

1.2.11 Convert the vector $\mathbf{B} = 3\mathbf{u}_r + 4\mathbf{u}_\theta + 5\mathbf{u}_\phi$ that is in spherical coordinates into Cartesian coordinates. Check your answer using MATLAB.

$$\begin{aligned}x &= r \sin \theta \cos \phi \\&= 3 \sin 4 \cos 5 \\&\approx -0.644\end{aligned}$$

$$\begin{aligned}y &= r \sin \theta \sin \phi \\&= 3 \sin 4 \sin 5 \\&\approx 2.18\end{aligned}$$

$$\begin{aligned}z &= r \cos \theta \\&= 3 \cos 4 \\&\approx -1.96\end{aligned}$$

The final vector in spherical coordinates is $\mathbf{B} \approx -0.644\mathbf{u}_x + 2.18\mathbf{u}_y - 1.96\mathbf{u}_z$.