

# Demographic Time-Bombs

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# What is a Demographic Time-Bomb?

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When the ageing population of a country is exacerbated by declining birth rates, which reduces the number of working age adults.

Demographic Time-Bombs form over years, sometimes decades and are worsened by the increase in life expectancy.



# Why should we care about them?

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- Economic contraction
- Country debt
- Higher tax rates
- Shortage of pension/social security-type funds
- Increase in retirement age



# Demographic Time Bomb Risk Model

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## Data Sources:

- World Bank
- Gapminder

## Breakdown:

- 2000 - 2015
- 163 countries

## Target:

- Potential Support Ratio (PSR)
- PSR (log) \*

$$\left[ \frac{\text{Working-age population}}{\text{Population over 60}} \right]$$

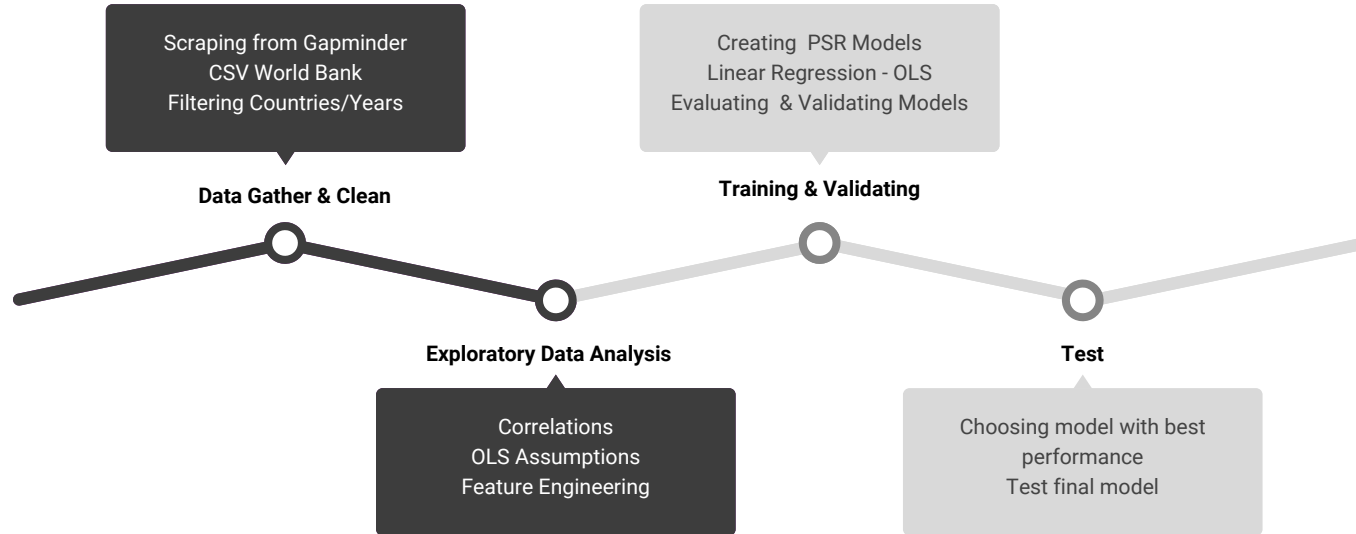
## Features:

- Fertility
- Birth Rate
- Death Rate
- Life Expectancy
- GDP
- Fertility (log) \*
- Death/Birth Rate \*
- Death Rate (2) \*

