

557_Project_2BS

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3/15/2017

No Command Lines Ever. Whoa

What the Factor Variables look like

What the Continuous Variables look like

Call:

```
lm(formula = class ~ ., data = seismic)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.57549	-0.07778	-0.03812	-0.00950	1.03232

Coefficients:

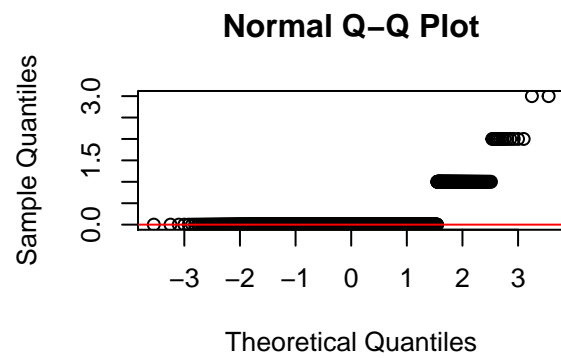
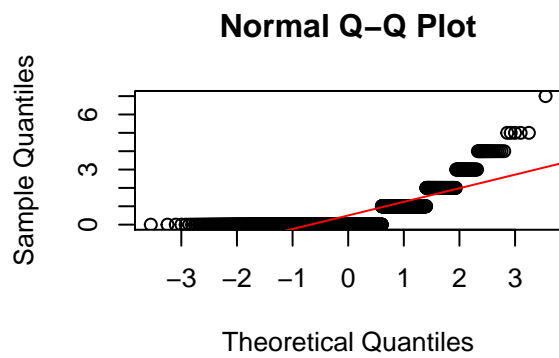
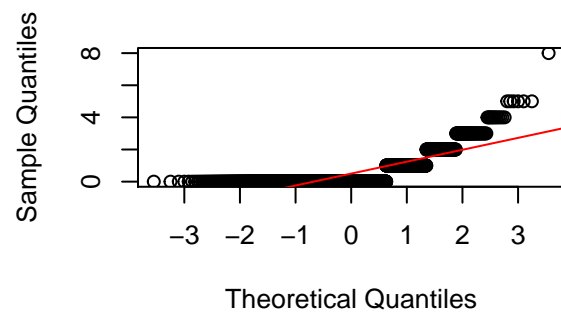
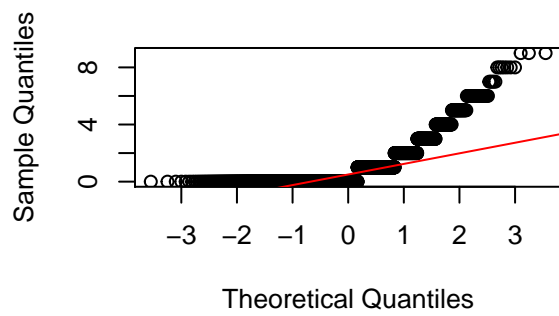
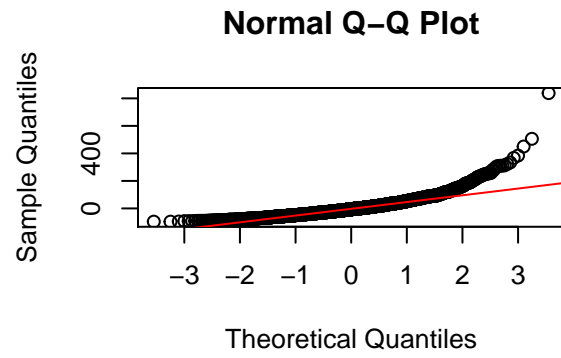
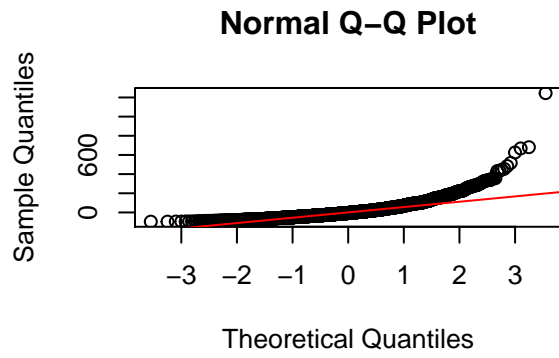
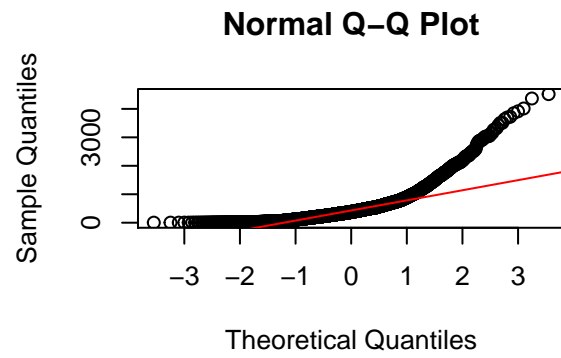
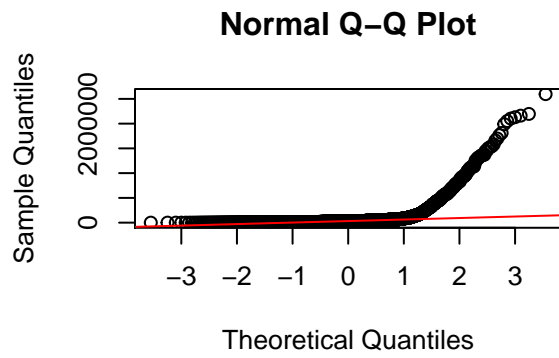
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-2.393e-02	2.565e-02	-0.933	0.35090
seismic	1.869e-02	1.076e-02	1.737	0.08254 .
seismoacoustic	2.610e-03	1.002e-02	0.260	0.79457
shift	6.190e-04	1.157e-02	0.054	0.95732
genergy	-8.698e-08	3.459e-08	-2.514	0.01199 *
gpuls	1.019e-04	1.670e-05	6.102	1.2e-09 ***
gdenergy	-6.943e-05	1.006e-04	-0.690	0.49009
gdpuls	-1.942e-04	1.368e-04	-1.420	0.15583
ghazard	-1.394e-02	1.608e-02	-0.867	0.38618
nbumps	4.674e-01	1.680e-01	2.783	0.00543 **
nbumps2	-4.282e-01	1.682e-01	-2.546	0.01096 *
nbumps3	-4.260e-01	1.681e-01	-2.535	0.01131 *
nbumps4	-4.622e-01	1.708e-01	-2.706	0.00685 **
nbumps5	-2.963e-01	2.332e-01	-1.270	0.20408
energy	2.536e-07	2.395e-06	0.106	0.91568
maxenergy	-1.054e-06	2.333e-06	-0.452	0.65164

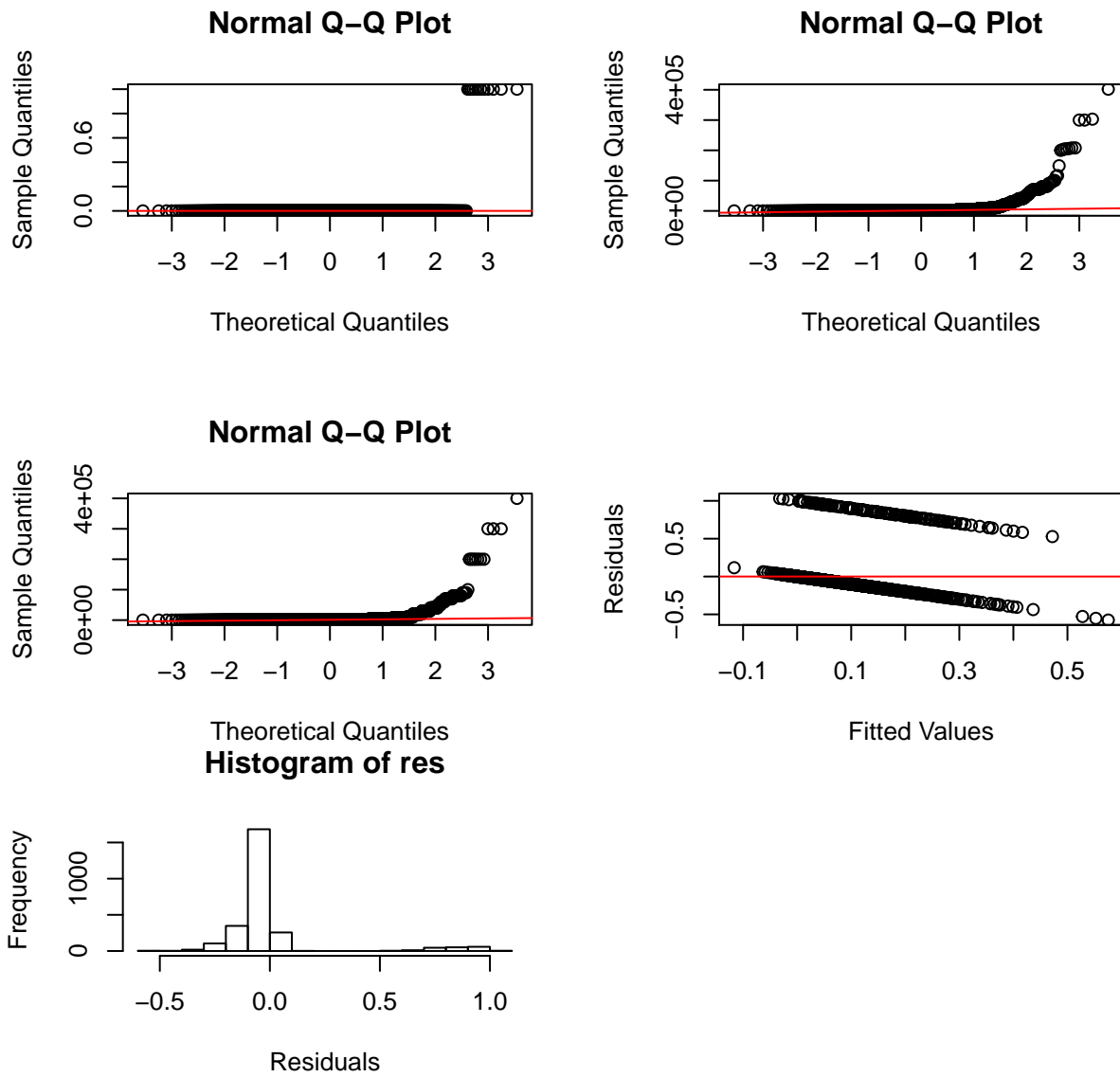
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.2371 on 2568 degrees of freedom

Multiple R-squared: 0.09128, Adjusted R-squared: 0.08597

F-statistic: 17.2 on 15 and 2568 DF, p-value: < 2.2e-16





Lots of multicollinearity to worry about during variable selection

