Homework 1

Calculus 2016

September 8, 2016

Problem 1

- a. If 0 < a < b, and c is any real number, rewrite the sets $\{x : a < |x-c| < b\}$ in terms of intervals. Do the same for a = 0, and also give a clear description in words. In this case, it will be something like "all the numbers between [something] and [something else] except for [these one(s)]
- b. Given a < b real numbers, describe the intervals (a,b) using the absolute value function. That is, write $(a,b) = \{x : ...\}$ where "..." is some condition using absolute value.
- c. Similarly, express $\{a,b\}$, i.e. the set containing precisely the two (different) numbers a and b (e.g. $\{-14.7, e+\pi\}$ or $\{1776, 1947\}$) using absolute values. ¹

¹Hint: choose any a and b you like, and work it out first to see how it goes for the general case. But remember that doing it for a specific example is not enough—it is supposed to be true for $\{any\}$ a, b, c (satisfying the relevant conditions), so you need to do something that works for all possible choices. In math, we don't show a statement true by making observations, unless it's possible to directly observe every single case; we have to make an argument that shows that the statement is true $\{always\}$. When there are infinitely many possible choices of a,b,c as above, we can't directly check each case by hand; we need to have a general argument.