquad \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix} \qquad + \qquad 100 \qquad = \qquad \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix}$$

$$(1, n) \qquad models \qquad + \qquad 100 \qquad = \qquad \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix} \qquad + \qquad 100 \qquad = \qquad \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix} \qquad + \qquad 100 \qquad = \qquad \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix}$$

Matlab/Octave: bsxfun

#### Outline of this Course

Week 1: Introduction

Week 2: Basics of Neural Network programming

Week 3: One hidden layer Neural Networks

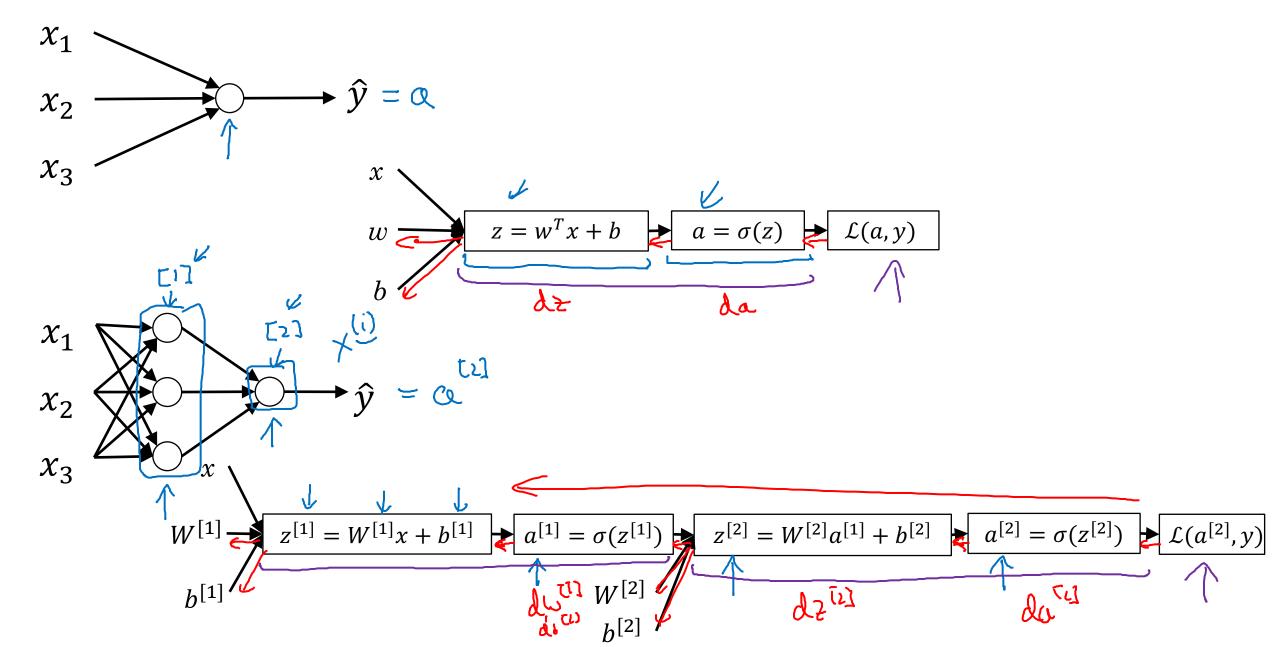
Week 4: Deep Neural Networks



## One hidden layer Neural Network

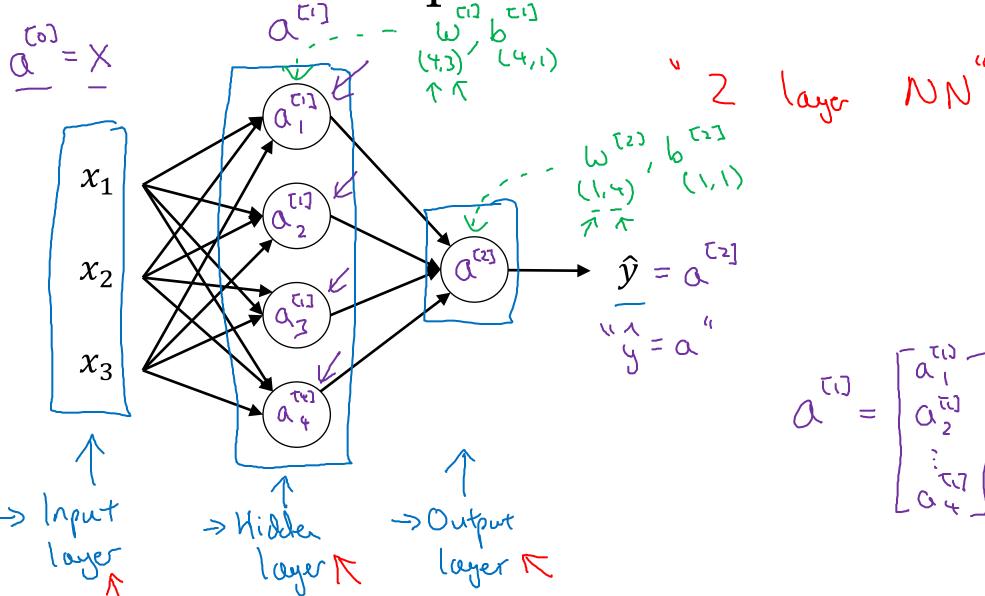
## Neural Networks Overview

#### What is a Neural Network?





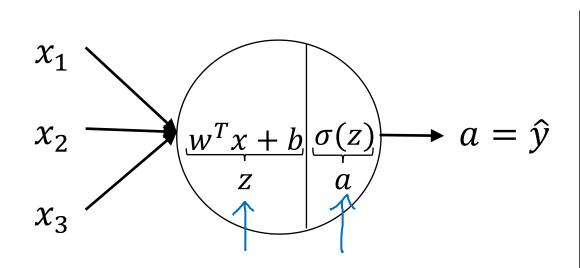
## One hidden layer Neural Network



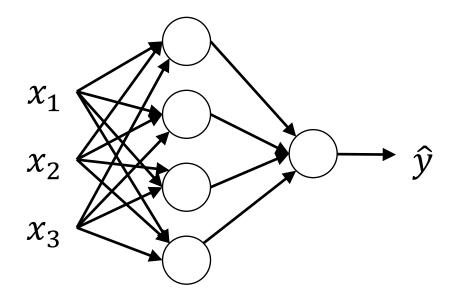


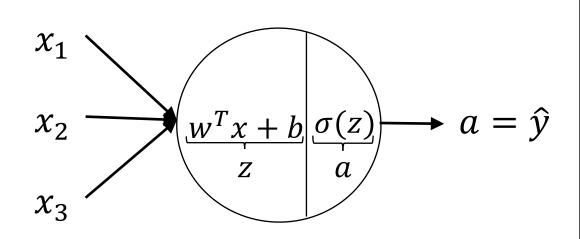
## One hidden layer Neural Network

Computing a Neural Network's Output

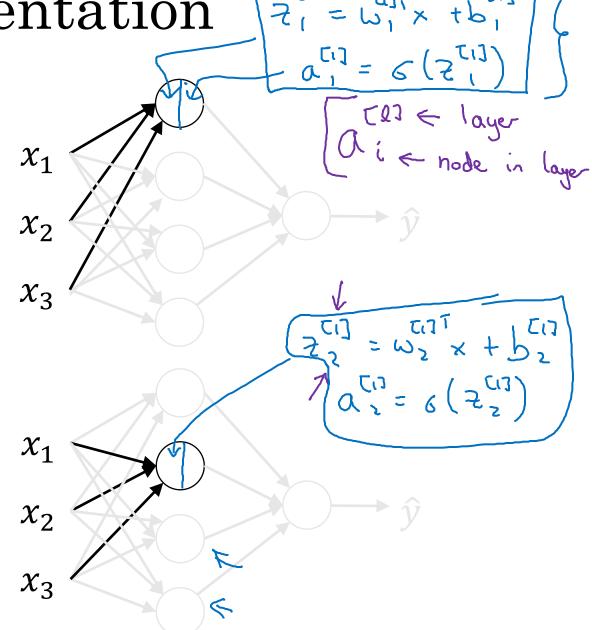


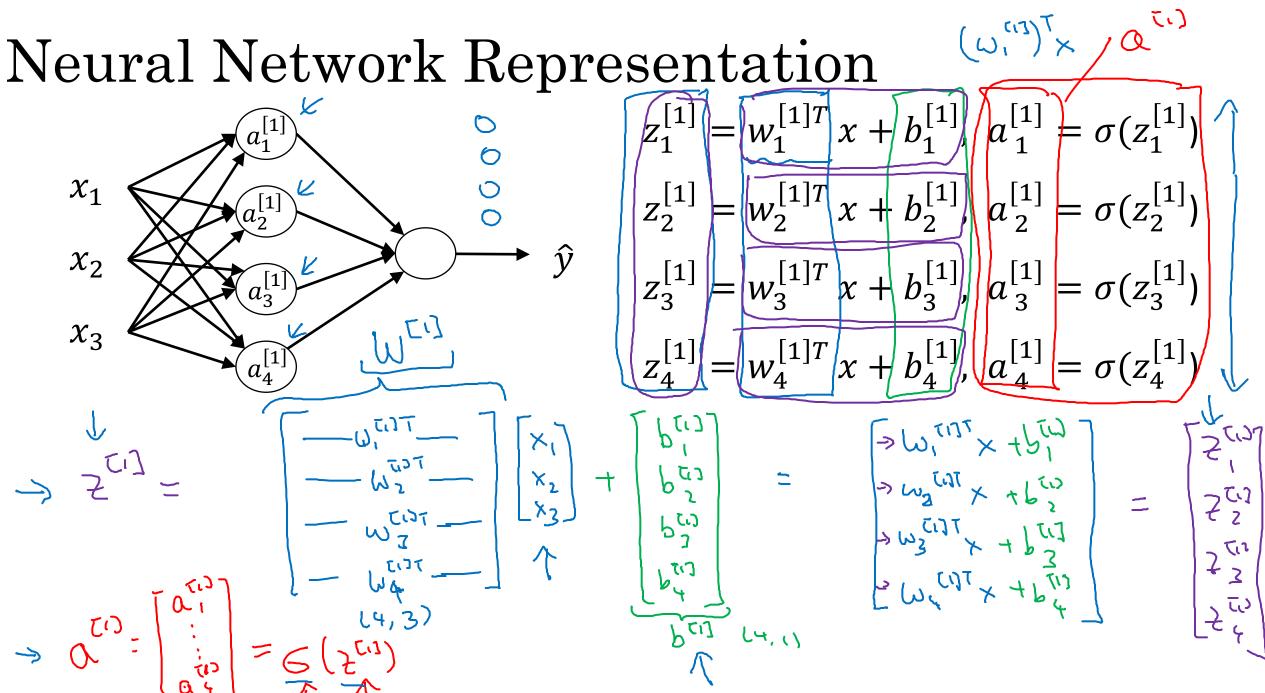
$$z = w^T x + b$$
$$a = \sigma(z)$$



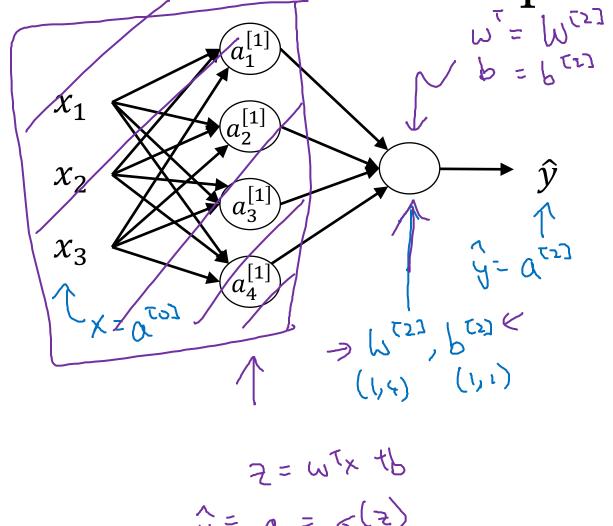


$$z = w^T x + b$$
$$a = \sigma(z)$$





Neural Network Representation learning



$$2 = \omega^{T_X} tb$$

$$\hat{y} = \alpha = 6(2)$$

Given input x:

$$z^{[1]} = W^{[1]} + b^{[1]}$$

$$a^{[1]} = \sigma(z^{[1]})$$

$$a^{[1]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = \sigma(z^{[2]})$$

$$a^{[2]} = \sigma(z^{[2]})$$

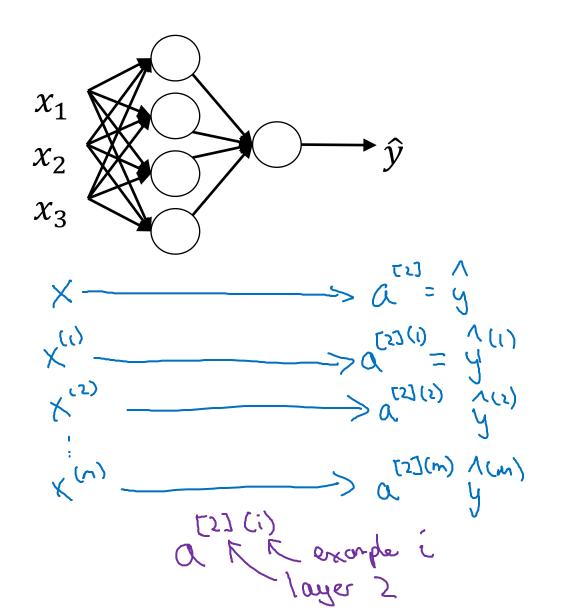
$$a^{[2]} = \sigma(z^{[2]})$$

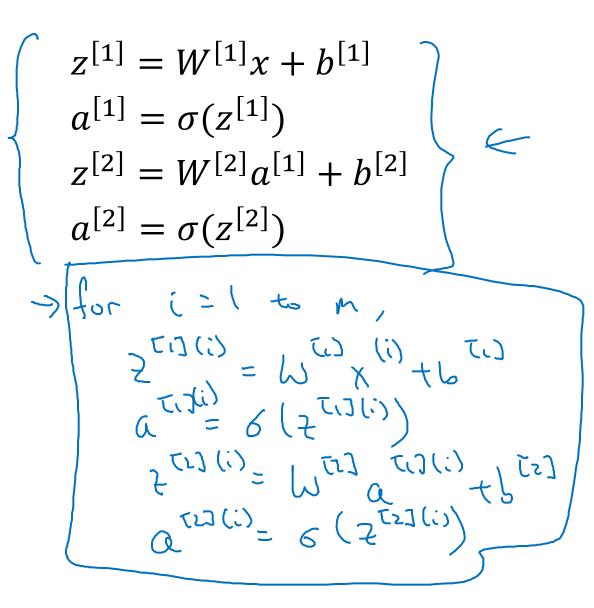


## One hidden layer Neural Network

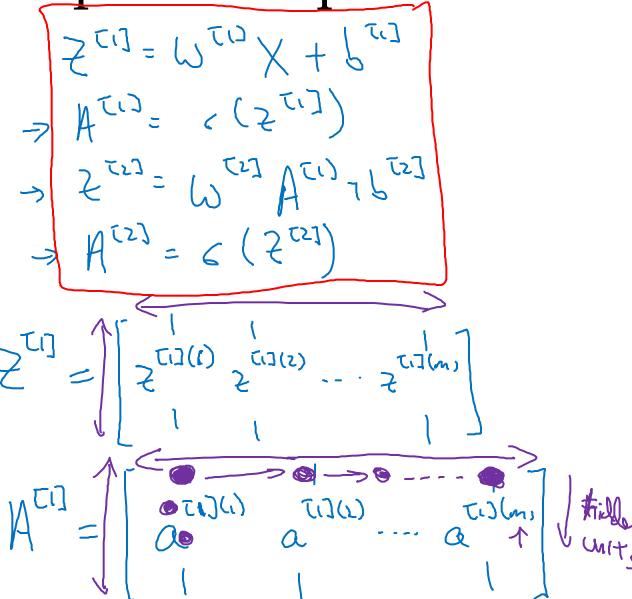
Vectorizing across multiple examples

### Vectorizing across multiple examples





Vectorizing across multiple examples

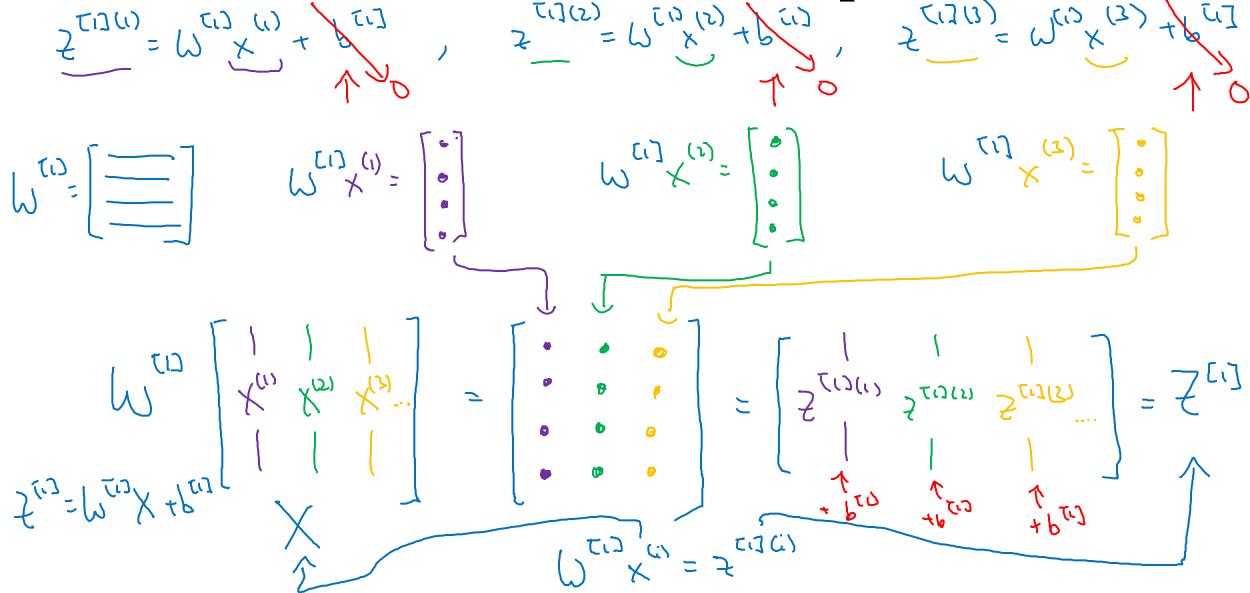




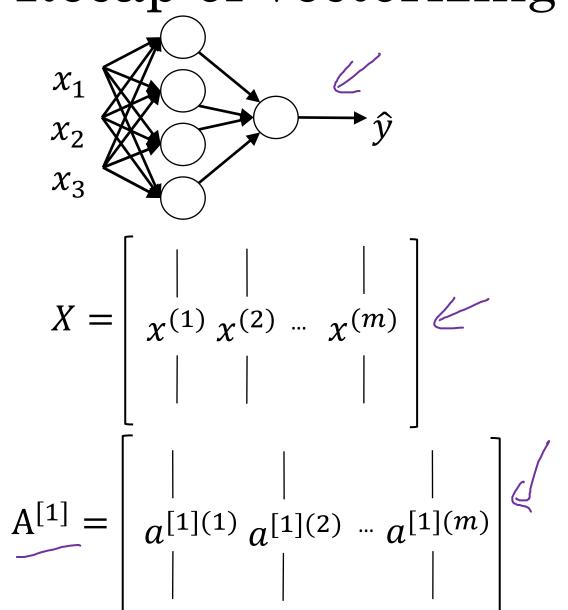
## One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



## Recap of vectorizing across multiple examples



```
for i = 1 to m
     \Rightarrow z^{[1](i)} = W^{[1]}x^{(i)} + \overline{b^{[1]}}
     \Rightarrow a^{[1](i)} = \sigma(z^{[1](i)})
     \Rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
    \Rightarrow a^{[2](i)} = \sigma(z^{[2](i)})
                         , A[0] X = a^{(0)} \times (i) = a^{(0)}(i)
 Z^{[1]} = W^{[1]}X + b^{[1]} \leftarrow W^{[1]}X^{(0)} + b^{[1]}
  A^{[1]} = \sigma(Z^{[1]})
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
 A^{[2]} = \sigma(Z^{[2]})
```



# One hidden layer Neural Network

### Activation functions

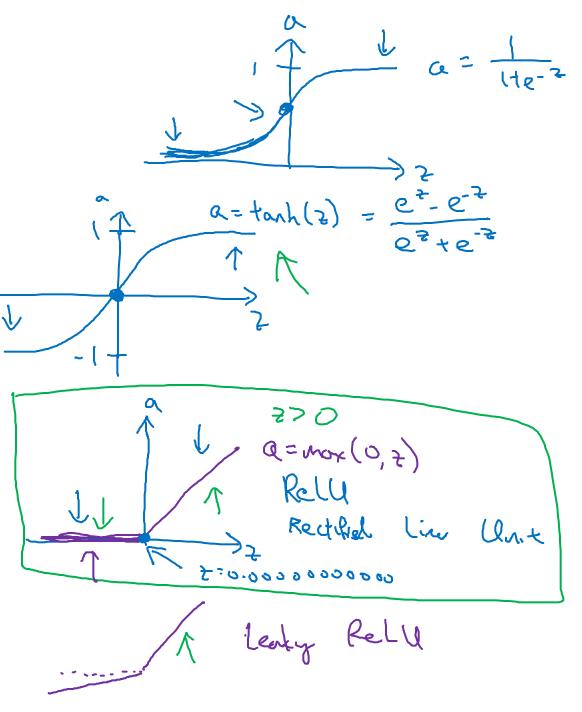
### Activation functions

Given x:

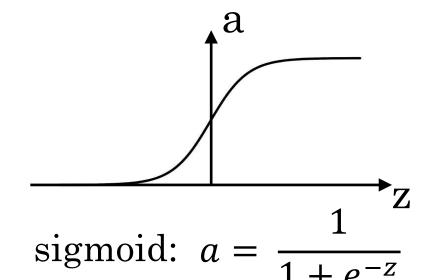
$$z^{[1]} = W^{[1]}x + b^{[1]}$$

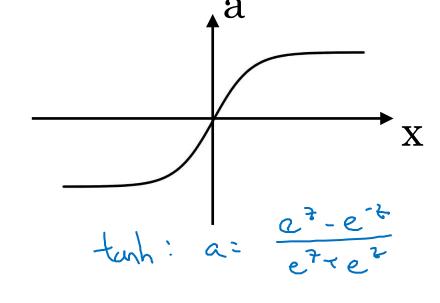
$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

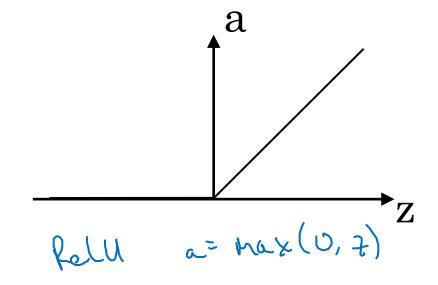
 $\Rightarrow a^{[2]} = \sigma(z^{[2]}) q^{(2)}$ 

