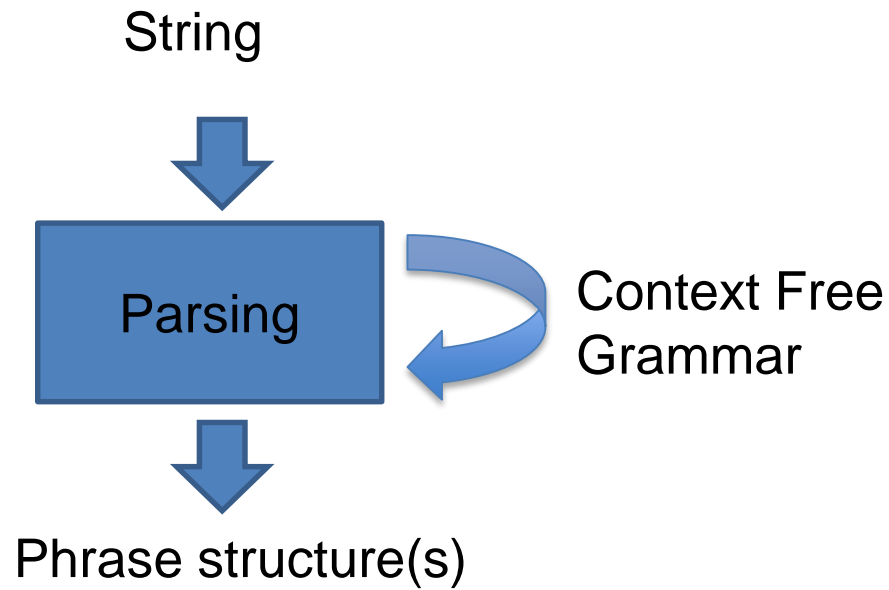


CE/CZ4045 Natural Language Processing

Syntactic Parsing (Chapter 13)

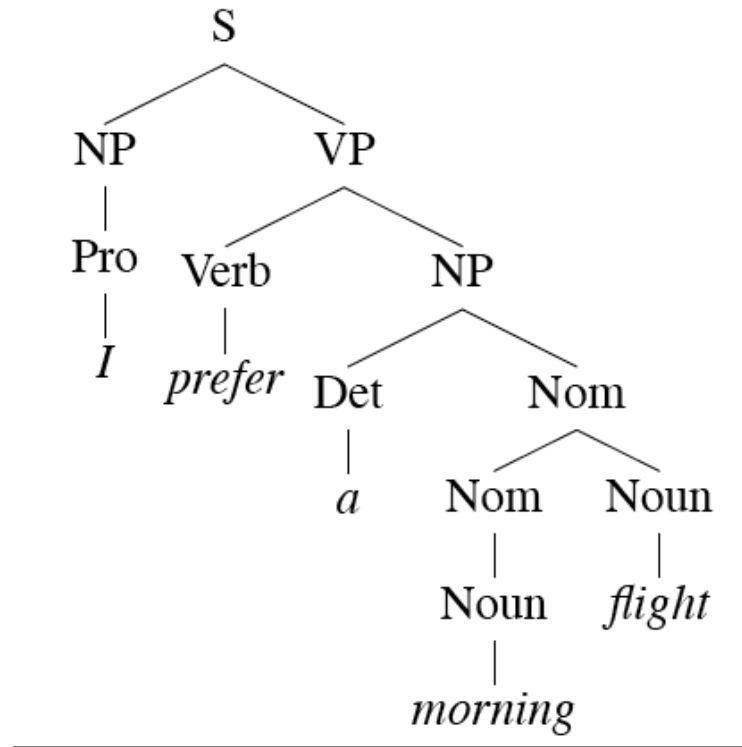


Syntactic parsing in the course



Phrase structure

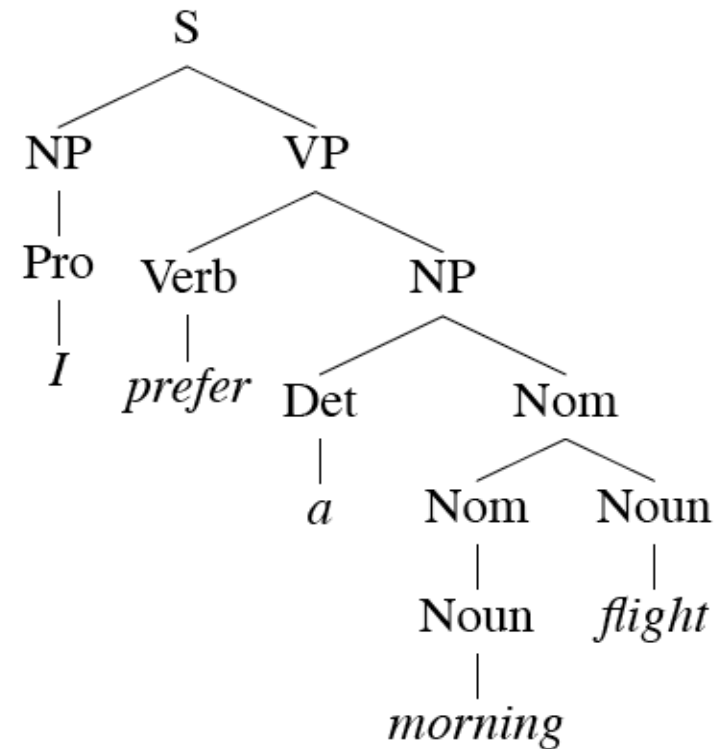
- Organizes words into nested constituents



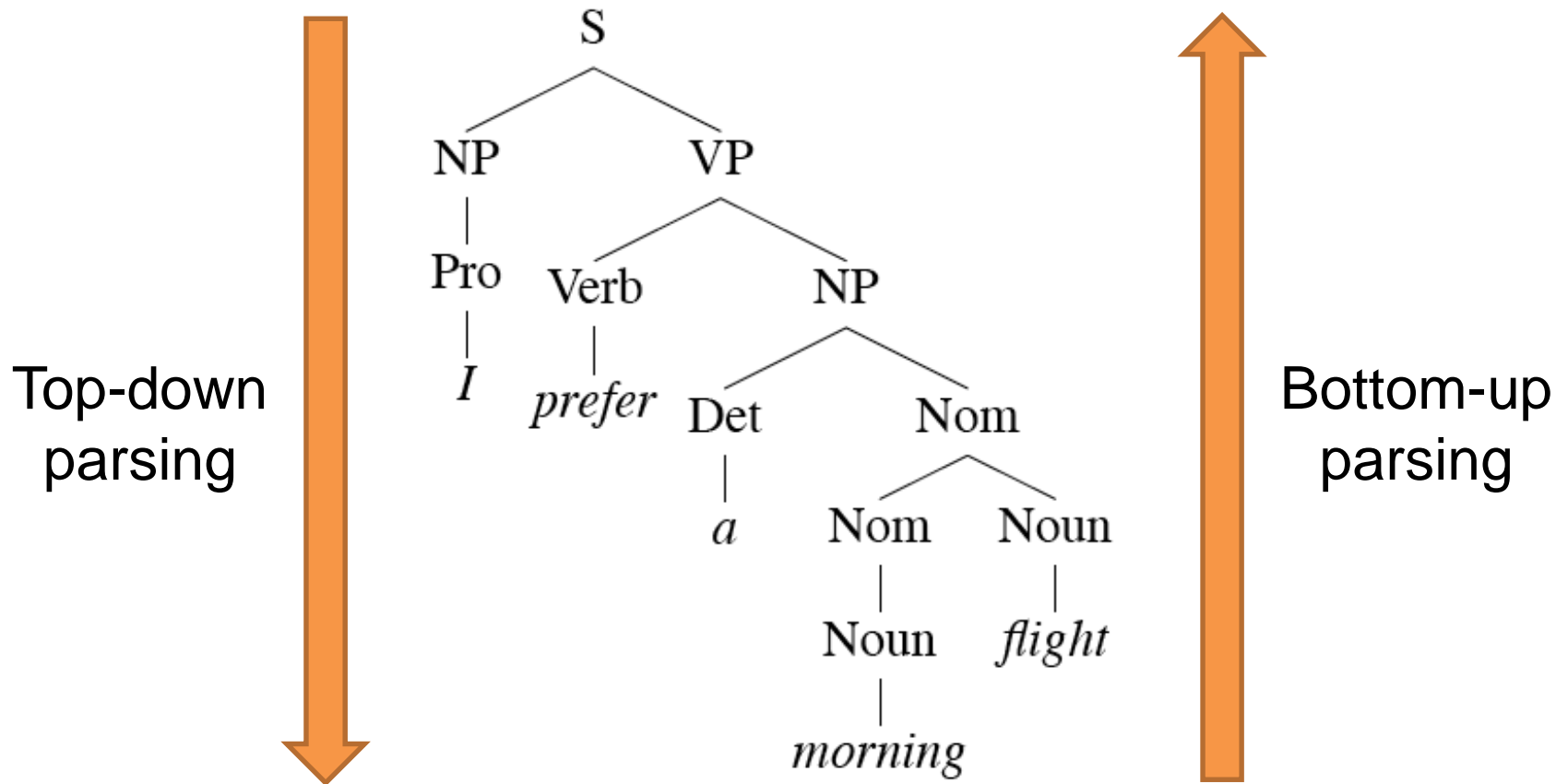
Context-free grammar

- $G = (T, N, S, R)$
 - T: a set of terminals (e.g. 'flight')
 - N: a set of non-terminals (e.g. Noun)
 - S: the start symbol, a non-terminal
 - R: rules of the form $X \rightarrow \gamma$
 - X: a non-terminal
 - γ : a sequence of terminals and non-terminals

