

# SCAN: Multi-Hop Calibration for Mobile Sensor Arrays

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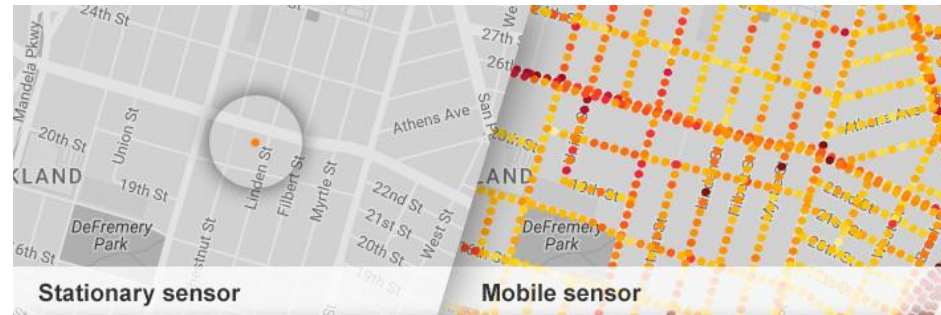


Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich



# Mobile Air Pollution Monitoring

- Mobile air quality sensors collect vast amounts of measurements with high resolution

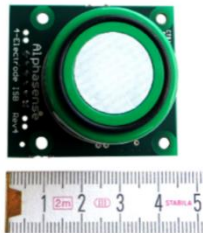


Air pollution measurements collected by Google Streetview cars in Oakland, CA

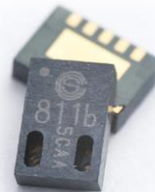
- Low cost air pollution sensors



SGX Sensortech  
MiCS-OZ-47 O<sub>3</sub>



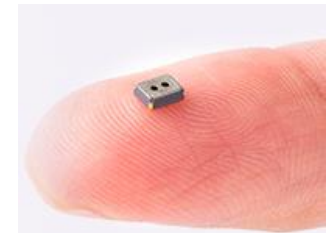
AlphaSense CO-B4



ams CCS811



Honeywell Particle Sensor

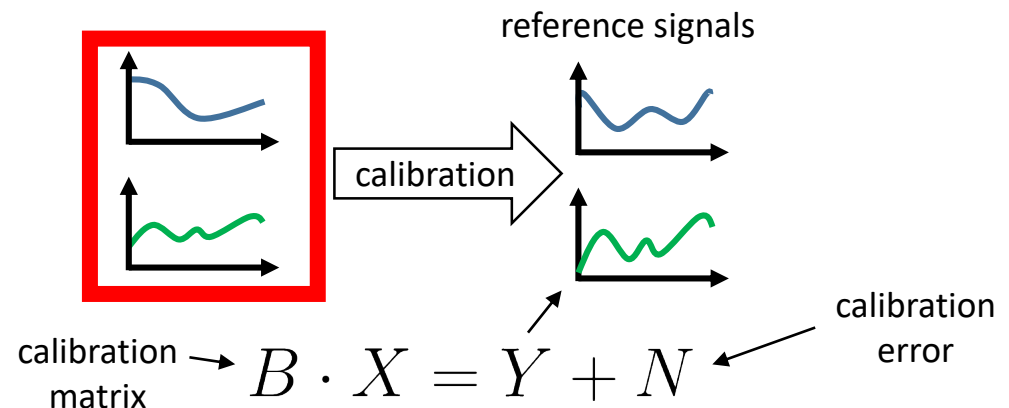
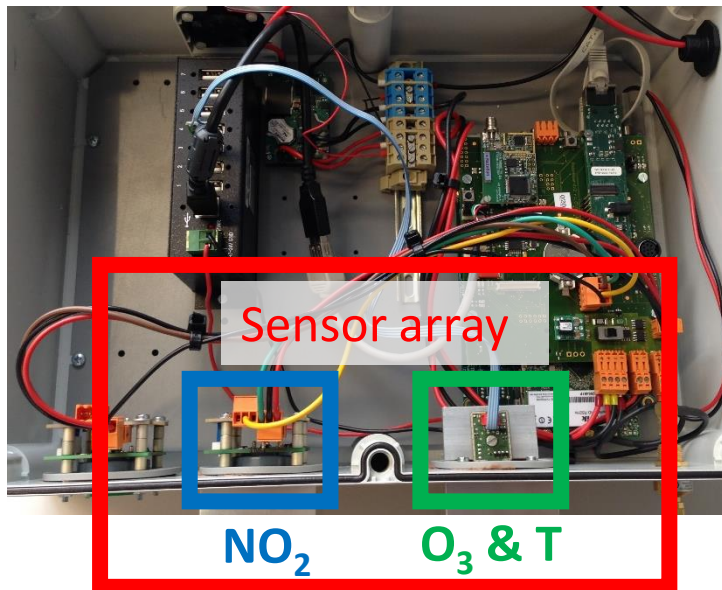


Figaro TGS8100

Reliable long-term monitoring with mobile low-cost sensors  
is challenging!

