

TOY DATA

ID	DEP DEL IS	PREV DEL DEL	AIR TIME GAP
1	1	1	15
2	1	0	2
3	1	0	35
4	0	0	40
5	0	1	68
6	0	0	30
7	0	0	90
8	0	0	28

THE SOURCE CODE FOR THE GBTClassifier() FUNCTION INDICATES THAT VARIANCE IS THE IMPURITY MEASURE

$$\text{IMPURITY (DGE)} = \text{var} [1, 1, 1, 0, 0, 0, 0, 0] = 0.268$$

PREV DEP DEL							
0	0	0	0	0	0	1	1
0	0	0	0	1	1	0	1

$$0.268 - \frac{3}{4} \times 0.267 - \frac{1}{4} \times 0.5 = -0.057$$

AIR TIME GAP							
2	15	28	30	35	40	68	90
1	1	0	0	1	0	0	0

$$\begin{aligned} \star [21.5 \text{ split}] & 0.268 - 0.75 \times 0 - 0.75 \times 0.167 = 0.143 \star \\ [32.5 \text{ split}] & 0.268 - 0.5 \times 0.333 - 0.5 \times 0.23 = -0.024 \\ [37.5 \text{ split}] & 0.268 - \frac{5}{7} \times 0.3 - \frac{2}{7} \times 0 = 0.085 \end{aligned}$$

INFO GAIN

= IMPURITY (NODE 0)

$$- \frac{N_{\text{LEFT}}}{N} \times \text{IMPURITY (NODE LEFT)}$$

$$- \frac{N_{\text{RIGHT}}}{N} \times \text{IMPURITY (NODE RIGHT)}$$

⇒ AIR TIME GAP = ROOT

LEFT BRANCH
(ALL RTI GAP < 21.5)

0	1
1	1

OUTCOME IS
HOMOGENEOUS.
NO MORE
SPLITTING.

RT BRANCH
(ALL RTI GAP ≥ 21.5)

0	0	0	0	1
0	0	0	1	0

$$0.147 - \frac{1}{6} \times 0 - \frac{5}{6} \times 0.2 = 0$$

(NO MORE SPLITTS POSS. THE
BECAUSE WE ARE OUT OF DIMENSIONS)

$$\Rightarrow \text{TREE} = \left\{ \begin{array}{ccccc} \text{idx} & \text{left} & \text{rt} & \text{Split} & \text{Value} \\ 0 & 1 & 2 & 21.5 & \text{null} \\ 1 & \text{null} & \text{null} & \text{null} & 1 \\ 2 & 3 & 4 & 0.5 & \text{null} \\ 3 & \text{null} & \text{null} & \text{null} & 0 \\ 4 & \text{null} & \text{null} & \text{null} & 0 \end{array} \right\} =$$

