From Mathematics to Generic Programming

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Solution.

We have a group with 101 distinct elements. Lagrange's Theorem tells us that *the order of any subgroup H in a finite group G divides the order of the group.* Well, 101 happens to be prime. So the only subgroups that can exist must have orders that are divisors of 101, otherwise we will have contradicted Lagrange's Theorem. The divisors of 101 are 1 and 101; the subgroups of G are $\{1\}$ and G, the trivial subgroups.