

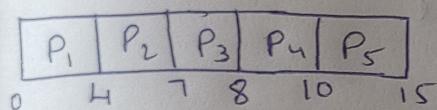
Operating System

FCFS: CPU scheduling . → Non-preemptive (once processor gets CPU, it doesn't release until it finishes its work)
 Drawback: Convoy effect (makes small duration it finishes its work)
 Processor wait for long time)

Process	Arrival time	Burst time
P ₁	0	4
P ₂	1	3
P ₃	2	1
P ₄	3	2
P ₅	4	5



⇒ Gantt chart



Process	Waiting time (starting time - arrival time)	Turn around time
P ₁	0 - 0 = 0	4 - 0 = 4
P ₂	4 - 1 = 3	7 - 1 = 6
P ₃	7 - 2 = 5	8 - 2 = 6
P ₄	8 - 3 = 5	10 - 3 = 7
P ₅	10 - 4 = 6	15 - 4 = 11

$$\text{Avg. waiting time} = \frac{0+3+5+5+6}{5}$$

$$= 3.8 \text{ m.sec}$$

$$\text{Avg. Turn around time} = \frac{4+7+8+10+15}{5}$$

$$= \frac{4+6+6+7+11}{5}$$

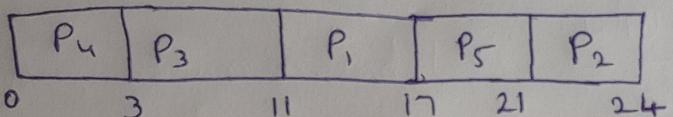
$$= 6.8 \text{ msec}$$

$$= 0.88 \text{ msec}$$

Ex:

Process	Arrival time	Burst time
P ₁	2	6
P ₂	5	3
P ₃	1	8
P ₄	0	3
P ₅	4	4

⇒ Gantt chart



Process	Waiting time	Turn around time
P ₁	$11 - 2 = 9$	$17 - 2 = 15$
P ₂	$21 - 5 = 16$	$24 - 5 = 19$
P ₃	$3 - 1 = 2$	$11 - 1 = 10$
P ₄	$0 - 0 = 0$	$3 - 0 = 3$
P ₅	$17 - 4 = 13$	$21 - 4 = 17$

$$\text{Avg. waiting time} = \frac{9 + 16 + 2 + 0 + 13}{5} \\ = 8 \text{ msec}$$

$$\text{Avg. turn around time} = \frac{15 + 19 + 10 + 3 + 17}{5} \\ = 12.8 \text{ msec.}$$

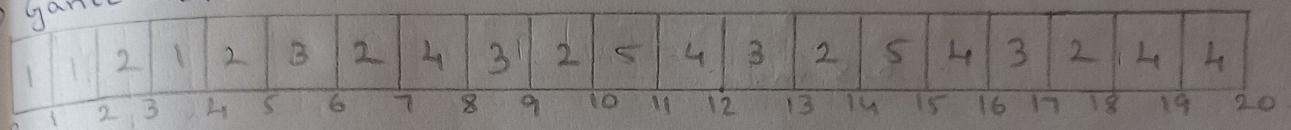
Advantage of FCFS: Easy and simple to implement.

Round robin (RR) scheduling: Pre-emptive version of FCFS scheduling.
time will be divided into small slice.

Process	Arrival time	Service time (burst time)
1	0	3
2	2	6
3	4	4
4	6	5
5	8	2

Time quantum or time slice = 1 msec.

=> Gantt chart.



Time Head Ready list, Tail.