# Sensor Array Calibration

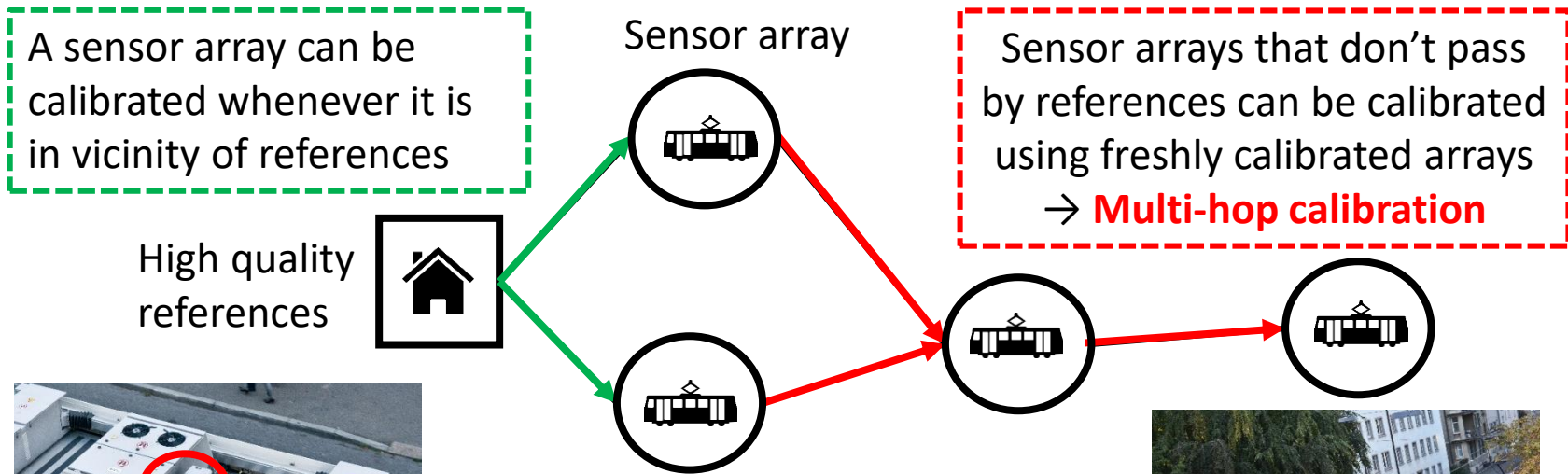
- **Problem 1:** Low-cost sensors suffer from **low selectivity** and dependencies on meteorological conditions
- **Solution:** Sensor array calibration
  - Compensate for cross-sensitivities by augmenting multiple low-cost sensor and collectively calibrate the signals to references
- State-of-the-art: Multiple Least Squares (MLS) based regression



Real-world example: A sensor array reduces the  $\text{NO}_2$  measurement error by a factor of 2 compared to a single  $\text{NO}_2$  sensor

# Multi-Hop Calibration

- **Problem 2:** Due to ageing effects and changing environmental conditions sensor arrays need **frequent recalibration**
- **Solution:** Opportunistic calibration during sensor rendez-vous