$NP \rightarrow Det\ Nominal$
$NP \rightarrow ProperNoun$
$Nominal \rightarrow Noun \mid Nominal\ Noun$

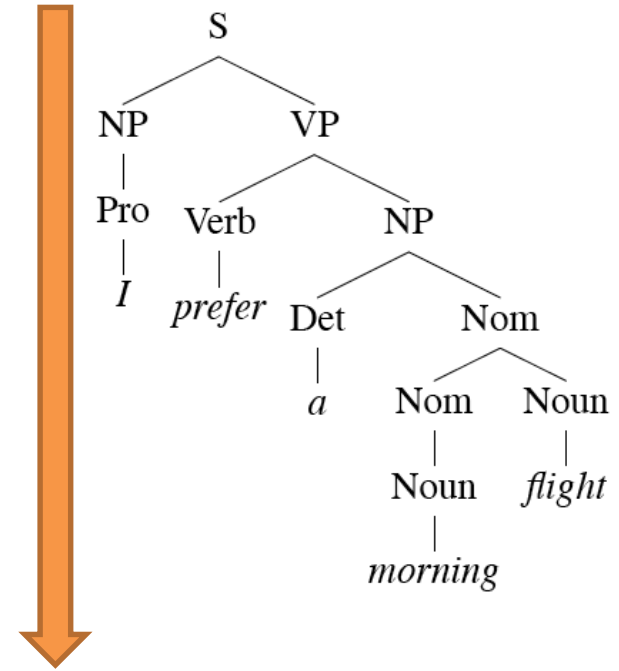


Parsing strategies



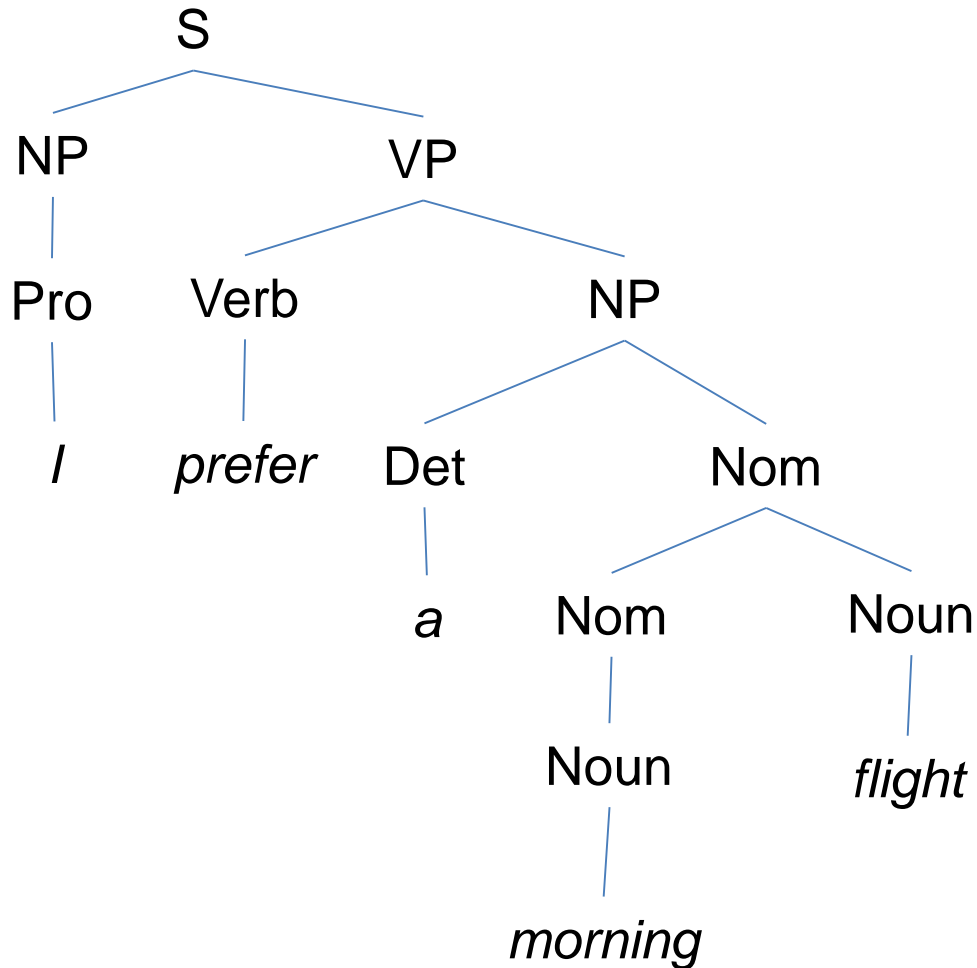
Top-down parsing

- Goal-directed
 - Start from 'S'
- Rewrite the goal(s) with the RHS of relevant rules, e.g,
 - $S \rightarrow NP VP$,
 - $VP \rightarrow Verb NP$
- Parsing is finished when the rewriting **generates** the whole string



Top-down
parsing

Top-down parsing: Example



I prefer a morning flight.

1. $S \rightarrow NP VP$
2. $NP \rightarrow Pro$
 $Pro \rightarrow I$
3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$
4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$
5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow flight$
6. $Nom \rightarrow Noun$
 $Noun \rightarrow morning$

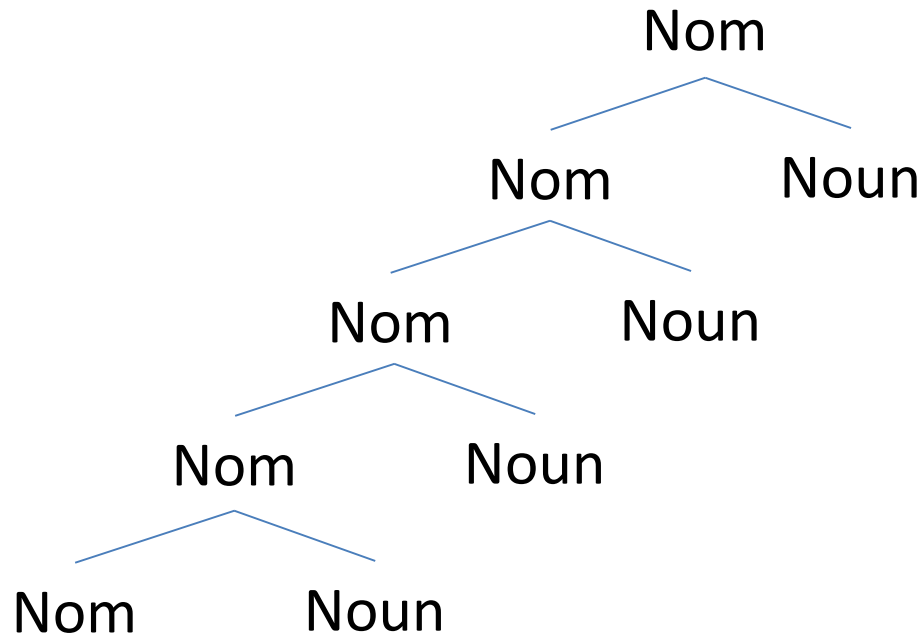


Top-down parsing: Issues (1/2)

- If a goal can be written in several ways, there is a choice of which rule to apply
 - Example: $NP \rightarrow Pro$, $NP \rightarrow Det\ Nom$
- Search problem
 - Search methods: Depth-first, breadth-first, goal-ordering, etc.
- Need grammar-driven control for optimization
 - May waste lots of time in trying rules that are inconsistent with the input string
 - Example: left recursive rules (e.g. $Nom \rightarrow Nom\ Noun$)



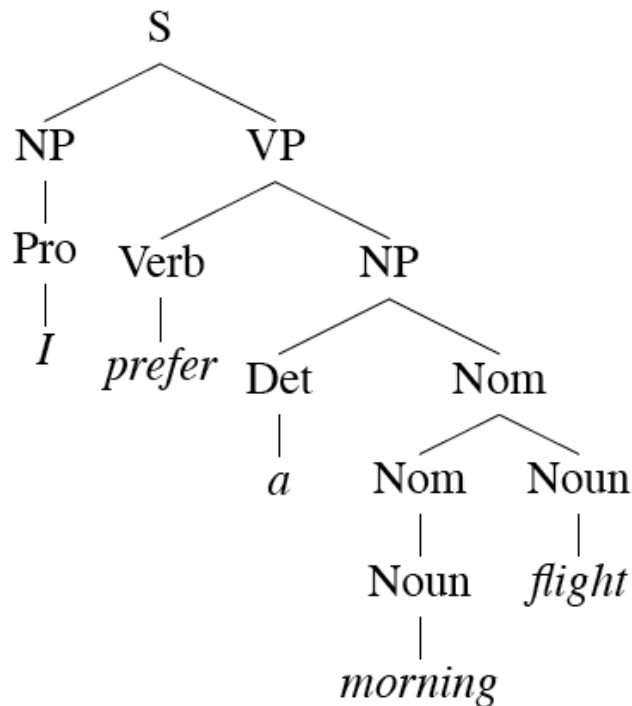
Top-down parsing: left recursive rules



Example: Southeast Asia Public Interest Research Group

Top-down parsing: Issues (2/2)

