Brady Metherall

$$\rho \bigg(\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} \bigg) = -\nabla p + \mu \nabla^2 \mathbf{u} + \rho \mathbf{g}$$

1 2d

$$\frac{\partial h}{\partial t} = \frac{1}{3} \nabla \left(h^3 \nabla h \right) \tag{1}$$

$$\int_{\mathbb{R}} h \, \mathrm{d}x \tag{2}$$

 $h(x,t)=t^{\alpha}f(\eta)$ where $\eta=xt^{-\beta}$ $\alpha=-1/5$ $\beta=1/5$

$$\frac{-3}{5}(\eta f' + f) = (f^3 f)'$$

$$f = \left(\frac{9}{10}\right)^{1/3} \left(\eta_*^2 - \eta^2\right)^{1/3}$$

$$\eta_* = \left(\frac{6075\Gamma^6(\frac{2}{3})\Gamma^6(\frac{11}{6})}{16\pi^9}\right)^{1/10}$$

$$\approx 0.747412$$

2 Polar

solve (1) and (2) in polar $\alpha = -1/4 \ \beta = 1/8$

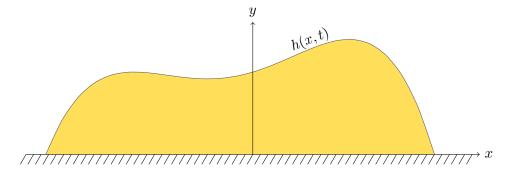


Figure 1: Beer spilled on a table.

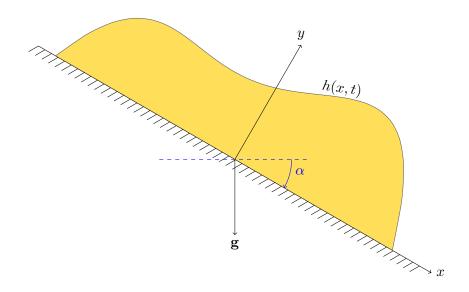


Figure 2: Beer spilled on a crooked table.

$$\frac{-3}{8} \left(2\eta f + \eta^2 f' \right) = \left(\eta f^3 f' \right)'$$

$$f = \left(\frac{9}{16}\right)^{1/3} \left(\eta_*^2 - \eta^2\right)^{1/3}$$

$$\eta_* = \left(\frac{1024}{243\pi^3}\right)^{1/8}$$
$$\approx 0.779212$$