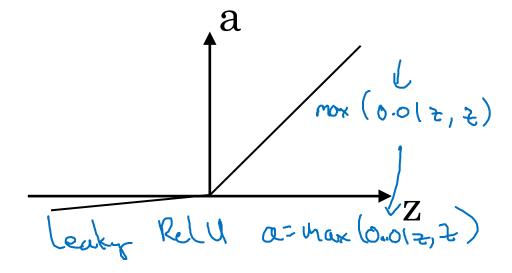


#### Pros and cons of activation functions







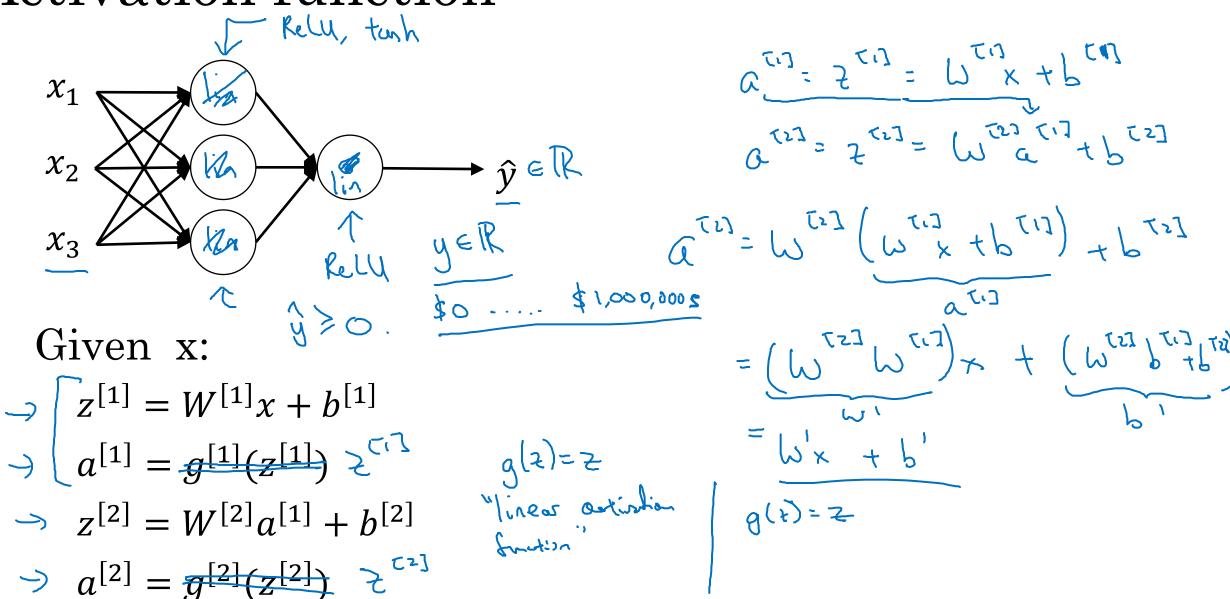




# One hidden layer Neural Network

Why do you need non-linear activation functions?

### Activation function





# One hidden layer Neural Network

# Derivatives of activation functions

## Sigmoid activation function

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

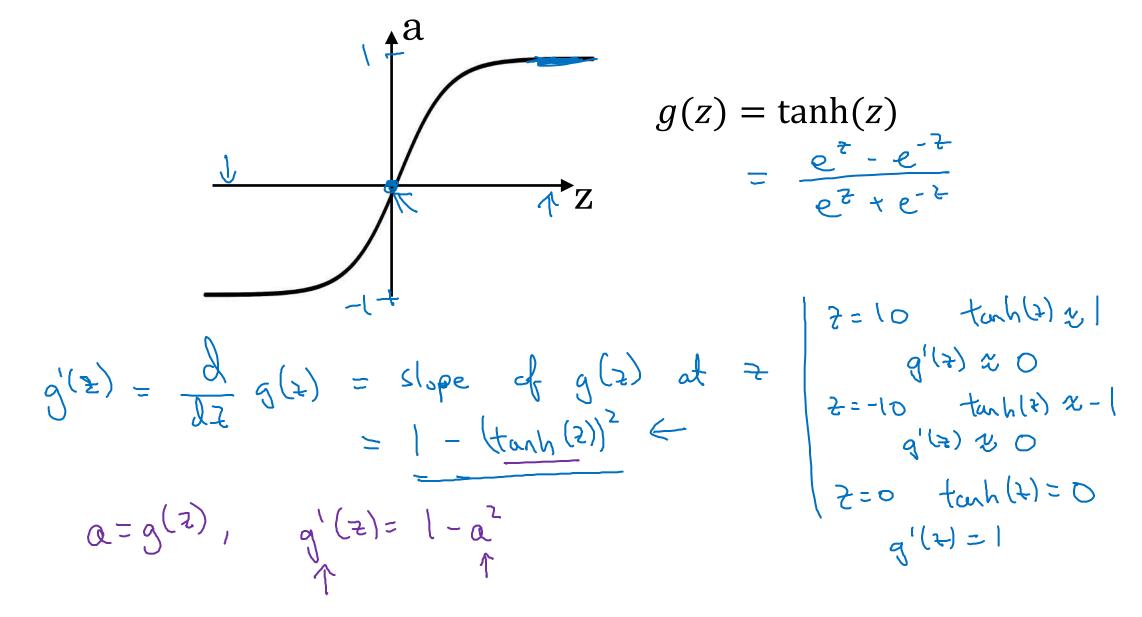
$$a = g(z) = \frac{1}{1 + e^{-z}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

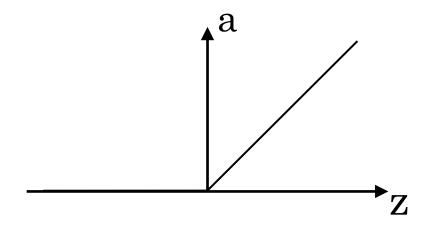
$$\frac{1}{1 + e^{-z}}$$

$$\frac{$$

#### Tanh activation function



### ReLU and Leaky ReLU

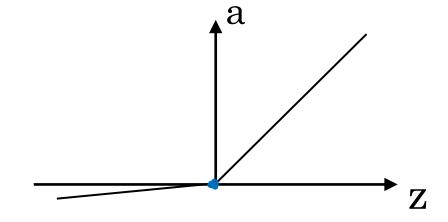


#### ReLU

$$g(t) = mox(0, 2)$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } t < 0 \\ 1 & \text{if } t > 0 \end{cases}$$

$$\Rightarrow g'(t) = \begin{cases} 1 & \text{if } t > 0 \\ 1 & \text{if } t > 0 \end{cases}$$



#### Leaky ReLU

$$g(z) = Mox(0.01z, z)$$
  
 $g'(z) = \begin{cases} 0.01 & \text{if } z < 0 \\ 1 & \text{if } z > 0 \end{cases}$ 



# One hidden layer Neural Network

# Gradient descent for neural networks

Gradient descent for neural networks

Parameters: 
$$(x^{r_3}, n^{t_{23}})$$
  $(n^{t_{23}}, n^{t_{23}})$   $(n^{t_{23}}, n^{t_{23}})$   $(n^{t_{23}}, n^{t_{23}})$   $(n^{t_{23}}, n^{t_{23}})$   $= \frac{1}{m} \sum_{i=1}^{m} f(\hat{y}, y)$ 

Corporate product  $(\hat{y}^{(i)}), (\hat{z}^{(i)}), (\hat{z}^{(i)}), (\hat{z}^{(i)}), (\hat{z}^{(i)}), \dots$ 

$$\frac{1}{m} \sum_{i=1}^{m} \frac{1}{m} \sum_{i=1}^{m} f(\hat{y}^{(i)}), (\hat{z}^{(i)}), \dots$$

$$\frac{1}{m} \sum_{i=1}^{m} \frac{1}{m} \sum_{i=1}^{m} f(\hat{y}^{(i)}), \dots$$

$$\frac{1}{m} \sum_{i=1}^{m} f(\hat{y}^{(i)}), \dots$$

$$\frac$$

Formulas for computing derivatives

Formal Propagation:
$$Z_{CIJ} = P_{CIJ}(S_{CIJ}) = e(S_{CIJ})$$

$$Y_{CIJ} = P_{CIJ}(S_{CIJ}) = e(S_{CIJ})$$

$$Y_{CIJ} = P_{CIJ}(S_{CIJ}) = e(S_{CIJ})$$

$$Y_{CIJ} = P_{CIJ}(S_{CIJ}) = e(S_{CIJ})$$

Formal propagation:

$$Z^{(1)} = L^{(2)} \times L^{(1)}$$
 $Z^{(2)} = L^{(2)} \times L^{(2)}$ 
 $Z^{(2)} = L^{(2)} \times L^{(2)} \times L^{(2)} \times L^{(2)}$ 
 $Z^{(2)} = L^{(2)} \times L^{($ 

