Recitation # 7: Exponential Models and Integration by Parts

Group work:

Problem 1 Vitameatavegamin is a strange substance that comes in two forms. V-I decays at a linear rate, while V-II decays at an exponential rate. Both have the property that 10 ounces will decrease to 7 ounces in 6 hours. For each of V-I and V-II, answer the following:

- (a) If we started with 80 ounces, how much will there be 6 hours later?
- (b) How long will it take to decrease from 15 ounces to 7.5 ounces?

Problem 2 Evaluate the following integrals

(a)
$$\int_{1}^{3} x^2 5^x dx$$

(b)
$$\int \sin(3x)e^{7x} dx$$

(c)
$$\int x^{\frac{5}{3}} (\ln x)^2 dx$$

Problem 3 Evaluate the following integrals

(a)
$$\int x^5 \cos\left(x^3\right) dx$$

(b)
$$\int \cos\left(\sqrt{x}\right) dx$$

(c)
$$\int x \cos x \sin x \, dx$$