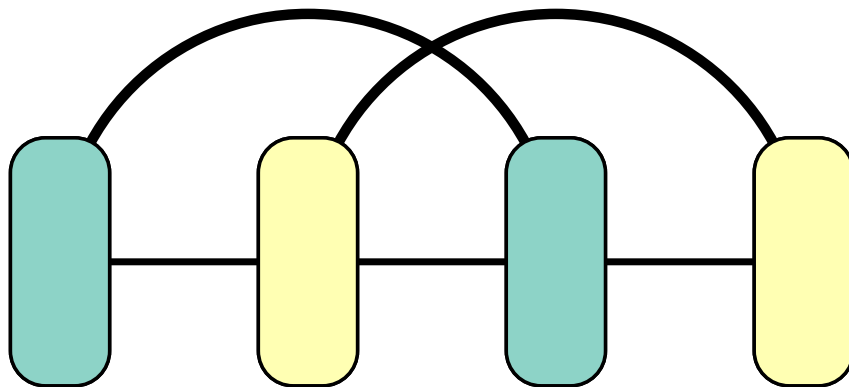


fatgraph name: H



a b c d e

first and last anchors, already given: a, h

$$A = \min (B [])$$

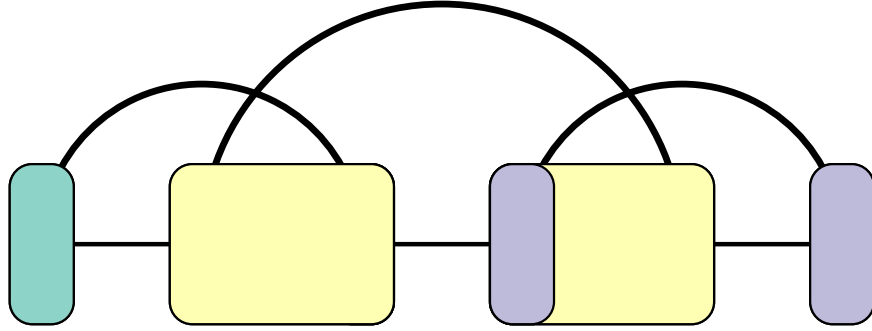
$$B = \min_{a,c,d,f,h} \left(D[a, f|c, d] + C[c, d, f, h] \right)$$

$$C[c, d, f, h] = \min_g \left(C_{\boxtimes}[c, d-1, g, h-1] \right)$$

$$D'[a, f|c, d] = \min \begin{cases} D'[a, f-1|c, d], & \text{if } f-1 \notin \{a, c, d\} \\ D[a+1, f-1|c, d] + \Delta G(a, f) & \text{if } \{a+1, f-1\} \cap \{c, d\} = \emptyset \end{cases}$$

$$D[a, f|c, d] = \min \begin{cases} D[a+1, f|c, d], & \text{if } a+1 \notin \{f, c, d\} \\ D'[a, f-1|c, d], & \text{if } f-1 \notin \{a, c, d\} \\ D[a+1, f-1|c, d] + \Delta G(a, f) & \text{if } \{a+1, f-1\} \cap \{c, d\} = \emptyset \end{cases}$$

fatgraph name: K



a b c d e f g

first and last anchors, already given: a, h

$$A = \min (B [])$$

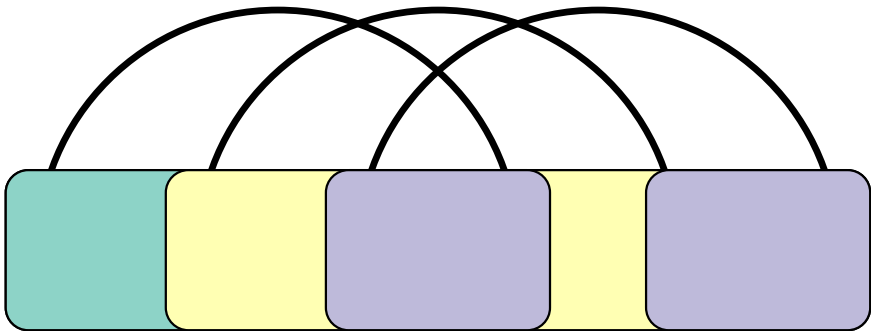
$$B = \min_{a,c,d,f,h} \left(D[a, f|c, d] + C[c, d, f, h] \right)$$