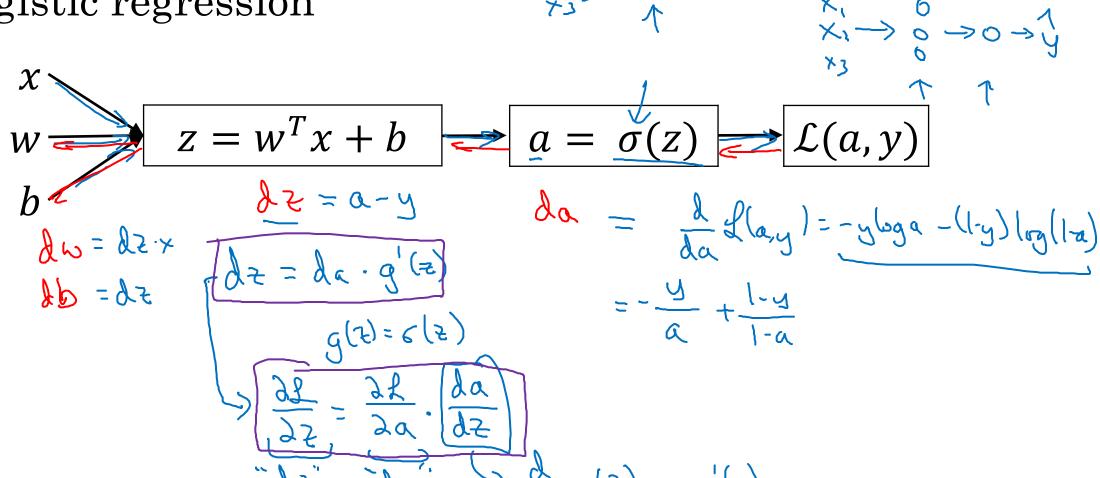


# One hidden layer Neural Network

Backpropagation intuition (Optional)

### Computing gradients

Logistic regression



Neural network gradients  $z^{[2]} = W^{[2]}x + b^{[2]}$ du = de a ->  $\left( \begin{array}{ccc} n & \zeta & \zeta & \zeta & \zeta \end{array} \right)$ 

### Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$
 $dW^{[2]} = dz^{[2]}a^{[1]^T}$ 
 $db^{[2]} = dz^{[2]}$ 
 $dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$ 
 $dW^{[1]} = dz^{[1]}x^T$ 
 $db^{[1]} = dz^{[1]}$ 

Vectorized Implementation:

$$z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

### Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dw^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dz^{[1]} = W^{[2]T}dz^{[1]}x^T$$