```
vif(fit)
```

```
##      seismic seismoacoustic      shift      genergy      gpuls
##      1.209814      1.286183      1.411216      2.889651      4.057018
##      gdenergy      gdpuls      ghazard      nbumps      nbumps2
##      3.000282      3.430524      1.395598      2414.689538      798.964152
##      nbumps3      nbumps4      nbumps5      energy      maxenergy
##      769.131960      104.402690      11.562237      110.283444      93.762895
```

```
sqrt(vif(fit)) > 2
```

```
##      seismic seismoacoustic      shift      genergy      gpuls
##      FALSE      FALSE      FALSE      FALSE      TRUE
```

##	gdenergy	gdpuls	ghazard	nbumps	nbumps2
##	FALSE	FALSE	FALSE	TRUE	TRUE
##	nbumps3	nbumps4	nbumps5	energy	maxenergy
##	TRUE	TRUE	TRUE	TRUE	TRUE

Correlation of the Variables

Separating into Test and Training Sets

```
##-----
## Setting up Test and Training Sets
##-----

n <- dim(seismic)[1]
p <- dim(seismic)[2]

set.seed(2016)
test <- sample(n, round(n/4))
train <- (1:n)[-test]
seismic.train <- seismic[train,]
seismic.test <- seismic[test,]

dim(seismic)
```

```
[1] 2584  16
```

```
dim(seismic.train)
```

```
[1] 1938  16
```

```
dim(seismic.test)
```

```
[1] 646  16
```

```
#View(seismic.train)
#View(seismic.test)
```

Linear regression of an indicator matrix

```
##-----
## Linear regression of indicator matrix
##-----

responseY <- seismic$class
predictorX <- seismic[,16]
```

```

# Following Le Bao's code
class1 <- which(responseY==1)
class0 <- which(responseY==0)
Y <- matrix(data = rep(0,length(responseY)*2),nrow = length(responseY))
Y[class0,1] <- 1
Y[class1,2] <- 1

betaHat <- solve(t(as.matrix(predictorX))%*%as.matrix(predictorX))%*%t(as.matrix(predictorX))%*%Y
Y1 <- as.matrix(predictorX)%*%betaHat[,1]
Y2 <- as.matrix(predictorX)%*%betaHat[,2]

pred.mx <- cbind(Y1,Y2)
pred <- rep(NA,length(Y1))
for(i in 1:length(Y1)){
  pred[i] <- which.max(pred.mx[i,]) - 1
}

# Confusion matrix
mx <- cbind(pred,responseY,pred-responseY)

confusion <- matrix(rep(NA,4), nrow = 2)
correct <- which(mx[,3] == 0)
confusion[1,1] <- length(which(mx[correct,1] == 0))
confusion[2,2] <- length(which(mx[correct,1] == 1))
confusion[1,2] <- length(which(mx[,3] == -1))
confusion[2,1] <- length(which(mx[,3] == 1))
confusion

##      [,1] [,2]
## [1,] 2411 169
## [2,]    3    1

sensitivity <- confusion[2,2]/sum(confusion[,2])
specificity <- confusion[1,1]/sum(confusion[,1])
error.rate <- (confusion[1,2] + confusion[2,1])/sum(confusion)
c(sensitivity, specificity, error.rate)

## [1] 0.005882353 0.998757249 0.066563467

```

Linear Discriminant Analysis on full model

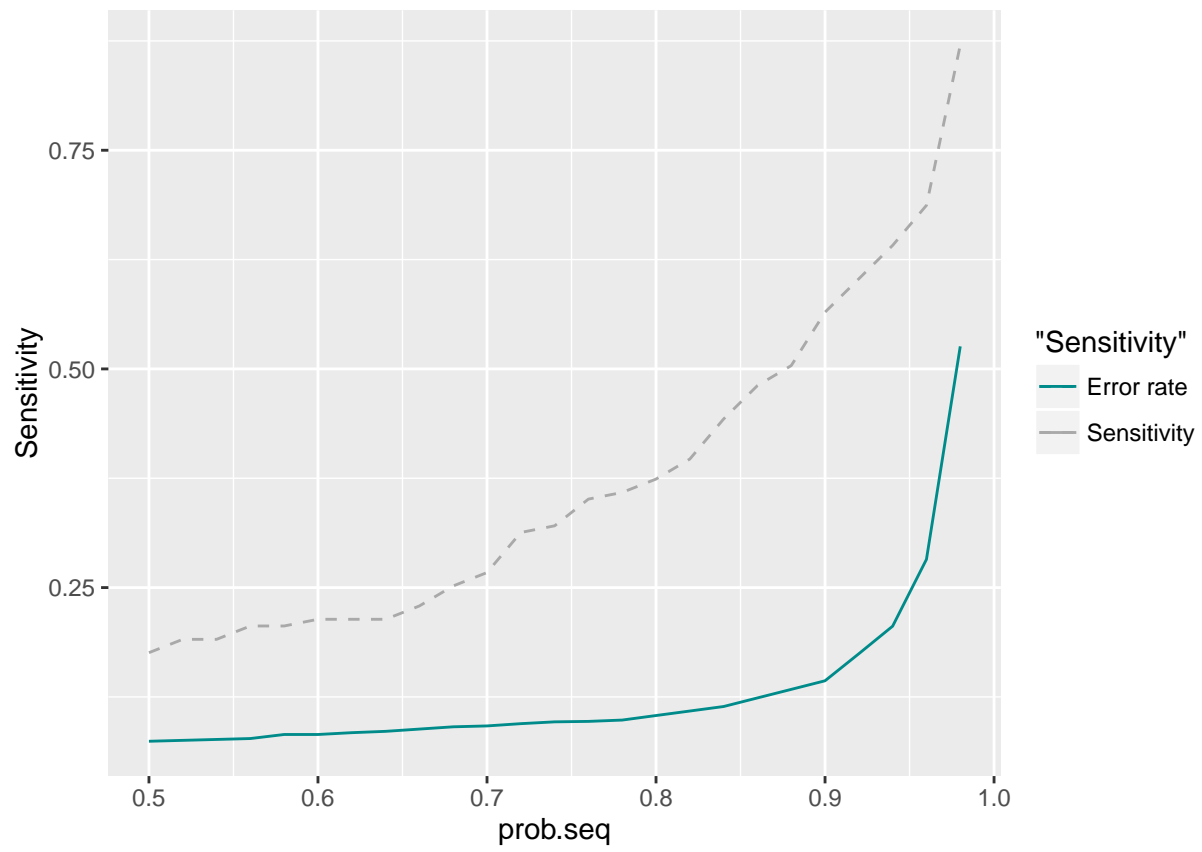
```

lda.class.train    0    1
                   0 1771 108
                   1   36  23

[1] 0.1755725

[1] 0.9800775

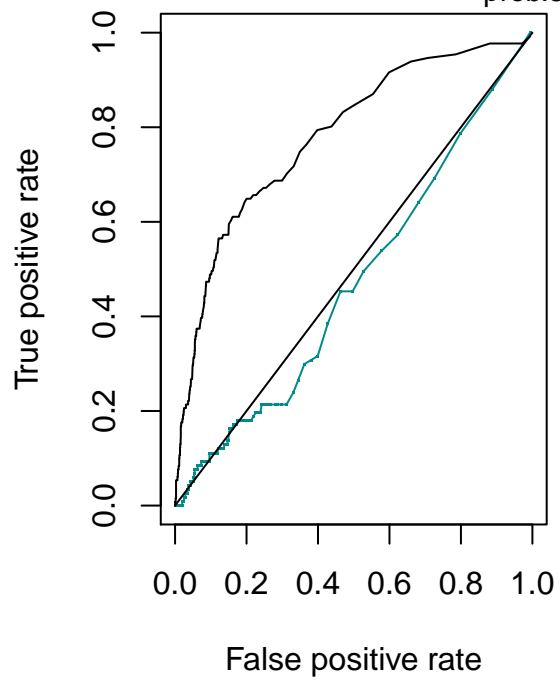
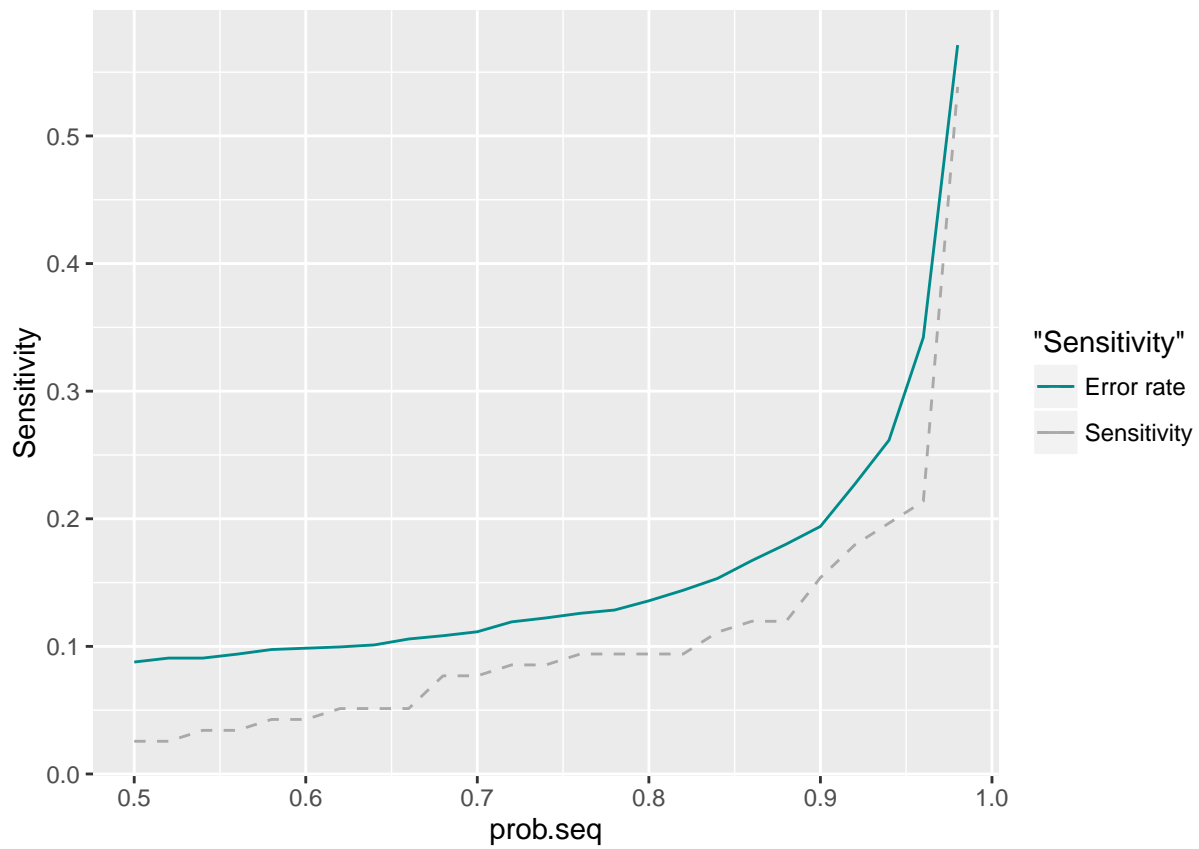
```