Sensor array on top of streetcar

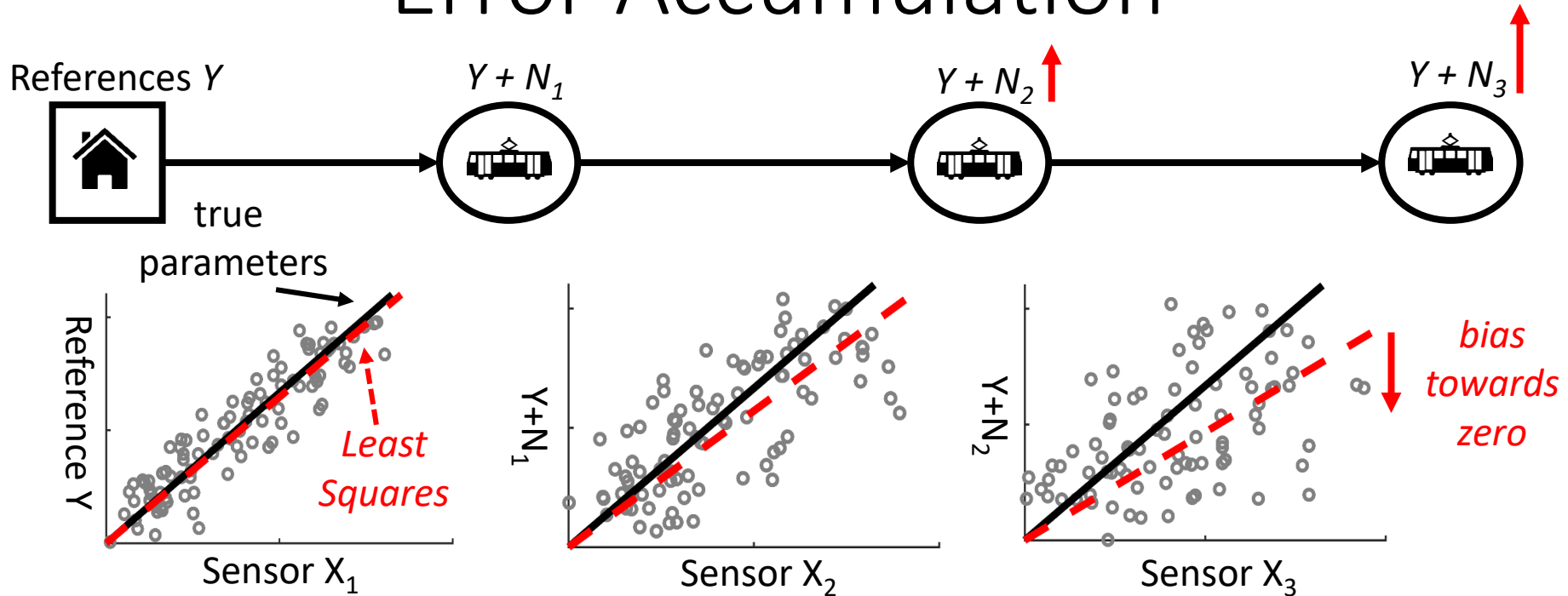


Rendez-vous between array and references



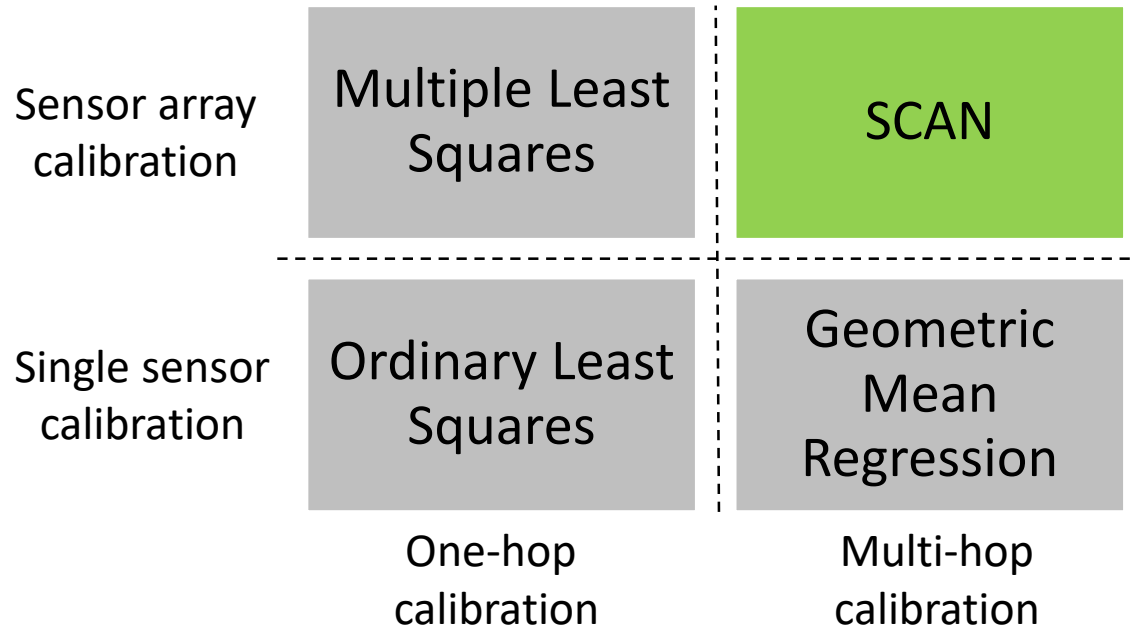
Rendez-vous between two arrays

# Error Accumulation



- Least Squares based regression suffers from error accumulation over multiple hops
  - Due to *regression dilution*, also known as *bias towards zero*
- Saukh et al. [IPSN15]: Geometric Mean Regression (GMR) minimizes error accumulation
- **Problem:** GMR is a single-variable model
  - Not applicable for sensor arrays
  - Poor performance when used to calibrate a cross-sensitive sensor

# Our Solution



- SCAN: Sensor Array Network Calibration
  - Multi-variable regression model applicable to typical **sensor arrays**
  - Minimizes error accumulation when applied to **multi-hop calibration**

# SCAN: Sensor Array Network Calibration

$$\min_B \text{tr} \left( (Y - B \cdot X)(Y - B \cdot X)^T \right)$$

subject to  $BXX^TB^T = YY^T$

- SCAN minimizes the **least squares error** with a novel **constraint** on the parameters B
- A **unique and closed-form** expression of the calibration matrix B always exists
- For single sensor calibration, i.e. a single variable regression problem, SCAN and GMR yield the same solution

# Calibration Matrix B

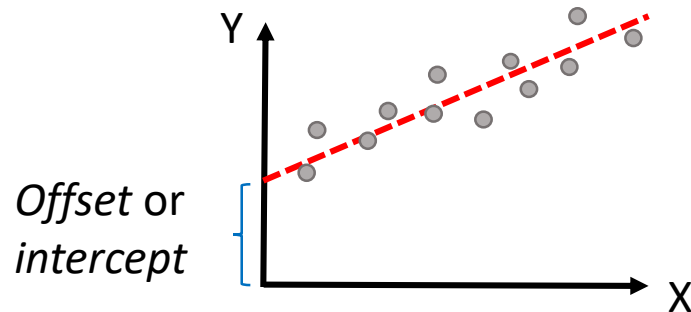
- Applicable to calibration matrices  $B$  with **general form**
  - For instance, there are not always the same set of reference signals available as low-cost sensor signals:

$$\begin{array}{c} \in \mathbb{R}^{2 \times 3} \end{array} \rightarrow B \cdot \begin{array}{c} \text{NO}_2, \text{O}_3 \text{ and } T \end{array} = \begin{array}{c} Y \end{array} + \begin{array}{c} N \end{array}$$

$\swarrow$   $\nwarrow$

NO<sub>2</sub> and O<sub>3</sub>

- SCAN can calculate an offset regression term similar to MLS





# No Bias Towards Zero

- Constraint is able to completely remove error accumulation if the error components  $N$  of both arrays exhibit the same covariance matrix

$$\begin{array}{ccc} \text{Uncalibrated array} & & \text{Calibrated array} \\ \overbrace{B(X X^T + N N^T)} & = & \overbrace{Y Y^T + N N^T} \\ \underbrace{N N^T} & \text{compensated} & \underbrace{N N^T} \end{array}$$

Although in reality the two covariance matrices are usually similar but not perfectly identical, SCAN is still minimizing error accumulation