$$dz^{[1]} = dz^{[1]}x^T$$

$$dz^{[1]} = dz^{[1]}x^T$$

$$dz^{[1]} = dz^{[1]}x^T$$

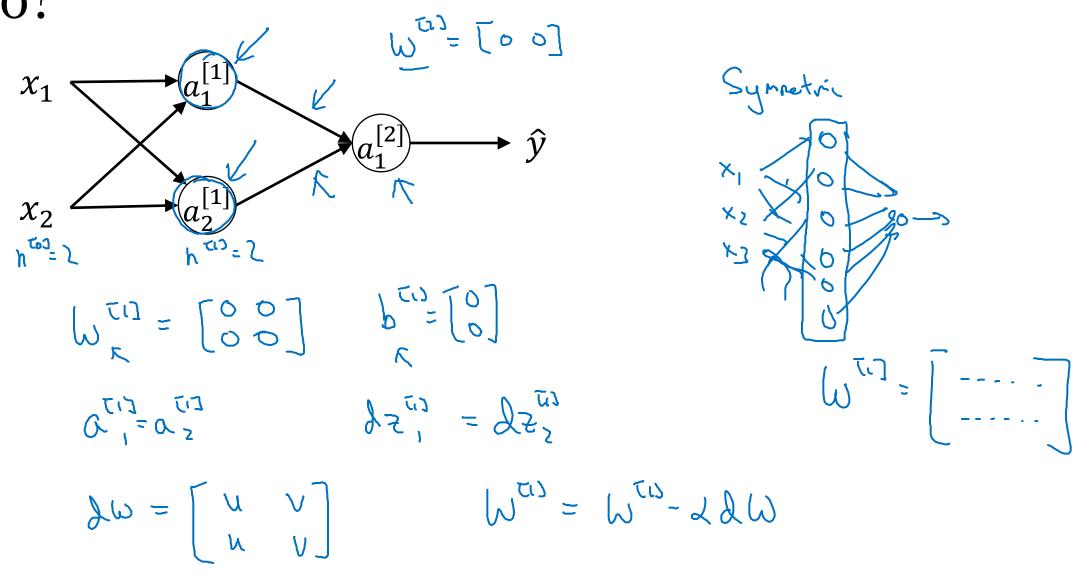
$$dz^{[1]} = dz^{[1]}x^T$$



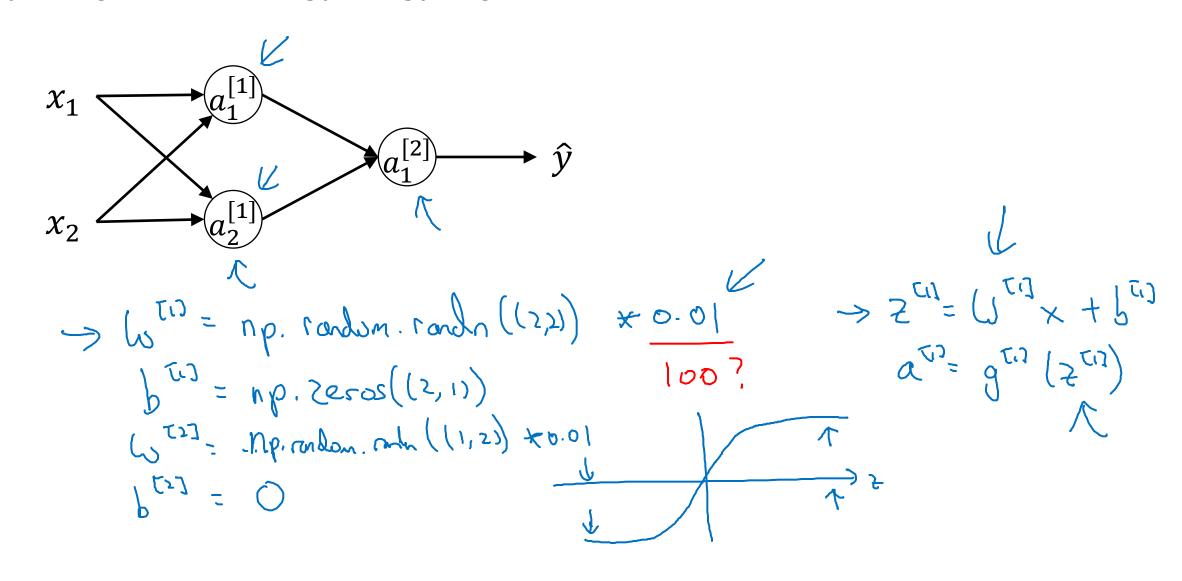
# One hidden layer Neural Network

### Random Initialization

# What happens if you initialize weights to zero?



#### Random initialization



#### Outline of this Course

Week 1: Introduction

Week 2: Basics of Neural Network programming

Week 3: One hidden layer Neural Networks

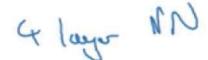
Week 4: Deep Neural Networks

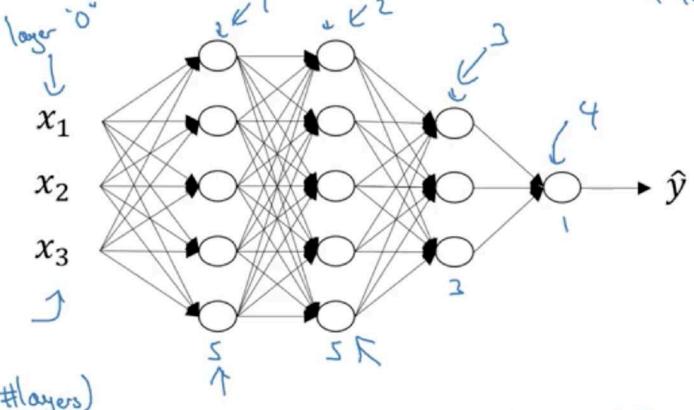


# Deep Neural Networks

Deep L-layer Neural network

### Deep neural network notation





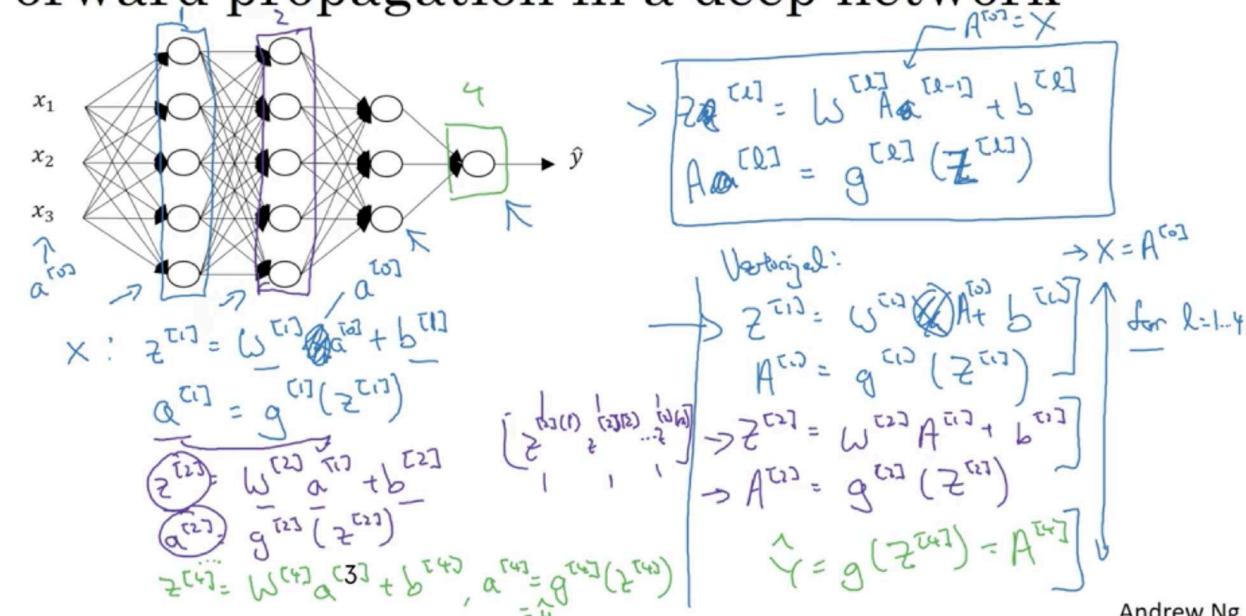
$$V_{C_{1}J} = V^{\times} = 3$$
 $V_{C_{1}J} = V^{\times} = 3$ 
 $V_{C_{2}J} = 2$ 
 $V_{C_{2}J} = 3$ 
 $V_{C_{2}J} = 3$ 
 $V_{C_{2}J} = 3$ 