```
lda.class.test  0   1
                0 591 34
                1  16  5
```

```
[1] 0.1282051
```

```
[1] 0.9736409
```



Quadratic Discriminant Analysis -INCOMPLETE

```
##-----  
## Fit QDA model  
##-----  
  
## Currently, can't perform QDA. This is probably due to multicollinearity in the model  
## (can't invert covariance matrix) but should be possible after variable selection  
  
#qda.fit <- qda(class~., data = seismic, subset = train)
```

Regularized Discriminant Analysis -INCOMPLETE

```
##-----  
## Fit RDA model  
##-----  
  
## Currently, can't perform RDA. This is probably due to multicollinearity in the model  
## (can't invert covariance matrix) but should be possible after variable selection  
  
par(mfrow=c(1,2))  
  
rda.fit <- rda(class~., data=seismic.train)  
rda.fit
```

```
## Call:  
## rda(formula = class ~ ., data = seismic.train)  
##  
## Regularization parameters:  
##      gamma      lambda  
## 0.005757679 0.291158452  
##  
## Prior probabilities of groups:  
##      0      1  
## 0.93240454 0.06759546  
##  
## Misclassification rate:  
##      apparent: 7.637 %  
## cross-validated: 7.69 %
```

```
##  
# Using model on TRAIN Data  
##  
rda.pred=predict(rda.fit, seismic.train, type="response")  
  
rda.class.train <- rda.pred$class  
  
posterior.train <- rda.pred$posterior  
truth.train <- seismic.train$class
```



```

## Confusion matrix
rda.train.confusion <- table(rda.class.train,seismic.train$class)
rda.train.sensitivity <- rda.train.confusion[2,2]/sum(rda.train.confusion[,2])
rda.train.specificity <- rda.train.confusion[1,1]/sum(rda.train.confusion[,1])

# Sensitivity, Specificity and Confusion
rda.train.confusion

##
## rda.class.train      0      1
##                0 1785   126
##                1   22     5

rda.train.sensitivity

## [1] 0.03816794

rda.train.specificity

## [1] 0.9878251

mod.posterior <- function(posterior, truth, prob, dimension = length(train)){
  idx0 <- which(posterior[,1] > prob)
  idx1 <- (1:dimension)[-idx0]

  prediction <- rep(NA,dimension)
  prediction[idx0] = 0
  prediction[idx1] = 1

  mx <- cbind(prediction,truth,prediction-truth)

  rda.train.confusion <- matrix(rep(NA,4), nrow = 2)
  correct <- which(mx[,3] == 0)
  rda.train.confusion[1,1] <- length(which(mx[correct,1] == 0))
  rda.train.confusion[2,2] <- length(which(mx[correct,1] == 1))
  rda.train.confusion[1,2] <- length(which(mx[,3] == -1))
  rda.train.confusion[2,1] <- length(which(mx[,3] == 1))

  sensitivity <- rda.train.confusion[2,2]/sum(rda.train.confusion[,2])
  specificity <- rda.train.confusion[1,1]/sum(rda.train.confusion[,1])
  error.rate <- (rda.train.confusion[1,2] + rda.train.confusion[2,1])/sum(rda.train.confusion)
  c(sensitivity, specificity, error.rate)
}

posterior.train <- rda.pred$posterior
truth.train <- seismic.train$class

prob.seq <- seq(.5,.98,by = .02)
output.train <- matrix(rep(NA,length(prob.seq)*2), ncol = 2)
colnames(output.train) <- c("Sensitivity", "Error.rate")

```

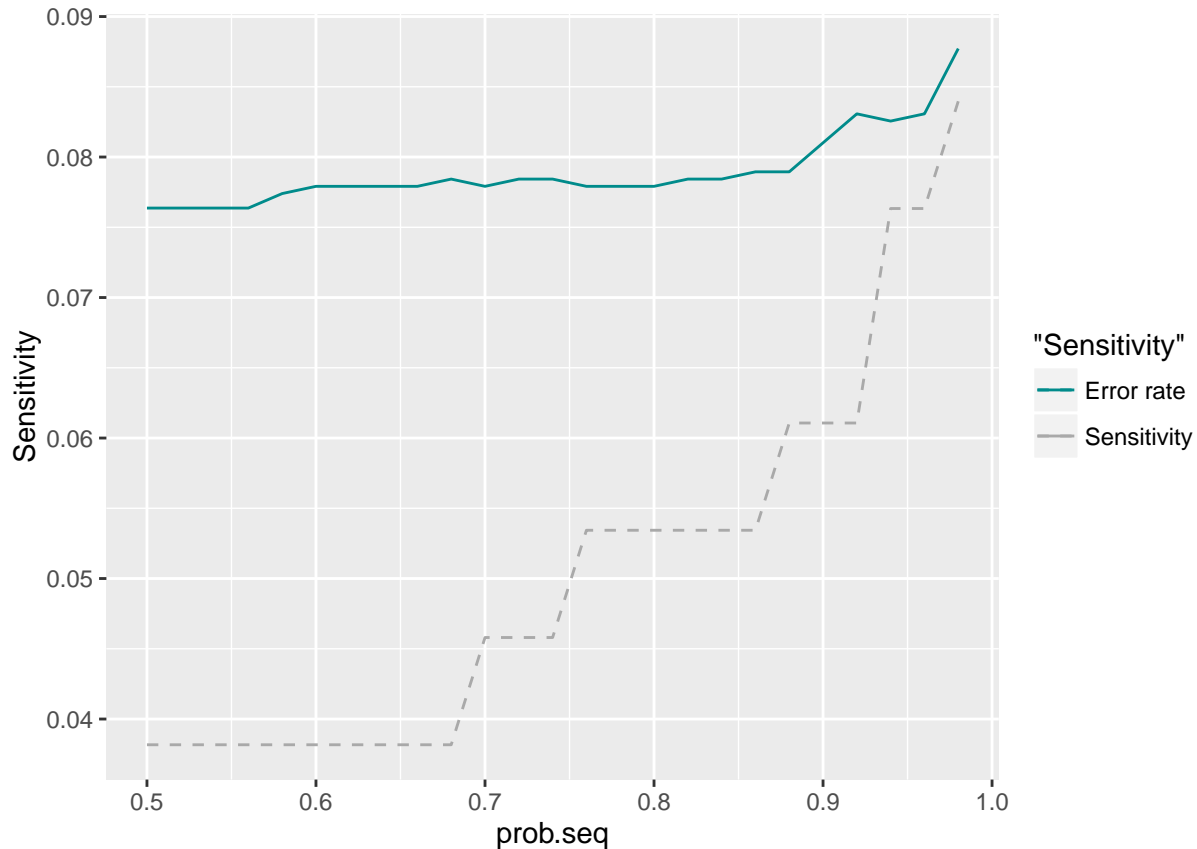
```

for(i in 1:length(prob.seq)){
  output.train[i,] <- mod.posterior(posterior.train,truth.train,prob.seq[i])[c(1,3)]
}

df1 <- as.data.frame(cbind(prob.seq,output.train))

ggplot(data = df1, aes(x=prob.seq)) +
  geom_line(aes(y = Sensitivity, colour = "Sensitivity"), linetype = "dashed") +
  geom_line(aes(y = Error.rate, colour = "Error rate")) +
  scale_colour_manual(values=c("dark cyan", "dark grey"))

```



```

##
# Using model on TEST Data
##
rda.pred=predict(rda.fit, seismic.test, type="response")

rda.class.test <- rda.pred$class

## Confusion matrix
rda.test.confusion <- table(rda.class.test,seismic.test$class)
rda.test.sensitivity <- rda.test.confusion[2,2]/sum(rda.test.confusion[,2])
rda.test.specificity <- rda.test.confusion[1,1]/sum(rda.test.confusion[,1])

mod.posterior <- function(posterior, truth, prob, dimension = length(train)){
  idx0 <- which(posterior[,1] > prob)
  idx1 <- (1:dimension)[-idx0]
}

```

```

prediction <- rep(NA,dimension)
prediction[idx0] = 0
prediction[idx1] = 1

mx <- cbind(prediction,truth,prediction-truth)

rda.test.confusion <- matrix(rep(NA,4), nrow = 2)
correct <- which(mx[,3] == 0)
rda.test.confusion[1,1] <- length(which(mx[correct,1] == 0))
rda.test.confusion[2,2] <- length(which(mx[correct,1] == 1))
rda.test.confusion[1,2] <- length(which(mx[,3] == -1))
rda.test.confusion[2,1] <- length(which(mx[,3] == 1))

sensitivity <- rda.test.confusion[2,2]/sum(rda.test.confusion[,2])
specificity <- rda.test.confusion[1,1]/sum(rda.test.confusion[,1])
error.rate <- (rda.test.confusion[1,2] + rda.test.confusion[2,1])/sum(rda.test.confusion)
c(sensitivity, specificity, error.rate)
}

posterior.train <- rda.pred$posterior
truth.train <- seismic.train$class

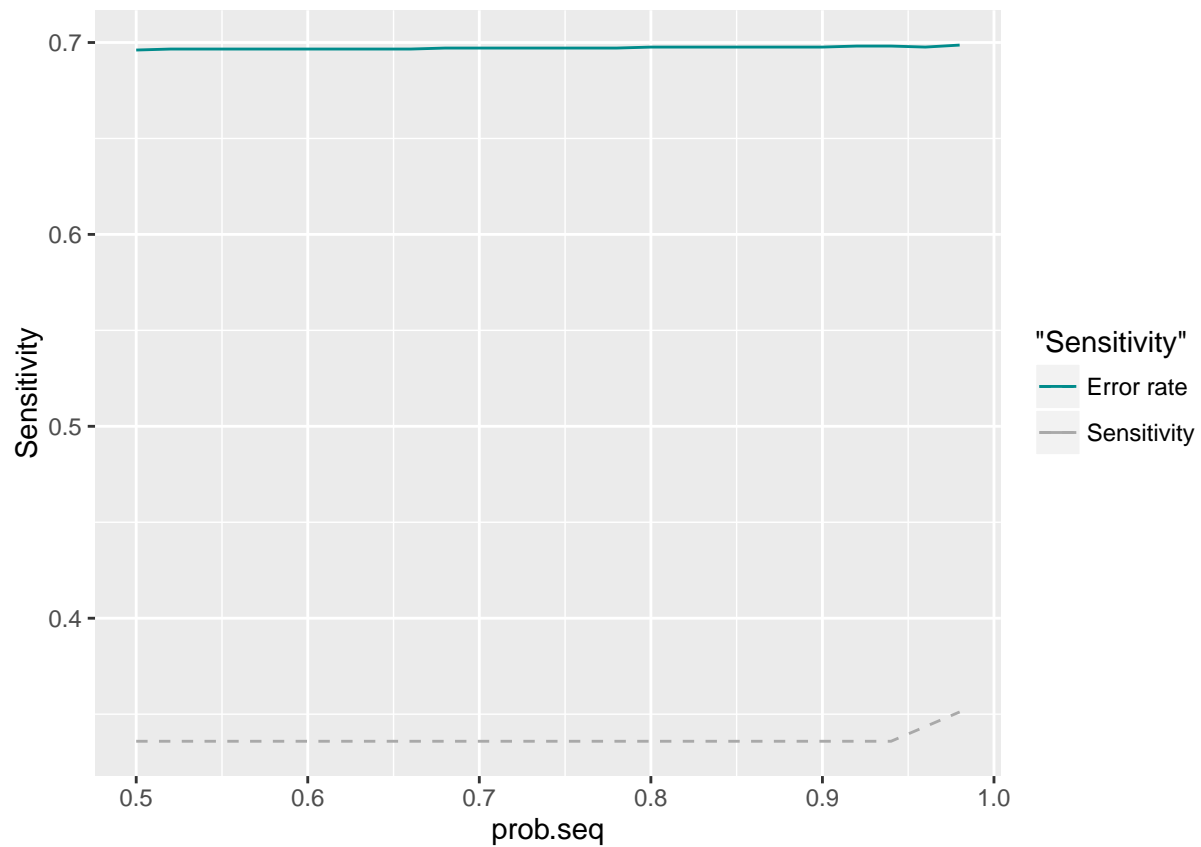
prob.seq <- seq(.5,.98,by = .02)
output.train <- matrix(rep(NA,length(prob.seq)*2), ncol = 2)
colnames(output.train) <- c("Sensitivity", "Error.rate")

