The DIM MATLAB toolbox

A practical user's guide

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1. What is the DIM MATLAB toolbox?

The DIM, which is abbreviation of developed inverse model, is a collection of MATLAB scripts to inversely estimate parameters of continuous time random walk-truncated power law (CTRW-TPL) model using teaching learning-based optimization (TLBO) algorithm. For detailed information about the CTRW-TPL model and the TLBO algorithm, the reader is referred to relevant literatures (e.g., Dentz et al., 2004; Berkowitz et al., 2006; Cortis and Berkowitz, 2004 and 2005; Rao et al., 2011; Rao, 2019). The DIM runs on MATLAB R2017a and higher versions of MATLAB; it has not been tested on earlier versions of MATLAB.

2. Introduction

The CTRW-TPL model has been successfully applied to simulate the contaminant transport in porous and fractured media (e.g., Cortis and Berkowitz, 2004; Gao et al., 2009; Rubin et al., 2012; Wang and Cardenas, 2014; Edery et al., 2016; Hu et al., 2020; Li et al., 2022; Zhou et al., 2024, among many others). The CTRW-TPL model has four input parameters: normalized transport velocity (v_φ), normalized dispersion coefficient (D_φ), power law exponent (β), and time scale of t_2, which have to be inversely identified. Cortis and Berkowitz (2005) presented a MATLAB toolbox to inversely estimate the CTRW parameters. Then, Cortis et al. (2020) expanded and

completed the toolbox. The main disadvantage of the toolbox is its sensitivity to initial guesses for the parameters. The DIM is an inverse model based on the TLBO algorithm to estimate the parameters of the CTRW-TPL model. The required scripts of the DIM were designed in MATLAB R2017a. As above-mentioned, the DIM can be run on MATLAB R2017a and the higher versions of MATLAB.

3. MATLAB scripts of the DIM

The MATLAB scripts of the DIM include two groups of files. The first group, which is located in Inverse_Group_1 folder, is used for the case where the tracer injection is continuous. The second group, which is located in Inverse_Group_2 folder, is used for the case where the tracer injection is instantaneous. Each group contains three files named tlbo.m, Experimental_data.m, and CTRW_TPL_fit.m. The tlbo.m file is the MATLAB script executing the TLBO algorithm, the Experimental_data.m file is the MATLAB script containing the experimental data and the tracer test characteristics, and the CTRW_TPL_fit.m is the MATLAB script calculating the objective function value.

4. How to use the DIM

First of all, unzip and open the Inverse_Group_1 or Inverse_Group_2 folder according to the type of the tracer injection. Then, follow the bellow steps:

Step 1: Enter the experimental data in the Experimental_data.m file. Note that the experimental data usually contain the tracer relative concentration values versus time values and the travel distance of the tracer. Enter the time values in t_meas matrix and the concentration values in Cr_meas matrix. Also, enter the travel distance value in L variable.

Step 2: Adjust minimum and maximum values of the CTRW-TPL parameters in the tlbo.m file according to previous studies or your knowledge about the case study. Note that VarMin matrix is

related to the minimum values of the parameters, while VarMax matrix is related to the maximum values of the parameters.

Step 3: Click on the run button of the tlbo.m file. It is observed that the following expression appears in Command Window of MATLAB:

"Maximum number of iterations:"

"Maximum number of iterations" is equal to $iter_{max}$, that the user can set its value according to his/her experience. After entering $iter_{max}$ value, the following expression appears in Command Window of MATLAB:

"Population size:"

"Population size" is equal to N_{pop} that the user can set its value according to his/her experience. After entering the N_{pop} and $iter_{max}$ values, the DIM looks for the optimum values of the CTRW-TPL parameters automatically using the TLBO algorithm. Finally, the user can observe the optimal values of the parameters and the best value of the objective function in BestSol. The BestSol consists of Position vector and Cost value. The Position vector, respectively, includes optimal values of the v_φ, D_φ, β, and t_2 parameters, and the Cost value is the best value of the objective function. Also, the DIM displays the variations of the objective function value versus iteration graphically. It is necessary to mention that due to the stochastic nature of the TLBO algorithm, the DIM has to be executed ten times for each case study, and, finally, the average of the optimal values of the CTRW-TPL parameters obtained in the ten runs has to be reported as the final optimal parameters.

5. One-dimensional forward modeling

In addition to the MATLAB scripts of the DIM, the required MATLAB scripts were designed for the one-dimensional forward modeling of the solute transport using the CTRW-TPL model. The

MATLAB scripts of the forward modeling include two groups of files. The first group, which is located in Forward_Group_1 folder, is used for the case where the tracer injection of is continuous. The second group, which is located in Forward_Group_2 folder, is used for the case where the tracer injection of is instantaneous.

Each group contains two files named Experimental_data.m and Forward_CTRW_TPL.m. The Experimental_data.m file is the MATLAB script containing the experimental data and the tracer test characteristics, and the Forward_CTRW_TPL.m file calculates the tracer concentration values using the CTRW-TPL model and compares them with the measured concentration values.

To use these scripts, first of all, unzip and open the Forward _Group_1 or Forward _Group_2 folder according to the type of the tracer injection. Then, follow the bellow steps:

Step 1: Enter the experimental data in the Experimental_data.m file. Note that the experimental data usually contain the tracer relative concentration values versus time values and the travel distance of the tracer. Enter the time values in the t_meas matrix and the concentration values in the Cr_meas matrix. Also, enter the travel distance value in the L variable.

Step 2: Enter the values of the v_φ, D_φ, β, and t_2 parameters in v_psi, D_psi, beta, and t2 variables of the Forward_CTRW_TPL.m. file, respectively. Note the dimensions of the v_psi, D_psi, and t2 variables depend on the dimensions of measurement times in the Experimental_data.m file. The beta variable and relative concentration values are dimensionless.

Step 3: Click on the run button of the Forward_CTRW_TPL.m. file. After executing the script, RMSE value appears in Command Window of MATLAB. Also, a graphical comparison of the measured and calculated concentration values is displayed.

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