

# From Mathematics to Generic Programming

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## 6.8

*Solution.*

Let  $b = g^n$  for some generating element  $g$  in  $G$ . Let  $a = g^m$ .

We want to show that our arbitrary  $a$  and  $b$  chosen from a cyclic group will satisfy

$$a \circ b = b \circ a$$

We can use the Commutativity of Powers (6.1) to show that a cyclic group is indeed *abelian*.

$$a \circ b = g^n g^m = g^m g^n = ba = b \circ a$$

This holds for any  $a$  and  $b$ , as  $a$  and  $b$  were chosen arbitrarily.