# Deep Neural Networks

Forward Propagation in a Deep Network

Forward propagation in a deep network



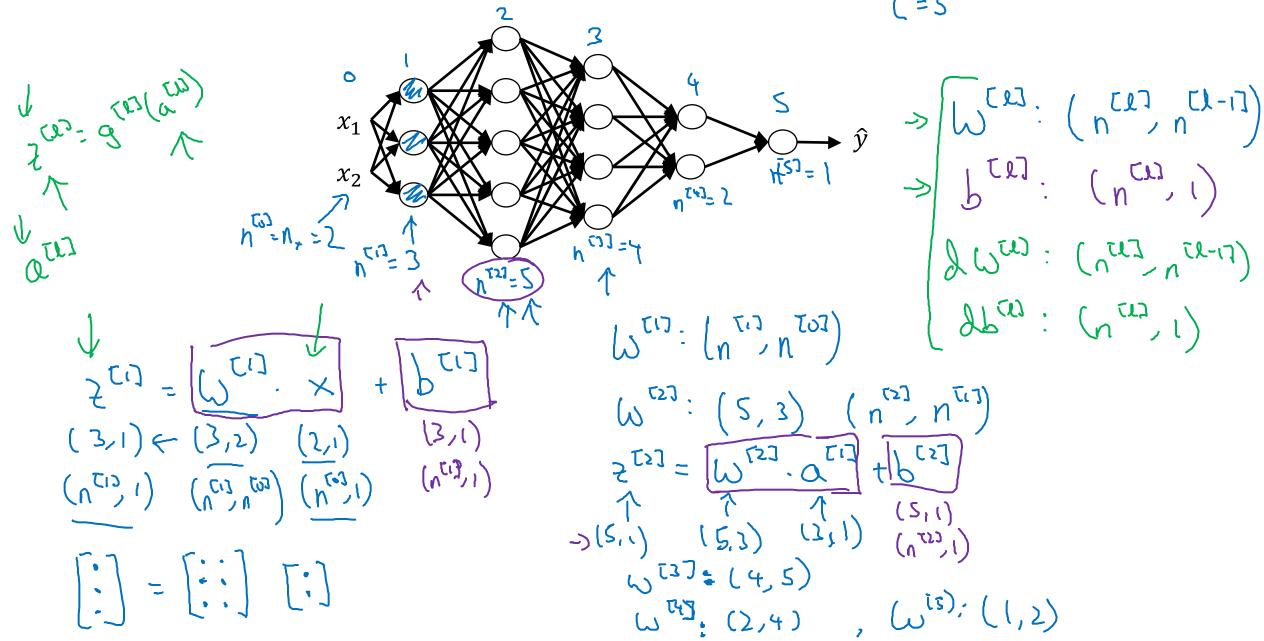
Andrew Ng



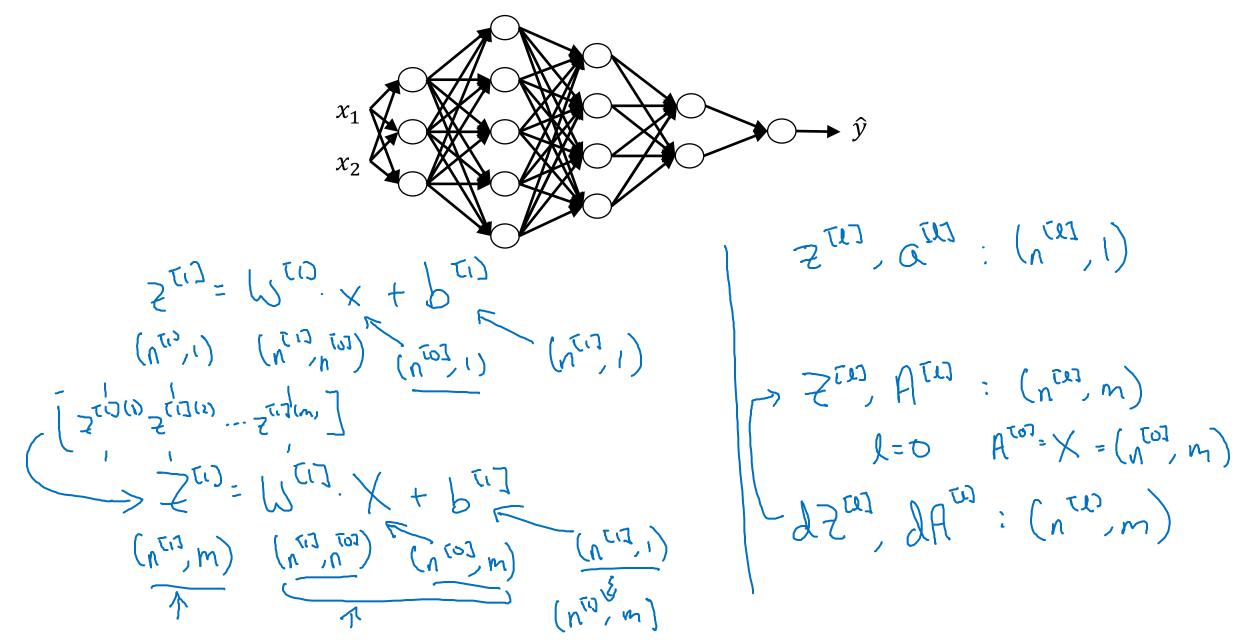
# Deep Neural Networks

Getting your matrix dimensions right

## Parameters $W^{[l]}$ and $b^{[l]}$



### Vectorized implementation

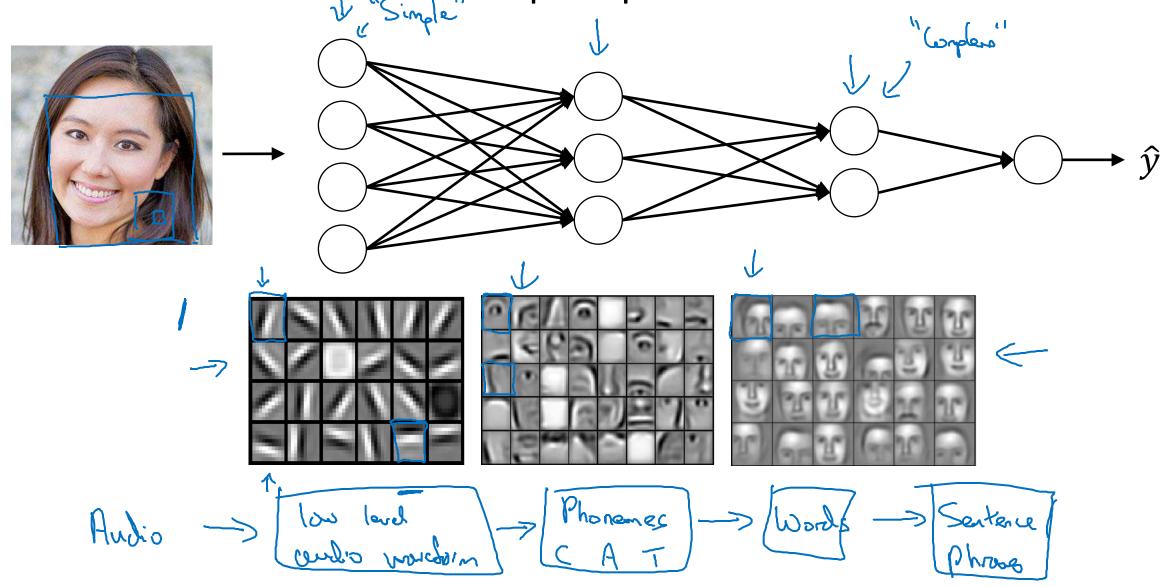




# Deep Neural Networks

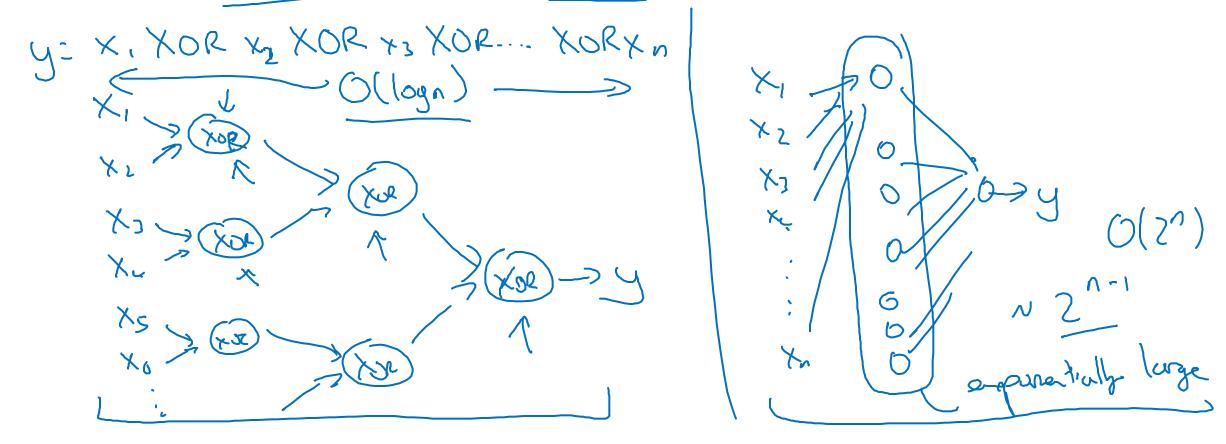
Why deep representations?

Intuition about deep representation