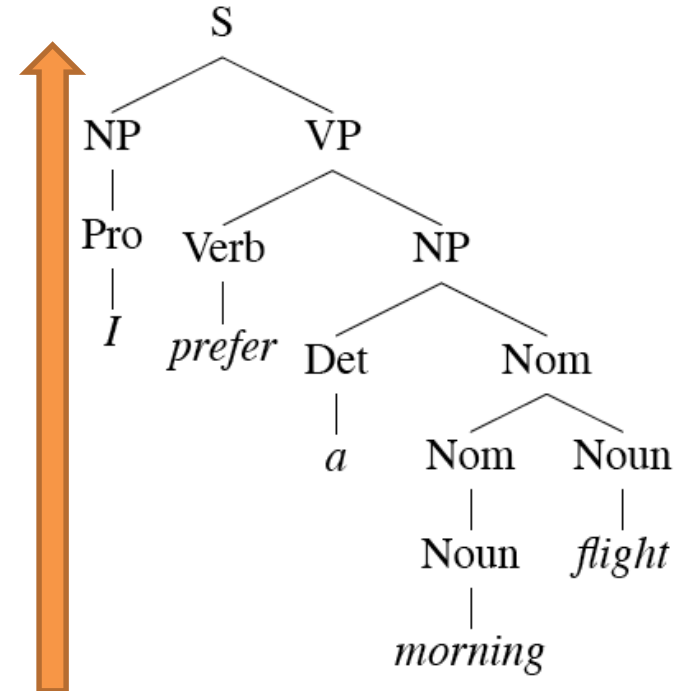
- A part-of-speech like Noun can be replaced with any noun
 - Trying out all rules of a part-of-speech is time consuming
- In practice, part-of-speech tags are predetermined



1. $S \rightarrow NP VP$
2. $NP \rightarrow Pro$
 $Pro \rightarrow I$
3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$
4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$
5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow flight$
6. $Nom \rightarrow Noun$
 $Noun \rightarrow morning$

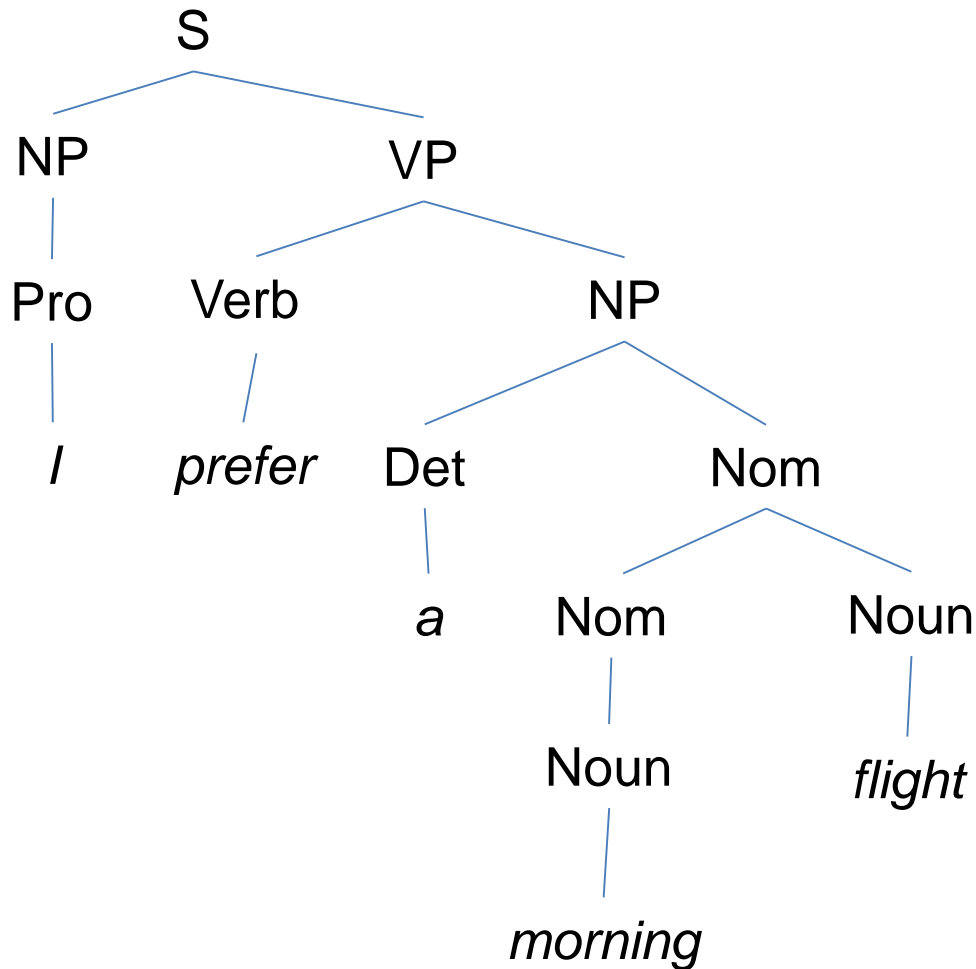
Bottom-up parsing

- Data-directed
 - Start with words
- If a substring matches the RHS of a rule, replace the substring with the LHS
 - Example: Nom → Noun (“morning”)
 - Example: Nom → Nom Noun
 (“*morning flight*”)
- Parsing is finished when the whole string is replaced with a goal



Bottom-up approach: Example

I prefer a morning flight.



6. $S \rightarrow NP VP$

5. $Pro \rightarrow I$
 $NP \rightarrow Pro$

4. $Verb \rightarrow prefer$
 $VP \rightarrow Verb NP$

3. $Det \rightarrow a$
 $NP \rightarrow Det Nom$

2. $Noun \rightarrow flight$
 $Nom \rightarrow Nom Noun$

1. $Noun \rightarrow morning$
 $Nom \rightarrow Noun$

Parsing strategies

Top-down parsing

- Goal-directed
 - Start from 'S'
- Rewrite the goal(s) with the RHS of relevant rules
 - Example: $S \rightarrow NP VP$
- Parsing is finished when the rewriting generates the whole string

Bottom-up parsing

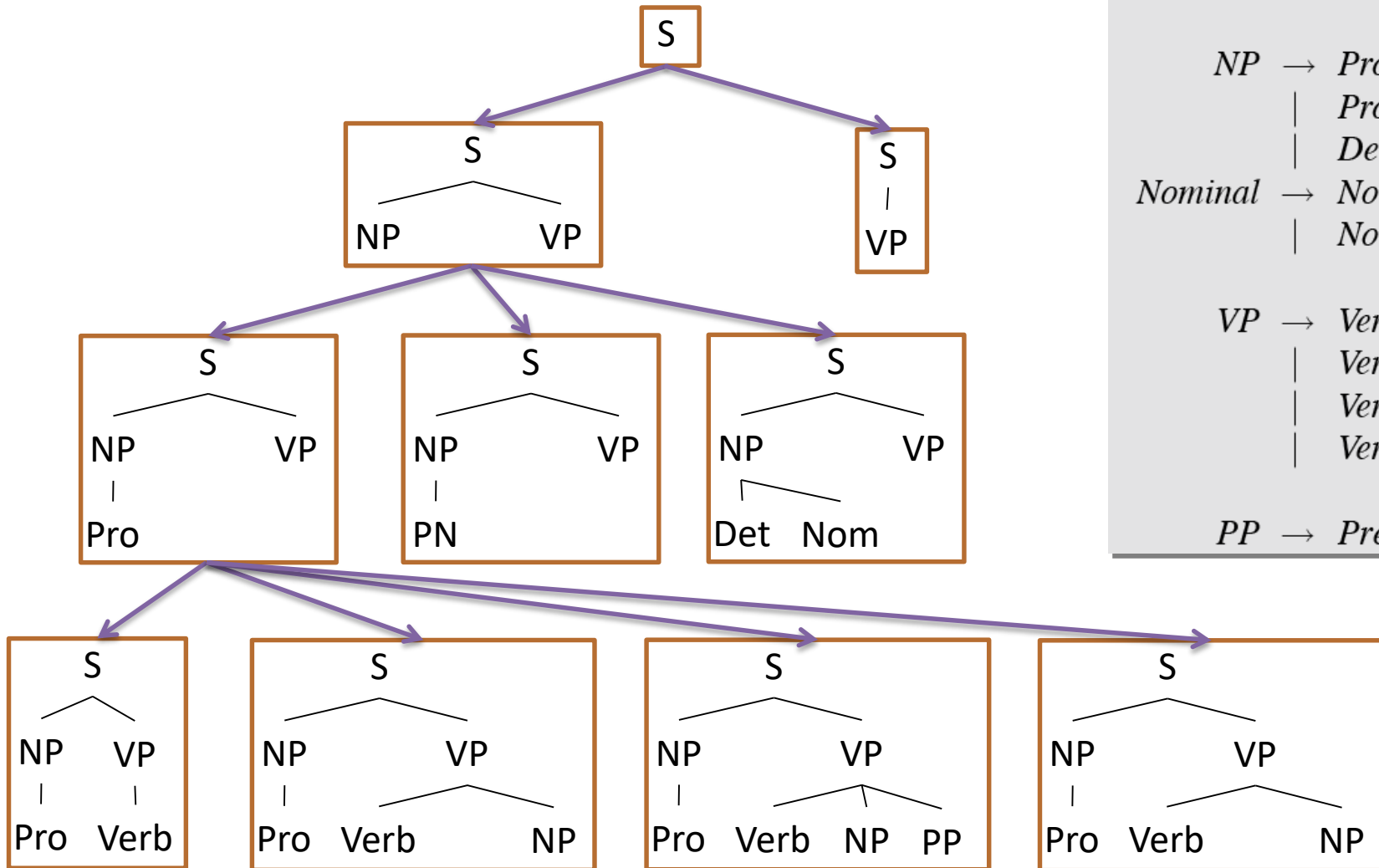
- Data-directed
 - Start with words
- - If a substring matches the RHS of a rule, replace the substring with the LHS
 - Example: $Nom \rightarrow Noun$
 - $Nom \rightarrow Nom Noun$
(*“morning flight”*)
- Parsing is finished when the whole string is replaced with a goal

