Assignment 1 Question 9

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CAP6619 Summer Term 2024

```
In [ ]: %matplotlib inline
   import matplotlib.pyplot as plt
   import numpy as np
   import pandas as pd
   import seaborn as sb

In [ ]: # Read housing.header.txt as a dataframe.
   df = pd.read_csv('housing.header.txt')
   df

# Report number of instances and features
   # There are 506 instances and 14 features in the dataset
Out[ ]: Crim Zn Indus Chas Nov Rm Age Dis Rad Tax Ptratio B Istances

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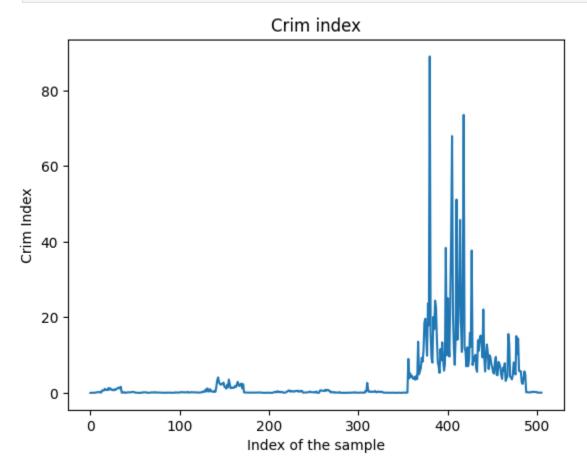
Out[ ]: Crim Zn Indus Chas Nov Rm Age Dis Rad Tax Ptratio B Istances
```

| Out[]: | | Crim | Zn | Indus | Chas | Nox | Rm | Age | Dis | Rad | Tax | Ptratio | В | Lsta |
|---------|-----|---------|------|-------|------|-------|-------|------|--------|-----|-----|---------|--------|------|
| | 0 | 0.00632 | 18.0 | 2.31 | 0 | 0.538 | 6.575 | 65.2 | 4.0900 | 1 | 296 | 15.3 | 396.90 | 4.9 |
| | 1 | 0.02731 | 0.0 | 7.07 | 0 | 0.469 | 6.421 | 78.9 | 4.9671 | 2 | 242 | 17.8 | 396.90 | 9.1 |
| | 2 | 0.02729 | 0.0 | 7.07 | 0 | 0.469 | 7.185 | 61.1 | 4.9671 | 2 | 242 | 17.8 | 392.83 | 4.0 |
| | 3 | 0.03237 | 0.0 | 2.18 | 0 | 0.458 | 6.998 | 45.8 | 6.0622 | 3 | 222 | 18.7 | 394.63 | 2.9 |
| | 4 | 0.06905 | 0.0 | 2.18 | 0 | 0.458 | 7.147 | 54.2 | 6.0622 | 3 | 222 | 18.7 | 396.90 | 5.3 |
| | ••• | | | | | | | | | | | | | |
| | 501 | 0.06263 | 0.0 | 11.93 | 0 | 0.573 | 6.593 | 69.1 | 2.4786 | 1 | 273 | 21.0 | 391.99 | 9.6 |
| | 502 | 0.04527 | 0.0 | 11.93 | 0 | 0.573 | 6.120 | 76.7 | 2.2875 | 1 | 273 | 21.0 | 396.90 | 9.0 |
| | 503 | 0.06076 | 0.0 | 11.93 | 0 | 0.573 | 6.976 | 91.0 | 2.1675 | 1 | 273 | 21.0 | 396.90 | 5.6 |
| | 504 | 0.10959 | 0.0 | 11.93 | 0 | 0.573 | 6.794 | 89.3 | 2.3889 | 1 | 273 | 21.0 | 393.45 | 6.4 |
| | 505 | 0.04741 | 0.0 | 11.93 | 0 | 0.573 | 6.030 | 80.8 | 2.5050 | 1 | 273 | 21.0 | 396.90 | 7.8 |

