

Outline: Bayesian sampling driven classical mechanics force field parameterization

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I. Objective: Test and validate use of Bayesian sampling driven parameterization procedure using inexpensively generated single molecule simulation data as experimental evidence

II. Intro:

A. Classical mechanics simulations have been useful in the study of chemistry, biology and materials ranging from the simple to very complex. However the force fields that scientists use in their studies aren't always consistent and an element of uncertainty to any study done.

1. Produce quantitatively different results depending on the force field [1, 2, 3, 4, 5]
2. Can make choice of force field more important than it should be

B. Current force field parameterization efforts are heuristic and often guided by the physical intuition of scientists rather than systematically. [6, 7, 8, 9, 10, 11, 12, 13]

1. Go through cited examples explicitly
2. ForceBalance: tries to be somewhat more quantitative by minimizing an objective function. However, weights are still chosen by hand. [more discussion][14, 15, 16]
3. Find more examples

C. Big reason behind this being how force fields are optimized to reproduce very specific types of "target data"[17, 18]

1. There is no single right way to optimize a force field to reproduce all kinds of observables

- a. Usually, when you optimize for certain observables, estimates of other observables can become less accurate
- 2. Additionally, it is difficult to update existing force fields with new kinds of data (either more molecular diversity or new properties) without changing the entire force field
 - a. Forcefield parameters are inherently coupled by nature of how they are designed (sometimes weakly, sometimes strongly)
 - b. Chemically/physically interactions and geometries at an atomic scale are coupled
 - c. You often need to adjust all (or many) parameters if you adjust one
 - d. Could be a lot, could be a little. Situations vary depending on how the changing interactions affect the overall system
- 3. **We would like to probabilistically determine all FAMILIES of force fields consistent with given data in a systematic manner. Also, given more data (new data), we would like a method to update extant force fields, so that new force fields could be determined to given this new data.**
- D. Bayesian statistics has been applied to a large number of big data and optimization problems [19, 20, 21, 22, 23, 24, 25, 26]
 - 1. add citations from the recent lit stuff on OpenFF Slack
- E. With this in mind the authors of this paper have developed a novel process for parameterizing classical mechanics force fields using experimental data as evidence for Bayesian inference driven parameterization. For this particular paper we have set up a toy case in order to test and validate the Bayesian inference parameterization.
 - 1. The experimental data used as evidence will be trajectory data produced from a force field developed by members of our force field parameterization team.[27]
 - 2. For simplicity and time considerations the simulated data is only of single molecules and hence the parameters being changed will be limited to those involved in bonded interactions. Specifically:
 - a. bonded force constants
 - b. equilibrium bond lengths
 - c. angular force constants
 - d. equilibrium bond angles
 - e. torsional force constants
 - 3. We will investigate if the Bayesian inference approach will recover the original force field parameters using the simulated data under the original force field as evidence if the force field is perturbed.

III. Methods

A. Molecules?

1. ≤ 3 carbons
2. ≤ 2 oxygens

Index	SMILES	C_count	O_count	AlkEthOH_id	IUPAC_names
0	C	1	1	AlkEthOH_c0	methane
15	CC	2	1	AlkEthOH_c38	ETHANE
339	CC(C)O	3	2	AlkEthOH_c488	Propan-2-ol
603	CCC	3	1	AlkEthOH_c901	PROPANE
789	CCCO	3	2	AlkEthOH_c11...	Propan-1-ol
804	CCO	2	2	AlkEthOH_c11...	ethanol
805	CCOC	3	2	AlkEthOH_c11...	Methoxyethane
896	CO	1	2	AlkEthOH_c12...	methanol
897	COC	2	2	AlkEthOH_c12...	Methoxymetha...
912	O	0	2	AlkEthOH_c13...	oxidane
105	C1COC1	3	2	AlkEthOH_r131	Oxetane

Figure 1: The molecules being used as the test set for this initial parameterization. Each row entry includes the SMILES string, C and O composition, ID from the AlkEthOH set and the IUPAC name for a given molecule.

B. Simulations

1. Generate simulation data by simulating a set of AlkEthOH molecules using the 'smirff99Frosst' forcefield
2. Simulation parameters:
 - a. Thermostated to 300 K
 - b. 0.5 ns time steps
 - c. Friction coefficient of 1 ps^{-1}
 - d. 4 ns simulations
 - e. Frame recored every 1000 steps
3. Currently making O-H LJ parameters small and finite in order to keep hydrogens from floating into other atoms

C. Sampling the Bayesian Posterior

1. Observables:
 - a. Bonds and Angles:
 - (1) Mean bond lengths and angles
 - (2) Variance of bond lengths and angles
 - b. Torsions:
 - (1) Fourier series coefficients and/or some measure of fitness to a fourier series model

2. Bayes' Theorem

- a. Simple version: $Pr(\theta|O) = \frac{Pr(O|\theta)Pr(\theta)}{Pr(O)}$
- b. Where $Pr()$ is a probability function and θ are parameters for a model estimating our observed data O

3. Prior probability models

- a. Simple uniform priors for all parameters
- b. Limits on uniforms dependent on parameter
 - (1) Equilibrium bond lengths and angles: $\pm 20\%$ of the true parameter value
 - (2) Force constants: 0 as the floor and twice the highest value in the force field as a ceiling
 - (a) Bonded force constant: 0 to 4000 $\left(\frac{\text{kcal}}{\text{mol} \cdot \text{\AA}^2}\right)$
 - (b) Angular force constant: 0 to 1400 $\left(\frac{\text{kcal}}{\text{mol} \cdot \text{rad}^2}\right)$
 - (c) Torsional force constant: 0 to 21 $\left(\frac{\text{kcal}}{\text{mol}}\right)$

