



NEW YORK UNIVERSITY

Urban Data Science: Mobility, Cities and Networks

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IC2S2'17, Tutorial

A Practical Introduction to Spatial Datasets and Urban Applications

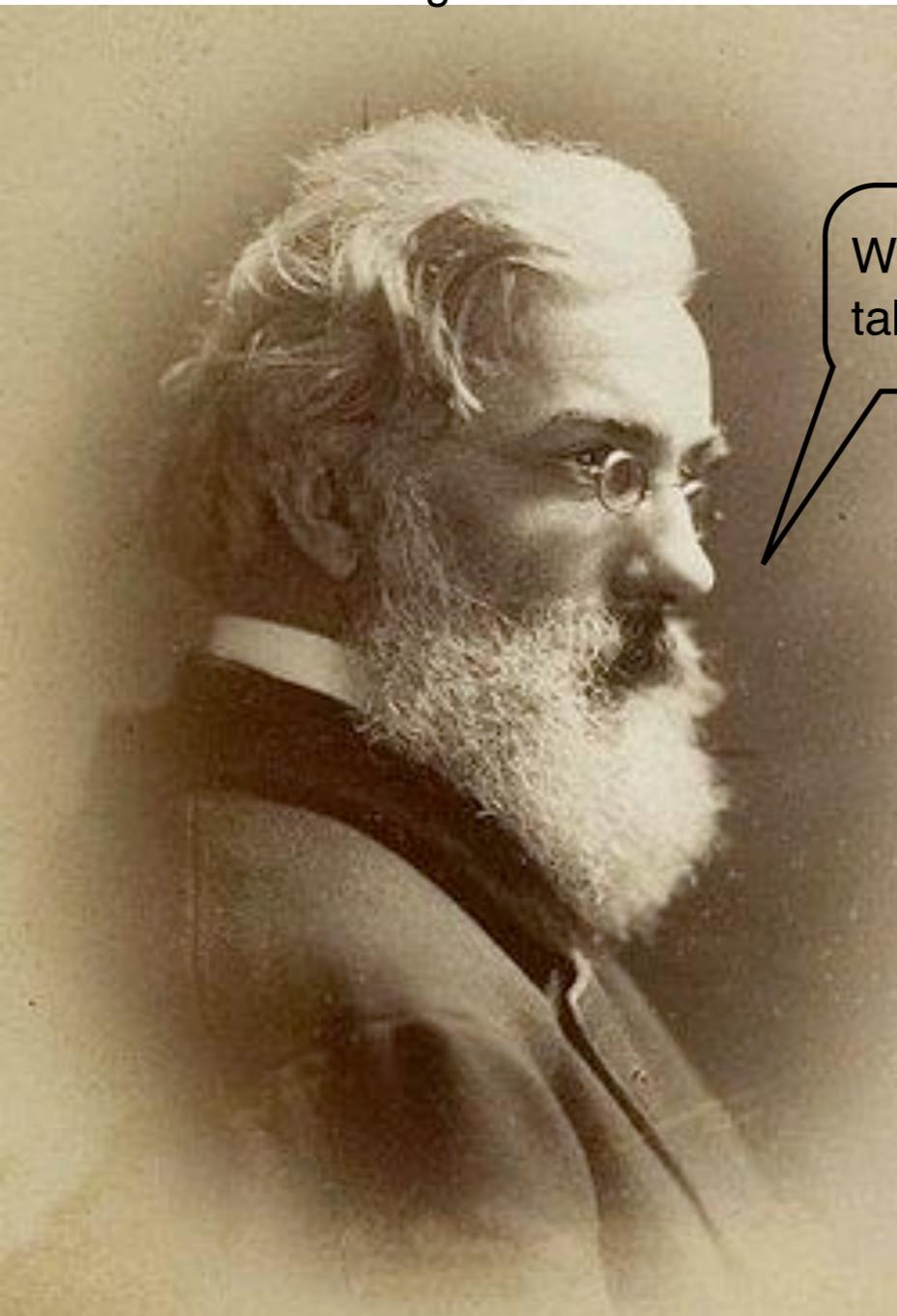
Cologne, Germany

Presentation Summary

- A Historic perspective on human mobility and related datasets.
- Human mobility and transport modelling.
- Deeper insights on urban mobility models.
- Multivariate human mobility models.
- From individual trajectories to aggregate mobility patterns.

