

$$\text{let } u = x^4$$

$$\text{then } du = 4x^3 dx$$

$$\frac{du}{4x^3} = dx$$

$$\text{and } u^{1/4} = x$$

$$u = 2^4 = 16$$

$$u = (-2)^4 = 16$$

$$= \int_{16}^{16} \frac{1}{(u^2-1)} \cdot \frac{du}{4u^{3/4}}$$

$$\text{but an integral } \int_a^a f(x) dx = 0$$

$$\text{so } \int_{-2}^2 \frac{1}{x^8-1} dx = 0$$