$$C[c, d, f, h] = \min_g \left(C_{\boxtimes}[c, d-1, g, h-1] \right)$$

$$D'[a, f|c, d] = \min \begin{cases} D'[a+1, f|c, d], & \text{if } a+1 \notin \{f, c, d\} \\ D[a+1, f-1|c, d] + \Delta G(a, f) & \text{if } \{a+1, f-1\} \cap \{c, d\} = \emptyset \end{cases}$$

$$D[a, f|c, d] = \min \begin{cases} D[a, f-1|c, d], & \text{if } f-1 \notin \{a, c, d\} \\ D'[a+1, f|c, d], & \text{if } a+1 \notin \{f, c, d\} \\ D[a+1, f-1|c, d] + \Delta G(a, f) & \text{if } \{a+1, f-1\} \cap \{c, d\} = \emptyset \end{cases}$$

fatgraph name: L



a_b c d e f_g

first and last anchors, already given: a, l

$$A = \min (B \; [])$$

$$B = \min_{a,b,d,g,h,k} \left(F[a,d,g,k] + C[b,d,h,k] + \textcolor{purple}{C_{\boxtimes}}[a,b-1,g,h-1] \right)$$

$$C[b,d,h,k] = \min_c (D[c,d,h,k])$$

$$D[c,d,h,k] = \min_j (E[c,d,h,j])$$

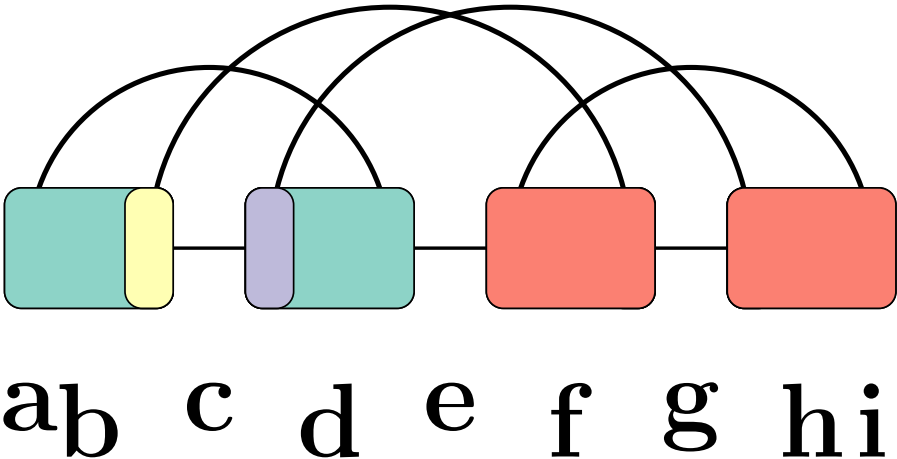
$$E[c,d,h,j] = \min_i \left(\textcolor{teal}{C_{\boxtimes}}[c,d-1,i,j-1] \right)$$

$$F[a,d,g,k] = \min_f (G[a,d,f,k])$$

$$G[a,d,f,k] = \min_l (H[d,f,k,l])$$

$$H[d,f,k,l] = \min_e \left(\textcolor{yellow}{C_{\boxtimes}}[e,f-1,k,l-1] \right)$$

fatgraph name: M



first and last anchors, already given: a, l

$$A = \min (B \; [])$$

$$B = \min_{a,b,d,g,h,k} \left(F[a,d,g,k] + C[b,d,h,k] + C_{\boxtimes}[a,b-1,g,h-1] \right)$$