0 1 — — => 1

1 1 — — => 1

2 — 2 — 1 => 21

3 1 — 2 => 12

4 2 3 — => 23

5 3 — 2 => 32

6 2 4 3 => 243

7 43 — 2 => 432

8 32 5 4 => 3254

9 254 — 3 => 2543

10 543 — 2 => 5432

11 432 — 5 => 4325

12 325 — 4 => 3254

13 254 — 3 => 2543

14 543 — 2 => 5432

15 432 — — => 432

16 32 — 4 => 324

17 24 — — => 24

18 4 — — => 4

19 4 — — => 4

Process	Waiting time value ^{last is left no. of processes before arrival time}	turn around time
1.	3 - 2 - 0 = 1	4 - 0 = 4
2	17 - 5 - 2 = 10	18 - 2 = 16
3.	16 - 3 - 4 = 9	17 - 4 = 13
4	19 - 4 - 6 = 9	20 - 6 = 14
5	14 - 1 - 8 = 5	15 - 8 = 7

$$\text{Avg. waiting time} = \frac{1+10+9+9+5}{5}$$

$$= 6.8 \text{ msec.}$$

$$\text{Avg. turn around time} = \frac{4+16+13+14+7}{5}$$

$$= 10.8 \text{ msec.}$$

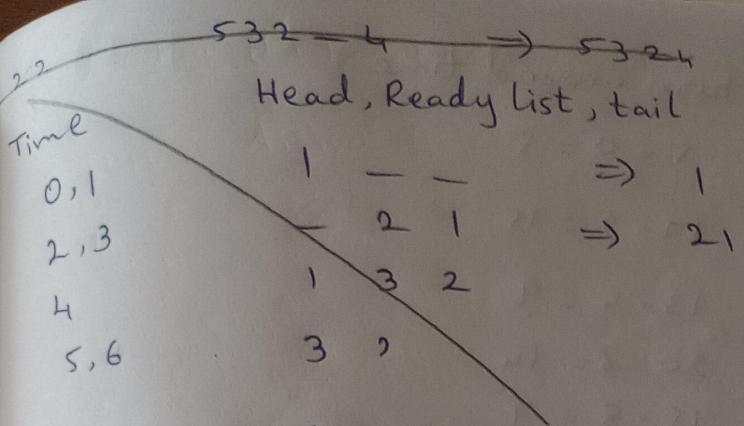
Ex:

Process	Arrival time	Service time
1	0	3
2	2	6
3	4	4
4	6	5
5	8	2

Time quantum = 2 msec.

=>

Time	Head, Ready list, tail
0	1 - - $\Rightarrow 1$
2	- 2 1 $\Rightarrow 21$
4	1 3 2 $\Rightarrow 132$
6	3 2 4 1 $\Rightarrow 3241$
8	2 4 1 5 3 $\Rightarrow 24153$
10	4 1 5 3 - 2 $\Rightarrow 41532$
12	1 5 3 2 - 4 $\Rightarrow 15324$
14	5 3 2 4 - - $\Rightarrow 5324$
16	3 2 4 - 5 $\Rightarrow 3245$
18	2 4 5 - 3 $\Rightarrow 2453$
20	4 5 3 - 2 $\Rightarrow 4532$



Time Head, Ready list, tail

0	1 - -	⇒ 1
1	1 - -	⇒ 1
2	- 2 1	⇒ 21
3	- 2 1	⇒ 21
4	1 3 2	⇒ 132
5	3 2 - -	⇒ 32
6	3 2 4 -	⇒ 324
7	2 4 - 3	⇒ 243
8	2 4 3 5 -	⇒ 2435
9	4 3 5 - 2	⇒ 4352
10	4 3 5 - 2	⇒ 4352
11	3 5 2 4	⇒ 3524
12	3 5 2 4	⇒ 3524
13	5 2 4 - 3	⇒ 5243
14	5 2 4 - 3	⇒ 5243
15	2 4 - -	⇒ 24
16	2 4 - -	⇒ 24
17	4 - -	⇒ 4
18	4 - -	⇒ 4
19	4 - -	⇒ 4.