- More details and proofs are in the paper

# Evaluation: Simulation

- We artificially generate sensor arrays  $X_i$  with

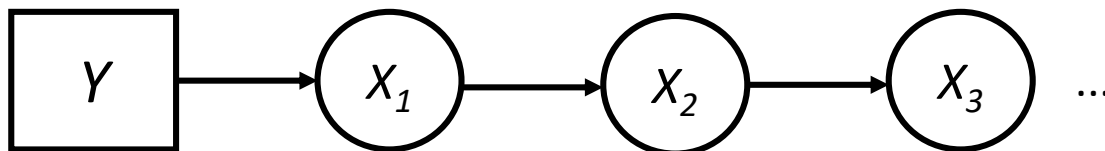
$$X_i = B^{-1}(Y_i + N_i)$$

*typical calibration matrices*

*4 reference signals*

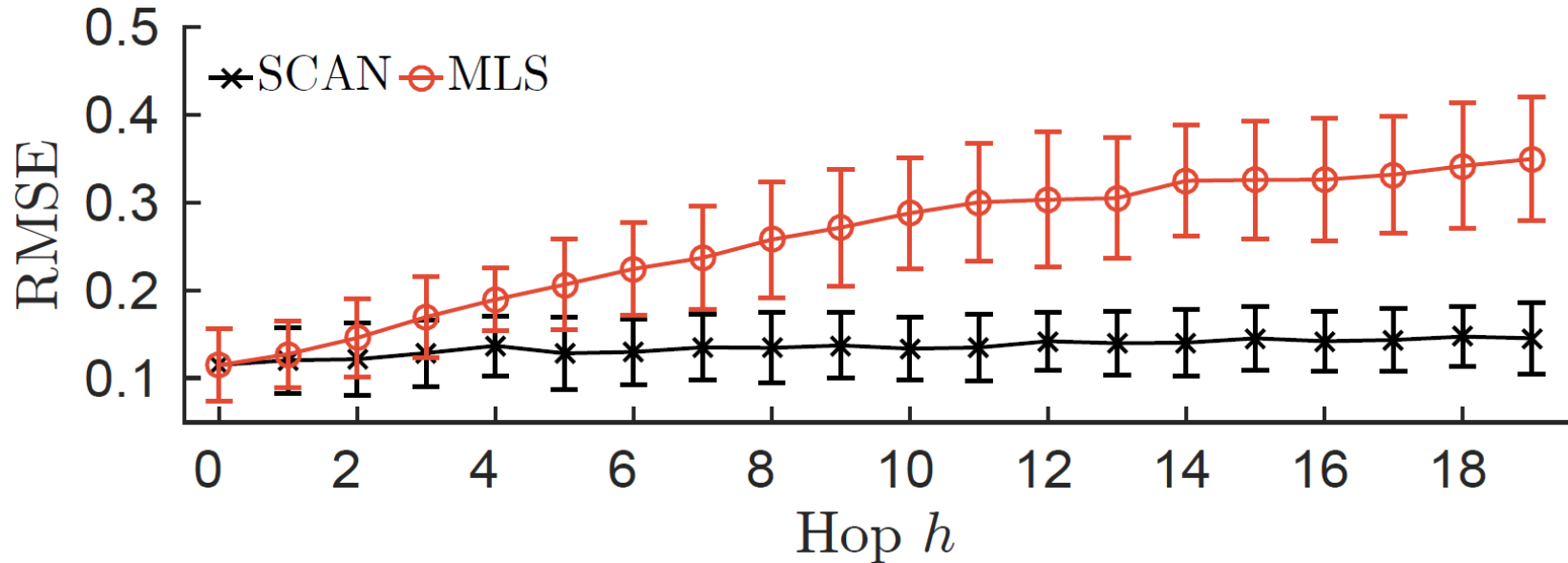
*typical error components*

- Sensor arrays  $X_i$  form a calibration path



- $X_1$  is calibrated to reference  $Y$
- $X_2$  to virtual reference provided by calibrated array  $X_1$
- 500 samples for training, 500 samples for testing

# Results: Simulation



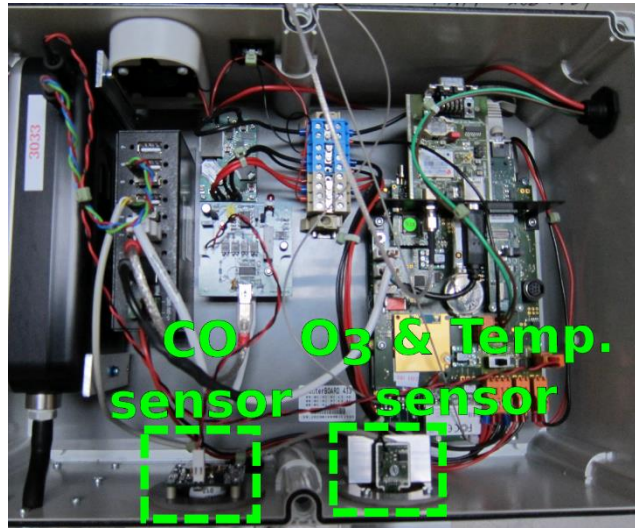
- Over a 20 hop calibration path SCAN clearly outperforms multiple least-squares
- MLS only performs better in the first hop

# Comparison with Other Methods

Method	Hop = 0	Hop = 5	Hop = 19
SCAN	0.12	0.12	0.14
Multiple least squares (MLS)	0.11	0.21	0.34
Geometric mean regression (GMR)	0.4	0.54	0.54
Total least squares (TLS)	0.14	0.62	4.2
Neural Networks	0.19	>100	>100
GMR Generalization by Draper	0.13	0.24	0.34
GMR Generalization by Tofallis	0.14	0.25	0.35

