# $\operatorname{CS}$ 467 - Cyber Security: Course Project

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## 1 RSA Cipher

## 1.1 Background

RSA, or Rivest–Shamir–Adleman, is a public-key cryptosystem that is widely used for secure data transmission. The security of RSA relies on the practical difficulty of factoring the product of two large prime numbers, the "factoring problem". RSA is a relatively slow algorithm. Because of this, it is not commonly used to directly encrypt user data. More often, RSA is used to transmit shared keys for symmetric key cryptography, which are then used for bulk encryption-decryption.<sup>1</sup>

#### 1.2 Problem

The following example of RSA cipher text is presented. Your task is to decrypt it. The public parameters of the systems are n=31313 and e=4913. In order to translate the plaintext back into ordinary English text, you need to know how alphabetic characters are encoded as elements in Zn. Each element of Zn represents three alphabetic characters as in the following examples:

```
DOG: 3x26^2 + 14x26 + 6 = 2398
CAT: 2x26^2 + 0x26 + 19 = 1371
ZZZ: 25x26^2 + 25x26 + 25 = 17575
```

 $6340\ 8309\ 14010\ 8936\ 27358\ 25023\ 16481\ 25809\ 23614\ 7135\ 24996\ 30590$   $27570\ 26486\ 30388\ 9395\ 27584\ 14999\ 4517\ 12146\ 29421\ 26439\ 1606\ 17881\ 25774$   $7647\ 23901\ 7372\ 25774\ 18436\ 12056\ 13547\ 7908\ 8635\ 2149\ 1908\ 22076\ 7372\ 8686$   $1304\ 4082\ 11803\ 5314\ 107\ 7359\ 22470\ 7372\ 22827\ 15698\ 30317\ 4685\ 14696\ 30388$   $8671\ 29956\ 15705\ 1417\ 26905\ 25809\ 28347\ 26277\ 7897\ 20240\ 21519\ 12437\ 1108$   $27106\ 18743\ 24144\ 10685\ 25234\ 30155\ 23005\ 8267\ 9917\ 7994\ 9694\ 2149\ 10042$   $27705\ 15930\ 29748\ 8635\ 23645\ 11738\ 24591\ 20240\ 27212\ 27486\ 9741\ 2149\ 29329$   $2149\ 5501\ 14015\ 30155\ 18154\ 22319\ 27705\ 20321\ 23254\ 13624\ 3249\ 5443\ 2149$   $16975\ 16087\ 14600\ 27705\ 19386\ 7325\ 26277\ 19554\ 23614\ 7553\ 4734\ 8091\ 23973$   $14015\ 107\ 3183\ 17347\ 25234\ 4595\ 21498\ 6360\ 19837\ 8463\ 6000\ 31280\ 29413\ 2066$   $369\ 23204\ 8425\ 7792\ 25973\ 4477\ 30989$ 

You will have to invert this process as the final step in your program.

## 1.3 Solution

The solution to the problem was done using the Python programming language. First, I needed to initialize my global variables that stored both my public parameters given in the problem and all letters to the alphabet to later be used for conversion.

 $<sup>^1\</sup>mathrm{RSA}$  (Cryptosystem): https://en.wikipedia.org/wiki/RSA\_(cryptosystem)

```
PUBLIC_KEY = {
    "n": 31313,
    "e": 4913
}
ALPHABET = [
'A', 'B', 'C', 'D', 'E', 'F', 'G', 'H', 'I', 'J', 'K', 'L', 'M',
'N', 'O', 'P', 'Q', 'R', 'S', 'T', 'U', 'V', 'W', 'X', 'Y', 'Z'
The three helper functions in my program were gcd(), phi(), modInverse(). They
are defined below:
def gcd(x:int, y:int) -> int:
    """The largest positive integer that divides each of the params."""
    if x == 0:
        return y
    return gcd(y % x, x)
def phi(n: int) -> int:
    """Euler's Totient Function, returns number of totatives of n"""
    result = 1
    for i in range(2, n):
        if gcd(i, n) == 1:
            result += 1
    return result
def modInverse(base: int, mod: int) -> int:
    """Modular multiplicative inverse"""
    return pow(base=base, exp=-1, mod=mod)
The function that had the task of decrypting the users input was the function
decryptMessage() defined below:
def decryptMessage():
    """Translates the plaintext back into ordinary English text"""
    exponents = [2, 1, 0]
    encryptedMessage = input("Please enter the RSA encrypted message: \n")
    messageSplit = encryptedMessage.split(" ")
    print("")
    for c in messageSplit:
        d = modInverse(PUBLIC_KEY["e"], phi(PUBLIC_KEY["n"]))
        p = (int(c) ** d) % PUBLIC_KEY["n"]
        for e in exponents:
            letter = math.trunc((p/pow(26, e)) % 26)
            print(ALPHABET[letter], end="")
        print(" ", end="")
```