506 rows × 14 columns

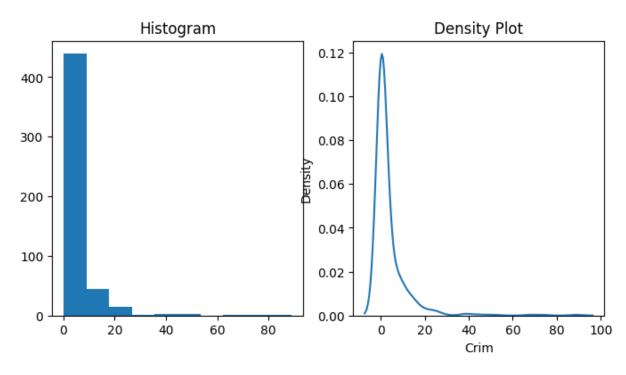
```
In []: #Report all samples with respect to the Crim index on a plot
    # (the x-axis shows the index of the sample, and the
    # y-axis shows the Crim index of the sample).
    y = df['Crim']
    x = df.index
    plt.plot(x,y)
    plt.title('Crim index')
    plt.xlabel('Index of the sample')
```

```
plt.ylabel('Crim Index')
plt.show()
```



```
In []: # Show both histogram of the Crim Index and the density of the
    # Crim index on a 1x2 frame (one row two columns).
    fig, (ax1, ax2) = plt.subplots(1,2, figsize=(8, 4))

ax1.hist(y)
ax1.set_title('Histogram')
ax2 = plt.subplot(1,2,2)
ax2.set_title('Density Plot')
sb.kdeplot(y)
plt.show()
```



```
In [ ]: # Show following four scatter plots in one frame (1x4),
        # - crim-medv, Rm-medv, Age-medv, Tax-medv
        fig, (ax1, ax2, ax3, ax4) = plt.subplots(1,4, figsize=(18, 4))
        ax1.scatter(df['Crim'],df['Medv'])
        ax1.set_xlabel('Crim Index')
        ax1.set ylabel('Medium house value (Medv)')
        ax1.set_title('Crim-Medv')
        ax2.scatter(df['Rm'], df['Medv'])
        ax2.set_xlabel('Rm')
        ax2.set_title('Rm-Medv')
        ax3.scatter(df['Age'], df['Medv'])
        ax3.set_xlabel('Age')
        ax3.set_title('Age-Medv')
        ax4.scatter(df['Tax'], df['Medv'])
        ax4.set_xlabel('Tax')
        ax4.set_title('Tax-Medv')
        plt.show()
                                                                                    Tax-Medv
                Crim-Medv
                                       Rm-Medv
                40 6
Crim Index
```

Explain how are they (Crim, Rm, Age, Tax) correlated to the medium house value

(Medv).

Crim index does not seem to be indicative of value at less than 1, but as the value of the Crim index grows, Medv trends downwards.

As Rm increases, Medv also increases in value.

Age does not seem to be related in any particular way to Medv.

Tax also does not seem to be related, but over a certain threshold, there does seem to be a decrease in value of Medv.