4. Likelihood function

- a. Forward models have already been determined and are simple (how do we calculate bond lengths and angles from a time series of coordinates?)
 - (1) Still need to write these out explicitly
- b. There are a few possible options for choices of likelihood functions

$$(1) L(O|\theta) = \frac{1}{\sqrt{2\pi\sigma_O^2}} \cdot \exp\left(-\frac{(\bar{O}-O_{mod}(\theta))^2}{2\sigma_O^2}\right)$$

$$(2) L(O|\theta) = \prod_{j=1}^M \frac{1}{\sqrt{2\pi\sigma_O^2}} \cdot \exp\left(-\frac{(O_j-O_{mod}(\theta))^2}{2\sigma_O^2}\right)$$

$$(3) L(O|\theta) = \exp\left(-\frac{\frac{1}{M} \sum_{j=1}^M (O_{mod}(\theta)-O_j)^2}{2\sigma_O^2}\right)$$

5. Sampling and choice of surrogate model

- a. What is a surrogate model?
 - (1) Surrogate models allow us to inexpensively determine outcomes that cannot be easily measured directly
 - (2) In the context of our force field parameterization, we use surrogate models to estimate simulated observables cheaply in order to inexpensively sample our posterior
 - (3) Surrogate models can allow us to accelerate posterior sampling and by updating the model frequently (as more data is available) provide an accurate final answer
 - (4) **Currently looking up best practices for making accurate surrogate models with sparse high dimensional data
 - (5) Will use lowest level of complexity possible here (like splining for example)

6. Multistate reweighting using MBAR

- a. Not too sure how useful this is going to be if we can use surrogate modeling to help assess likelihood instead
- b. Maybe just demonstrate surrogate modeling vs. using MBAR to help speed sampling on smaller scale?
- c. Utility of MBAR
 - (1) Way more efficient than direct simulation
 - (2) Able to describe parameters of estimated distribution when there is significant configurational overlap with the original
- d. Utilized in the same way surrogate modeling would be, but less efficient (we think)
- e. Preliminary results have shown that reweighting with MBAR is accurate within conservative changes of 5% in bonded force constant and 3% change in minimum bond length. Thus, each move during posterior construction will end in a new simulation on that cusp to generate new evidence before the next reweighting move.

IV. Results and Analyses

A. Ideas for deliverables/presentation of results:

1. I think it would be worthwhile to show the evolution of the posterior distribution over iterations, so maybe show a few snapshots of the posterior heat map for select SMIRKS (k vs x_0 , or the equivalent for the angle parameters) over iterations, i.e.
2. Show any non-gaussian posteriors
3. Want to compare our final Bayesian sampled forcefield to the original
 - a. How different are they?
 - b. Compare observables
 - c. Error
 - d. Confidence intervals on final parameter values pulled from posterior (need to investigate best way to go about this)
4. Efficiency of process with and without surrogate modeling (just simulation vs with MBAR vs with surrogate modeling)

V. Conclusions

- A. Impacts of study and implication for uses of classical force field parameterization
- B. Highlight that, despite practical complexity, the parameterization process can and will get much more complex
- C. We have presented a novel and fully automated process for parameterization of classical force fields driven by Bayesian inference given some experimental data. Not only does the process provide fully automated parameter optimization and selection based on probability, but also a means to update extant classical force fields with new experimental data. The original force field parameters were all recovered within the uncertainties that we determined from their posterior distributions (let's assume).

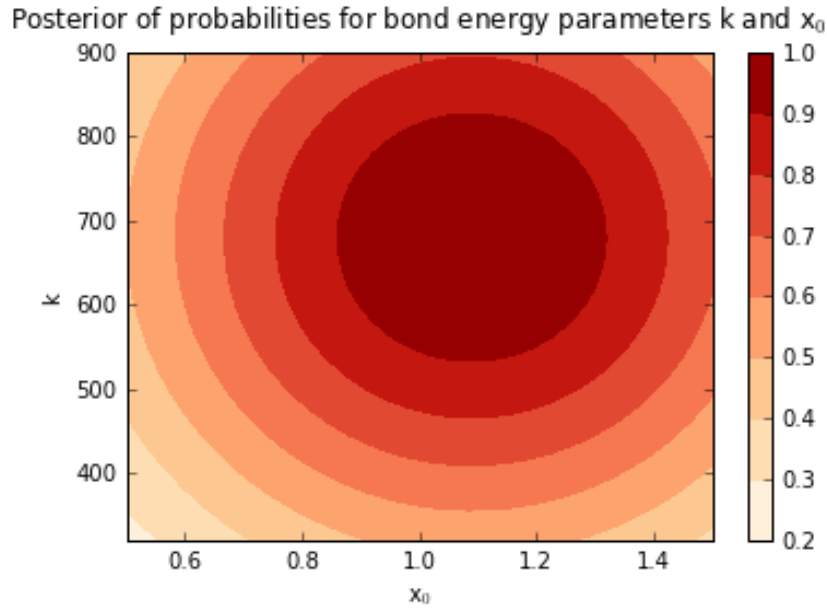


Figure 2: Final iteration of 2D heatmap representation of posterior probability distribution marginalized over all others.

D. While we have only presented a toy problem to test the validity and efficiency of the process; we have well demonstrated the challenges presented by force field parameterization. Moreover, we have shown that using simple surrogate models in order to cheaply calculate observables a function of parameter greatly decreases the costs of assessing the likelihood function. While this was not imperative to the success of this initial parameterization problem, it will be as we move towards using bulk phase properties as evidence where large scale simulations will become a prohibitive computational expense when assessing the likelihood function.

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