for(i in 1:length(prob.seq)){
  output.train[i,] <- mod.posterior(posterior.train,truth.train,prob.seq[i])[c(1,3)]
}

df1 <- as.data.frame(cbind(prob.seq,output.train))

ggplot(data = df1, aes(x=prob.seq)) +
  geom_line(aes(y = Sensitivity, colour = "Sensitivity"), linetype = "dashed") +
  geom_line(aes(y = Error.rate, colour = "Error rate")) +
  scale_colour_manual(values=c("dark cyan", "dark grey"))

```



```
# Sensitivity, Specificity and Confusion
rda.test.confusion
```

```
##
## rda.class.test    0    1
##                0 593  39
##                1  14   0
```

```
rda.test.sensitivity
```

```
## [1] 0
```

```
rda.test.specificity
```

```
## [1] 0.9769357
```

```
sum(rda.pred$posterior[,1]>=.5)
```

```
## [1] 632
```

```
sum(rda.pred$posterior[,1]<.5)
```

```
## [1] 14
```

Logistic Regression.

Call:

```
glm(formula = class ~ ., family = binomial, data = seismic.train)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.8471	-0.3860	-0.2851	-0.1566	3.0825

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-6.343e+00	7.721e-01	-8.215	< 2e-16 ***
seismic	4.808e-01	2.111e-01	2.278	0.022727 *
seismoacoustic	2.159e-01	1.993e-01	1.084	0.278524
shift	1.179e+00	3.573e-01	3.301	0.000965 ***
genergy	-2.471e-07	5.044e-07	-0.490	0.624239
gpuls	7.095e-04	2.474e-04	2.868	0.004136 **
gdenrgy	-1.904e-04	2.177e-03	-0.087	0.930292
gdpuls	-2.997e-03	3.093e-03	-0.969	0.332500
ghazard	-2.335e-01	3.509e-01	-0.666	0.505671
nbumps	1.807e+01	5.354e+02	0.034	0.973080
nbumps2	-1.773e+01	5.354e+02	-0.033	0.973590
nbumps3	-1.771e+01	5.354e+02	-0.033	0.973611
nbumps4	-1.806e+01	5.354e+02	-0.034	0.973097
nbumps5	-1.604e+01	5.354e+02	-0.030	0.976095
energy	1.622e-06	4.033e-05	0.040	0.967929
maxenergy	-7.101e-06	3.969e-05	-0.179	0.858012

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 958.82 on 1937 degrees of freedom
Residual deviance: 813.40 on 1922 degrees of freedom
AIC: 845.4

Number of Fisher Scoring iterations: 12

[1] 0.9329205

glm.pred	0	1
	0 1802	125
	1 5	6

[1] 0.04580153

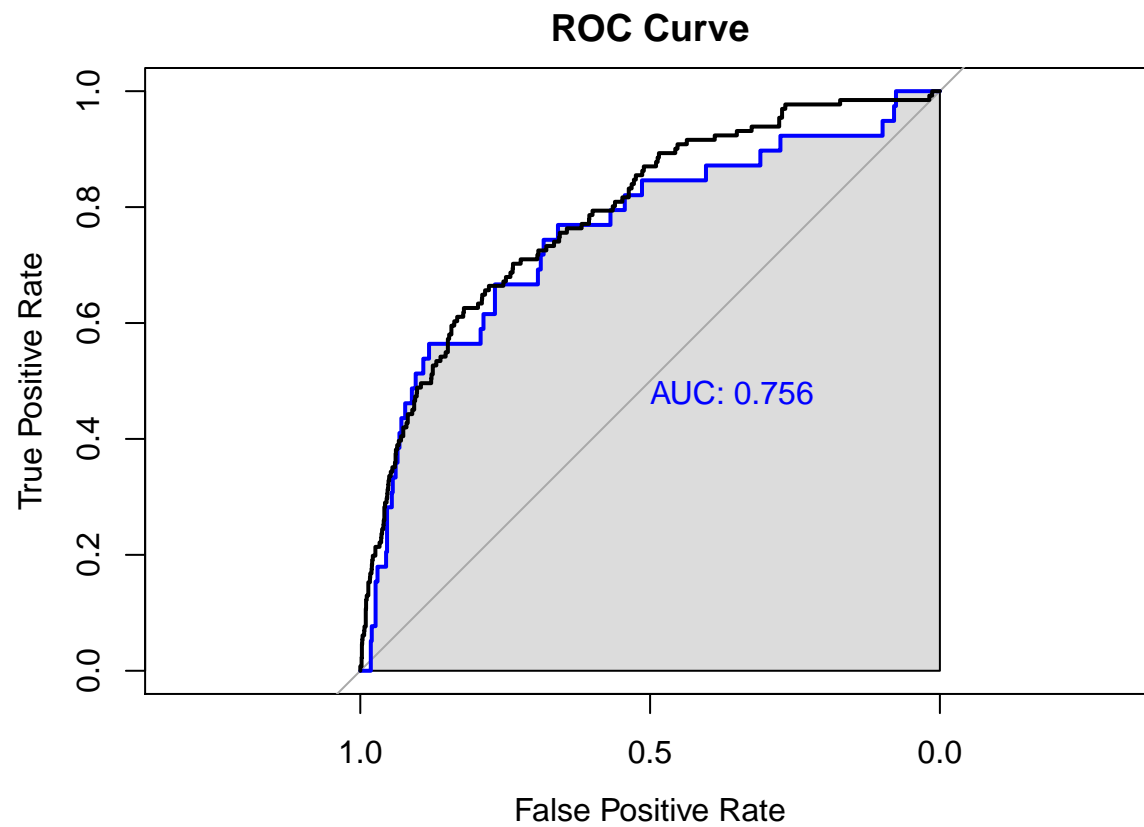
[1] 0.997233

[1] 0.9349845

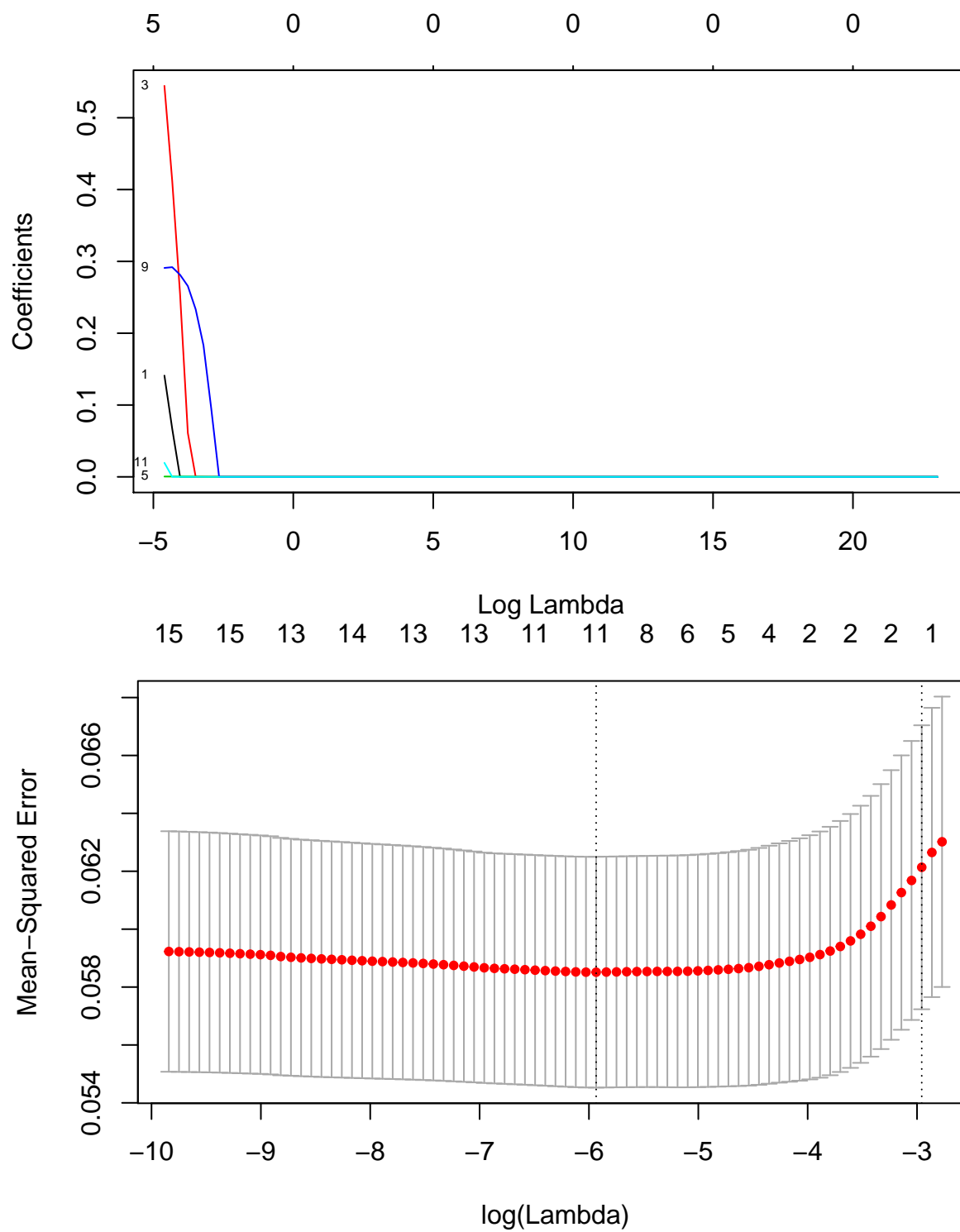
```
glm.pred  0  1
          0 604 39
          1   3  0
```

```
[1] 0
```

```
[1] 0.9950577
```