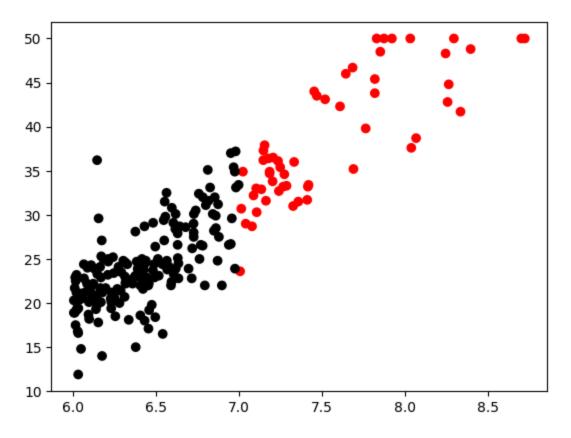
```
In [ ]: # Create a subset which only includes properties with Crim less than 1 (inclusive)
# and Rm greater than 6 (inclusive).

subset = df[(df['Crim']<=1) & (df['Rm'] >= 6)]
subset.head()
```

```
Out[]:
             Crim
                    Zn Indus Chas
                                     Nox
                                            Rm Age
                                                         Dis Rad Tax Ptratio
                                                                                   B Lstat
        0 0.00632 18.0
                          2.31
                                  0 0.538 6.575 65.2 4.0900
                                                                1 296
                                                                          15.3 396.90
                                                                                       4.98
        1 0.02731
                          7.07
                                  0 0.469 6.421 78.9 4.9671
                    0.0
                                                                2 242
                                                                          17.8 396.90
                                                                                       9.14
        2 0.02729
                          7.07
                                  0 0.469 7.185 61.1 4.9671
                                                                          17.8 392.83
                                                                                       4.03
                    0.0
                                                                2 242
        3 0.03237
                    0.0
                          2.18
                                  0 0.458 6.998 45.8 6.0622
                                                                3 222
                                                                          18.7 394.63
                                                                                       2.94
        4 0.06905
                    0.0
                          2.18
                                  0 0.458 7.147 54.2 6.0622
                                                                3 222
                                                                          18.7 396.90
                                                                                       5.33
```

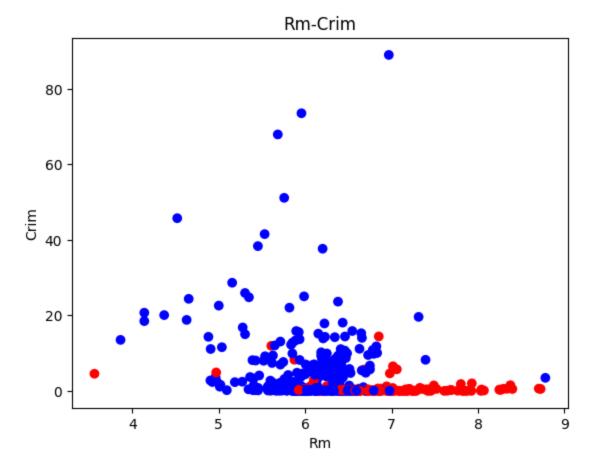
```
In []: # Show a scatter plot between Rm and Medv (x=Rm, y=Medv)
# Color >= 7 Rm values as red, rest as black

color = np.where(subset['Rm'] >= 7, 'r', np.where(subset['Medv'], 'k','r'))
plt.scatter(subset['Rm'], subset['Medv'], c=color)
plt.show()
```



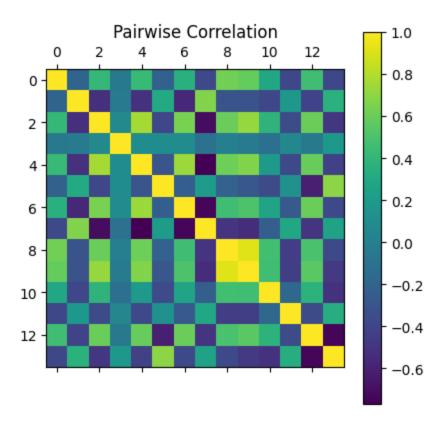
In []: # Create a scatter plot between Rm and Crim and show all 506 properties on the plot
Color properties where Medv >= 24 as red, and rest as blue.

color = np.where(df['Medv'] >= 24, 'r', np.where(df['Crim'], 'b','r'))
scatter = plt.scatter(df['Rm'], df['Crim'], c=color)
plt.title('Rm-Crim')
plt.xlabel("Rm")
plt.ylabel("Crim")
plt.show()



```
In [ ]: # Report the pairwise correlation between every two variables
    # (either as a matrix or as a level plot)

pc = df.corr('pearson')
plt.matshow(pc)
plt.title('Pairwise Correlation')
cb = plt.colorbar()
cb.ax.tick_params(labelsize=10)
plt.show()
```