\* Feature Engineered

# Methodology

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# Model Performance

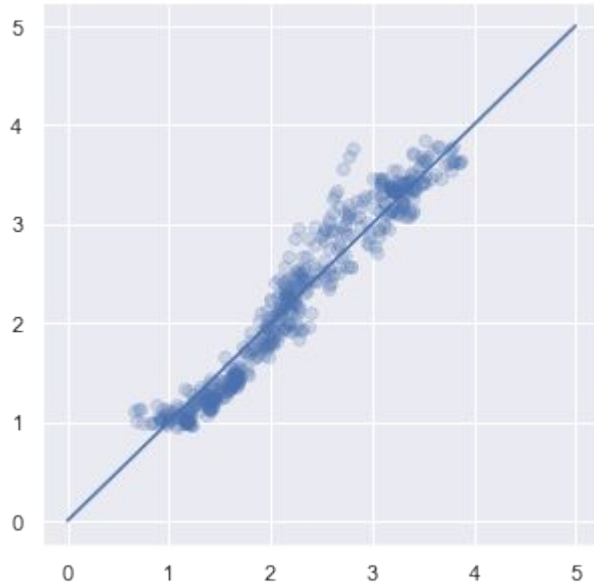
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Model	Root Mean Squared Error (RMSE)	R <sup>2</sup> (Validation)
Model 1	2.819	0.936
Model 2	0.278	0.900
Model 3	2.766	0.938
Model 4	0.247	0.920
Model 5 (LASSO)	2.398	0.954
Model 6 (LASSO)*	0.216	0.939
Model 7 (Ridge M2)	0.278	0.900
Model 8 (Ridge M4)*	0.216	0.920
Model 9 (Random Forest)	0.245	0.922

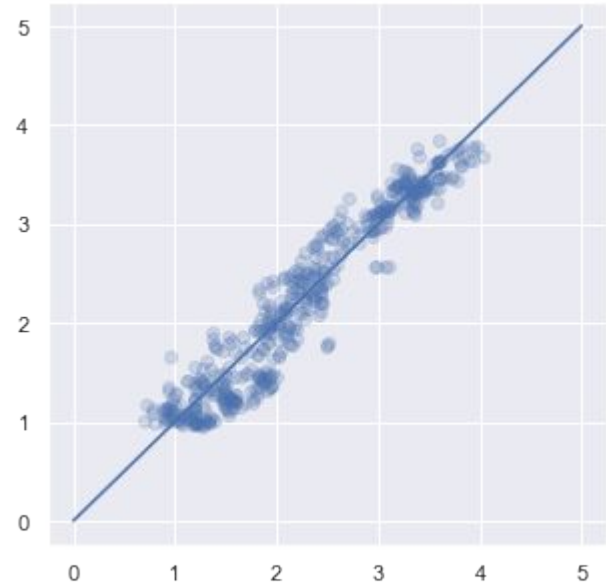
# Comparing Predictions

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Model 6 (LASSO  $y_{\log}$ )



Model 8 (Ridge on Model 4)



# Conclusion - Testing Final Model

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## Applied Model on Test

- Select countries representing low, medium, high PSR values
- $R^2 = 0.937$
- $RMSE = 0.239$

## Features

- Fertility
- Life Expectancy
- Death Rate (Squared)
- Death/Birth Ratio





# Future Work

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- Try model with additional features such as:
  - Men/Women Ratio
  - Unemployment
  - Women Education
  - Immigration

# Appendix

### Model 1

<b>Dep. Variable:</b>	psr	<b>R-squared:</b>	0.929
<b>Model:</b>	OLS	<b>Adj. R-squared:</b>	0.929
<b>Method:</b>	Least Squares	<b>F-statistic:</b>	6771.
<b>Date:</b>	Thu, 24 Jan 2019	<b>Prob (F-statistic):</b>	0.00
<b>Time:</b>	19:38:44	<b>Log-Likelihood:</b>	-3888.1
<b>No. Observations:</b>	1560	<b>AIC:</b>	7784.
<b>Df Residuals:</b>	1556	<b>BIC:</b>	7806.
<b>Df Model:</b>	3		
<b>Covariance Type:</b>	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
<b>const</b>	-5.7877	0.230	-25.132	0.000	-6.239	-5.336
<b>fertility</b>	6.9858	0.052	134.445	0.000	6.884	7.088
<b>death_rate</b>	-0.1508	0.025	-6.108	0.000	-0.199	-0.102
<b>gdp</b>	0.0361	0.013	2.680	0.007	0.010	0.063

<b>Omnibus:</b>	185.843	<b>Durbin-Watson:</b>	2.082
<b>Prob(Omnibus):</b>	0.000	<b>Jarque-Bera (JB):</b>	641.375
<b>Skew:</b>	0.566	<b>Prob(JB):</b>	5.34e-140
<b>Kurtosis:</b>	5.930	<b>Cond. No.</b>	31.8