- As expected GMR performs poorly when applied to cross-sensitive sensors
- Over multiple hops SCAN outperforms all other methods

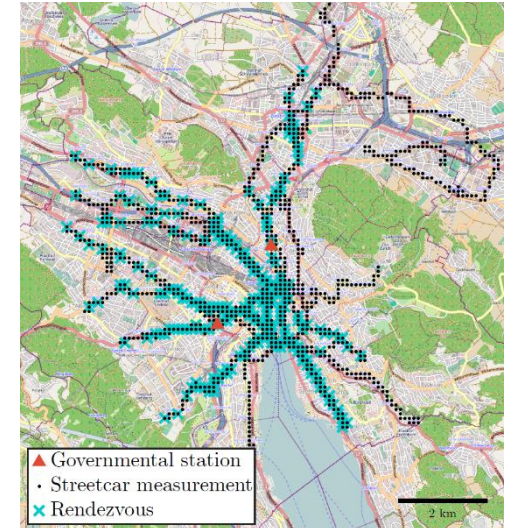
# Evaluation: Streetcar Deployment



Sensors



Box on streetcar

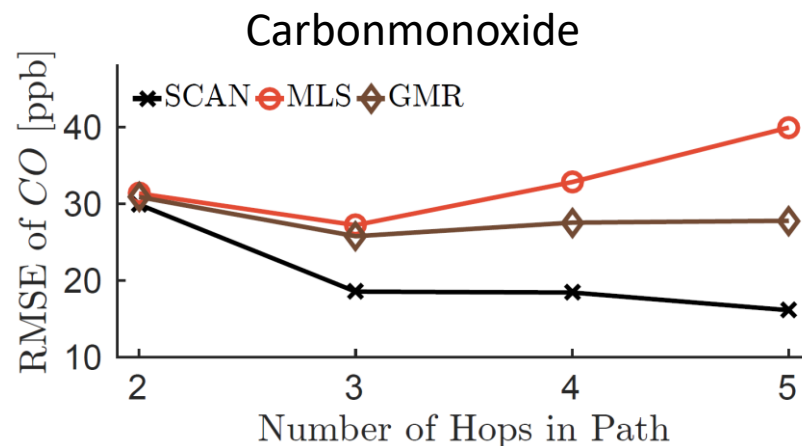
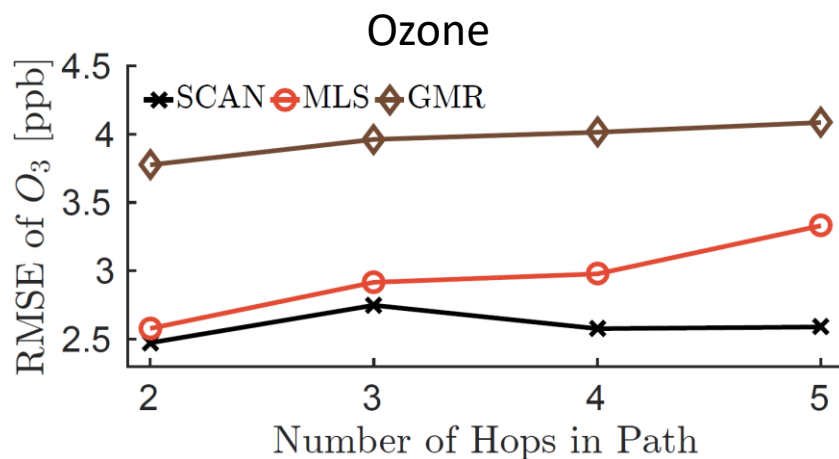


Measurement coverage

- 7 sensor arrays deployed on streetcars in the city of Zürich, Switzerland
  - Ozone (O<sub>3</sub>), carbon monoxide (CO) and temperature sensor
  - Gas sensors suffer from substantial meteorological dependencies
- Reference measurements provided by two governmental stations
- 56 Mio. measurements recorded between 03/2014 and 03/2016
  - Trained on at least 200 within 4 weeks
  - Tested on data from consecutive 4 weeks

# Results: Streetcar Deployment

- Network-wide calibration
  - At most three streetcars pass by reference stations
  - Multi-hop calibration allows to calibrate all seven streetcars in 94% of all months
- SCAN outperforms GMR by up to 42% and MLS by up to 60% over 5 hops



# Conclusion

- Multi-hop sensor array calibration is a powerful tool to provide reliable data over long time periods in mobile low-cost sensor deployments
- We propose SCAN, novel constrained multi-variable linear regression technique that
  - calibrates sensor arrays and
  - reduces error accumulation over multiple hops
- Evaluation based on two different datasets show that SCAN is able to outperform different calibration techniques

# Thank you!

## Questions?

Streetcar data is publicly available:

[www.opensense.ethz.ch](http://www.opensense.ethz.ch)