Variable Selection-LASSO



[1] 8.670049

Variables selected through LASSO

```
(Intercept) seismic  shift gpuls  nbumps
1      -0.00814  0.0088 0.00798 5e-05 0.03118
```

Principal Component Analysis from the Book - INCOMPLETE

```
Data:  X dimension: 2584 15
       Y dimension: 2584 1
Fit method: svdpc
Number of components considered: 15
```

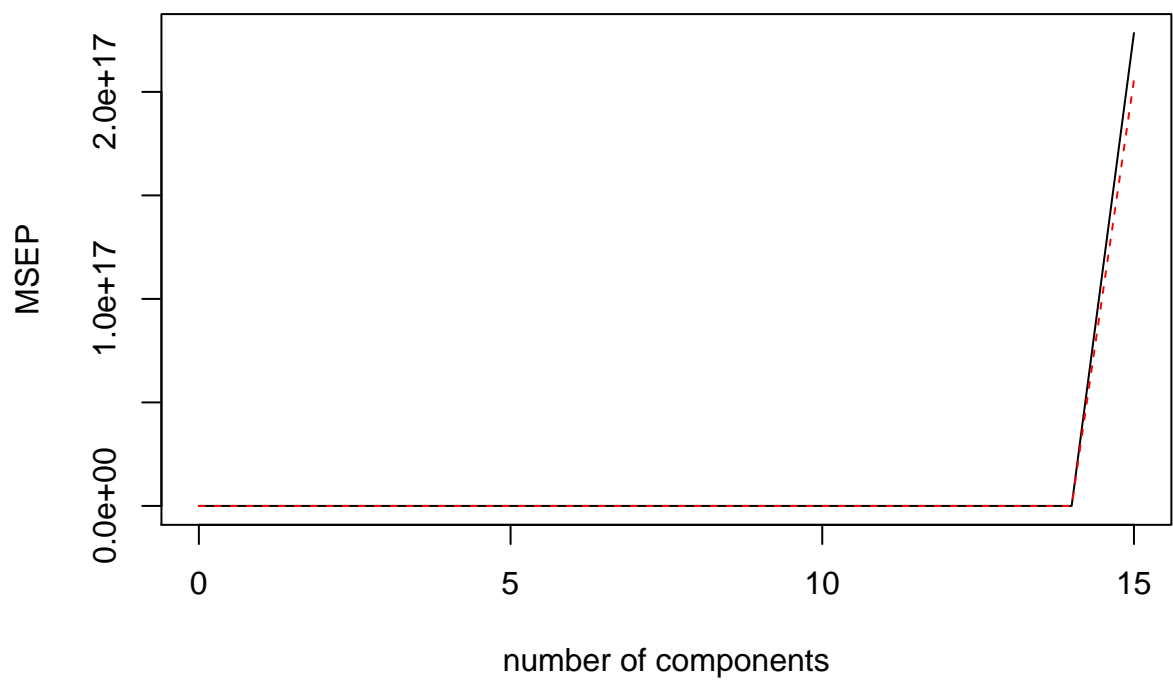
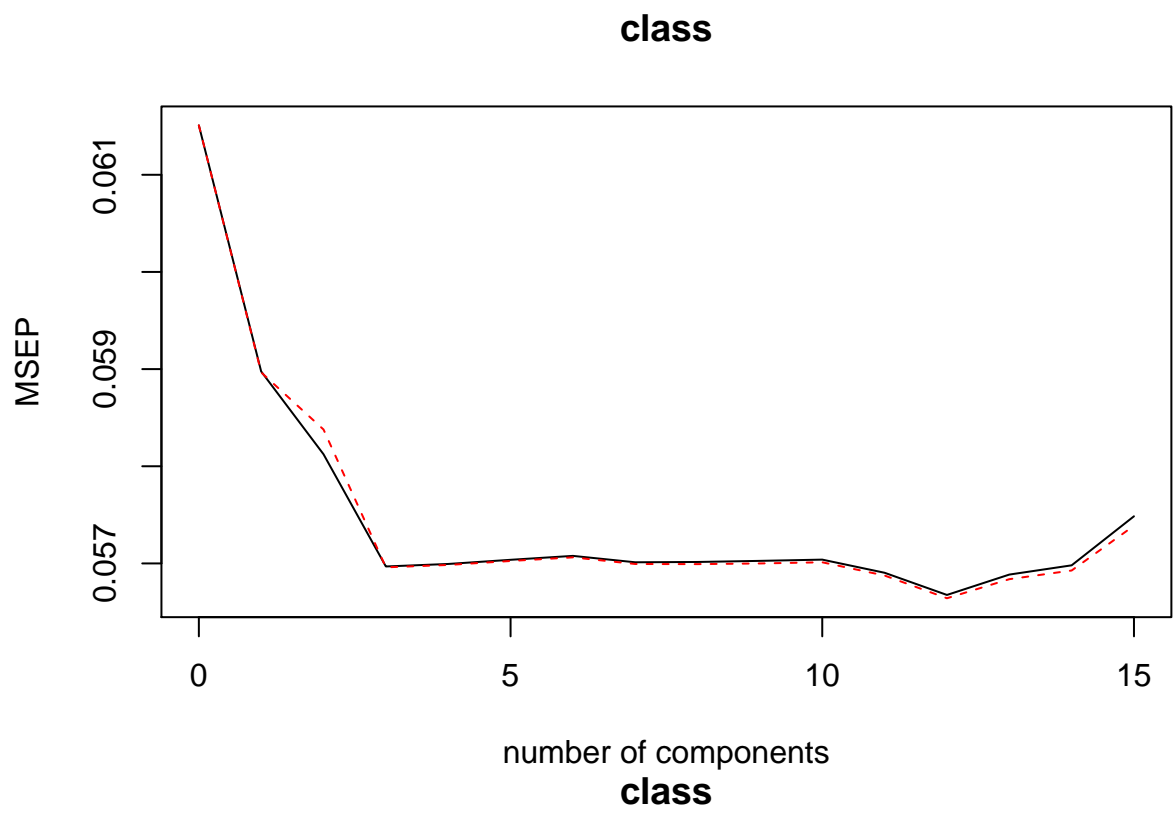
VALIDATION: RMSEP

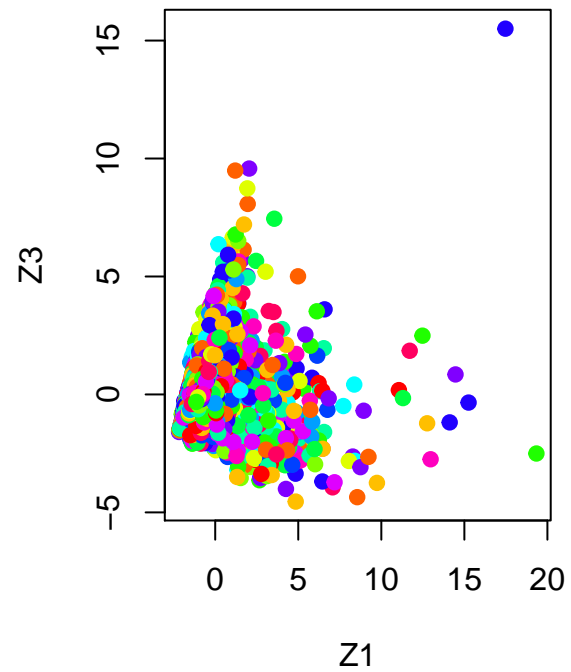
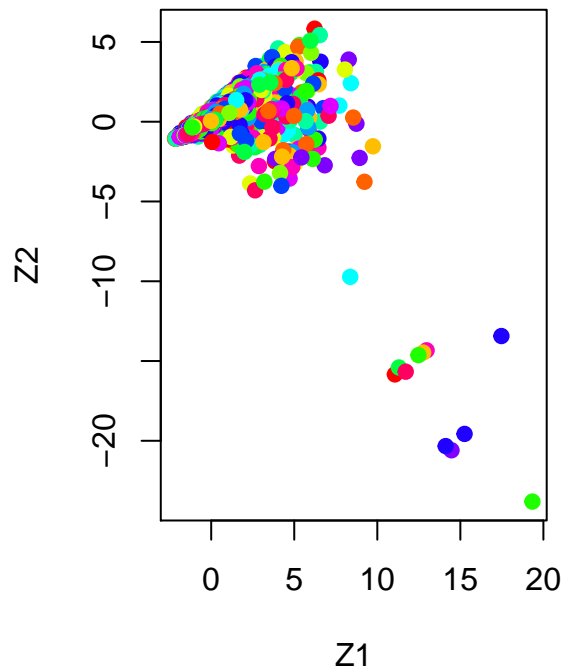
Cross-validated using 10 random segments.

	(Intercept)	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps
CV	0.248	0.2428	0.2411	0.2387	0.2387	0.2388	0.2389
adjCV	0.248	0.2428	0.2416	0.2387	0.2387	0.2388	0.2389
	7 comps	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps
CV	0.2388	0.2388	0.2388	0.2388	0.2385	0.2381	0.2385
adjCV	0.2387	0.2387	0.2387	0.2388	0.2385	0.2380	0.2384
	14 comps	15 comps					
CV	0.2387	0.2398					
adjCV	0.2386	0.2396					

TRAINING: % variance explained

	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps	7 comps
X	25.306	40.680	55.704	64.926	72.401	79.396	85.185
class	4.225	5.285	7.573	7.577	7.584	7.592	7.792
	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps	14 comps
X	89.627	93.557	97.005	98.398	99.294	99.97	99.998
class	7.917	8.022	8.026	8.289	8.847	8.87	8.872
	15 comps						
X	100.000						
class	9.128						