### Model 2

<b>Dep. Variable:</b>	psr_log	<b>R-squared:</b>	0.871
<b>Model:</b>	OLS	<b>Adj. R-squared:</b>	0.871
<b>Method:</b>	Least Squares	<b>F-statistic:</b>	3502.
<b>Date:</b>	Thu, 24 Jan 2019	<b>Prob (F-statistic):</b>	0.00
<b>Time:</b>	19:38:45	<b>Log-Likelihood:</b>	-382.34
<b>No. Observations:</b>	1560	<b>AIC:</b>	772.7
<b>Df Residuals:</b>	1556	<b>BIC:</b>	794.1
<b>Df Model:</b>	3		
<b>Covariance Type:</b>	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
<b>const</b>	1.1375	0.024	46.735	0.000	1.090	1.185
<b>fertility</b>	0.5560	0.005	101.252	0.000	0.545	0.567
<b>death_rate</b>	-0.0614	0.003	-23.537	0.000	-0.067	-0.056
<b>gdp</b>	0.0050	0.001	3.510	0.000	0.002	0.008

<b>Omnibus:</b>	40.533	<b>Durbin-Watson:</b>	2.017
<b>Prob(Omnibus):</b>	0.000	<b>Jarque-Bera (JB):</b>	48.042
<b>Skew:</b>	0.332	<b>Prob(JB):</b>	3.70e-11
<b>Kurtosis:</b>	3.546	<b>Cond. No.</b>	31.8

### Model 3

<b>Dep. Variable:</b>	psr	<b>R-squared:</b>	0.930
<b>Model:</b>	OLS	<b>Adj. R-squared:</b>	0.930
<b>Method:</b>	Least Squares	<b>F-statistic:</b>	5159.
<b>Date:</b>	Thu, 24 Jan 2019	<b>Prob (F-statistic):</b>	0.00
<b>Time:</b>	19:38:45	<b>Log-Likelihood:</b>	-3876.2
<b>No. Observations:</b>	1560	<b>AIC:</b>	7762.
<b>Df Residuals:</b>	1555	<b>BIC:</b>	7789.
<b>Df Model:</b>	4		
<b>Covariance Type:</b>	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
<b>const</b>	-8.4058	0.446	-18.834	0.000	-9.281	-7.530
<b>fertility</b>	7.4748	0.114	65.485	0.000	7.251	7.699
<b>gdp</b>	0.0313	0.013	2.329	0.020	0.005	0.058
<b>death_birth_ratio</b>	0.3680	0.078	4.702	0.000	0.214	0.521
<b>death_rate2</b>	-0.0171	0.002	-7.288	0.000	-0.022	-0.012

<b>Omnibus:</b>	188.823	<b>Durbin-Watson:</b>	2.063
<b>Prob(Omnibus):</b>	0.000	<b>Jarque-Bera (JB):</b>	583.764
<b>Skew:</b>	0.610	<b>Prob(JB):</b>	1.73e-127
<b>Kurtosis:</b>	5.737	<b>Cond. No.</b>	677.

### Model 4

<b>Dep. Variable:</b>	psr_log	<b>R-squared:</b>	0.915
<b>Model:</b>	OLS	<b>Adj. R-squared:</b>	0.915
<b>Method:</b>	Least Squares	<b>F-statistic:</b>	5575.
<b>Date:</b>	Thu, 24 Jan 2019	<b>Prob (F-statistic):</b>	0.00
<b>Time:</b>	19:38:46	<b>Log-Likelihood:</b>	-58.003
<b>No. Observations:</b>	1560	<b>AIC:</b>	124.0
<b>Df Residuals:</b>	1556	<b>BIC:</b>	145.4
<b>Df Model:</b>	3		
<b>Covariance Type:</b>	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
<b>const</b>	0.9627	0.031	31.111	0.000	0.902	1.023
<b>fertility_log</b>	1.5230	0.019	81.624	0.000	1.486	1.560
<b>gdp</b>	0.0068	0.001	5.878	0.000	0.005	0.009
<b>death_birth_ratio</b>	-0.0491	0.004	-12.242	0.000	-0.057	-0.041

<b>Omnibus:</b>	12.609	<b>Durbin-Watson:</b>	2.059
<b>Prob(Omnibus):</b>	0.002	<b>Jarque-Bera (JB):</b>	12.791
<b>Skew:</b>	-0.201	<b>Prob(JB):</b>	0.00167
<b>Kurtosis:</b>	3.188	<b>Cond. No.</b>	37.1