```
t.test(m$y1,m$y2,paired=TRUE)
        Paired t-test
data: m$y1 and m$y2
t = 0.55539, df = 944, p-value = 0.5788
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval: -0.06434363 0.11513728
sample estimates:
mean of the differences
              0.02539683
> t.test(m$y1,m$y2)
        Welch Two Sample t-test
       m$y1 and m$y2
t = 0.38647, df = 1887.5, p-value = 0.6992
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -0.1034859 0.1542796
sample estimates:
mean of x mean of
 6.304762 6.279365
> fit=lm(y~tm+ap+ta+tx+c,d)
> summary(fit)
call:
lm(formula = y \sim tm + ap + ta + tx + c, data = d)
Residuals:
                     Median
     Min
                1Q
                                            Max
-2.91151 -0.29215 -0.02047 0.25583
                                        2.99790
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)
              0.095831
                          0.118748
                                      0.807
                                                0.420
              0.019482
                          0.016694
                                      1.167
                                                0.243
                                               <2e-16 ***
                          0.013197
              0.138149
                                    10.468
ap
                                              <2e-16 ***
                                    41.740
              0.566629
                          0.013575
ta
                                     20.944
              0.271685
                          0.012972
                                              <2e-16 ***
tx
             -0.001603
                          0.018309
                                     -0.088
                                                0.930
C
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.5959 on 1884 degrees of freedom
Multiple R-squared: 0.8263, Adjusted R-squared: 0.8259
F-statistic: 1793 on 5 and 1884 DF, p-value: < 2.2e-16
> AIC(fit)
[1] 3414.845
> anova(lm(y~b+a,d))
Analysis of Variance Table
Response: y
             Df Sum Sq Mean Sq F value
                                            Pr(>F)
                         0.391 0.1989
                  1.2
b
                                            0.8972
                        37.208 18.9114 2.936e-15 ***
                 148.8
Residuals 1882 3702.8
                          1.967
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
> anova(lm(y~b+a+dc,d))
```

```
Analysis of Variance Table
Response: y
               Df Sum Sq Mean Sq F value
                                                  Pr(>F)
                            0.391 0.2005 0.896077
37.208 19.0661 2.204e-15 ***
5.706 2.9241 0.003017 **
                     1.2
b
                   \substack{148.8\\45.7}
                4
a
dc
Residuals 1874 3657.1
                             1.952
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
> t.test(a1$y,a2$y,alternative="less")
         Welch Two Sample t-test
data: a1y and a2y t = -2.3469, df = 1149.2, p-value = 0.00955 alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
          -Inf -0.05633864
sample estimates:
mean of x mean of y
 6.052478 6.241176
> t.test(a2$y,a3$y,alternative="less")
         Welch Two Sample t-test
data: a2$y and a3$y
t = 0.84219, df = 208.59, p-value = 0.7997
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
-Inf 0.3388753
sample estimates:
mean of x mean of y
 6.241176 6.126761
> t.test(a3$y,a4$y,alternative="less")
         Welch Two Sample t-test
data: a3$y and a4$y
t = -2.5154, df = 266.19, p-value = 0.006239
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
-Inf -0.1271618
sample estimates:
mean of x mean of y
 6.126761 6.496622
> t.test(a4$y,a5$y,alternative="less")
         Welch Two Sample t-test
data: a4\$y and a5\$y t = -3.2965, df = 536.93, p-value = 0.0005219 alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
         -Inf -0.1970673
sample estimates:
mean of x mean of y
 6.496622 6.890625
> fit2=lm(y~b+a+dc,d)
> summary(fit2)
```

```
lm(formula = y \sim b + a + dc, data = d)
Residuals:
    Min
              1Q
                  Median
-4.7757 -0.9331
                          0.9543
                                   3.1774
                  0.0133
Coefficients: (1 not defined because of singularities)
              Estimate Std. Error t value Pr(>|t|)
                                             < 2e-16 ***
(Intercept)
              5.720356
                         0.131783
                                    43.407
bbrand b
             -0.002381
                         0.096400
                                    -0.025 0.980298
              0.146024
bbrand c
                         0.162598
                                     0.898 0.369266
bbrand d
              0.102214
                         0.162598
                                     0.629 0.529667
                                     2.607 0.009199 **
aage2
              0.213963
                         0.082064
                                     0.885 0.376116
aage3
              0.115235
                         0.130167
                                     5.110 3.55e-07 ***
              0.503513
                         0.098537
aage4
                                            < 2e-16 ***
aage5
              0.887742
                         0.103943
                                     8.541
                                     1.192 0.233554
              0.169283
                         0.142059
dcday 10
dcday 2
              0.169946
                         0.160588
                                     1.058 0.290068
dcday 3
              0.303225
                         0.161135
                                     1.882 0.060017
dcday 4
                                     2.161 0.030842 *
              0.326283
                         0.151006
dcday 5
              0.522798
                         0.150095
                                     3.483 0.000507 ***
dcday 6
              0.184160
                         0.136251
                                     1.352 0.176657
                                      1.687 0.091712
dcday 7
              0.223093
                         0.132219
                                      3.165 0.001573 **
dcday 8
              0.442943
                         0.139932
dcday 9
                    NA
                                NA
                                         NA
                                                  NA
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 1.397 on 1874 degrees of freedom
Multiple R-squared: 0.05078, Adjusted R-squared: 0.04319 F-statistic: 6.684 on 15 and 1874 DF, p-value: 3.111e-14
> a=lmer(formula = y \sim b + a + (1 | d), data = d)
 summary(a)
Linear mixed model fit by REML ['lmerMod']
Formula: y \sim b + a + (1 | d)
   Data: d
REML criterion at convergence: 6653.9
Scaled residuals:
              1Q Median
    Min
                                       Max
-3.4438 -0.6862 -0.0141 0.6818
                                  2.2227
Random effects:
                       Variance Std.Dev.
 Groups
          Name
 d
           (Intercept) 0.02042 0.1429
                                 1.3970
 Residual
                       1.95156
Number of obs: 1890, groups: d, 10
Fixed effects:
              Estimate Std. Error t value
(Intercept)
              5.999422
                         0.105101
                                      57.08
bbrand b
             -0.002381
                          0.096401
                                      -0.02
bbrand c
              0.077628
                         0.129179
                                       0.60
bbrand d
              0.033818
                         0.129179
                                       0.26
              0.205903
aage2
                         0.081946
                                       2.51
                         0.129779
                                      0.80
aage3
              0.103431
aage4
              0.485163
                         0.098210
                                       4.94
                                       8.43
              0.873768
aage5
                         0.103710
```