Top-down vs. Bottom-up parsing

- Top-down
 - Waste lots of time in trying inconsistent rule applications
 - The application of the rules does not lead the generation of the given string
 - Never explore subtrees that cannot find a place in some S-rooted tree
 - All trees are generated starting with S.
- Bottom-up
 - Never suggest trees that are not grounded in the input string
 - All trees are generated based on input string
 - Trees that have no hope of leading to an S are generated
 - Some trees cannot proceed further to reach S



Parsing as search (e.g. I prefer a morning flight)



Grammar Rules

$S \rightarrow NP VP \mid VP$

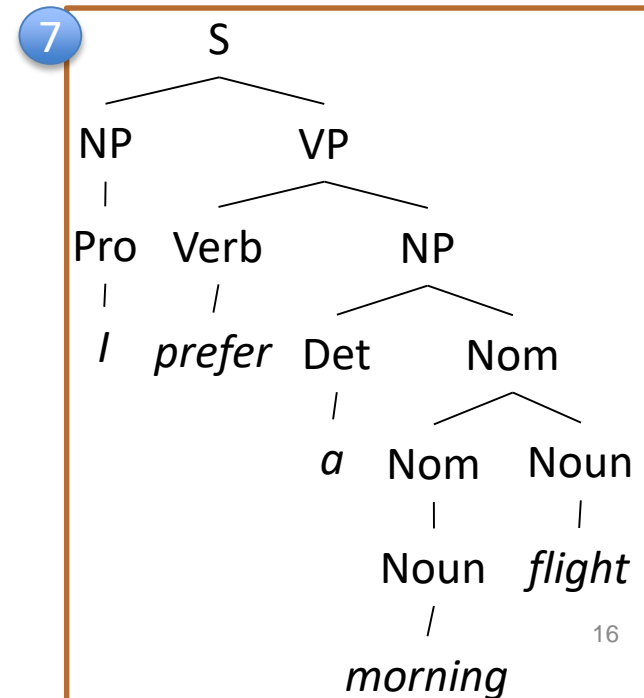
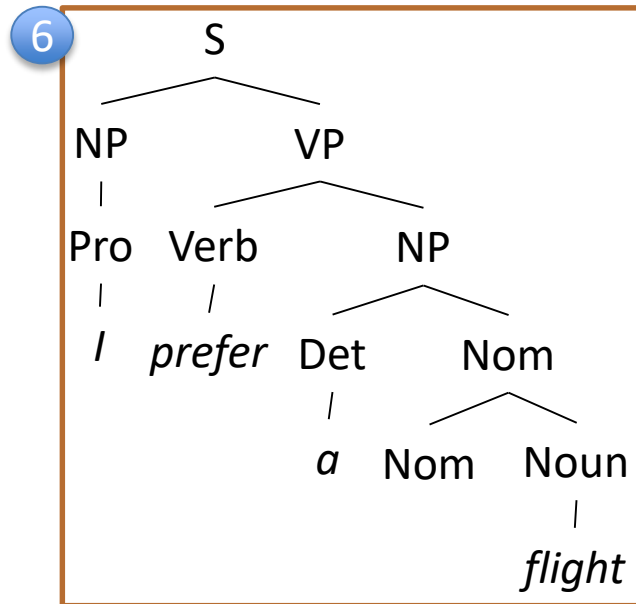
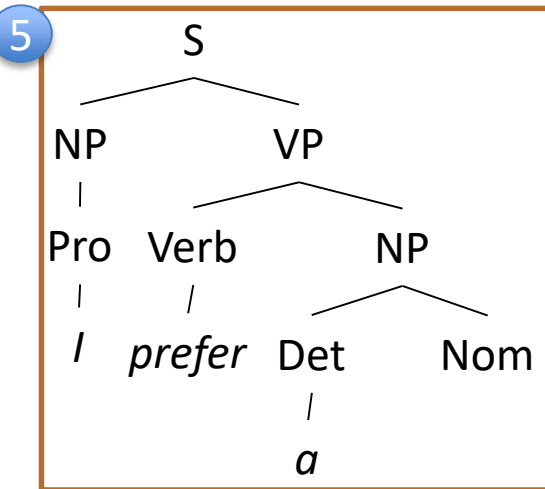
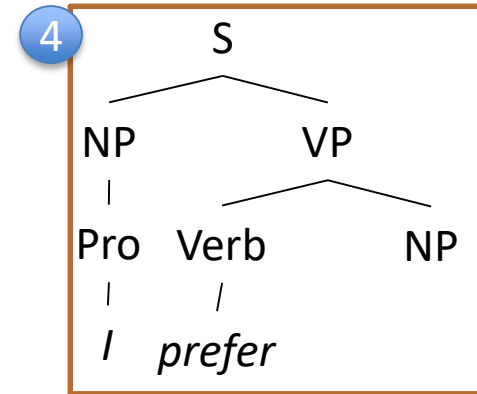
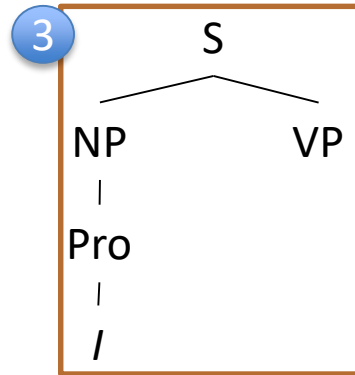
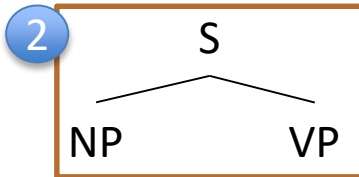
$NP \rightarrow \begin{array}{l} \textit{Pronoun} \\ \textit{Proper-Noun} \\ \textit{Det Nominal} \end{array}$

$Nominal \rightarrow \begin{array}{l} \textit{Nominal Noun} \\ \textit{Noun} \end{array}$

$VP \rightarrow \begin{array}{l} \textit{Verb} \\ \textit{Verb NP} \\ \textit{Verb NP PP} \\ \textit{Verb PP} \end{array}$

$PP \rightarrow \textit{Preposition NP}$

Parsing as search



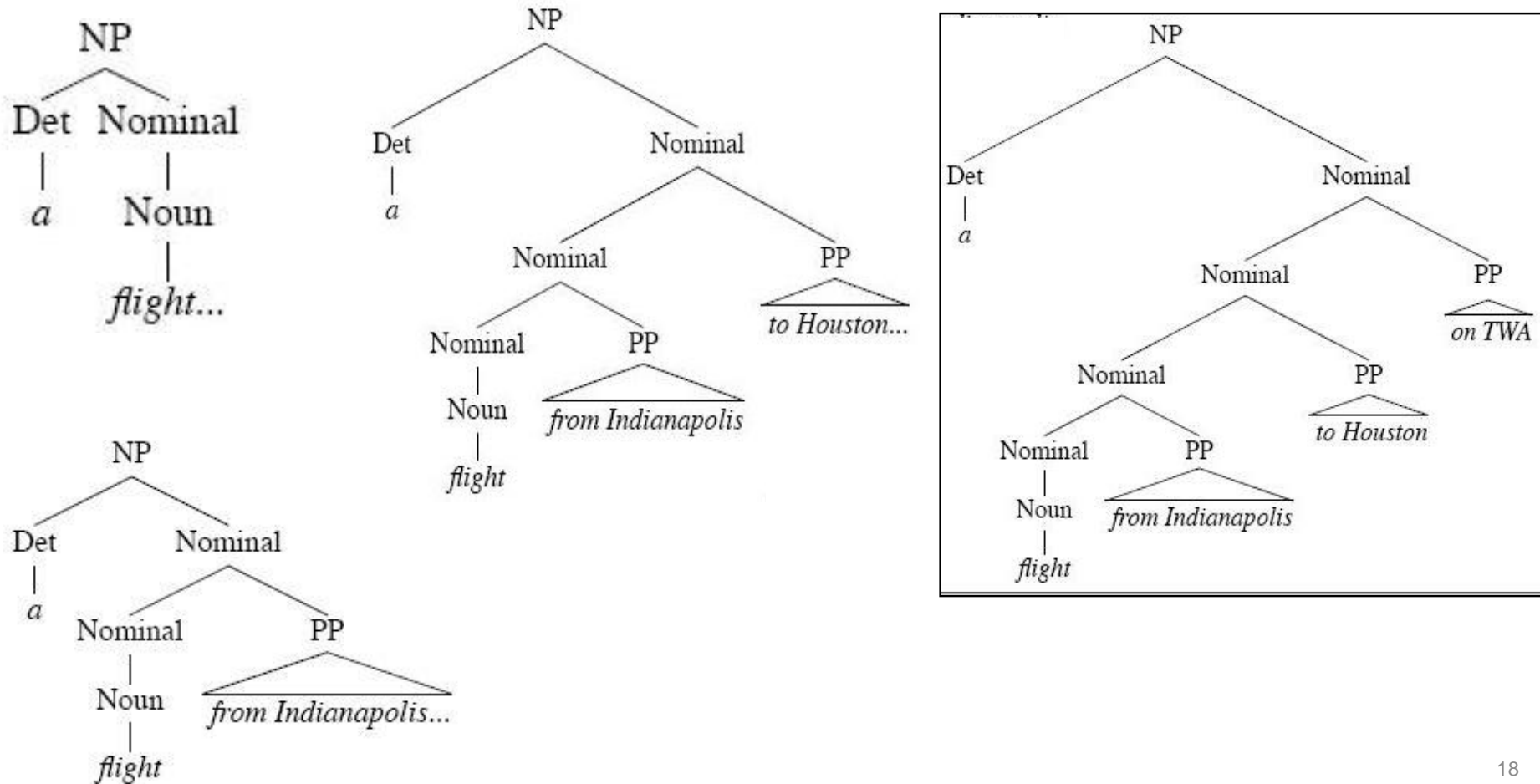
Exercise: Parsing as search

- Draw a search space for parsing “I sleep” in a top-down parsing based on L0 grammar