### Circuit theory and deep learning

Informally: There are functions you can compute with a "small" L-layer deep neural network that shallower networks require exponentially more hidden units to compute.

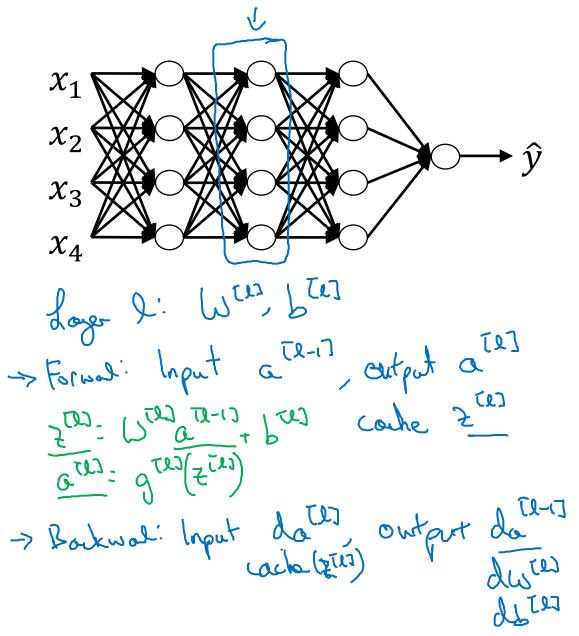


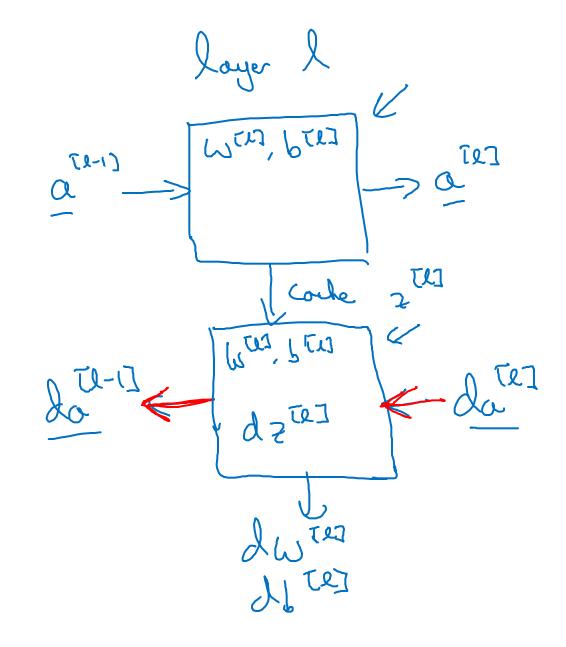


# Deep Neural Networks

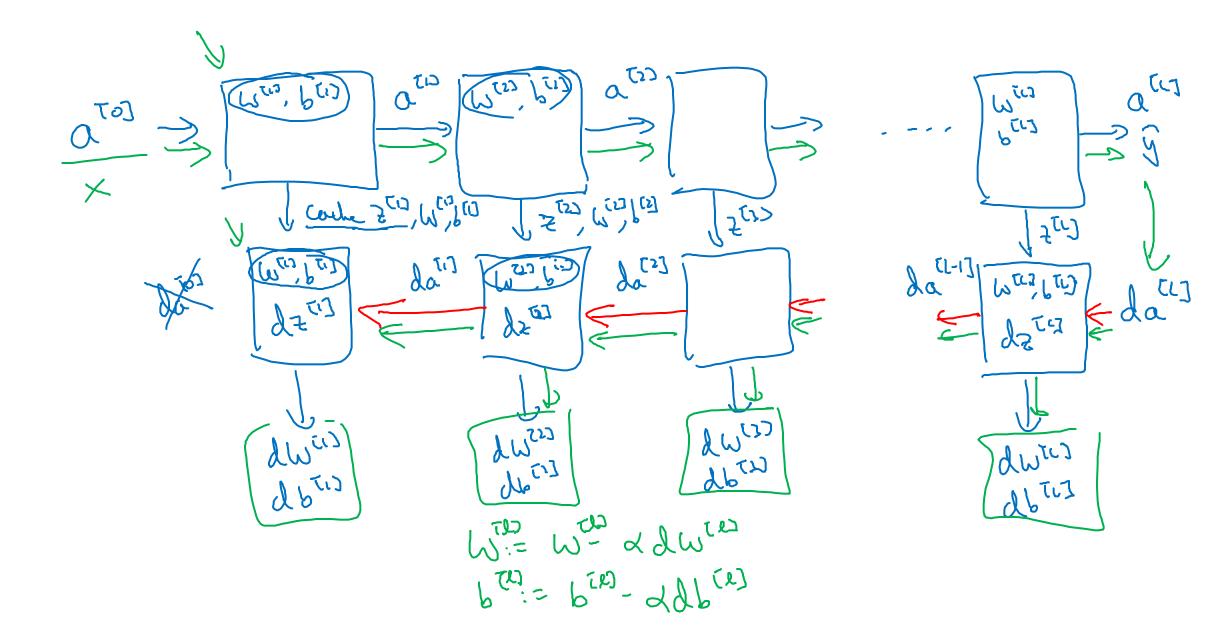
Building blocks of deep neural networks

#### Forward and backward functions





#### Forward and backward functions





# Deep Neural Networks

Forward and backward propagation

### Forward propagation for layer I

⇒ Input 
$$a^{[l-1]} \leftarrow \bigcup_{\substack{i \in I \\ j \in I}} \bigcup_{\substack{i$$

