

$$AB \left(\begin{array}{ccccc|c} 5_{11} & 7_{12} & 6_{13} & 5_{14} & 23 \\ 7_{21} & 10_{22} & 8_{23} & 7_{24} & 32 \\ 6_{31} & 8_{32} & 10_{33} & 9_{34} & 33 \\ 5_{41} & 7_{42} & 9_{43} & 10_{44} & 31 \end{array} \right) \quad \begin{array}{l} i = (1; n-1) \\ j = (i; n+1) \\ k = (i+1; n) \end{array}$$

1-я строка лежит на $(i=1)$:

$$\tilde{a}_{11} = 1 \quad \tilde{a}_{12} = \frac{7}{5} \quad \tilde{a}_{13} = \frac{6}{5} \quad \tilde{a}_{14} = 1 \quad \tilde{a}_{15} = \frac{23}{5}$$

Легонько:

$$\tilde{a}_{21} = 7 - 1 \cdot 7 = 0 \quad \tilde{a}_{22} = 10 - 1 \cdot 7 = \frac{1}{5} \quad \tilde{a}_{23} = 8 - \frac{6}{5} \cdot 7 = -\frac{2}{5}$$

$$\tilde{a}_{24} = 7 - 1 \cdot 7 = 0 \quad \tilde{a}_{25} = 32 - \frac{1}{5} \cdot 7 = -\frac{1}{5}$$

$$\tilde{a}_{31} = 6 - 1 \cdot 6 = 0 \quad \tilde{a}_{32} = 8 - \frac{7}{5} \cdot 6 = -\frac{2}{5}$$

$$\tilde{a}_{33} = 10 - 1 \cdot 10 = 0 \quad \tilde{a}_{34} = 9 - 6 \cdot 1 = 3$$

$$\tilde{a}_{35} = 33 - \frac{1}{5} \cdot 10 = \frac{23}{5}$$

$$\tilde{a}_{41} = 5 - 1 \cdot 5 = 0 \quad \tilde{a}_{42} = 7 - 5 \cdot \frac{7}{5} = 0 \quad \tilde{a}_{43} = 9 - 5 \cdot \frac{6}{5} = 3$$

$$\tilde{a}_{44} = 31 - \frac{1}{5} \cdot 9 = 8$$

Неприменим:

$$\left(\begin{array}{ccccc|c} 1 & \frac{7}{5} & \frac{6}{5} & 1 & \frac{23}{5} \\ 0 & \frac{1}{5} & -\frac{3}{5} & 0 & -\frac{1}{5} \\ 0 & -\frac{2}{5} & \frac{14}{5} & 3 & \frac{27}{5} \\ 0 & 0 & 3 & 5 & 8 \end{array} \right)$$

2-я строка лежит на $(i=2)$:

$$\tilde{a}_{22} = 1 \quad \tilde{a}_{23} = -\frac{2}{5} \cdot 1 = -2 \quad \tilde{a}_{24} = 0 \quad \tilde{a}_{25} = -\frac{1}{5} \cdot 1 = -\frac{1}{5}$$

Легонько:

$$\tilde{a}_{32} = -\frac{2}{5} \cdot (-\frac{7}{5}) \cdot 1 = 0 \quad \tilde{a}_{33} = \frac{14}{5} \cdot (-\frac{3}{5}) \cdot -2 = 2 \quad \tilde{a}_{34} = 5 \cdot (-\frac{3}{5}) \cdot 0 = 0$$

$$\tilde{a}_{35} = 8 \cdot (-\frac{1}{5}) \cdot (-1) \cdot (-\frac{7}{5}) = -\frac{14}{5} \quad \frac{27}{5} \cdot (-1) \cdot (-\frac{1}{5}) = 5$$

$$\tilde{a}_{42} = 0 \quad \tilde{a}_{43} = 8 \quad \tilde{a}_{44} = 5 \quad \tilde{a}_{45} = 8$$

~~30~~ 3 5 8

неприменим:

$$\left(\begin{array}{cccc|c} 1 & \frac{7}{5} & \frac{6}{5} & 1 & \frac{23}{5} \\ 0 & 1 & -2 & 0 & -1 \\ 0 & 0 & 2 & 3 & 5 \\ 0 & 0 & 3 & 5 & 8 \end{array} \right)$$

3 строка левая ($i=3$):

$$\tilde{a}_{33} = 1 \quad \tilde{a}_{34} = \frac{3}{2} \quad \tilde{a}_{35} = \frac{5}{2}$$

левомест:

$$\tilde{a}_{43} = 0 \quad \tilde{a}_{44} = 5 - 3 \cdot \frac{3}{2} = \frac{1}{2}$$

$$\tilde{a}_{45} = 8 - 3 \cdot \frac{5}{2} = \frac{1}{2}$$

неприменим:

$$\left(\begin{array}{cccc|c} 1 & \frac{7}{5} & \frac{6}{5} & 1 & \frac{23}{5} \\ 0 & 1 & -2 & 0 & -1 \\ 0 & 0 & 1 & \frac{3}{2} & \frac{5}{2} \\ 0 & 0 & 0 & 1/2 & 1/2 \end{array} \right)$$

Оформим x_0 :

$$x_4 = \frac{1}{2} \cdot \frac{2}{1} = 1$$

$$x_3 = \tilde{a}_{35} - \left(\frac{3}{2} \cdot x_4 + \dots \right)$$

$$x_3 = \frac{5}{2} - \frac{3}{2} \cdot 1 = 1$$

$$x_2 = \frac{2}{1/2} = 2$$

$$x_1 = -1 - (0 \cdot x_4 - 2 \cdot x_3)$$

$$x_1 = -1 - 0 + 2 = 1$$

$$x_1 = \frac{23}{5} - \left(1 \cdot x_4 + \frac{6}{5} \cdot x_3 + \frac{1}{5} \cdot x_2 \right) =$$

$$= \frac{23}{5} - \frac{5 + 6 + 1}{5} = \frac{5}{5} = 1$$

Ответ: $x_1 = 1$
 $x_2 = 1$
 $x_3 = 1$
 $x_4 = 1$