Grammar Rules	
S	$\rightarrow NP VP$
NP	\rightarrow $\begin{array}{l} \textit{Pronoun} \\ \textit{Proper-Noun} \\ \textit{Det Nominal} \end{array}$
$Nominal$	\rightarrow $\begin{array}{l} \textit{Nominal Noun} \\ \textit{Noun} \end{array}$
VP	\rightarrow $\begin{array}{l} \textit{Verb} \\ \textit{Verb NP} \\ \textit{Verb NP PP} \\ \textit{Verb PP} \end{array}$
PP	$\rightarrow \textit{Preposition NP}$

Repeated work in parsing-as-search

- Parsing: “a flight from Indianapolis to Houston on TWA” (Figure 13.7)



Dynamic programming parsing methods

- Parsing-as-search may have exponentially many parse states
- Dynamic programming solves the problem of doing repeated work
 - Memorization (remembering solved subproblems)
- Bottom-up approach: **CKY parsing**
 - Parse table
- Top-down approach: **Earley parsing**
 - Dotted rules



Parse table

- Cell $[i, j]$ contains the syntactic structures of the substring from the $(i + 1)$ -th word to the j -th word

0	Book	1	the	2	flight	3	through
S, VP, Verb Nominal, Noun [0,1]			S,VP,X2 [0,3]				[0,4]
	Det [1,2]		NP [1,3]				[1,4]
			Nominal, Noun [2,3]				[2,4]
						Prep [3,4]	

\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow Aux NP VP$

$S \rightarrow VP$

$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

$NP \rightarrow Pronoun$

$NP \rightarrow Proper-Noun$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow Noun$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow Verb$

$VP \rightarrow Verb NP$

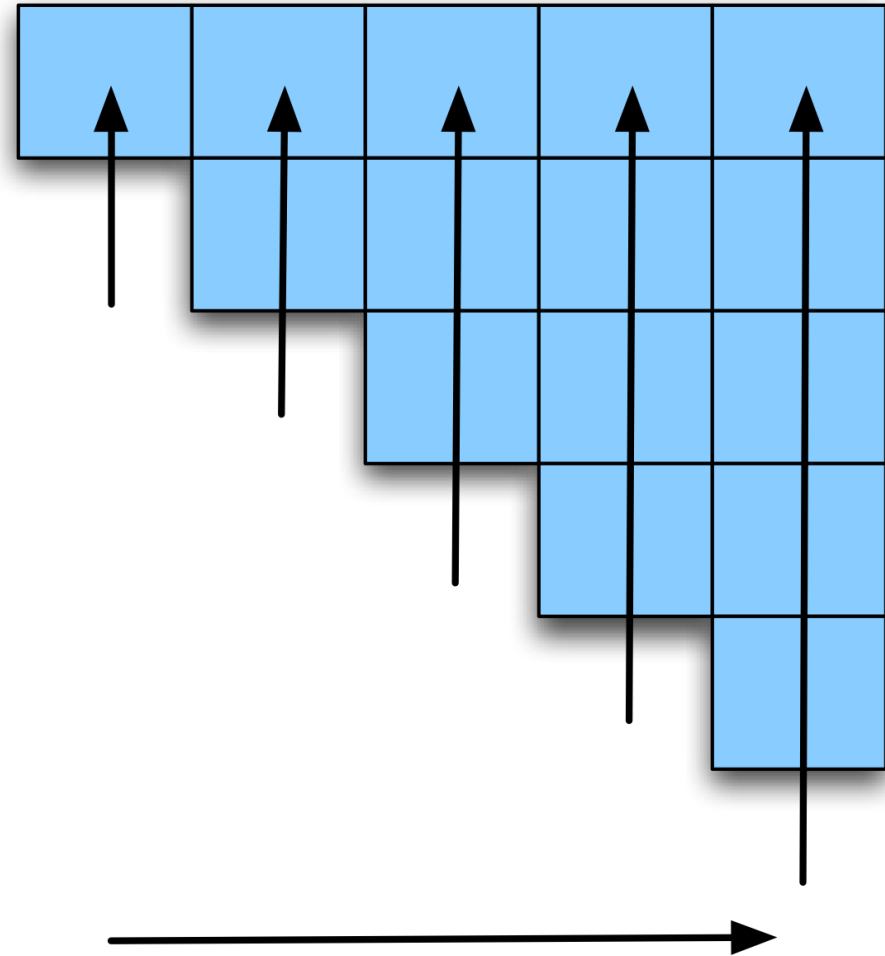
$VP \rightarrow Verb NP PP$



Parse table: Parsing sequence

Book the flight through Houston

S, VP, Verb Nominal, Noun [0,1]		S,VP,X2 [0,3]		S,VP,X2 [0,5]
	Det [1,2]	NP [1,3]		NP [1,5]
		Nominal, Noun [2,3]		Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]



Parse table: A fast method of filling in each cell

Assume an RHS has
exactly two items ($X \rightarrow Y Z$)

[book₁] [the₂ flight₃ through₄ Houston₅]
[0,1] [1,5]

[book₁ the₂] [flight₃ through₄ Houston₅]
[0,2] [2,5]

...

[book₁ the₂ flight₃ through₄] [Houston₅]
[0,4] [4,5]

[0,5] \rightarrow [0,k] [k,5] for $0 < k < 5$

0	Book	1	the	2	flight	3	through	4	Houston	5
S, VP, Verb Nominal, Noun [0,1]				S,VP,X2 [0,3]				S,VP,X2 [0,5]		
	Det [1,2]			NP [1,3]				NP [1,5]		
				Nominal, Noun [2,3]				Nominal [2,5]		
								Prep [3,4]	PP [3,5]	
									NP, Proper- Noun [4,5]	

Parse table: A fast method of filling in each cell

NOT assume an RHS has exactly two items

[book₁] [the₂] [flight₃] [through₄] [Houston₅]

[0,1] [1,2] [2,3] [3,4] [4,5]

[book₁ the₂] [flight₃] [through₄] [Houston₅]

[0,2] [2,3] [3,4] [4,5]

[book₁] [the₂ flight₃] [through₄] [Houston₅]

[0,1] [1,3] [3,4] [4,5]

...

[book₁ the₂ flight₃ through₄] [Houston₅]

[0,4] [4,5]

[0,5]
all possible
combinations
 $2^4 = 16$
cf. 4 binary
combinations

Parse table:

Assume an RHS
has exactly two items

$[\text{word}_{i+1}] [\text{word}_{i+2} \text{ word}_{i+3} \dots \text{word}_j]$

$[i, i+1] [i+1, j]$

$[\text{word}_{i+1} \text{ word}_{i+2}] [\text{word}_{i+3} \dots \text{word}_j]$

$[i, i+2] [i+2, j]$

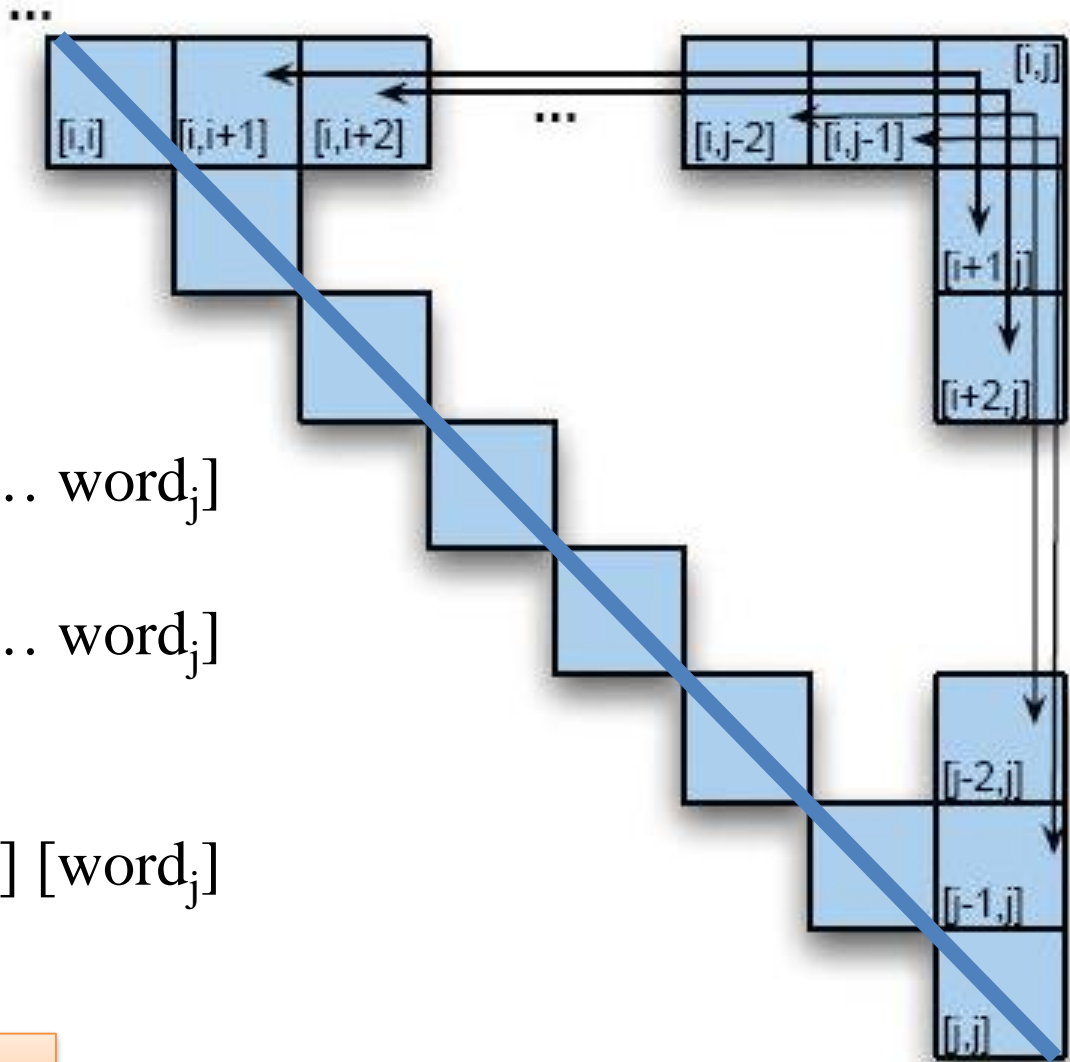
...