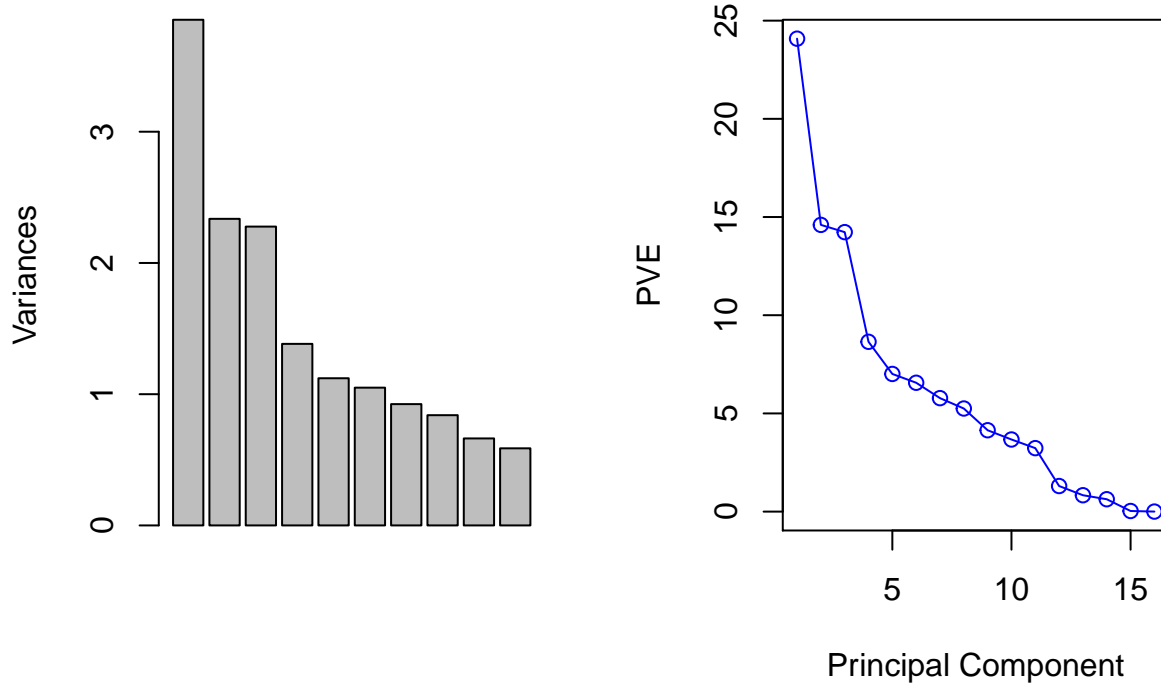




Importance of components:

	PC1	PC2	PC3	PC4	PC5	PC6
Standard deviation	1.9629	1.5284	1.5089	1.17618	1.05902	1.02457
Proportion of Variance	0.2408	0.1460	0.1423	0.08646	0.07009	0.06561
Cumulative Proportion	0.2408	0.3868	0.5291	0.61559	0.68568	0.75129
	PC7	PC8	PC9	PC10	PC11	PC12
Standard deviation	0.96145	0.9165	0.81413	0.76650	0.71908	0.45631
Proportion of Variance	0.05777	0.0525	0.04143	0.03672	0.03232	0.01301
Cumulative Proportion	0.80907	0.8616	0.90299	0.93971	0.97203	0.98504
	PC13	PC14	PC15	PC16		
Standard deviation	0.36522	0.3174	0.07039	0.01562		
Proportion of Variance	0.00834	0.0063	0.00031	0.00002		
Cumulative Proportion	0.99338	0.9997	0.99998	1.00000		

pr.out



Data: X dimension: 2584 15
 Y dimension: 2584 1
 Fit method: svdpc
 Number of components considered: 15

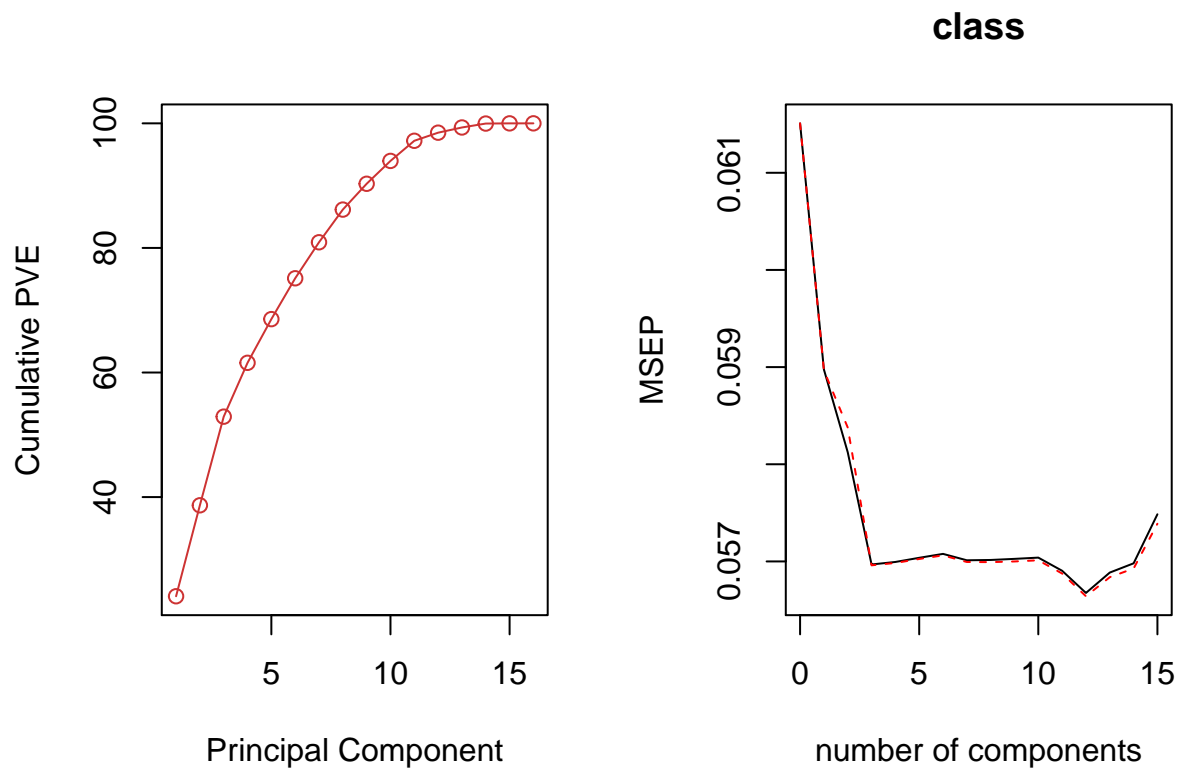
VALIDATION: RMSEP

Cross-validated using 10 random segments.

	(Intercept)	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps
CV	0.248	0.2428	0.2411	0.2387	0.2387	0.2388	0.2389
adjCV	0.248	0.2428	0.2416	0.2387	0.2387	0.2388	0.2389
	7 comps	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps
CV	0.2388	0.2388	0.2388	0.2388	0.2385	0.2381	0.2385
adjCV	0.2387	0.2387	0.2387	0.2388	0.2385	0.2380	0.2384
	14 comps	15 comps					
CV	0.2387	0.2398					
adjCV	0.2386	0.2396					

TRAINING: % variance explained

	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps	7 comps
X	25.306	40.680	55.704	64.926	72.401	79.396	85.185
class	4.225	5.285	7.573	7.577	7.584	7.592	7.792
	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps	14 comps
X	89.627	93.557	97.005	98.398	99.294	99.97	99.998
class	7.917	8.022	8.026	8.289	8.847	8.87	8.872
	15 comps						
X	100.000						
class	9.128						



[1] 0.05357258

Data: X dimension: 1938 15

Y dimension: 1938 1

Fit method: svdpc

Number of components considered: 15

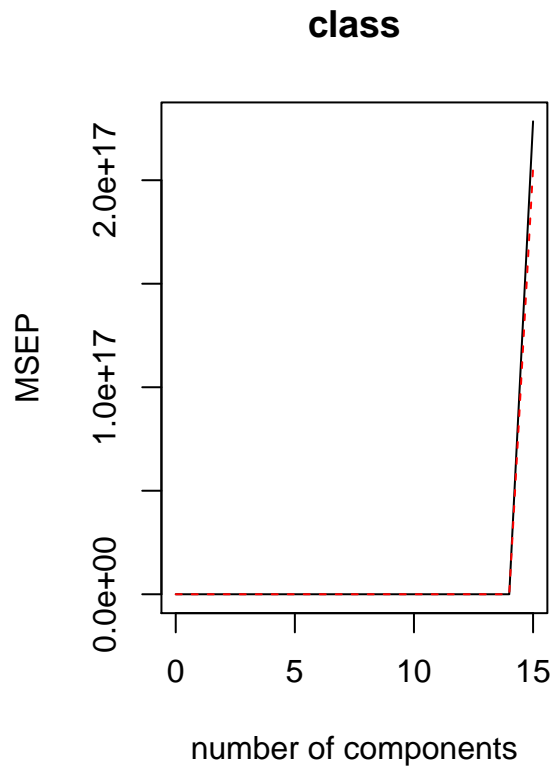
VALIDATION: RMSEP

Cross-validated using 10 random segments.

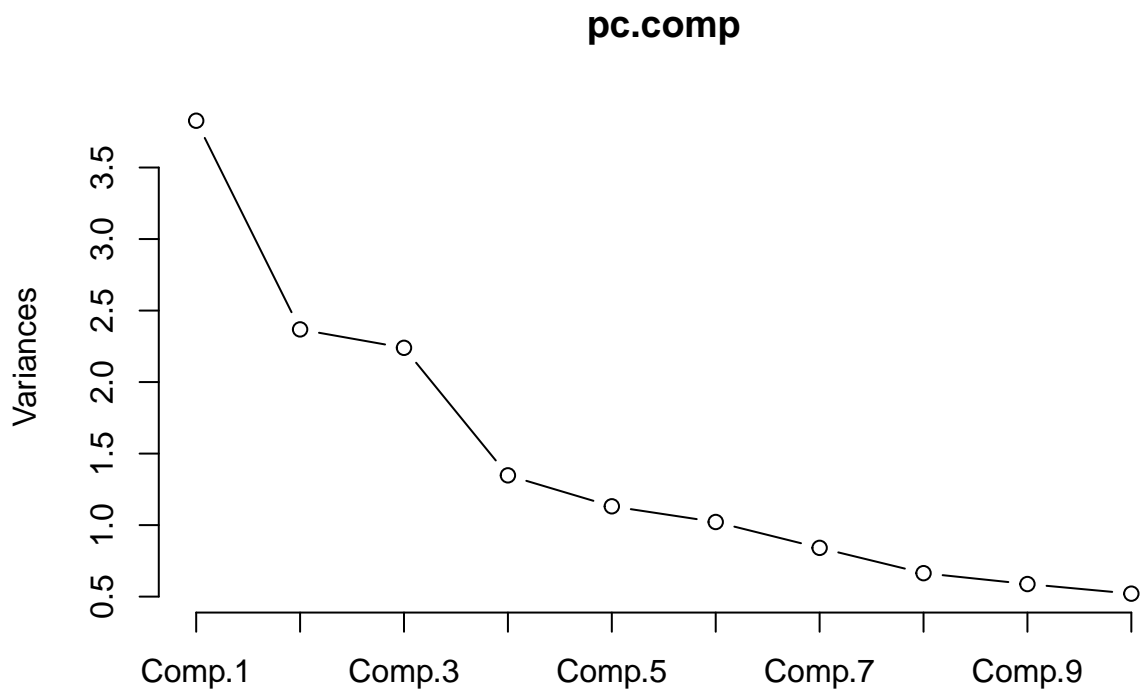
	(Intercept)	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps
CV	0.2512	0.2454	0.2417	0.2413	0.2417	0.2417	0.242
adjCV	0.2512	0.2453	0.2415	0.2413	0.2416	0.2417	0.242
	7 comps	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps
CV	0.2421	0.2421	0.2421	0.2422	0.2422	0.2420	0.2422
adjCV	0.2420	0.2420	0.2420	0.2421	0.2421	0.2419	0.2421
	14 comps	15 comps					
CV	0.2431	477953634					
adjCV	0.2429	453530602					