History of modern human mobility studies

Ernst Georg Ravenstein



WTF is this dude
talkin' about?

Human migration
follows no definitive
law ...



William Farr ... or
Dark Vader



the main man ...

The laws of human migration

The following was a standard list after Ravenstein's (1834-1913) proposal in the 1880s. The theories are as follows:

1. *every migration flow generates a return or countermigration.*
2. *the majority of migrants move a short distance.*
3. *migrants who move longer distances tend to choose big-city destinations.*
4. *urban residents are often less migratory than inhabitants of rural areas.*
5. *families are less likely to make international moves than young adults.*
6. *most migrants are adults.*
7. *large towns grow by migration rather than natural increase.*

Ravenstein exploited census data from the United Kingdom to support empirically his findings ...

E. G. Ravenstein. The laws of migration. Journal of the Royal Statistical Society, 1885.

Urban Transport Modeling

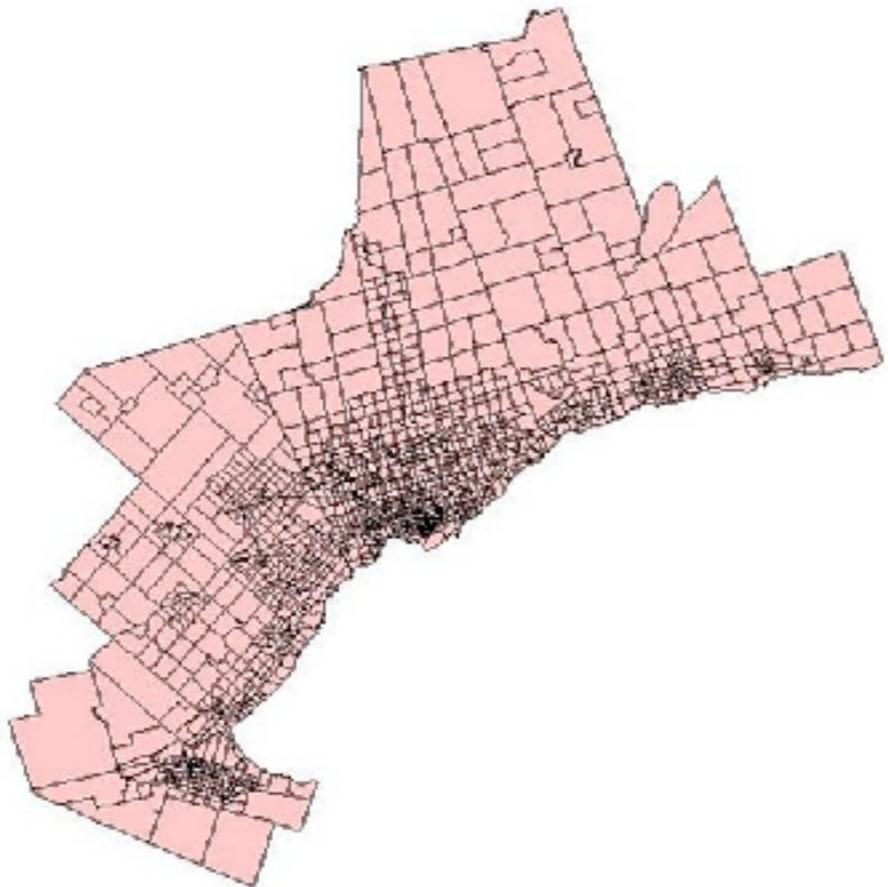


Table: Illustrative trip table

Origin \ Destination	1	2	3	z
1	T_{11}	T_{12}	T_{13}	T_{1z}
2	T_{21}			
3	T_{31}			
z	T_{z1}			T_{zz}