$[\text{word}_{i+1} \text{ word}_{i+2} \text{ word}_{i+3} \dots] [\text{word}_j]$

$[i, j-1] [j-1, j]$

$[i, j] \rightarrow [i, k] [k, j] \text{ for } i < k < j$

How can we create a CFG following the assumption?



CKY parsing

- Requirement
 - All rules should be in Chomsky normal form (CNF)
- CNF rules have the form of either
 - $A \rightarrow B C$ or $A \rightarrow w$ (w is a terminal)
 - RHS must have two non-terminals or one terminal
- Conversion to CNF
 - Read Section 13.4.1

POS Tagging



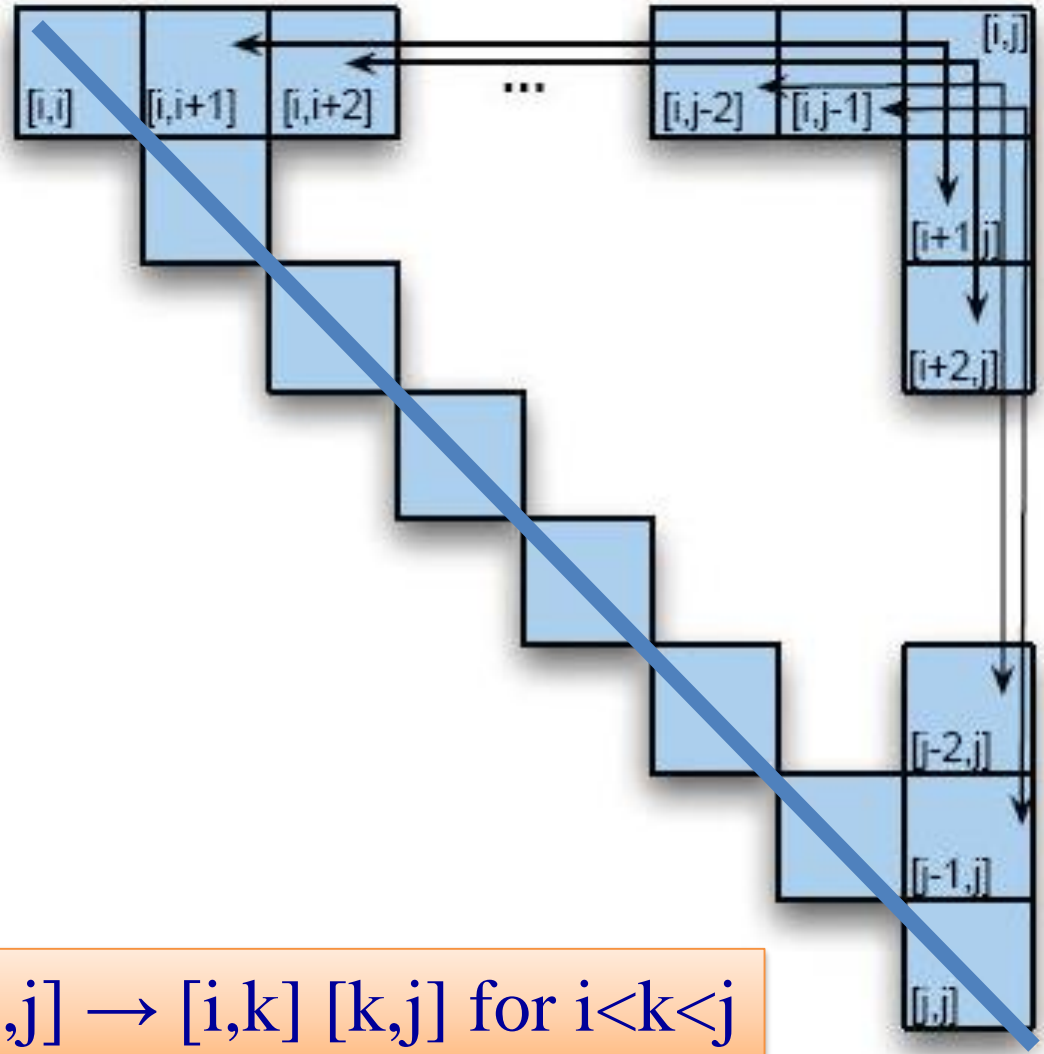
CNF grammar: example

\mathcal{L}_1 Grammar	\mathcal{L}_1 in CNF
$S \rightarrow NP VP$	$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$	$S \rightarrow X1 VP$
	$X1 \rightarrow Aux NP$
$S \rightarrow VP$	$S \rightarrow book \mid include \mid prefer$
	$S \rightarrow Verb NP$
	$S \rightarrow X2 PP$
	$S \rightarrow Verb PP$
	$S \rightarrow VP PP$
$NP \rightarrow Pronoun$	$NP \rightarrow I \mid she \mid me$
$NP \rightarrow Proper-Noun$	$NP \rightarrow TWA \mid Houston$
$NP \rightarrow Det Nominal$	$NP \rightarrow Det Nominal$
$Nominal \rightarrow Noun$	$Nominal \rightarrow book \mid flight \mid meal \mid money$
$Nominal \rightarrow Nominal Noun$	$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$	$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$	$VP \rightarrow book \mid include \mid prefer$
$VP \rightarrow Verb NP$	$VP \rightarrow Verb NP$
$VP \rightarrow Verb NP PP$	$VP \rightarrow X2 PP$
	$X2 \rightarrow Verb NP$
$VP \rightarrow Verb PP$	$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$	$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$	$PP \rightarrow Preposition NP$

CKY parsing for $[i,j]$ cell...

- CNF rule for non-terminal
 - $A \rightarrow B C$
- $W_{i+1}, W_{i+2}, \dots, W_j$
 - $[W_{i+1}], [W_{i+2}, \dots, W_j]$
 - $[i,j] \rightarrow [i,i+1] [i+1,j]$
 - $[W_{i+1}, W_{i+2}], [\dots, W_j]$
 - $[i,j] \rightarrow [i,i+2] [i+2,j]$
 - ...
 - $[W_{i+1}, W_{i+2}, \dots, W_{j-1}], [W_j]$
 - $[i,j] \rightarrow [i,j-1] [j-1,j]$

$[i,j] \rightarrow [i,k] [k,j]$ for $i < k < j$



Example : filling the 5th column

0	<i>Book</i>	1	<i>the</i>	2	<i>flight</i>	3	<i>through</i>	4	<i>Houston</i>	5
S, VP, Verb, Nominal, Noun [0,1]		[0,2]		S,VP,X2 [0,3]		[0,4]		[0,5]		
	Det [1,2]			NP [1,3]		[1,4]		[1,5]		
				Nominal, Noun [2,3]		[2,4]		[2,5]		
						Prep [3,4]		[3,5]		
								NP, Proper- Noun [4,5]		

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal \mid$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

Example : filling the 5th column

$PP \rightarrow \textit{Preposition NP}$

$$S \rightarrow NP VP$$
$$S \rightarrow X1 VP$$
$$X1 \rightarrow Aux NP$$
$$S \rightarrow book \mid include \mid prefer$$
$$S \rightarrow Verb NP$$
$$S \rightarrow X2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP PP$$
$$NP \rightarrow I \mid she \mid me$$
$$NP \rightarrow TWA \mid Houston$$
$$NP \rightarrow Det \textit{ Nominal}$$
$$Nominal \rightarrow book \mid flight \mid meal \mid$$

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$$VP \rightarrow book \mid include \mid prefer$$
$$VP \rightarrow Verb NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP PP$$
$$PP \rightarrow \textit{Preposition NP}$$

Example : filling the 5th column

0	Book	1	the	2	flight	3	through	4	Houston	5
S, VP, Verb, Nominal, Noun [0,1]			S,VP,X2 [0,3]							
	Det [1,2]		NP [1,3]						NP [1,5]	
			Nominal, Noun [2,3]						Nominal [2,5]	
							Prep [3,4]		PP [3,5]	
									NP, Proper- Noun [4,5]	