TRAINING: % variance explained

	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps	7 comps
X	25.528	41.325	56.263	65.253	72.800	79.615	85.224
class	4.815	7.847	7.952	7.953	7.967	8.025	8.255
	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps	14 comps
X	89.653	93.574	97.048	98.456	99.324	99.978	99.999
class	8.362	8.466	8.502	8.574	8.905	8.943	8.981
	15 comps						
X	100.000						
class	9.781						

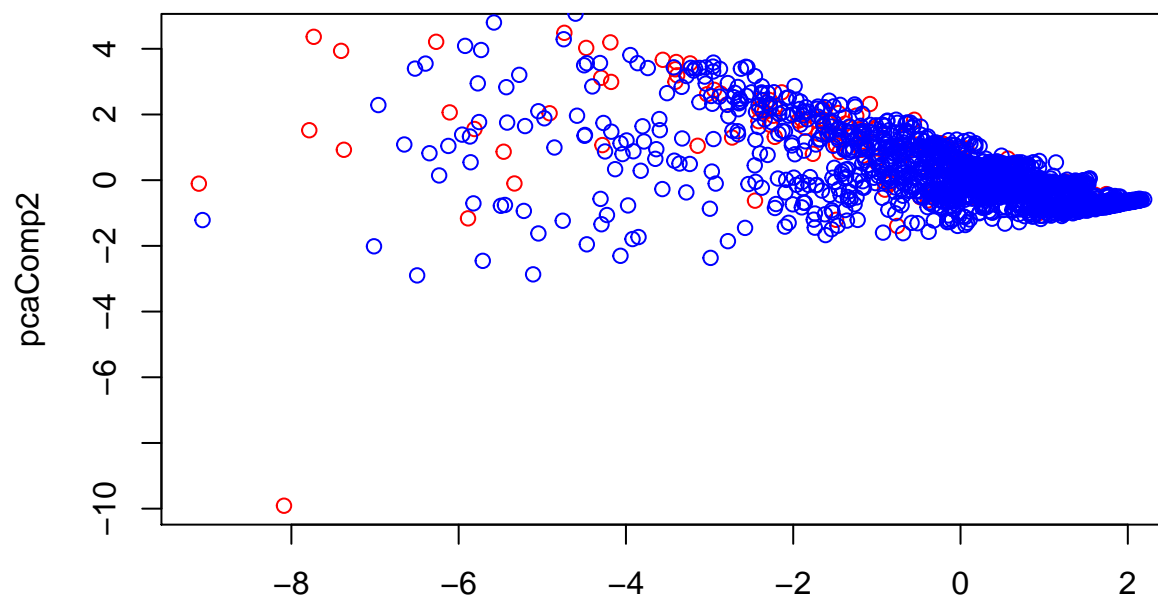


Variable Selection - PCA - INCOMPLETE

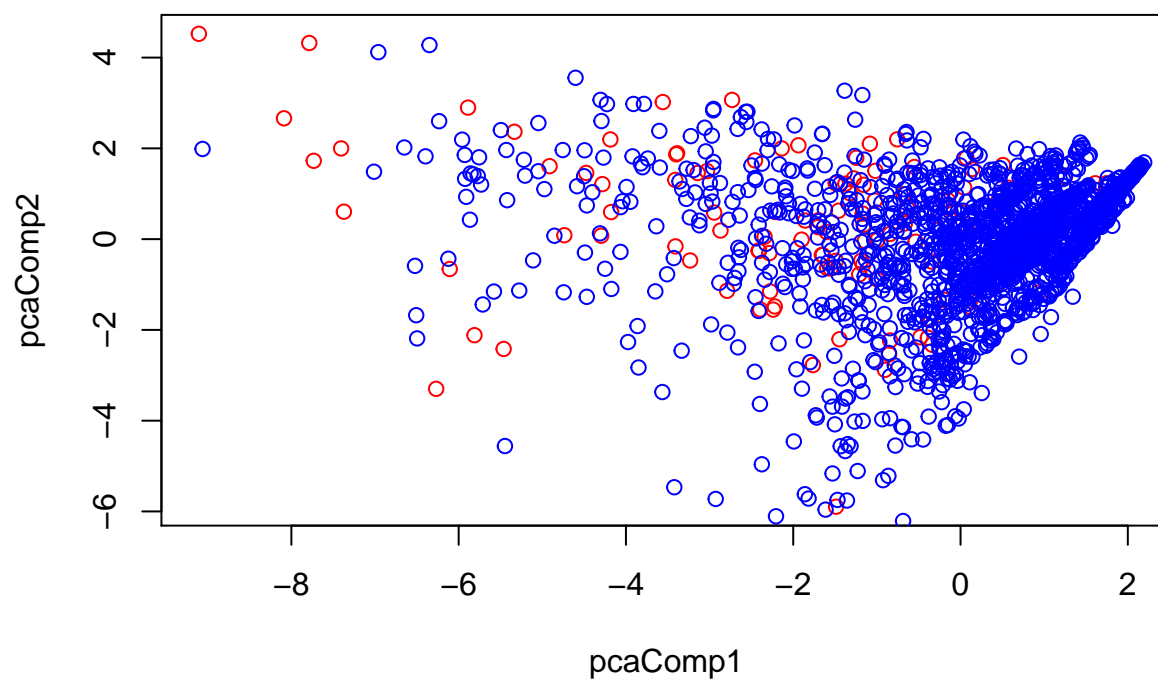


Variable Selection - PCA - INCOMPLETE

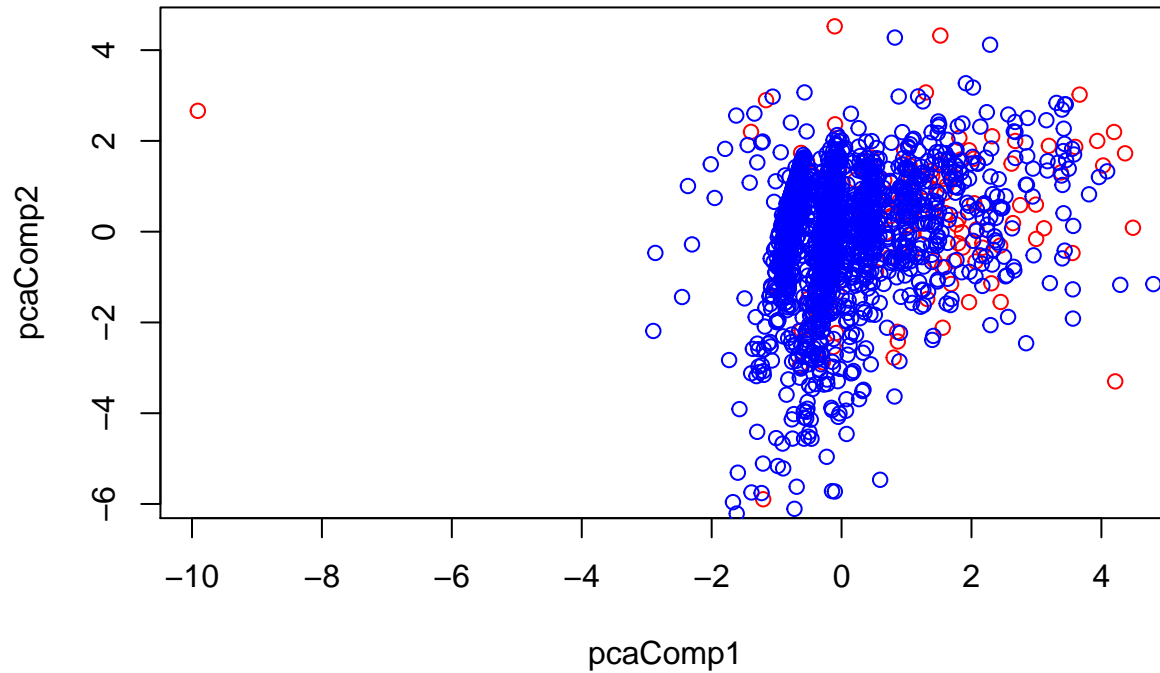
PC1 vs PC2



PC1 vs PC3



PC2 vs PC3



Data: X dimension: 2584 15
Y dimension: 2584 1
Fit method: svdpc
Number of components considered: 15

