

## Section 6.4: Volume by Shells

### Warm up:

**Problem 1** Determine whether you should integrate in terms of  $x$  or  $y$  in the given scenarios:

- (a) You are revolving around the  $y$ -axis and using shells.
  - (b) You are revolving around  $y = 2$  and using washers.
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**Problem 2** Determine whether you should use washers or shells:

- (a) You are revolving around  $x = 3$  and want to integrate in terms of  $y$ .
  - (b) You are revolving around the  $x$ -axis and want to integrate in terms of  $y$ .
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### Group work:

**Problem 3** Consider the region bounded by  $y = 2 - 2x$ ,  $y = 2$ , and  $x = 1$ . Use both the washer and shell method to find the volume of the solid formed by revolving this region around  $y = -1$ . Do your answers match?

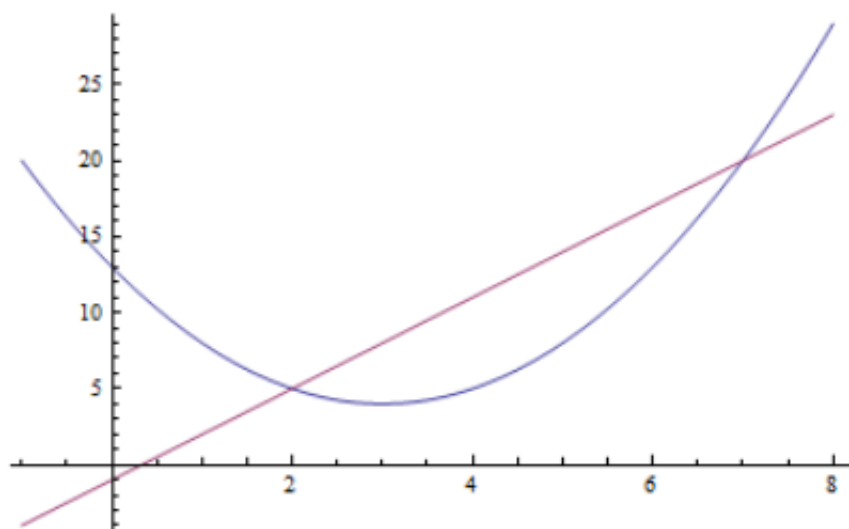
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**Problem 4** Set up an integral that will compute the volume of the solid generated by revolving the region bounded by the curves  $y = x^2 - 6x + 13$  (i.e.  $x = 3 \pm \sqrt{y - 4}$ ) and  $y = 3x - 1$  about the given axes. Use the best/easier method for each problem.

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Learning outcomes:

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- (a) *the  $x$ -axis*
- (b)  $y = -4$
- (c)  $y = 22$
- (d)  $x = 9$