Nominal → *Nominal PP*

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

Example : filling the 5th column

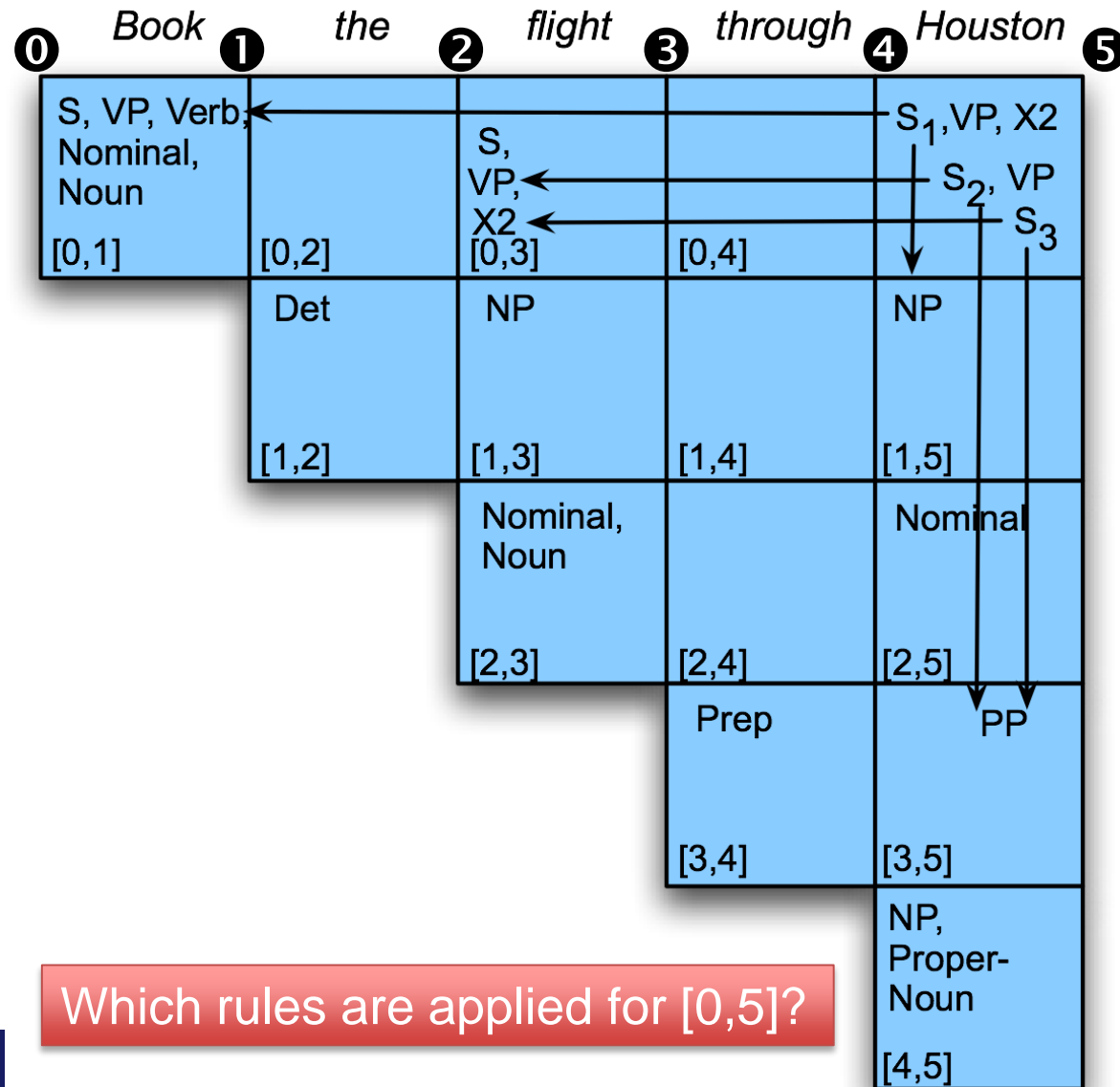
Book the flight through Houston

0	1	2	3	4	5
S, VP, Verb, Nominal, Noun [0,1]		S,VP,X2 [0,3]			
	Det ←	NP		NP	
	[1,2]	[1,3]	[1,4]	[1,5]	
		Nominal, Noun [2,3]		Nominal [2,5]	
			Prep [3,4]	PP [3,5]	
				NP, Proper- Noun [4,5]	

$NP \rightarrow Det\ Nominal$

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal \mid$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

Exercise: CKY parsing



Which rules are applied for [0,5]?

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$
 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$
 $Nominal \rightarrow book \mid flight \mid meal$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$
 $PP \rightarrow Preposition NP$

CKY algorithm

0	1	2	3	4	5
S, VP, Verb Nominal, Noun [0,1]		S,VP,X2 [0,3]		S,VP,X2 [0,5]	
	Det [1,2]	NP [1,3]		NP [1,5]	
		Nominal, Noun [2,3]		Nominal [2,5]	
			Prep [3,4]	PP [3,5]	
				NP, Proper- Noun [4,5]	

function CKY-PARSE(*words*, *grammar*) **returns** *table*

for $j \leftarrow$ **from** 1 **to** LENGTH(*words*) **do**

$table[j-1, j] \leftarrow \{A \mid A \rightarrow words[j] \in grammar\}$

for $i \leftarrow$ **from** $j-2$ **downto** 0 **do**

for $k \leftarrow i+1$ **to** $j-1$ **do**

$table[i, j] \leftarrow table[i, j] \cup$

$\{A \mid A \rightarrow BC \in grammar,$
 $B \in table[i, k],$
 $C \in table[k, j]\}$

CKY parsing: summary

- Requirement: CNF grammar
 - Binarization: $[i,j] \rightarrow [i,k] [k,j]$ for $i < k < j$
- Bottom-up approach
 - Process from $[j-1,j]$ to $[0,j]$
 - This assures us that whenever we're filling a cell, the parts needed to fill it are already in the table (to the left and below)
 - It's somewhat natural in that it processes the input, from left to right, a word at a time

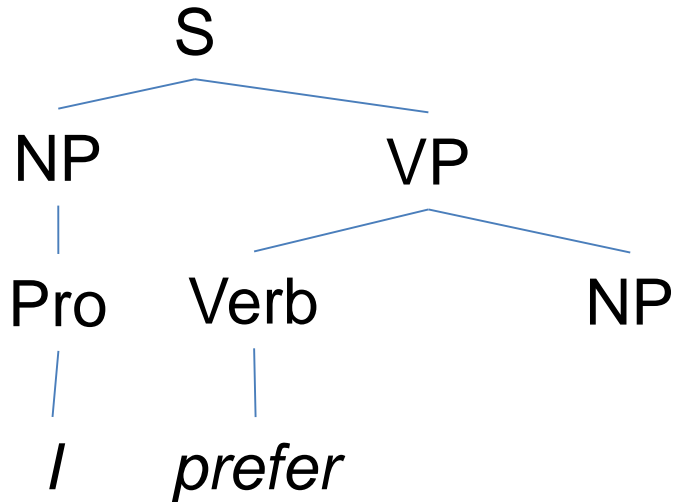


CKY parsing: Issue

- Trees that have no hope of leading to an S are generated
 - To avoid this we can switch to a top-down control strategy
 - Or we can add some kind of filtering that blocks constituents where they cannot happen in a final analysis.

<i>Book</i>	<i>the</i>	<i>flight</i>	<i>through</i>	<i>Houston</i>
S, VP, Verb Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	S,VP,X2 [0,5]
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]

Top-down parsing: intermediate state example



1. $S \rightarrow NP VP$

2. $NP \rightarrow Pro$
 $Pro \rightarrow I$

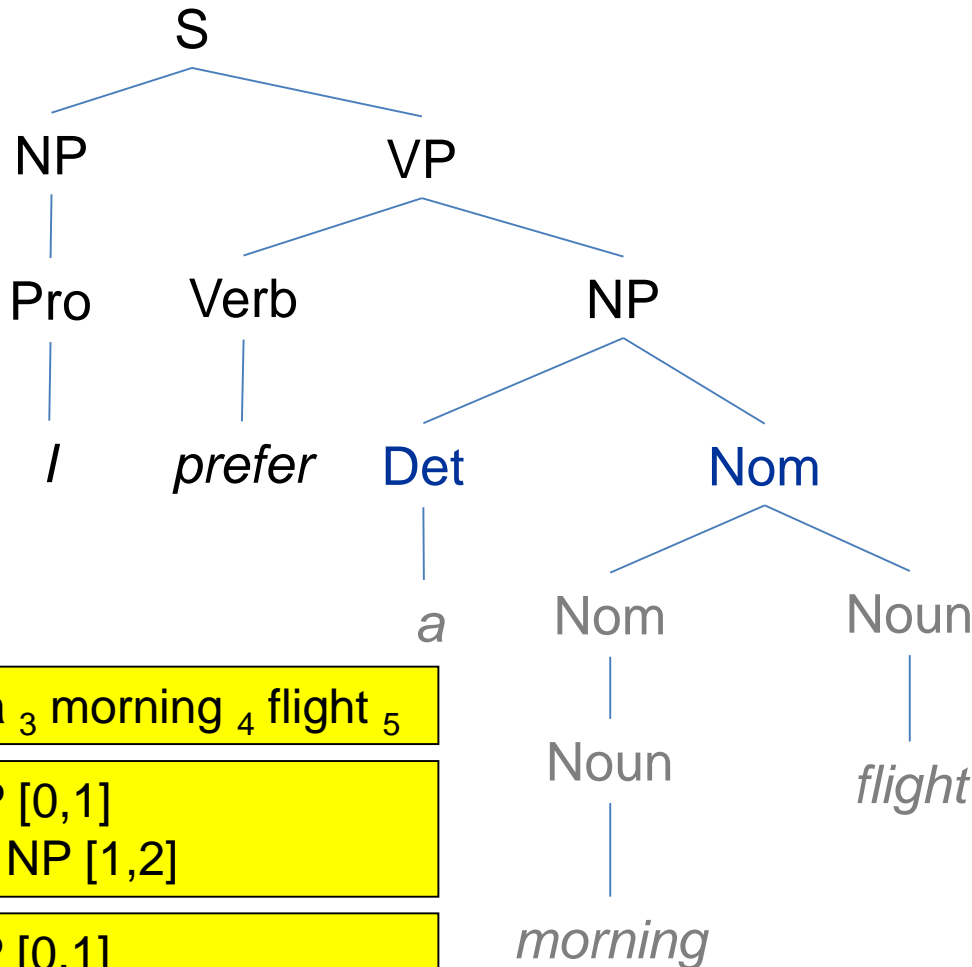
3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$

