

**1.3.8** Find the surface area of a cylindrical surface by setting up and evaluating the integral  $\oint \mathbf{A} \bullet \mathbf{ds}$  where  $\mathbf{A} = \mathbf{u}_\rho + 2\mathbf{u}_z$ . *Note: Diagram not shown.*

The radius of the cylinder is  $a$ .

$$\begin{aligned}
 \oint \mathbf{A} \bullet \mathbf{ds} &= \int_{\phi=0}^{2\pi} \int_{z=0}^{\mathcal{L}} (\mathbf{u}_\rho + 2\mathbf{u}_z) \bullet (\rho d\phi dz \mathbf{u}_\rho + \rho d\rho d\phi \mathbf{u}_z) \\
 &= \int_{\phi=0}^{2\pi} \int_{z=0}^{\mathcal{L}} \rho dz d\phi + \int_{\phi=0}^{2\pi} \int_{z=0}^{\mathcal{L}} 2\rho d\rho d\phi \\
 &= \int_{\phi=0}^{2\pi} \rho z \Big|_{z=0}^{\mathcal{L}} d\phi \\
 &= \int_{\phi=0}^{2\pi} \rho \mathcal{L} d\phi \\
 &= \rho \mathcal{L} \phi \Big|_{\phi=0}^{2\pi} \\
 &= 2\pi \rho \mathcal{L} \\
 &= 2\pi a \mathcal{L}
 \end{aligned}$$