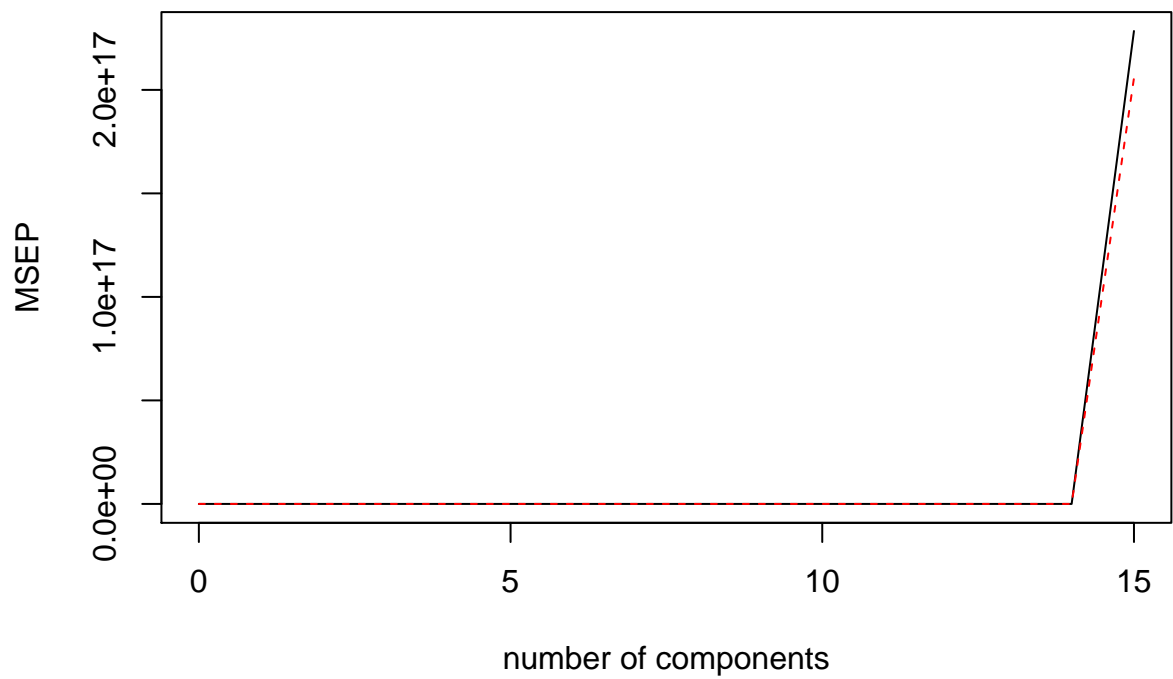
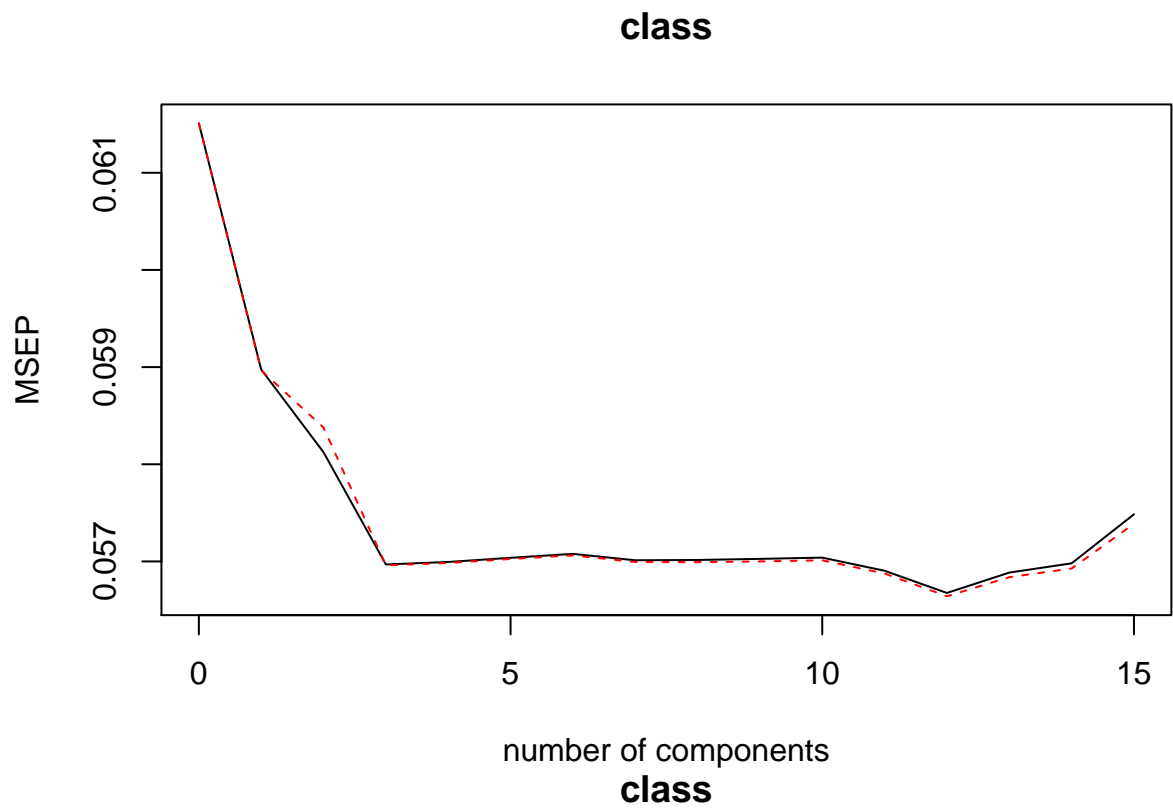
VALIDATION: RMSEP

Cross-validated using 10 random segments.

	(Intercept)	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps
CV	0.248	0.2428	0.2411	0.2387	0.2387	0.2388	0.2389
adjCV	0.248	0.2428	0.2416	0.2387	0.2387	0.2388	0.2389
	7 comps	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps
CV	0.2388	0.2388	0.2388	0.2388	0.2385	0.2381	0.2385
adjCV	0.2387	0.2387	0.2387	0.2388	0.2385	0.2380	0.2384
	14 comps	15 comps					
CV	0.2387	0.2398					
adjCV	0.2386	0.2396					

TRAINING: % variance explained

	1 comps	2 comps	3 comps	4 comps	5 comps	6 comps	7 comps
X	25.306	40.680	55.704	64.926	72.401	79.396	85.185
class	4.225	5.285	7.573	7.577	7.584	7.592	7.792
	8 comps	9 comps	10 comps	11 comps	12 comps	13 comps	14 comps
X	89.627	93.557	97.005	98.398	99.294	99.97	99.998
class	7.917	8.022	8.026	8.289	8.847	8.87	8.872
	15 comps						
X	100.000						
class	9.128						



[1] 0.05357258

Logistic Regression after Variable Selection

```
Call:
glm(formula = class ~ seismic + shift + gpuls + nbumps, family = binomial,
    data = seismic.train)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.6270	-0.3846	-0.2947	-0.1627	2.9781

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-5.9508244	0.6490468	-9.169	< 2e-16 ***
seismic	0.3641160	0.1944250	1.873	0.061098 .
shift	1.1371057	0.3402674	3.342	0.000832 ***
gpuls	0.0004913	0.0001283	3.829	0.000129 ***
nbumps	0.3231048	0.0507286	6.369	1.9e-10 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 958.82 on 1937 degrees of freedom
Residual deviance: 828.98 on 1933 degrees of freedom
AIC: 838.98

Number of Fisher Scoring iterations: 6

```
[1] 0.9318885
```

```
glm.pred  0  1
          0 1803 128
          1   4   3
```

```
[1] 0.02290076
```

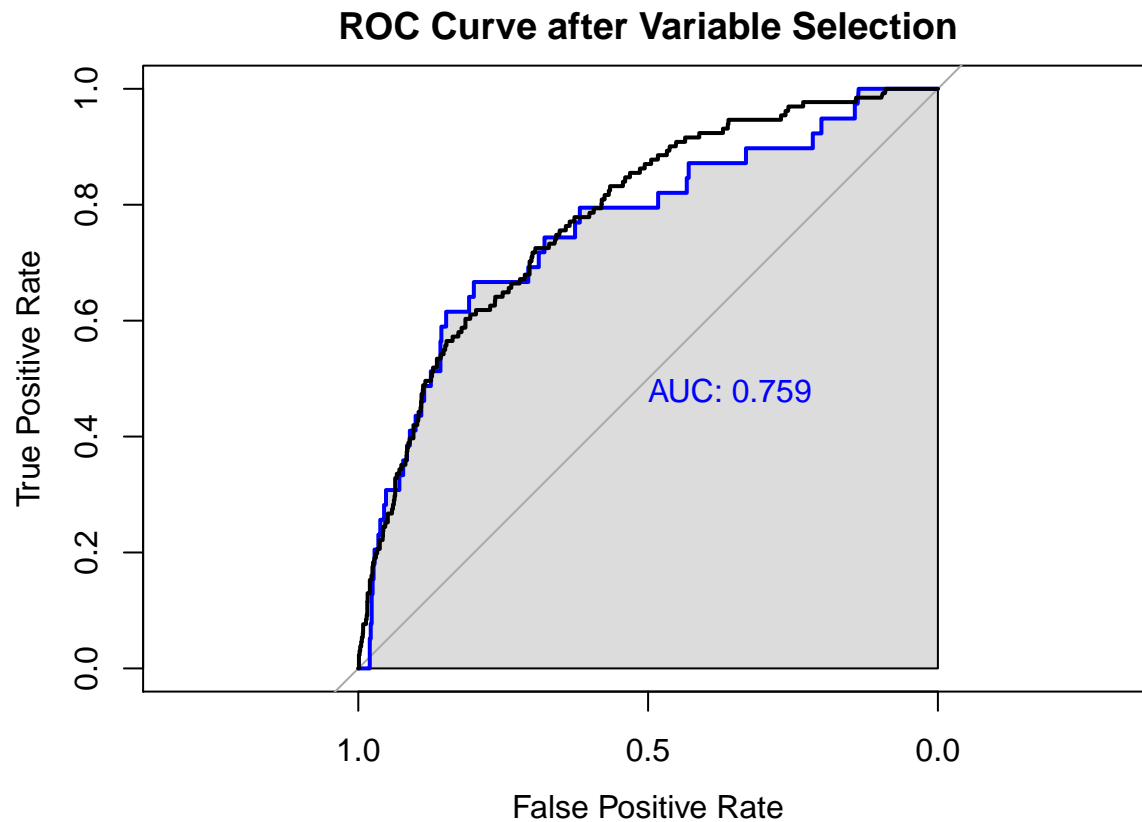
```
[1] 0.9977864
```

```
[1] 0.9380805
```

```
glm.pred  0  1
          0 606 39
          1   1   0
```

```
[1] 0
```

```
[1] 0.9983526
```



Quadratic Discriminant Analysis after variable selection

```
##-----
## Fit QDA model after variable selection
##-----

# Model 1
qda.fit <- qda(class~seismic+shift+gpuls+nbumps, data=seismic.train)
qda.class=predict(qda.fit,seismic.test)$class
confusion <- table(qda.class ,seismic.test$class)

sensitivity <- confusion[2,2]/sum(confusion[,2])
specificity <- confusion[1,1]/sum(confusion[,1])

confusion
```

```
##
## qda.class    0    1
##           0 565  27
##           1  42  12
```

```
sensitivity
```

```
## [1] 0.3076923
```

```
specificity
```

```
## [1] 0.9308072
```

```
# Model 2
```

```
qda.fit <- qda(class ~ genergy + gpuls + nbumps + nbumps2 + nbumps4, data=seismic.train)  
qda.class=predict(qda.fit,seismic.test)$class
```

```
confusion <- table(qda.class ,seismic.test$class)
```

```
sensitivity <- confusion[2,2]/sum(confusion[,2])
```

```
specificity <- confusion[1,1]/sum(confusion[,1])
```

```
confusion
```

```
##
```

```
## qda.class    0    1
```

```
##           0 527  23
```

```
##           1  80  16
```

```
sensitivity
```

```
## [1] 0.4102564
```

```
specificity
```

```
## [1] 0.8682043
```

Regularized Discriminant Analysis after variable selection

```
rda.class    0    1  
             0 595  35  
             1  12   4
```

```
[1] 0.1025641
```

```
[1] 0.9802306
```

```
rda.class    0    1  
             0 572  33  
             1  35   6
```

```
[1] 0.1538462
```

```
[1] 0.9423394
```

Pre-Variable Selection

Model	Test Specificity	Test Sensitivity	Training Specificity	Training Sensitivity
Indicator	123	123	123	123
LDA	123	123	123	123
QDA	123	123	123	123
RDA	123	123	123	123
Log Regression	123	123	123	123

Post-Variable Selection

Model	Test Specificity	Test Sensitivity	Training Specificity	Training Sensitivity
Indicator	123	123	123	123
LDA	123	123	123	123
QDA	123	123	123	123
RDA	123	123	123	123
Log Regression	123	123	123	123