In this decryptMessage function, the first step was to initialize the exponent values. Because we know that each integer value in the encrypted message represents three characters, the exponents that should be available will be [2,1,0] (from the problem  $a*26^2 + b*26^1 + c*26^0 = p$ ). Next, was to retrieve the encrypted message from the user and split the message on the spaces. Now that we have an array of all the integer values, we can now get our private key by following the formula:  $d = e^{-1} mod(\phi(n))$  using any helper function we already have in the code. Using the private key, we now can get our decrypted plaintext using the formula:  $p = c^d mod(n)$ . Lastly, all we need to do is get our a, b, and c values by taking p and dividing it by 26 raised to the first exponent in the exponent list modulus 26. The truncated value will give us our first index to use to get our first letter from our 'ALPHABET' global variable. This process is then repeated to give us the next two letters, and so on.

## 1.4 Output

LAK EWO BEG ONI SMO STL YPO ORS AND YSO ILA NDE VER YSP RIN GTH EEA RTH HEA VES UPA NEW CRO POF ROC KSP ILE SOF ROC KST ENF EET HIG HIN THE COR NER SOF FIE LDS PIC KED BYG ENE RAT ION SOF USM ONU MEN TST OOU RIN DUS TRY OUR ANC EST ORS CHO SET HEP LAC ETI RED FRO MTH EIR LON GJO URN EYS ADF ORH AVI NGL EFT THE MOT HER LAN DBE HIN DAN DTH ISP LAC ERE MIN DED THE MOF THE RES OTH EYS ETT LED HER EFO RGE TTI NGT HAT THE YHA DLE FTT HER EBE CAU SET HEL AND WAS NTS OGO ODS OTH ENE WLI FET URN EDO UTT OBE ALO TLI KET HEO LDE XCE PTT HEW INT ERS ARE WOR SEZ

## 2 ElGamal Cipher

## 2.1 Background

ElGamal encryption system is an asymmetric key encryption algorithm for public-key cryptography which is based on the Diffie–Hellman key exchange. ElGamal encryption can be defined over any cyclic group G, like multiplicative group of integers modulo n. Its security depends upon the difficulty of a certain problem in G related to computing discrete logarithms.

## 2.2 Problem

Decrypt the ElGamal ciphertext presented in the following table. The parameters of the system are the prime number p=31847, primitive root e1=5, e2=18074. Each element of Zn represents three alphabetic characters as in the above problem.

#### ElGamal Ciphertext

(3781, 14409) (31552, 3930) (27214, 15442) (5809, 30274) (5400, 31486) (19936, 30274)

721) (27765, 29284) (29820, 7710) (31590, 26470) (3781, 14409) (15898, 30844) (19048, 12914) (16160, 3129) (301, 17252) (24689, 7776) (28856, 15720) (30555, 15720)24611) (20501, 2922) (13659, 5015) (5740, 31233) (1616, 14170) (4294, 2307) (2320, 29174)(3036, 20132)(14130, 22010)(25910, 19663)(19557, 10145)(18899,27609) (26004, 25056) (5400, 31486) (9526, 3019) (12962, 15189) (29538, 5408) (3149, 7400) (9396, 3058) (27149, 20535) (1777, 8737) (26117, 14251) (7129, 7129)18195) (25302, 10248) (23258, 3468) (26052, 20545) (21958, 5713) (346, 31194) (8836, 25898) (8794, 17358) (1777, 8737) (25038, 12483) (10422, 5552) (1777, 8737) (3780, 16360) (11685, 133) (25115, 10840) (14130, 22010) (16081, 16414) (28580, 20845) (23418, 22058) (24139, 9580) (173, 17075) (2016, 18131) (19886, 18131)22344) (21600, 25505) (27119, 19921) (23312.16906) (21563, 7891) (28250, 21321) (28327, 19237) (15313, 28649) (24271, 8480) (26592, 25457) (9660, 7939) (10267, 9660)20623) (30499, 14423) (5839, 24179) (12846, 6598) (9284, 27858) (24875, 17641) (1777, 8737) (18825, 19671) (31306, 11929) (3576, 4630) (26664, 27572) (27011, 1929)29164) (22763, 8992) (3149, 7400) (8951, 29435) (2059, 3977) (16258, 30341) (21541, 19004) (5865, 29526) (10536, 6941) (1777, 8737) (17561, 11884) (2209, 19004)6107) (10422, 5552) (19371, 21005) (26521, 5803) (14884, 14280) (4328, 8635) (28250, 21321) (28327, 19237) (15313, 28649)

## 2.3 Solution

## 2.4 Output