Process waiting time turn

Gantt chart:

1	1	2	2	1	3	3	2	2	4	4	3	3	5	5	2	2	4	4	4
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	

Process	Waiting time	turn around time
1	$4 - 2 - 0 = 2$	$5 - 0 = 5$
2	$16 - 5 - 2 = 9$	$17 - 2 = 15$
3	$12 - 3 - 4 = 5$	$13 - 4 = 9$
4	$19 - 4 - 6 = 9$	$20 - 6 = 14$
5	$14 - 1 - 8 = 5$	$15 - 8 = 7$

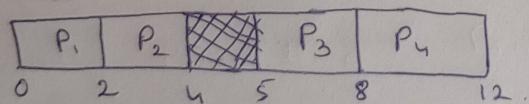
$$\text{Avg. waiting time} = \frac{2+9+5+9+5}{5} \\ = 6 \text{ msec.}$$

$$\text{Avg. turn around time} = \frac{5+15+9+14+7}{5} \\ = 10 \text{ msec.}$$

Ex: FCFS

Process	Arrival time	Burst time
P ₁	0	2
P ₂	1	3
P ₃	5	2
P ₄	6	4

⇒ Gantt chart.



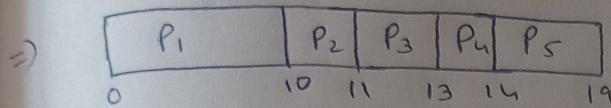
Process	Waiting time	turn around time
P ₁	$0 - 0 = 0$	$2 - 0 = 2$
P ₂	$2 - 0 = 2$	$4 - 1 = 3$
P ₃	$5 - 5 = 0$	$8 - 5 = 3$
P ₄	$8 - 6 = 2$	$12 - 6 = 6$

$$\text{Avg. waiting time} = \frac{0+1+0+2}{4} = 0.75 \text{ msec.}$$

$$\text{Avg. turn around time} = \frac{2+3+3+6}{4} = 3.5 \text{ msec.}$$

Ex: FCFS

process	Burst time
P ₁	10
P ₂	1
P ₃	2
P ₄	1
P ₅	5



process waiting time Turn around
Break time.

$$P_1 \quad 0 - 0 = 0 \quad 10 - 0 = 10$$

$$P_2 \quad 10 - 0 = 10 \quad 11 - 0 = 11$$

$$P_3 \quad 11 - 0 = 11 \quad 13 - 0 = 13$$

$$P_4 \quad 13 - 0 = 13 \quad 14 - 0 = 14$$

$$P_5 \quad 14 - 0 = 14 \quad 19 - 0 = 19$$

$$\text{Avg. waiting time} = \frac{0+10+11+13+14}{5} \\ = 9.6 \text{ msec.}$$

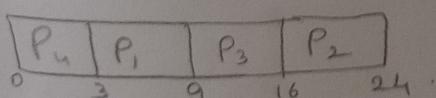
$$\text{Avg Turn around time} = \frac{10+11+13+14+19}{5} \\ = 13.4 \text{ msec.}$$

Shortest Job First (SJF) scheduling: Non-preemptive & preemptive

Shortest burst time processor uses the CPU first.

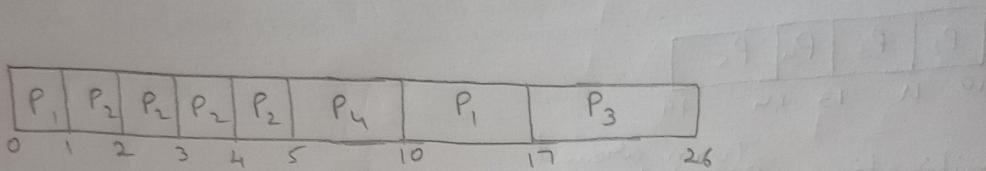
Less waiting time compared to FCFS.

Process	Burst Time	Turn Around time	Waiting time
P ₁	6	9	3
P ₂	8	24	16
P ₃	7	16	9
P ₄	3	3	0
		Avg = 13.	Avg = 7.



Pre-emptive SJF : SRTF (shortest remaining time first).