₀ I ₁ prefer ₂ a ₃ morning ₄ flight ₅

Dotted rules

$S \rightarrow NP \bullet VP [0,1]$
 $VP \rightarrow Verb \bullet NP [1,2]$

Top-down parsing: Next state



₀ I ₁ prefer ₂ a ₃ morning ₄ flight ₅

$S \rightarrow NP \bullet VP$ [0,1]
 $VP \rightarrow Verb \bullet NP$ [1,2]

$S \rightarrow NP \bullet VP$ [0,1]
 $VP \rightarrow Verb \bullet NP$ [1,2]
 $NP \rightarrow \bullet Det Nom$ [2,2]

1. $S \rightarrow NP VP$

2. $NP \rightarrow Pro$
 $Pro \rightarrow I$

3. $VP \rightarrow Verb NP$
 $Verb \rightarrow prefer$

4. $NP \rightarrow Det Nom$
 $Det \rightarrow a$

5. $Nom \rightarrow Nom Noun$
 $Noun \rightarrow flight$

6. $Nom \rightarrow Noun$
 $Noun \rightarrow morning$

Earley algorithm: States

0 I 1 prefer 2 a 3 morning 4 flight 5

- $NP \rightarrow \bullet \text{ Det Nom } [2,2]$
 - A Det is predicted at position 2
- $VP \rightarrow \text{ Verb } \bullet \text{ NP } [1,2]$
 - A VP is in progress; the Verb goes from 1 to 2
- $VP \rightarrow \text{ Verb NP } \bullet [1,4]$
 - A VP has been found, starting at 1 and ending at 4
- $S \rightarrow \alpha \bullet [0,N]$
 - Parsing is finished

Earley algorithm: How it works

1. Predict all the states you can upfront [**Predictor**]
2. Read a word [**Scanner**]
 - Extend states based on matches [**Completer**]
 - Generate new predictions
 - Repeat step 2
3. When you're out of words, look at the chart to see if you have a winner



Earley algorithm: Example (1) 0 **Book** 1 **that** 2 **flight** 3

S0	$\gamma \rightarrow \bullet S$	[0,0]	Dummy start state
S1	$S \rightarrow \bullet NP VP$	[0,0]	Predictor
S2	$S \rightarrow \bullet Aux NP VP$	[0,0]	Predictor
S3	$S \rightarrow \bullet VP$	[0,0]	Predictor
S4	$NP \rightarrow \bullet Pronoun$	[0,0]	Predictor
S5	$NP \rightarrow \bullet Proper-Noun$	[0,0]	Predictor
S6	$NP \rightarrow \bullet Det Nominal$	[0,0]	Predictor
S7	$VP \rightarrow \bullet Verb$	[0,0]	Predictor
S8	$VP \rightarrow \bullet Verb NP$	[0,0]	Predictor
S9	$VP \rightarrow \bullet Verb NP PP$	[0,0]	Predictor
S10	$VP \rightarrow \bullet Verb PP$	[0,0]	Predictor
S11	$VP \rightarrow \bullet VP PP$	[0,0]	Predictor

\mathcal{L}_1 Grammar
$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$
$S \rightarrow VP$
$NP \rightarrow Pronoun$
$NP \rightarrow Proper-Noun$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow Noun$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$
$VP \rightarrow Verb NP$
$VP \rightarrow Verb NP PP$
$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$

Note that given a grammar, these entries are the same for all inputs; they can be pre-loaded.

Earley algorithm: Example (2) 0 **Book** 1 **that** 2 **flight** 3

S12	<i>Verb</i> → <i>book</i> •	[0,1]	Scanner
S13	<i>VP</i> → <i>Verb</i> •	[0,1]	Completer
S14	<i>VP</i> → <i>Verb</i> • <i>NP</i>	[0,1]	Completer
S15	<i>VP</i> → <i>Verb</i> • <i>NP PP</i>	[0,1]	Completer
S16	<i>VP</i> → <i>Verb</i> • <i>PP</i>	[0,1]	Completer
S17	<i>S</i> → <i>VP</i> •	[0,1]	Completer
S18	<i>VP</i> → <i>VP</i> • <i>PP</i>	[0,1]	Completer
S19	<i>NP</i> → • <i>Pronoun</i>	[1,1]	Predictor
S20	<i>NP</i> → • <i>Proper-Noun</i>	[1,1]	Predictor
S21	<i>NP</i> → • <i>Det Nominal</i>	[1,1]	Predictor
S22	<i>PP</i> → • <i>Prep NP</i>	[1,1]	Predictor

\mathcal{L}_1 Grammar
<i>S</i> → <i>NP VP</i>
<i>S</i> → <i>Aux NP VP</i>
<i>S</i> → <i>VP</i>
<i>NP</i> → <i>Pronoun</i>
<i>NP</i> → <i>Proper-Noun</i>
<i>NP</i> → <i>Det Nominal</i>
<i>Nominal</i> → <i>Noun</i>
<i>Nominal</i> → <i>Nominal Noun</i>
<i>Nominal</i> → <i>Nominal PP</i>
<i>VP</i> → <i>Verb</i>
<i>VP</i> → <i>Verb NP</i>
<i>VP</i> → <i>Verb NP PP</i>
<i>VP</i> → <i>Verb PP</i>
<i>VP</i> → <i>VP PP</i>
<i>PP</i> → <i>Preposition NP</i>

Note that “Noun → book• [,] can be also scanned

Earley algorithm: Example (3) 0 **Book** 1 **that** 2 **flight** 3

S23	<i>Det</i> → <i>that</i> •	[1,2]	Scanner
S24	<i>NP</i> → <i>Det</i> • <i>Nominal</i>	[1,2]	Completer
S25	<i>Nominal</i> → • <i>Noun</i>	[2,2]	Predictor
S26	<i>Nominal</i> → • <i>Nominal Noun</i>	[2,2]	Predictor
S27	<i>Nominal</i> → • <i>Nominal PP</i>	[2,2]	Predictor

S28	<i>Noun</i> → <i>flight</i> •	[2,3]	Scanner
S29	<i>Nominal</i> → <i>Noun</i> •	[2,3]	Completer
S30	<i>NP</i> → <i>Det Nominal</i> •	[1,3]	Completer
S31	<i>Nominal</i> → <i>Nominal</i> • <i>Noun</i>	[2,3]	Completer
S32	<i>Nominal</i> → <i>Nominal</i> • <i>PP</i>	[2,3]	Completer
S33	<i>VP</i> → <i>Verb NP</i> •	[0,3]	Completer
S34	<i>VP</i> → <i>Verb NP</i> • <i>PP</i>	[0,3]	Completer
S35	<i>PP</i> → • <i>Prep NP</i>	[3,3]	Predictor
S36	<i>S</i> → <i>VP</i> •	[0,3]	Completer
S37	<i>VP</i> → <i>VP</i> • <i>PP</i>	[0,3]	Completer

\mathcal{L}_1 Grammar
<i>S</i> → <i>NP VP</i>
<i>S</i> → <i>Aux NP VP</i>
<i>S</i> → <i>VP</i>
<i>NP</i> → <i>Pronoun</i>
<i>NP</i> → <i>Proper-Noun</i>
<i>NP</i> → <i>Det Nominal</i>
<i>Nominal</i> → <i>Noun</i>
<i>Nominal</i> → <i>Nominal Noun</i>
<i>Nominal</i> → <i>Nominal PP</i>
<i>VP</i> → <i>Verb</i>
<i>VP</i> → <i>Verb NP</i>
<i>VP</i> → <i>Verb NP PP</i>
<i>VP</i> → <i>Verb PP</i>
<i>VP</i> → <i>VP PP</i>
<i>PP</i> → <i>Preposition NP</i>

Earley algorithm: Summary (Pseudo codes: Section 13.4.2)

- Top-down approach
 - Breadth-first search
 - State representation
 - (compare with the cells of parse tree in CKY algorithm: subtrees)
- Waste lots of time in trying inconsistent rule applications

S31	$Nominal \rightarrow Nominal \bullet Noun$	[2,3]	Completer
S32	$Nominal \rightarrow Nominal \bullet PP$	[2,3]	Completer
S33	$VP \rightarrow Verb NP \bullet$	[0,3]	Completer
S34	$VP \rightarrow Verb NP \bullet PP$	[0,3]	Completer
S35	$PP \rightarrow \bullet Prep NP$	[3,3]	Predictor
S36	$S \rightarrow VP \bullet$	[0,3]	Completer
S37	$VP \rightarrow VP \bullet PP$	[0,3]	Completer

Top-down vs. Bottom-up parsing

- Top-down
 - Waste lots of time in trying inconsistent rule applications
 - The application of the rules does not lead the generation of the given string
 - Never explore subtrees that cannot find a place in some S-rooted tree
 - All trees are generated starting with S.
- Bottom-up
 - Never suggest trees that are not grounded in the input string
 - All trees are generated based on input string
 - Trees that have no hope of leading to an S are generated
 - Some trees cannot proceed further to reach S

Soundness and completeness

- A parser is *sound* if every parse result it returns is valid/correct
- A parser *terminates* if it is guaranteed to not go off into an infinite loop
- A parser is *complete* if for any given grammar and string,
 - It is sound
 - It produces all valid parse results for the string, and
 - It terminates
- For practical purposes, we settle for sound and terminating, but incomplete parsers
 - E.g. *k*-best parse results

Full parsing vs. Partial parsing

- Full parsing
 - Identify the complete syntactic structure of a sentence
 - Oftentimes, parsing is the most time-consuming part
- Partial parsing
 - Identify parts of the syntactic structure of a sentence
 - Not all applications require full syntactic structures. Example: only Noun phrases need to be extracted in some applications but not the full syntactic structure of the sentence.
- Read Section 13.5



Summary