$$C[b,d,h,k] = \min_c (D[c,d,h,k])$$

$$D[c,d,h,k] = \min_j (E[c,d,h,j])$$

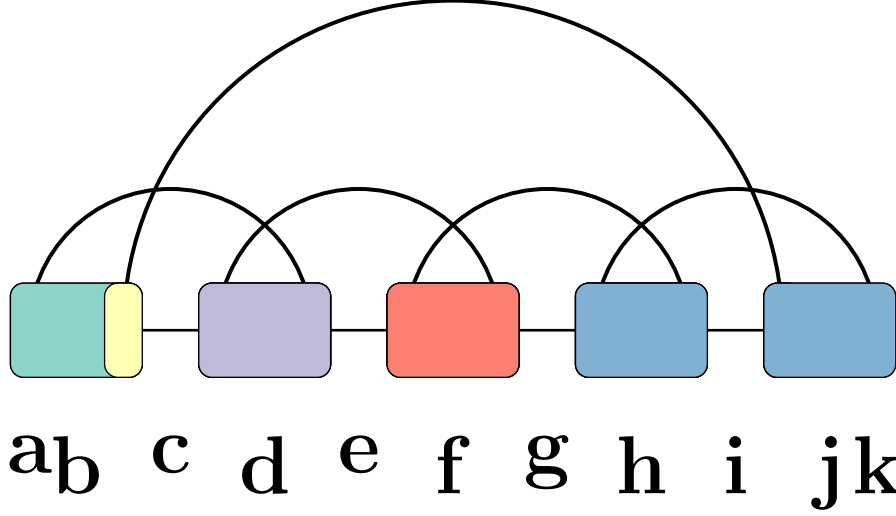
$$E[c,d,h,j] = \min_i \left(C_{\boxtimes}[c,d-1,i,j-1] \right)$$

$$F[a,d,g,k] = \min_f (G[a,d,f,k])$$

$$G[a,d,f,k] = \min_l (H[d,f,k,l])$$

$$H[d,f,k,l] = \min_e \left(C_{\boxtimes}[e,f-1,k,l-1] \right)$$

fatgraph name: C5



first and last anchors, already given: a, l

$$A = \min (B \square)$$

$$B = \min_{a,c,f,h,l} \left(\textcolor{teal}{G}[a, h|c, f] + \textcolor{yellow}{C}[c, l|f, h] \right)$$

$$\textcolor{yellow}{C}'[c, l|f, h] = \min \begin{cases} \textcolor{yellow}{C}'[c+1, l|f, h], & \text{if } c+1 \notin \{l, f, h\} \\ \textcolor{yellow}{C}[c+1, l-1|f, h] + \Delta G(c, l) & \text{if } \{c+1, l-1\} \cap \{f, h\} = \emptyset \end{cases}$$

$$\textcolor{yellow}{C}[c, l|f, h] = \min \begin{cases} \textcolor{yellow}{C}[c, l-1|f, h], & \text{if } l-1 \notin \{c, f, h\} \\ \textcolor{yellow}{C}'[c+1, l|f, h], & \text{if } c+1 \notin \{l, f, h\} \\ \textcolor{yellow}{C}[c+1, l-1|f, h] + \Delta G(c, l) & \text{if } \{c+1, l-1\} \cap \{f, h\} = \emptyset \end{cases}$$