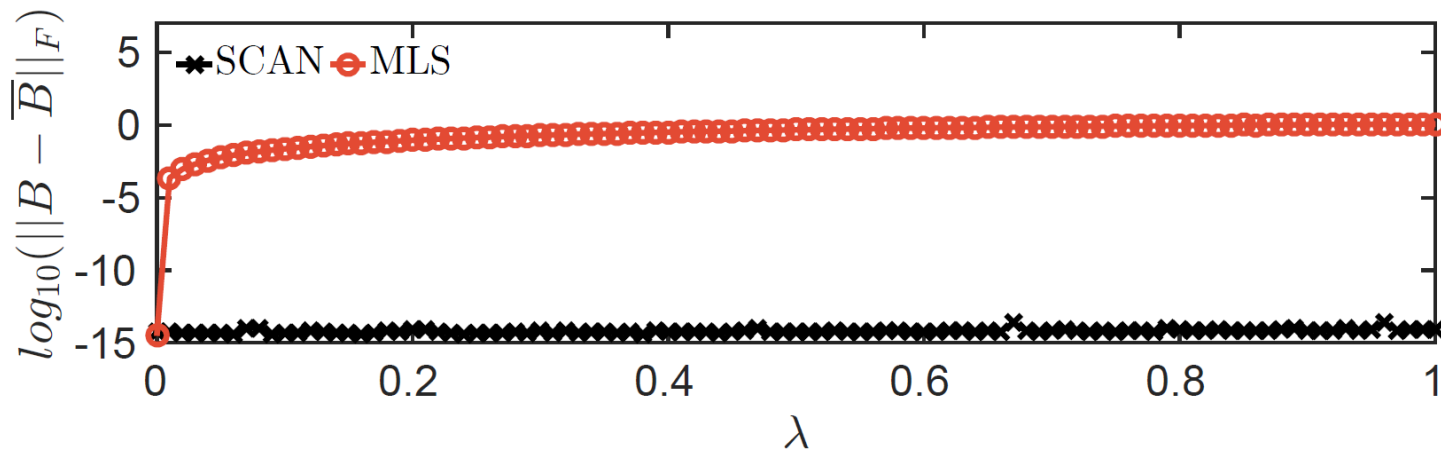
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Swiss Federal Institute of Technology Zurich



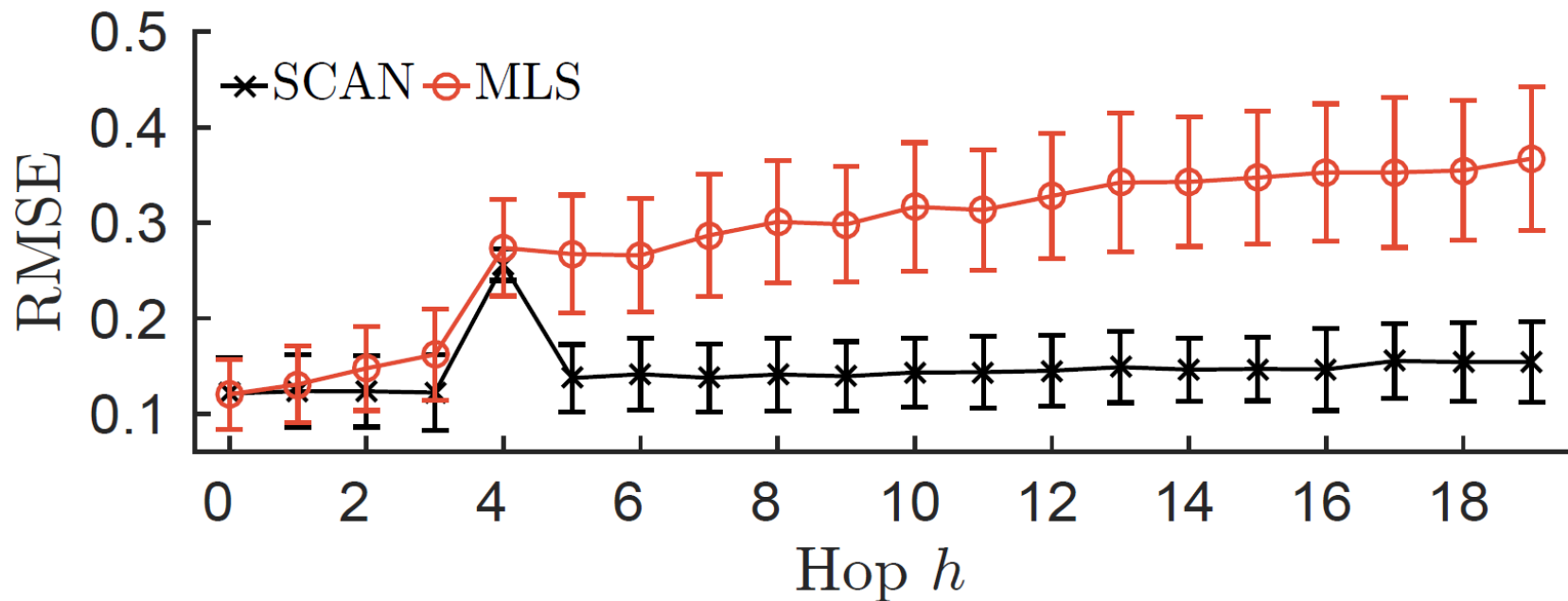


# Backup: No Bias Towards Zero

- If calibration error is uncorrelated, i.e.  $NN^T = \sigma I$  SCAN is able to recover the true underlying calibration matrix  $B$
- Simulation:

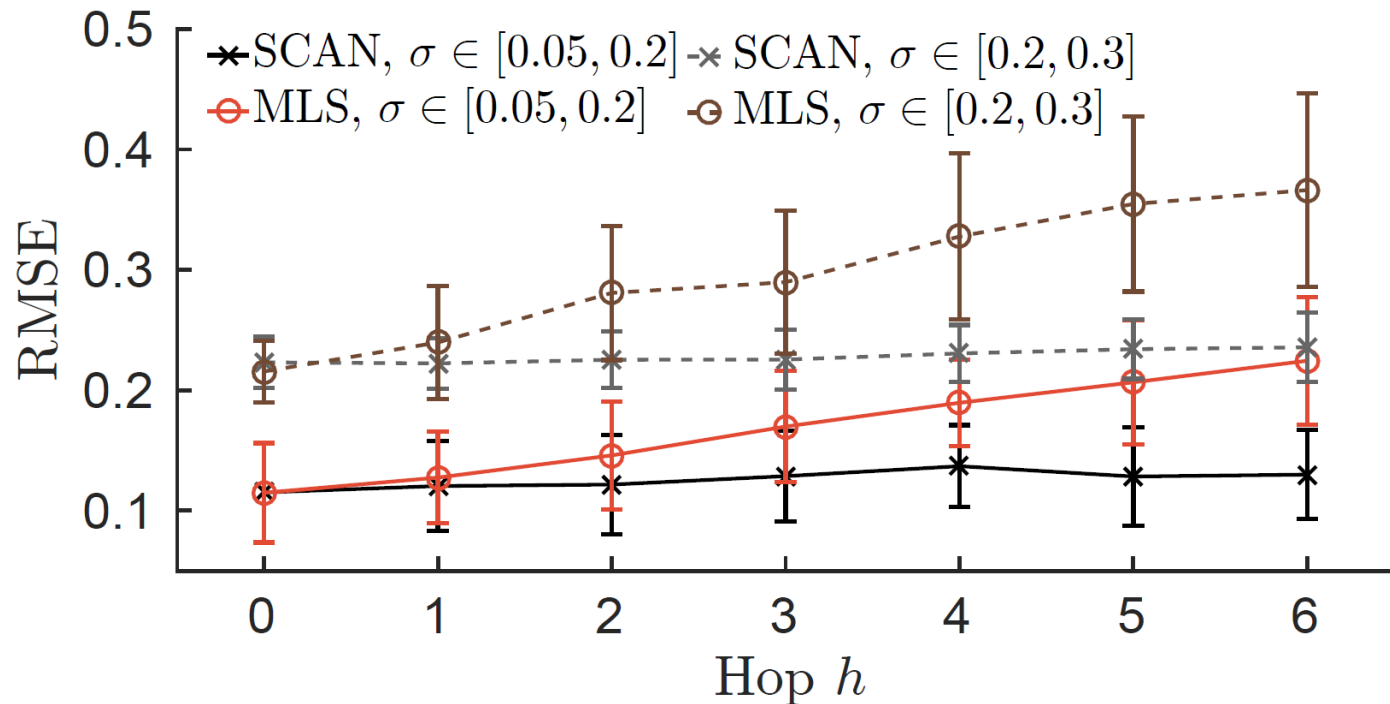


# Backup: Increased noise variance



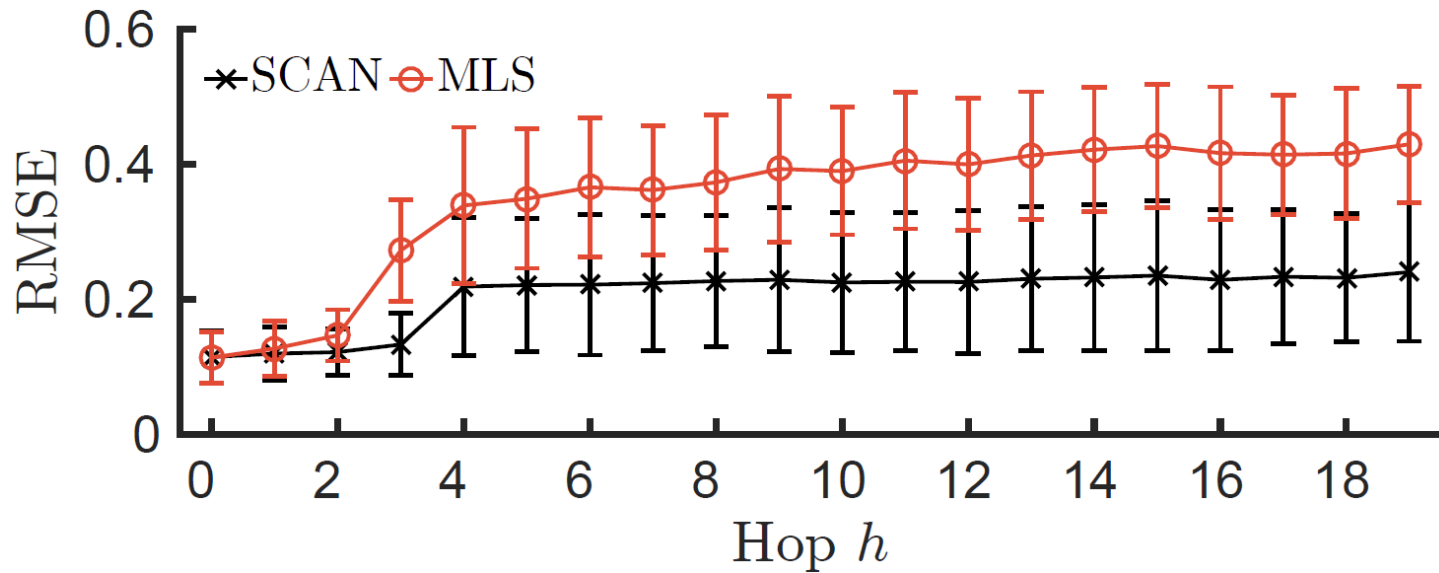
Increased noise in measurements (2x standard deviation) of node 4 has no effect on nodes after hop 5

