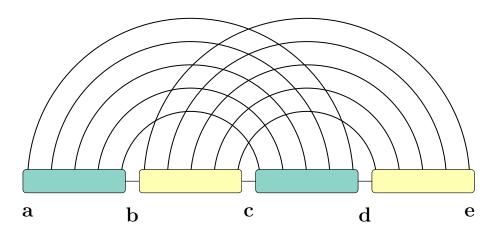
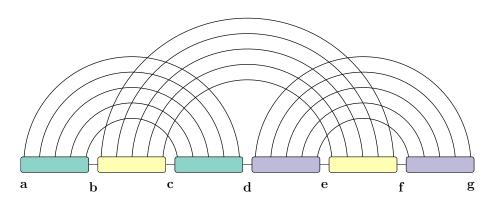
fatgraph name: H



first and last anchors, already given: $\boldsymbol{a}, \boldsymbol{e}$

fatgraph name: K



first and last anchors, already given: a, q

$$A = \min_{d} \left(B \left[a, d | d, g \right] \right)$$

$$B'[a,d|d',g] = \min \begin{cases} B'[a,d-1|d',g], & \text{if } d-1,\notin \{a,d',g\} \\ B[a+1,d-1|d',g] + \Delta G(a,d) & \text{if } \{a+1,d-1\} \cap \{d',g\} = \emptyset \end{cases}$$

$$B[a,d|d',g] = \min \begin{cases} B[a+1,d|d',g], & \text{if } a+1\notin \{d,d',g\} \\ B[a,d-1|d',g], & \text{if } d-1,\notin \{a,d',g\} \\ B[a+1,d-1|d',g] + \Delta G(a,d) & \text{if } \{a+1,d-1\} \cap \{d',g\} = \emptyset, \end{cases}$$

$$C'[d,g|b,c] = \min \begin{cases} C'[d,g-1|b,c], & \text{if } g-1,\notin \{d,b,c\} \\ C[d+1,g-1|b,c] + \Delta G(d,g) & \text{if } \{d+1,g-1\} \cap \{b,c\} = \emptyset \end{cases}$$

$$C[d,g|b,c] = \min \begin{cases} C[d+1,g|b,c], & \text{if } d+1\notin \{g,b,c\} \\ C[d+1,g-1|b,c] + \Delta G(d,g) & \text{if } \{d+1,g-1\} \cap \{b,c\} = \emptyset, \end{cases}$$

$$C[d,g|b,c] = \min \begin{cases} C[d+1,g|b,c], & \text{if } g-1,\notin \{d,b,c\} \\ C[d+1,g-1|b,c] + \Delta G(d,g) & \text{if } \{d+1,g-1\} \cap \{b,c\} = \emptyset, \end{cases}$$

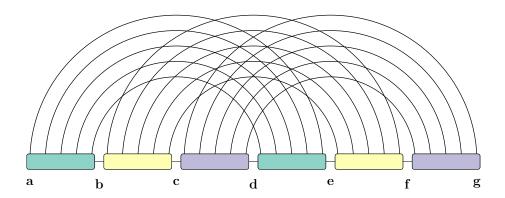
$$C[d+1,g-1|b,c], & \text{if } g-1,\notin \{d,b,c\} \\ C[d+1,g-1|b,c], & \text{if } g-1,\notin \{d,b,c\} \end{cases}$$

$$C[d+1,g-1|b,c], & \text{if } g-1,\notin \{d,b,c\} \\ C[d+1,g-1|b,c], & \text{if } g-1,\notin \{d,b,c\} \end{cases}$$

$$C'[d,g|b,c] = \min \left\{ \begin{array}{ll} C'[d,g-1|b,c], & \text{if } g-1,\notin \{d,b,c\} \\ \hline C[d+1,g-1|b,c] + \Delta G(d,g) & \text{if } \{d+1,g-1\} \cap \{b,c\} = \emptyset \end{array} \right.$$

$$C [d,g|b,c] = \min \begin{cases} C [d+1,g|b,c], & \text{if } d+1 \notin \{g,b,c\} \\ C'[d,g-1|b,c], & \text{if } g-1, \notin \{d,b,c\} \\ C [d+1,g-1|b,c] + \Delta G(d,g) & \text{if } \{d+1,g-1\} \cap \{b,c\} = \emptyset, \\ C_{\boxtimes}'[b,c-1,d,g+1-1] \end{cases}$$