Process	Arrival time	Burst time
P ₁	0	8
P ₂	1	4
P ₃	2	9
P ₄	3	5

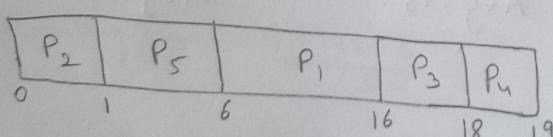


Process	Turn around time	Waiting time
P ₁	17 - 0 = 17	10 - 1 - 0 = 9
P ₂	5 - 1 = 4	4 - 3 - 1 = 0
P ₃	26 - 2 = 24	17 - 0 - 2 = 15
P ₄	10 - 3 = 7	5 - 0 - 3 = 2
Avg	13	Avg = 6.5

Drawback: We cannot predict whether the upcoming process has less burst time or not.

Priority scheduling:

Process	Burst time	Priority
P ₁	10	3
P ₂	1	1
P ₃	2	4
P ₄	1	5
P ₅	5	2



If two processors have same priority order, it works on first come first basis. If the arrival times are also same, the

processor with less subscript gets higher priority.

Process	Turn Around time	Waiting time
P ₁	16	6
P ₂	1	0
P ₃	18	16
P ₄	19	18
P ₅	6	1
	Avg = 12	Avg = 8.2

8. Process Burst
Arrived time Priority

P ₁	10	3
P ₂	1	1
P ₃	2	3
P ₄	1	4
P ₅	5	2

$P_1 > P_3$ lesser subscript high priority

P ₂	P ₅	P ₁	P ₃	P ₄
0	1	6	16	18

Process TAT WT

P ₁	16	6
P ₂	1	0
P ₃	18	16
P ₄	19	18
P ₅	6	1
	Avg = 12	Avg = 8.2

9. Process Burst time Priority

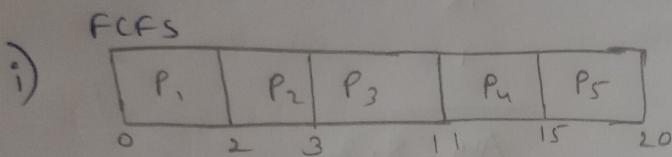
P ₁	2	2
P ₂	1	1
P ₃	8	4
P ₄	4	2
P ₅	5	3

i) FCFS

ii) Non preemptive SJF

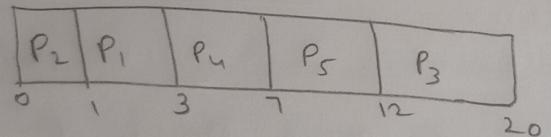
iii) Non Preemptive priority (larger no. high priority)

iv) RR ($Q=2$)



Process	TAT	WT
P ₁	2	0
P ₂	3	2
P ₃	11	3
P ₄	15	11
P ₅	20	15
Avg = 10.2		6.2

iii) Non-preemptive SJF



Process	TAT	WT
P ₁	3	1
P ₂	1	0
P ₃	20	12
P ₄	7	3
P ₅	12	7
Avg = 8.6		Avg = 4.6

Non Preemptive Priority.

	P ₅	P ₁	P ₄	P ₂
	8	13	15	19 20

Process	TAT	WT
P ₁	15	13
P ₂	20	19
P ₃	8	0
P ₄	19	15
P ₅	13	8
	Avg = 15	Avg = 11

iv) RR ($\Delta=2$)

P ₁	P ₂	P ₃	P ₄	P ₅	P ₃	P ₄	P ₅	P ₃	P ₅	P ₃
0	2	3	5	7	9	11	13	15	17	18 20

Process	TAT	WT
P ₁	2	0
P ₂	3	2
P ₃	20	19 - 7 = 12
P ₄	13	12 - 3 = 9
P ₅	18	17 - 4 = 13
	Avg = 11.2	Avg = 10.2

Page replacement algorithms in virtual memory:

FIFO: oldest page is replaced.