# Backup: Noise Independence



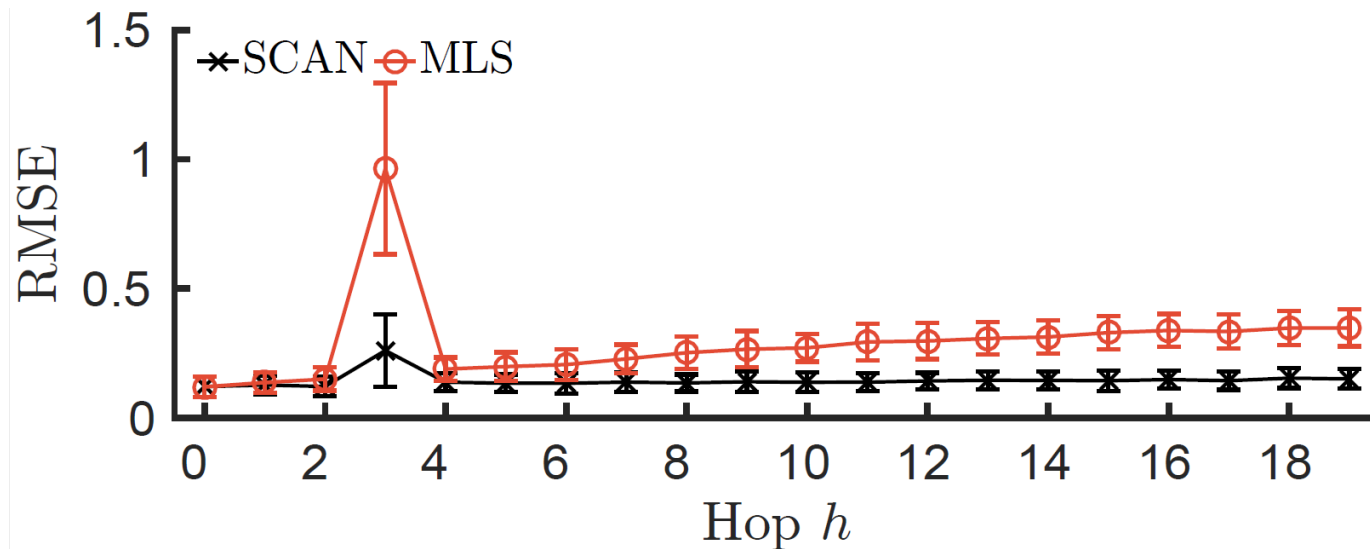
Increased noise in measurements has only an effect on the average calibration error but not on the error accumulation

# Backup: Measurement range 1/2



- 3x smaller measurement range of rendezvous between array 3 and 4
- Measurement range = interval defined by the smallest and highest absolute value of the phenomena measurements
- General problem for any method due to missing training data

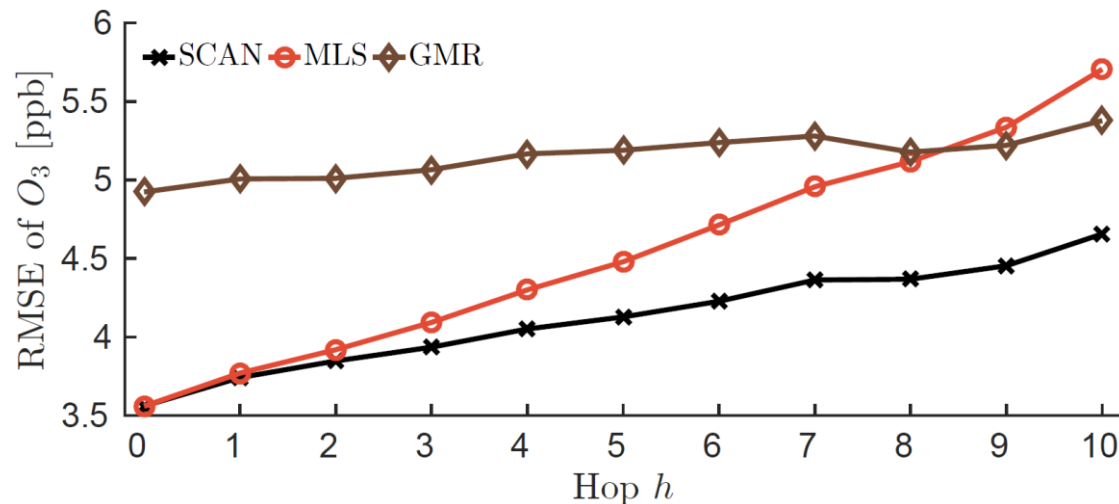
# Backup: Measurement Range 2/2



- 3x higher measurement range of rendezvous between array 3 and 4
- Only affects array 4, because calibration parameters are only valid for the measurement range of all other arrays

# Backup: Metaloxide Sensors

- Calibration path with 11 sensor arrays consisting of
  - 2 different metaloxide low-cost gas sensors
  - 1 temperature sensor
- Deployed next to high quality reference station in Switzerland
- Calibrated to ozone ( $O_3$ ) provided by reference station
- 10 Mio. samples recorded between 07/2015 and 07/2016
  - 200 samples for training within two weeks
  - 200 samples for testing within consecutive two weeks



Over all hops SCAN achieves a 16% to 38% smaller error than GMR and an up to 23% smaller error than MLS

# Backup: Typical Calibration Error

- Based on metal-oxide sensors
- Variance of calibration error shows strong similarity to diagonal matrix

$O_3$	0.24	0.03
T	0.03	0.24
	$O_3$	T