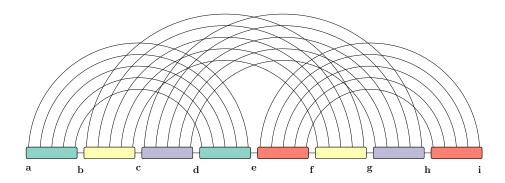
fatgraph name: L



first and last anchors, already given: a,g

$$A = \min_{c,d,f} \left(B\left[a,c,d,f\right] + \boxed{C_{\boxtimes}} \left[c,d-1,f,g-1\right] \right)$$

fatgraph name: M



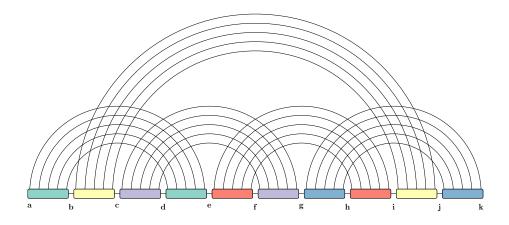
first and last anchors, already given: a, i

$$A = \min_{e,f,h} \left(B\left[a,e,f,h\right] + \begin{array}{|c|c|c|c|} \hline C_{\boxtimes} & [e,f-1,h,i-1] \right)$$

$$B\left[a,e,f,h\right] = \min_{b,d} \left(\begin{array}{|c|c|c|} \hline C_{\boxtimes} & [a,b-1,d,e-1] + C\left[b,d,f,h\right] \right)$$

$$C\left[b,d,f,h\right] = \min_{c,g} \left(\begin{array}{|c|c|c|} \hline C_{\boxtimes} & [c,d-1,g,h-1] + \begin{array}{|c|c|c|} \hline C_{\boxtimes} & [b,c-1,f,g-1] \right)$$

fatgraph name: C5



first and last anchors, already given: a, k

$$A = \min_{g,h,j} \left(B\left[a,g,h,j\right] + \boxed{\textbf{C}_{\boxtimes}} \left[g,h-1,j,k-1\right] \right)$$

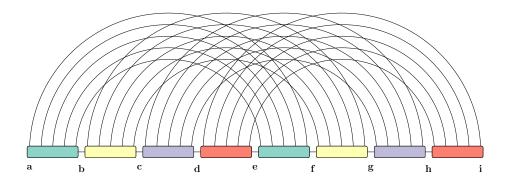
$$B\left[a,g,h,j\right] = \min_{e,f,i} \left(C_{\boxtimes} \left[e,f-1,h,i-1\right] + C \left[a,e|f,g,i,j\right] \right)$$

$$C'[a,e|f,g,i,j] = \min \begin{cases} C'[a,e-1|f,g,i,j], & \text{if } e-1,\notin\{a,f,g,i,j\} \\ C[a+1,e-1|f,g,i,j] + \Delta G(a,e) & \text{if } \{a+1,e-1\} \cap \{f,g,i,j\} = \emptyset \end{cases}$$

$$C[a,e|f,g,i,j] = \min \begin{cases} C[a+1,e|f,g,i,j], & \text{if } a+1\notin\{e,f,g,i,j\} \\ C'[a,e-1|f,g,i,j], & \text{if } e-1,\notin\{a,f,g,i,j\} \\ C[a+1,e-1|f,g,i,j] + \Delta G(a,e) & \text{if } \{a+1,e-1\} \cap \{f,g,i,j\} = \emptyset, \\ D'[a,e+1,f,g,i,j] \end{cases}$$

$$D\left[b,d,f,g,i,j\right] = \min_{c} \left(\boxed{C_{\boxtimes}} \left[c,d-1,f,g-1\right] + \boxed{C_{\boxtimes}} \left[b,c-1,i,j-1\right] \right)$$

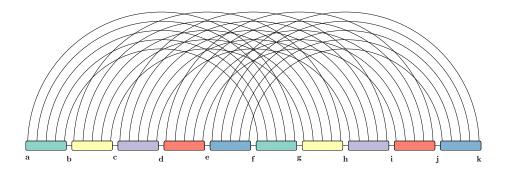
fatgraph name: K4



first and last anchors, already given: a, i

$$\begin{split} A &= \min_{d,e,h} \left(B\left[a,d,e,h\right] + \begin{array}{|c|c|c|c|} \hline C_{\boxtimes} & [d,e-1,h,i-1] \right) \\ \\ B\left[a,d,e,h\right] &= \min_{c,g} \left(C\left[a,c,e,g\right] + \begin{array}{|c|c|} \hline C_{\boxtimes} & [c,d-1,g,h-1] \right) \\ \\ C\left[a,c,e,g\right] &= \min_{b,f} \left(\begin{array}{|c|c|c|} \hline C_{\boxtimes} & [b,c-1,f,g-1] + \begin{array}{|c|c|} \hline C_{\boxtimes} & [a,b-1,e,f-1] \right) \\ \end{split}$$

fatgraph name: K5



first and last anchors, already given: a, k

$$\begin{split} A &= \min_{e,f,j} \Big(B \left[a,e,f,j \right] + \boxed{C_{\boxtimes}} \left[e,f-1,j,k-1 \right] \Big) \\ B \left[a,e,f,j \right] &= \min_{d,i} \Big(C \left[a,d,f,i \right] + \boxed{C_{\boxtimes}} \left[d,e-1,i,j-1 \right] \Big) \\ C \left[a,d,f,i \right] &= \min_{b,g} \Big(D \left[b,d,g,i \right] + \boxed{C_{\boxtimes}} \left[a,b-1,f,g-1 \right] \Big) \\ D \left[b,d,g,i \right] &= \min_{c,h} \Big(\boxed{C_{\boxtimes}} \left[c,d-1,h,i-1 \right] + \boxed{C_{\boxtimes}} \left[b,c-1,g,h-1 \right] \Big) \end{split}$$