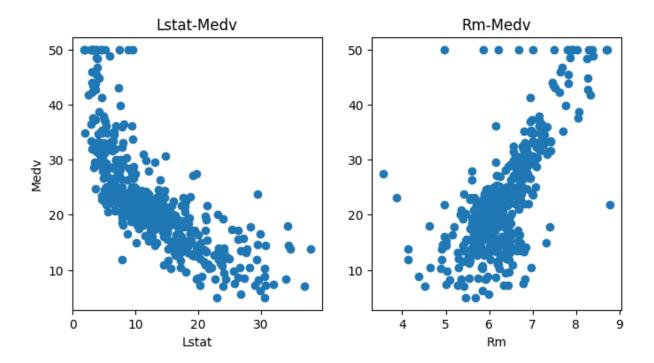


Please explain which variable is most positively correlated to Medv, and which variable is most negatively correlated to Medv.

The variable that is most positively correlated to Medv seems to be Rm; based on the pairwise correlation level plot, it is the closest to 1.0 of all the features, which suggests that it is the most positively correlated to Medv.

The variable that is most negatively correlated to Medv is Lstat; it has a correlation value of between roughly -0.6 and -0.8, which means that when Medv value goes up, Lstat value trends downwards, and vice versa.

```
In []: # Draw scatterplots to show relationship between each attribute and Medv
fig, (ax1, ax2) = plt.subplots(1,2, figsize=(8, 4))
ax1.scatter(df['Lstat'], df['Medv'])
ax1.set_title('Lstat-Medv')
ax1.set_xlabel('Lstat')
ax1.set_ylabel('Medv')
ax2.scatter(df['Rm'], df['Medv'])
ax2.scatter(df['Rm-Medv')
ax2.set_title('Rm-Medv')
plt.show()
```



Explain how to use scatterplots to find attributes which are positively correlated, negatively correlated, or independent of Medv, respectively.

Scatterplots can give us a good indication or visualization how the data points trend with regards to two variables. If the general slope of the data points are positive, and most points are in the trajectory of the best fit line, then there is a strong correlation between the attribute and Medv. The strength of the correlation depends on how many data points seem to adhere to this line. This is the same for negatively correlated attributes, just based on a negative/downwords slope.

If there is no pattern that can be seen, it is a good indicator that the attribute is simply independent of Medv.

```
# Create a new instance with the mentioned attribute values.
In [ ]:
        tmp = {'Crim':1.0, 'Zn':0.2, 'Indus':6, 'Chas':0.1, 'Nox':6.5, 'Rm':5,
               'Age':100, 'Dis':4.1,'Rad':4.5,'Tax':21,'Ptratio':20,'B':300,
               'Lstat':12, 'Medv':20.5}
        df.loc[len(df)] = tmp
        print(df.tail(1))
            Crim
                   Zn
                      Indus Chas Nox
                                          Rm
                                                                                 В
                                                Age
                                                     Dis
                                                          Rad
                                                               Tax
                                                                    Ptratio
       506
             1.0
                  0.2
                         6.0
                               0.1 6.5 5.0 100.0 4.1
                                                         4.5
                                                                21
                                                                       20.0 300.0
            Lstat Medv
             12.0 20.5
       506
In [ ]: # Report the number of instances and features of the new dataframe.
        # There are 507 instances and 14 features.
```