### Backward propagation for layer I

$$\rightarrow$$
 Input  $da^{[l]}$ 

$$\rightarrow$$
 Output  $da^{[l-1]}$ ,  $dW^{[l]}$ ,  $db^{[l]}$ 

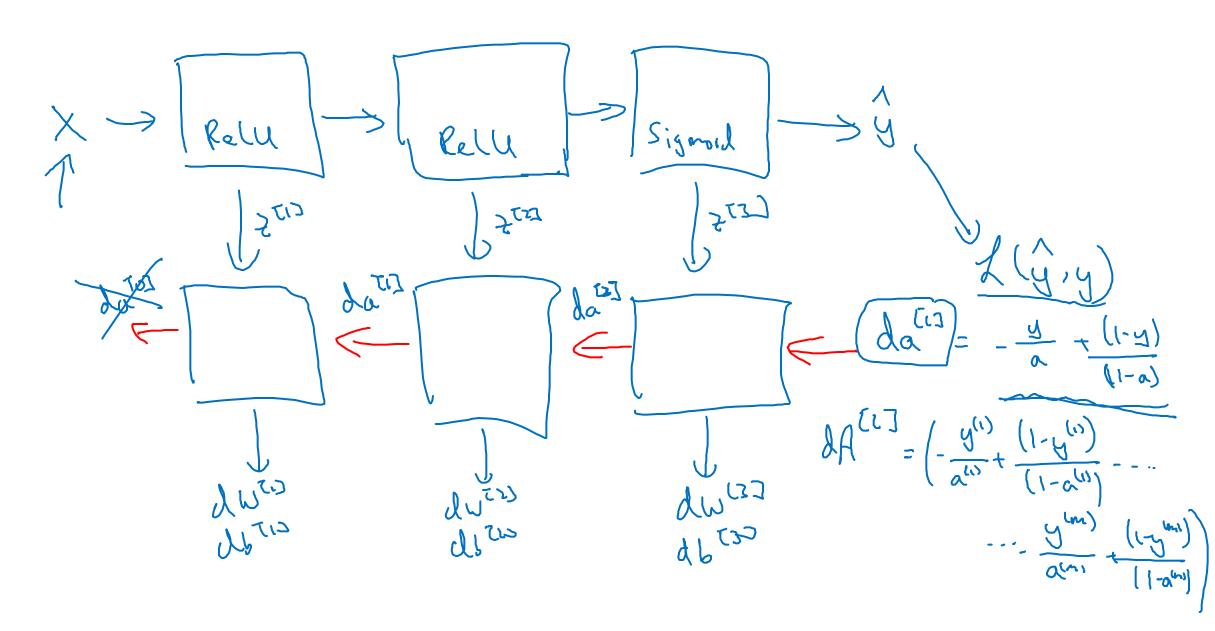
$$\frac{dz^{TD}}{dz^{TD}} = \frac{dz^{TD}}{dz^{TD}} \times g^{TD} \cdot (z^{TD})$$

$$\frac{dz^{TD}}{dz^{TD}} = \frac{dz^{TD}}{dz^{TD}} \cdot a^{TD-1}$$

$$\frac{dz^{TD}}{dz^{TD}} = \frac{dz^{TD}}{dz^{TD}} \cdot dz^{TD}$$

$$\frac{dz^{TD}}{dz^{TD}} = \frac{dz^{TD}}{dz^{TD}} \cdot dz^{TD} \cdot (z^{TD})$$

### Summary





# Deep Neural Networks

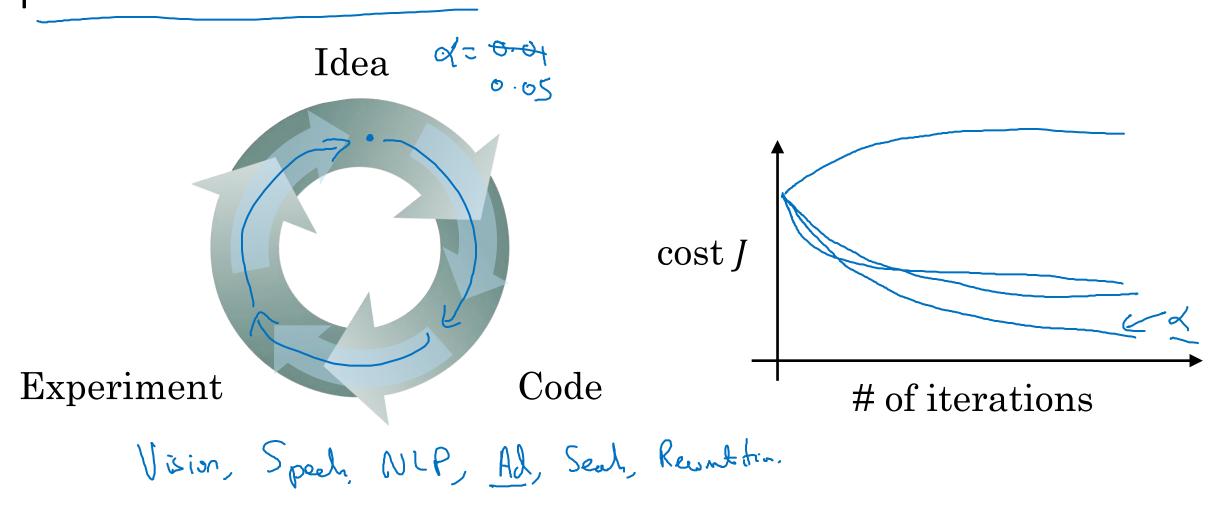
Parameters vs Hyperparameters

### What are hyperparameters?

Parameters:  $W^{[1]}$  ,  $b^{[1]}$  ,  $W^{[2]}$  ,  $b^{[2]}$  ,  $W^{[3]}$  ,  $b^{[3]}$  ...

Hyperparameters: Learning rate & #hilder layer L # hedden cents N [12] ~ [2] choice of autivortion frontion dot: Monatur, min-Loth (ize, regularjohns...

# Applied deep learning is a very empirical process





# Deep Neural Networks

What does this have to do with the brain?

#### Forward and backward propagation

$$Z^{[1]} = W^{[1]}X + b^{[1]}$$

$$A^{[1]} = g^{[1]}(Z^{[1]})$$

$$Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}$$

$$A^{[2]} = g^{[2]}(Z^{[2]})$$

$$\vdots$$

$$A^{[L]} = g^{[L]}(Z^{[L]}) = \hat{Y}$$

$$\begin{split} dZ^{[L]} &= A^{[L]} - Y \\ dW^{[L]} &= \frac{1}{m} dZ^{[L]} A^{[L]^T} \\ db^{[L]} &= \frac{1}{m} np. \, \text{sum}(dZ^{[L]}, axis = 1, keepdims = True) \\ dZ^{[L-1]} &= dW^{[L]^T} dZ^{[L]} g'^{[L]} (Z^{[L-1]}) \\ &\vdots \\ dZ^{[1]} &= dW^{[L]^T} dZ^{[2]} g'^{[1]} (Z^{[1]}) \\ dW^{[1]} &= \frac{1}{m} dZ^{[1]} A^{[1]^T} \\ db^{[1]} &= \frac{1}{m} np. \, \text{sum}(dZ^{[1]}, axis = 1, keepdims = True) \end{split}$$

