

Math 415 ADG

Name: *Solution*

Quiz # 9

April 18, 2014

No notes, electronic devices, or interpersonal communication allowed. **Show work to get credit.** Use the methods from this class.

Find the eigenvalues and (bases for) the corresponding eigenspaces of the matrix $\underbrace{\begin{bmatrix} 1 & 1 \\ -2 & 4 \end{bmatrix}}_A$.

$$\det(A - \lambda I) = \det \begin{pmatrix} 1-\lambda & 1 \\ -2 & 4-\lambda \end{pmatrix}$$

$$= (1-\lambda)(4-\lambda) + 2 = \lambda^2 - 5\lambda + 6 = (\lambda-2)(\lambda-3)$$

so e'vals are 2 & 3.

$$\begin{aligned} E_2 &= \text{Nul}(A - 2I) = \text{Nul} \begin{pmatrix} -1 & 1 \\ -2 & 2 \end{pmatrix} \xrightarrow{R_2 = 2R_1} \text{Nul} \begin{pmatrix} -1 & 1 \\ 0 & 0 \end{pmatrix} = \text{Span} \left\{ \begin{bmatrix} 1 \\ 1 \end{bmatrix} \right\} \\ E_3 &= \text{Nul}(A - 3I) = \text{Nul} \begin{pmatrix} -2 & 1 \\ -2 & 1 \end{pmatrix} \xrightarrow{R_2 = R_1} \text{Nul} \begin{pmatrix} -2 & 1 \\ 0 & 0 \end{pmatrix} = \text{Span} \left\{ \begin{bmatrix} 1 \\ 2 \end{bmatrix} \right\} \end{aligned} \quad \text{bases}$$