

**1.3.7** Evaluate the closed-surface integral of the vector  $\mathbf{A} = 3\mathbf{u}_r$  over the spherical surface that has a radius  $a$ .

$$\begin{aligned}
 \oint \mathbf{A} \bullet \mathbf{ds} &= \int_{\phi=0}^{2\pi} \int_{\theta=0}^{\pi} 3\mathbf{u}_r \bullet r^2 \sin \theta d\theta d\phi \mathbf{u}_r \\
 &= \int_{\phi=0}^{2\pi} \int_{\theta=0}^{\pi} 3r^2 \sin \theta d\theta d\phi \\
 &= - \int_{\phi=0}^{2\pi} 3r^2 \cos \theta \Big|_{\theta=0}^{\pi} d\phi \\
 &= - \int_{\phi=0}^{2\pi} 3r^2 (-1 - 1) d\phi \\
 &= \int_{\phi=0}^{2\pi} 6r^2 d\phi \\
 &= 6r^2 \phi \Big|_{\phi=0}^{2\pi} \\
 &= 12\pi r^2 \\
 &= 12\pi a^2
 \end{aligned}$$