Frame String:	7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0
Page Arrival:	7	7	7	3	3	3	3	2	2	2	2	2	2	2	2	2	2	2	2

Page faults = 10

Ex: Reference string:

1 2 3 4 1 2 5 1 2 3 4 5

3 frames:

1	1	1	4	4	4	5	5	5
2	2	2	1	1	1	3	3	4
3	3	3	2	2	2	2	2	2

Page faults = 9

4 frames:

1	1	1	1	5	5	5	5	4
2	2	2	2	2	1	1	1	5
3	3	3	3	3	2	2	2	2
4	4	4	4	4	3	3	3	3

page faults = 10.

With increase in frame the page faults should decrease but in some problems because of Belady's Anomaly, page faults also increase.

Drawback: Belady's Anomaly.

2. Optimal Algorithm:

Reference string:

7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1
2	7	7	7	3	3	0	0	0	1	0	0	1	0	1	0	1	7	0	2
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2

Page faults = 8.

3. Least Recently used (LRU) Algorithm:

7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	0	1	7	0	1
2	7	7	7	3	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	

Page faults = 8.

Deadlock:

Banker's algorithm: Used to avoid deadlock.

Consider the following snapshot of a system:

	<u>Allocation</u>			<u>Max</u>			<u>Available</u>		
	A	B	C	A	B	C	A	B	C
P ₀	0	1	0	7	5	3	3	3	2
P ₁	2	0	0	3	2	2			
P ₂	3	0	2	9	0	2			
P ₃	2	1	1	2	2	2			
P ₄	0	0	2	4	3	3			

Total: A = 10 instances of resource A are available

$$B = 5$$

$$C = 7$$

	<u>Allocation</u>	<u>Max</u>	(Total-Allocation)			(Max-Allocation)			<u>safe sequence</u>
			<u>Available</u>	<u>Remaining Need</u>					
P ₀	0 1 0	7 5 3	3 3 2	7 4 3	✓				P ₁
P ₁	2 0 0	3 2 2	5 3 2	1 2 2	✓				P ₃
P ₂	3 0 2	9 0 2	7 4 3	6 0 0	✓				P ₄
P ₃	2 1 1	2 2 2	7 4 5	0 1 1	✓				P ₀
P ₄	0 0 2	4 3 3	7 5 5	4 3 1	✓				P ₂

∴ The system is safe

Suppose that process P₁ requests one instance of resource type A and two instances of resource type C, can this request be granted immediately. (1 0 2)

	<u>Allocation</u>	<u>Max</u>	<u>Available</u>	<u>Remaining Need</u>		
				A	B	C
	A B C	A B C	A B C	3 3 2	7 4 3	✓
P ₀	0 1 0	7 5 3	2 3 0	7	4	3
P ₁	3 0 2	1 3 2	5 3 2	0	2	0
P ₂	3 0 2	9 0 2	7 4 3	6	0	0
P ₃	2 1 1	2 2 2	7 4 5	0	1	1
P ₄	0 0 2	4 3 3	7 5 5	4	3	1
			3 0 2	10	5	7

∴ System is safe.

Q. Request 2 by Process P₄ = 3,3,0

⇒ The request cannot be granted since, the resources are not available. (2 3 0 \times 3 3 0)

Q. Request 3 by process P₀ = 0,2,0

	<u>Allocation</u>	<u>Max</u>	<u>Available</u>	<u>Remaining Need</u>		
				A	B	C
P ₀	(0 1 0 + 0 2 0)	7 5 3	(2 3 0 - 0 2 0)	2 1 0	7	2 3 X
P ₁	3 0 2	3 2 2	5 1 2	0	2 0 X	
P ₂	3 0 2	9 0 2	7 2 3	6	0 0 X	
P ₃	2 1 1	2 2 2	7 2 5	0	1 1 X	
P ₄	0 0 2	4 3 3	7 5 5	4	3 1 X	

∴ System is safe.

System is not safe.

Request cannot be granted.