$$D[d, f, h, k] = \min_j (E[d, f, h, j])$$

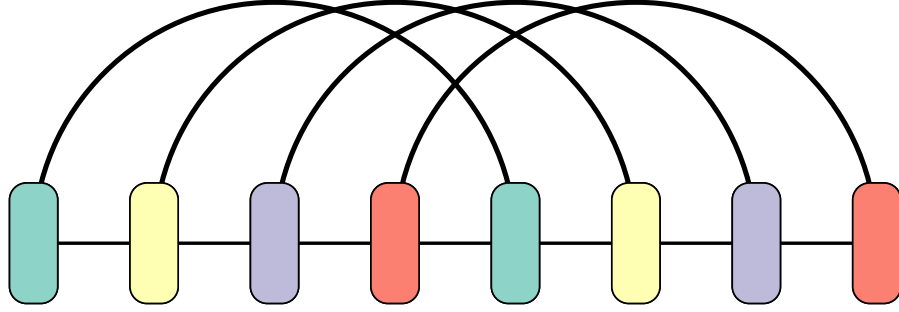
$$E[d, f, h, j] = \min_e (F[e, f, h, j])$$

$$F[e, f, h, j] = \min_i \left(\textcolor{purple}{C}_{\boxtimes}[e, f-1, i, j-1] \right)$$

$$\textcolor{teal}{G}'[a, h|c, f] = \min \begin{cases} \textcolor{teal}{G}'[a, h-1|c, f], & \text{if } h-1 \notin \{a, c, f\} \\ \textcolor{teal}{G}[a+1, h-1|c, f] + \Delta G(a, h) & \text{if } \{a+1, h-1\} \cap \{c, f\} = \emptyset \end{cases}$$

$$\textcolor{teal}{G}[a, h|c, f] = \min \begin{cases} \textcolor{teal}{G}[a+1, h|c, f], & \text{if } a+1 \notin \{h, c, f\} \\ \textcolor{teal}{G}'[a, h-1|c, f], & \text{if } h-1 \notin \{a, c, f\} \\ \textcolor{teal}{G}[a+1, h-1|c, f] + \Delta G(a, h) & \text{if } \{a+1, h-1\} \cap \{c, f\} = \emptyset \end{cases}$$

fatgraph name: K4



a b c d e f g h i

first and last anchors, already given: a, p

$$A = \min (B [])$$

$$B = \min_{a,c,e,h,j,m} (I[a,c,h,j] + F[c,e,j,m] + C[a,e,h,m])$$

$$C[a,e,h,m] = \min_{f,n} \left(C_{\boxtimes}[e,f-1,m,n-1] + D[a,f,h,n] \right)$$

$$D[a,f,h,n] = \min_o \left(E[h,o|a,f] \right)$$

$$E'[h,o|a,f] = \min \begin{cases} E'[h-1,o|a,f], & \text{if } h-1 \notin \{o,a,f\} \\ E[h-1,o+1|a,f] + \Delta G(h,o) & \text{if } \{h-1,o+1\} \cap \{a,f\} = \emptyset \end{cases}$$

$$E[h,o|a,f] = \min \begin{cases} E[h,o+1|a,f], & \text{if } o+1 \notin \{h,a,f\} \\ E'[h-1,o|a,f], & \text{if } h-1 \notin \{o,a,f\} \\ E[h-1,o+1|a,f] + \Delta G(h,o) & \text{if } \{h-1,o+1\} \cap \{a,f\} = \emptyset \end{cases}$$

