

Recitation 23: Parametric equations & Polar coordinates

Warm up:

Describe the motion given by $x = 8$, $y = 7 \sin(t)$ for all t .

Group work:

Problem 1 Try to figure out the shape of the following curve and then eliminate the parameter and check your intuition.

$$x = \ln t - 1 \quad y = (\ln t)^2$$

Problem 2 Find parametric equations for the path of a particle moving around the circle

$$(x - 3)^2 + (y + 7)^2 = 4$$

- (a) one time around clockwise starting at $(5, -7)$.
- (b) three times around counterclockwise starting at $(5, -7)$.
- (c) halfway around clockwise starting at $(1, -7)$.

Problem 3 Find the intersection point(s) of the lines

$$x = -6 + 9t, \quad y = 3 - 2t \tag{1}$$

and

$$x = 3 + t, \quad y = -4 - 2t. \tag{2}$$

Do they intersect at the same time?

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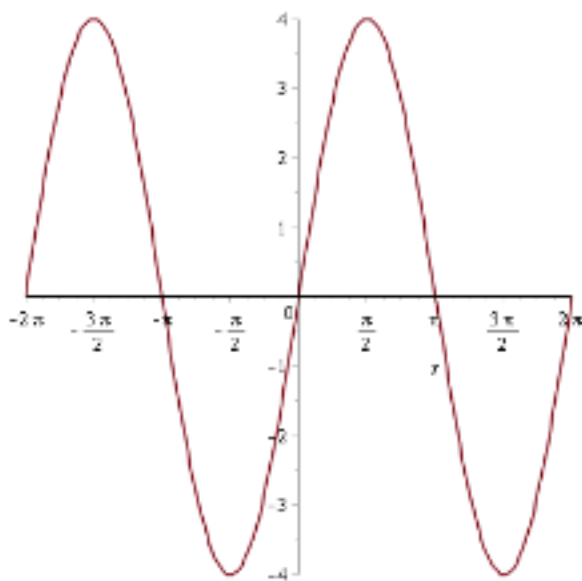
Problem 4 Consider the curve defined by the parameterization $x = t^2$, $y = t^3 - 3t$. Show that this curve has two tangent lines at $(3,0)$, and find the equations of the tangent lines there.

Problem 5 Plot the following (polar) points in the xy -plane and then rewrite them as rectangular coordinates.

(a) $\left(3, \frac{5\pi}{4}\right)$ (b) $\left(3, -\frac{5\pi}{4}\right)$ (c) $\left(-3, \frac{5\pi}{4}\right)$ (d) $\left(-3, -\frac{5\pi}{4}\right)$

Problem 6 Rewrite the rectangular point $(3,5)$ in polar coordinates in three different ways.

Problem 7 The graph of the curve $r = 4 \sin \theta$ is a circle. Use the graph below to sketch this circle. Can you verify this algebraically? What is the period of the polar curve? Is $0 \leq \theta \leq 2\pi$ necessary to complete the graph?



Problem 8 Graph $r = 2 + 4 \cos \theta$ using the “Cartesian-to-Polar” method.
