

1.2.6 Find the vector product of the two vectors defined by $\mathbf{A} = 3\mathbf{u}_x + 4\mathbf{u}_y + 5\mathbf{u}_z$ and $\mathbf{B} = -5\mathbf{u}_x + 4\mathbf{u}_y - 3\mathbf{u}_z$. Check your answer using MATLAB.

The vector product of \mathbf{A} and \mathbf{B} is

$$\begin{aligned}\mathbf{A} \times \mathbf{B} &= (A_y B_z - A_z B_y)\mathbf{u}_x + (A_z B_x - A_x B_z)\mathbf{u}_y + (A_x B_y - A_y B_x)\mathbf{u}_z \\ &= (4 \cdot -3 - 5 \cdot 4)\mathbf{u}_x + (5 \cdot -5 - 3 \cdot -3)\mathbf{u}_y + (3 \cdot 4 - 4 \cdot -5)\mathbf{u}_z \\ &= -32\mathbf{u}_x - 16\mathbf{u}_y + 32\mathbf{u}_z.\end{aligned}$$