$$F[c,e,j,m] = \min_l (G[c,e,j,l])$$

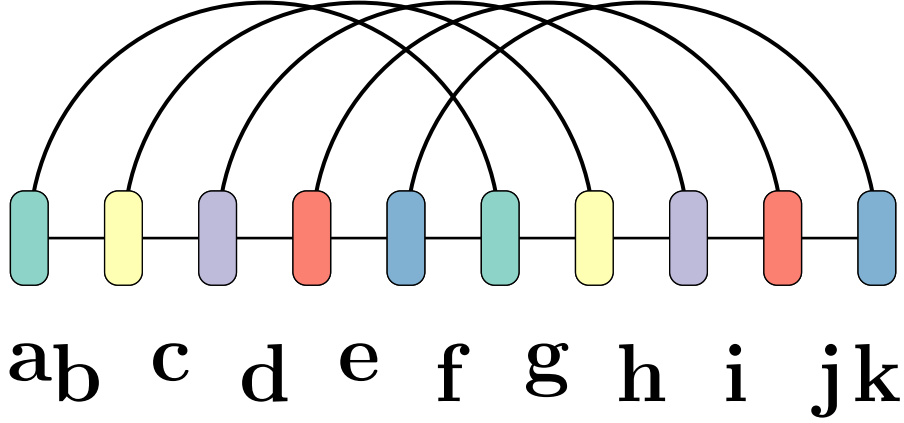
$$G[c,e,j,l] = \min_d (H[c,d,j,l])$$

$$H[c,d,j,l] = \min_k \left(C_{\boxtimes}[c,d-1,k,l-1] \right)$$

$$I[a,c,h,j] = \min_i (J[a,c,i,j])$$

$$J[a,c,i,j] = \min_b \left(C_{\boxtimes}[a,b-1,i,j-1] \right)$$

fatgraph name: K5



first and last anchors, already given: a, t

$$A = \min (B [])$$

$$B = \min_{a,c,g,j,l,q} \left(L[a,l|c,j] + G[c,g,l,q] + C[a,g,j,q] \right)$$

$$C[a,g,j,q] = \min_{h,r} \left(C_{\boxtimes}[g,h-1,q,r-1] + D[a,h,j,r] \right)$$

$$D[a,h,j,r] = \min_i (E[a,i,j,r])$$

$$E[a,i,j,r] = \min_t (F[i,j,r,t])$$

$$F[i,j,r,t] = \min_s \left(C_{\boxtimes}[i,j-1,s,t-1] \right)$$

$$G[c,g,l,q] = \min_{d,n} (I[d,g,n,q] + H[c,d,l,n])$$

$$H[c,d,l,n] = \min_m \left(C_{\boxtimes}[c,d-1,m,n-1] \right)$$

$$I[d,g,n,q] = \min_p (J[d,g,n,p])$$

$$J[d,g,n,p] = \min_e \left(K[e,p|g,n] \right)$$

$$K'[e,p|g,n] = \min \begin{cases} K'[e,p-1|g,n], & \text{if } p-1 \notin \{e,g,n\} \\ K[e+1,p-1|g,n] + \Delta G(e,p) & \text{if } \{e+1,p-1\} \cap \{g,n\} = \emptyset \end{cases}$$

$$\begin{aligned}
\textcolor{blue}{K}[e, p|g, n] &= \min \begin{cases} \textcolor{blue}{K}[e+1, p|g, n], & \text{if } e+1 \notin \{p, g, n\} \\ \textcolor{blue}{K}[e, p-1|g, n], & \text{if } p-1 \notin \{e, g, n\} \\ \textcolor{blue}{K}[e+1, p-1|g, n] + \Delta G(e, p) & \text{if } \{e+1, p-1\} \cap \{g, n\} = \emptyset \end{cases} \\
\textcolor{yellow}{L}'[a, l|c, j] &= \min \begin{cases} \textcolor{yellow}{L}'[a+1, l|c, j], & \text{if } a+1 \notin \{l, c, j\} \\ \textcolor{yellow}{L}[a+1, l-1|c, j] + \Delta G(a, l) & \text{if } \{a+1, l-1\} \cap \{c, j\} = \emptyset \end{cases} \\
\textcolor{yellow}{L}[a, l|c, j] &= \min \begin{cases} \textcolor{yellow}{L}[a, l-1|c, j], & \text{if } l-1 \notin \{a, c, j\} \\ \textcolor{yellow}{L}'[a+1, l|c, j], & \text{if } a+1 \notin \{l, c, j\} \\ \textcolor{yellow}{L}[a+1, l-1|c, j] + \Delta G(a, l) & \text{if } \{a+1, l-1\} \cap \{c, j\} = \emptyset \end{cases}
\end{aligned}$$