Problem Background:

- Suppose a hedge fund owns **\$1,000,000** of stock and used *\$50,000* of its own capital and *\$950,000* in borrowed money for the purchase.
- Suppose that if the value of the stock falls below \$950,000 at the end of any trading day, then the hedge fund will sell all the stock and repay the loan.
- This will wipe out its \$50,000 investment.

The hedge fund is said to be leveraged 20:1 since its position is 220 times the amount of its own capital invested.

Suppose that the daily log returns on the stock have a mean of 0.05/year and a standard deviation of 0.23/year.

These can be converted to rates per trading day by dividing by 253 and sqrt(253), respectively.

Initialization

```
# number of iterations in the sim.
niter <- 1e5
seed.capital <- 5e4
initial.investment <- log(1e6)
profit.threshold <- log(1.1e6)</pre>
loss.threshold <- log(9.5e5)
target.profit <- 1e5</pre>
ret.avg <- 0.05
ret.sd <- 0.23
market.open <- 253
simulate_market <- function(days) {</pre>
  # generate random returns for N days
  r <- rnorm(days, mean = ret.avg / market.open,
            sd = ret.sd / sqrt(market.open))
  # return the final log price after N days.
  cumsum(r)
}
```

Problem 4

What is the probability that the value of the stock will be below \$950,000 at the close of at least one of the next 45 trading days?

```
# reproducible
set.seed(2009)

# setup storage
outcomes <- list(below = rep(0, niter))

# Simulation: Probability dips below $950,000.
for (i in 1:niter) {

# simulate 45 trading days.
   logPrice = initial.investment + simulate_market(45)

# miniumum price over next 45 days
   minlogP = min(logPrice)

outcomes$below[i] = as.numeric(minlogP < loss.threshold)
}</pre>
```

Probability the value of the stock is below \$950,000 at least one of next 45 sessions: 50.99%

Suppose the hedge fund will:

- sell the stock for a profit of at least \$100,000 if the value of the stock rises to at least \$1,100,000 at the end of one of the first 100 trading days,
- sell it for a loss if the value falls below \$950,000 at the end of one of the first 100 trading days,
- or sell it (for "FMV") after 100 trading days if the closing price has stayed between \$950,000 and \$1,100,000.

```
# reproducible
set.seed(2009)
outcomes <- list(above = rep(0, niter),
                 below = rep(0, niter),
                 middle = rep(0, niter),
                 pnl = rep(0, niter),
                 ret = rep(0, niter))
for (i in 1:niter) {
  # simulate 100 trading days.
  logPrice = initial.investment + simulate_market(100)
  suppressWarnings({
    # ignore Inf returned if condition not meet.
    profit.day <- min(which(logPrice >= profit.threshold))
    loss.day <- min(which(logPrice <= loss.threshold))</pre>
  })
  is.market <- profit.day == Inf && loss.day == Inf
  # What was the exit condition of the position, hince the final price of the stock?
  days.open <- ifelse(is.market, length(logPrice),</pre>
                       min(profit.day, loss.day))
  outcomes$above[i] <- min(profit.day) < min(loss.day)</pre>
  outcomes$middle[i] <- is.market</pre>
  outcomes$below[i] <- min(loss.day) < min(profit.day)</pre>
  # p&l = ending value - initial investment
  pnl <- exp(logPrice[days.open]) - exp(initial.investment)</pre>
  # market pnl = use FMV, otherwise cap p/l
  outcomes$pnl[i] <- pnl
```

```
# Calculate return (time-weighted)
outcomes$ret[i] <- (outcomes$pnl[i] / seed.capital) / days.open
}
# Verify we captured every simulation outcome.
stopifnot(sum(outcomes$above) + sum(outcomes$below) + sum(outcomes$middle) == niter)</pre>
```

Problem 5

What is the probability that the hedge fund (strategy) will make a profit of at least \$100,000?

```
prob.profit <- sum(outcomes$above) / length(outcomes$pnl)
p5 <- round(mean(prob.profit), 4) * 100</pre>
```

Probability the hedge fund (strategy) returns over \$100,000 in profit: 38.78%

Problem 6

What is the probability that the hedge fund (strategy) will suffer a loss?

```
prob.loss <- sum(outcomes$below) / length(outcomes$below)

p6 <- round(mean(prob.loss), 4) * 100</pre>
```

Probability the hedge fund (strategy) returns a loss: 58.84%

Problem 7

What is the expected profit from this trading strategy?

```
p7 <- currency(mean(outcomes$pn1))
```

Expected profit/loss of the hedge fund (strategy): \$8,910.54

Problem 8

What is the expected return?

```
p8 <- round(mean(outcomes$ret), 5) * 100
```

Expected (time-weighted) return of the hedge fund (strategy): -2.273%