| Out[]: | | Crim | Zn | Indus | Chas | Nox | Rm | Age | Dis | Rad | Tax | Ptratio | В | Ls |
|---------|-----|---------|------|-------|------|-------|-------|-------|--------|-----|-----|---------|--------|-----|
| | 0 | 0.00632 | 18.0 | 2.31 | 0.0 | 0.538 | 6.575 | 65.2 | 4.0900 | 1.0 | 296 | 15.3 | 396.90 | 4. |
| | 1 | 0.02731 | 0.0 | 7.07 | 0.0 | 0.469 | 6.421 | 78.9 | 4.9671 | 2.0 | 242 | 17.8 | 396.90 | 9. |
| | 2 | 0.02729 | 0.0 | 7.07 | 0.0 | 0.469 | 7.185 | 61.1 | 4.9671 | 2.0 | 242 | 17.8 | 392.83 | 4. |
| | 3 | 0.03237 | 0.0 | 2.18 | 0.0 | 0.458 | 6.998 | 45.8 | 6.0622 | 3.0 | 222 | 18.7 | 394.63 | 2. |
| | 4 | 0.06905 | 0.0 | 2.18 | 0.0 | 0.458 | 7.147 | 54.2 | 6.0622 | 3.0 | 222 | 18.7 | 396.90 | 5. |
| | ••• | | | | | | | | | | | | | |
| | 502 | 0.04527 | 0.0 | 11.93 | 0.0 | 0.573 | 6.120 | 76.7 | 2.2875 | 1.0 | 273 | 21.0 | 396.90 | 9. |
| | 503 | 0.06076 | 0.0 | 11.93 | 0.0 | 0.573 | 6.976 | 91.0 | 2.1675 | 1.0 | 273 | 21.0 | 396.90 | 5. |
| | 504 | 0.10959 | 0.0 | 11.93 | 0.0 | 0.573 | 6.794 | 89.3 | 2.3889 | 1.0 | 273 | 21.0 | 393.45 | 6. |
| | 505 | 0.04741 | 0.0 | 11.93 | 0.0 | 0.573 | 6.030 | 80.8 | 2.5050 | 1.0 | 273 | 21.0 | 396.90 | 7. |
| | 506 | 1.00000 | 0.2 | 6.00 | 0.1 | 6.500 | 5.000 | 100.0 | 4.1000 | 4.5 | 21 | 20.0 | 300.00 | 12. |

507 rows × 14 columns

```
Crim
              Zn Indus Chas
                                Nox
                                      Rm
                                             Age
                                                    Dis Rad Tax \
                                            65.2 4.0900 1.0
0
    0.00632 18.0
                   2.31
                          0.0 0.538 6.575
                                                              296
                   7.07
                                            78.9 4.9671 2.0 242
1
    0.02731
             0.0
                          0.0 0.469 6.421
    0.02729
                                            61.1 4.9671 2.0 242
2
             0.0
                  7.07
                          0.0 0.469 7.185
3
    0.03237
             0.0
                   2.18
                         0.0 0.458 6.998
                                            45.8 6.0622 3.0 222
4
    0.06905
                  2.18
                         0.0 0.458 7.147
                                            54.2 6.0622 3.0 222
             0.0
. .
        . . .
              . . .
                  . . .
                          . . .
                               . . .
                                     . . .
                                             . . .
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                                                              . . .
502 0.04527
             0.0 11.93
                         0.0 0.573 6.120
                                            76.7 2.2875 1.0
                                                              273
503 0.06076
             0.0 11.93
                         0.0 0.573 6.976
                                            91.0 2.1675 1.0 273
504 0.10959
             0.0 11.93
                         0.0 0.573 6.794
                                            89.3 2.3889 1.0 273
505 0.04741
             0.0 11.93
                         0.0 0.573 6.030
                                            80.8 2.5050 1.0 273
506 1.00000
             0.2
                   6.00
                          0.1 6.500 5.000 100.0 4.1000 4.5 21
    Ptratio
                 B Lstat Medv Dummy
0
       15.3 396.90
                    4.98
                          24.0
                                    0
       17.8 396.90
                     9.14 21.6
                                    2
1
2
       17.8 392.83
                     4.03
                          34.7
                                    3
3
       18.7 394.63
                     2.94 33.4
                                    3
4
       18.7 396.90
                     5.33 36.2
                                    2
       . . .
             . . .
                     . . .
                           . . .
. .
                                 . . .
       21.0 396.90
502
                     9.08 20.6
                                    4
       21.0 396.90
                     5.64 23.9
                                    4
503
504
       21.0 393.45
                     6.48 22.0
                                    2
505
       21.0 396.90
                     7.88 11.9
                                    3
506
       20.0 300.00 12.00 20.5
                                    0
```

[507 rows x 15 columns]