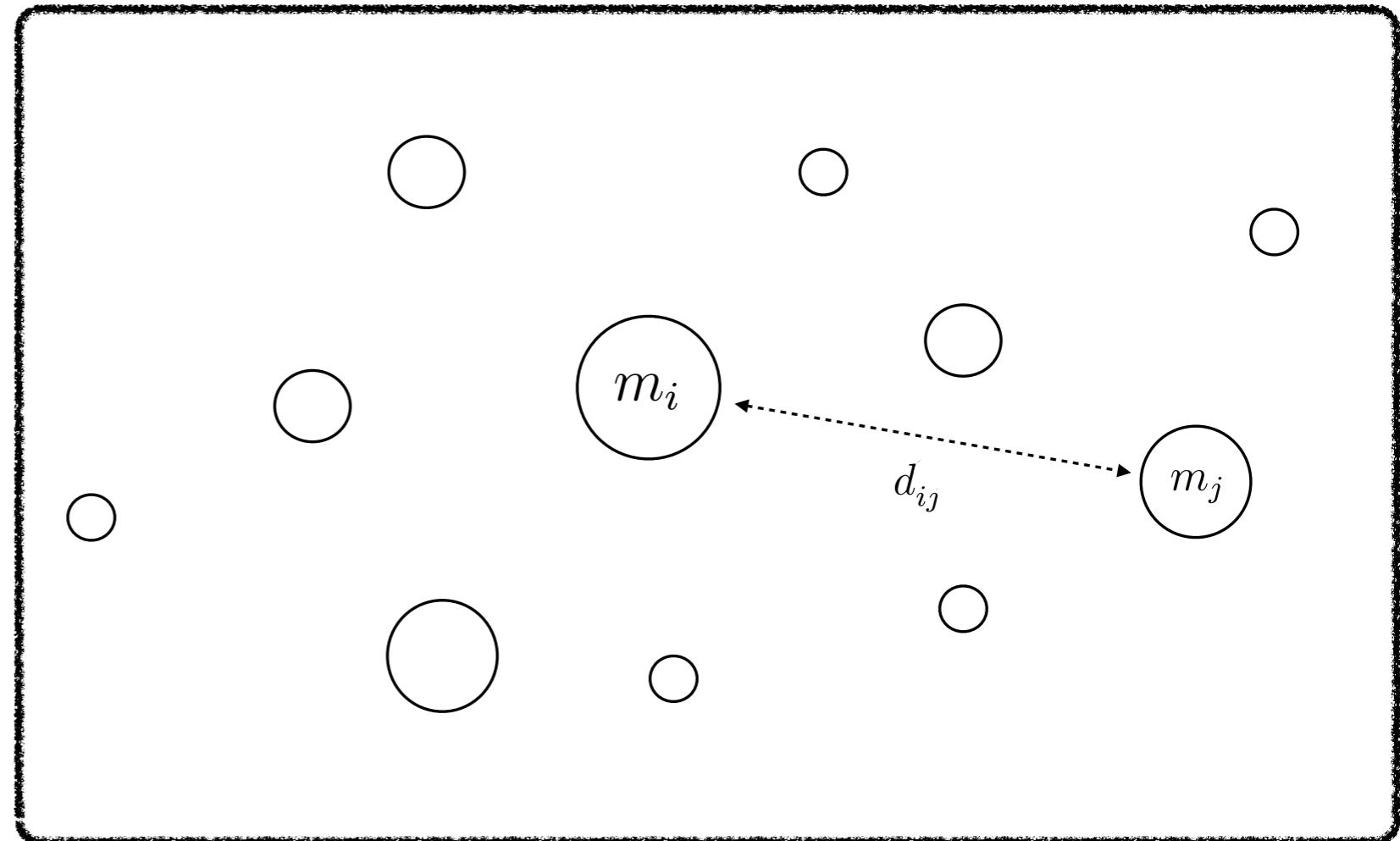
Data in urban transport modeling
has been based primarily on surveys...

$$T_{ij} = k \frac{O_i D_j}{d_{ij}^2}$$

Gravity Models



Inspired by Newtonian physics, gravity models suggest that two places attraction is proportional to their **mass** and inversely proportional to their **geographic distance**.

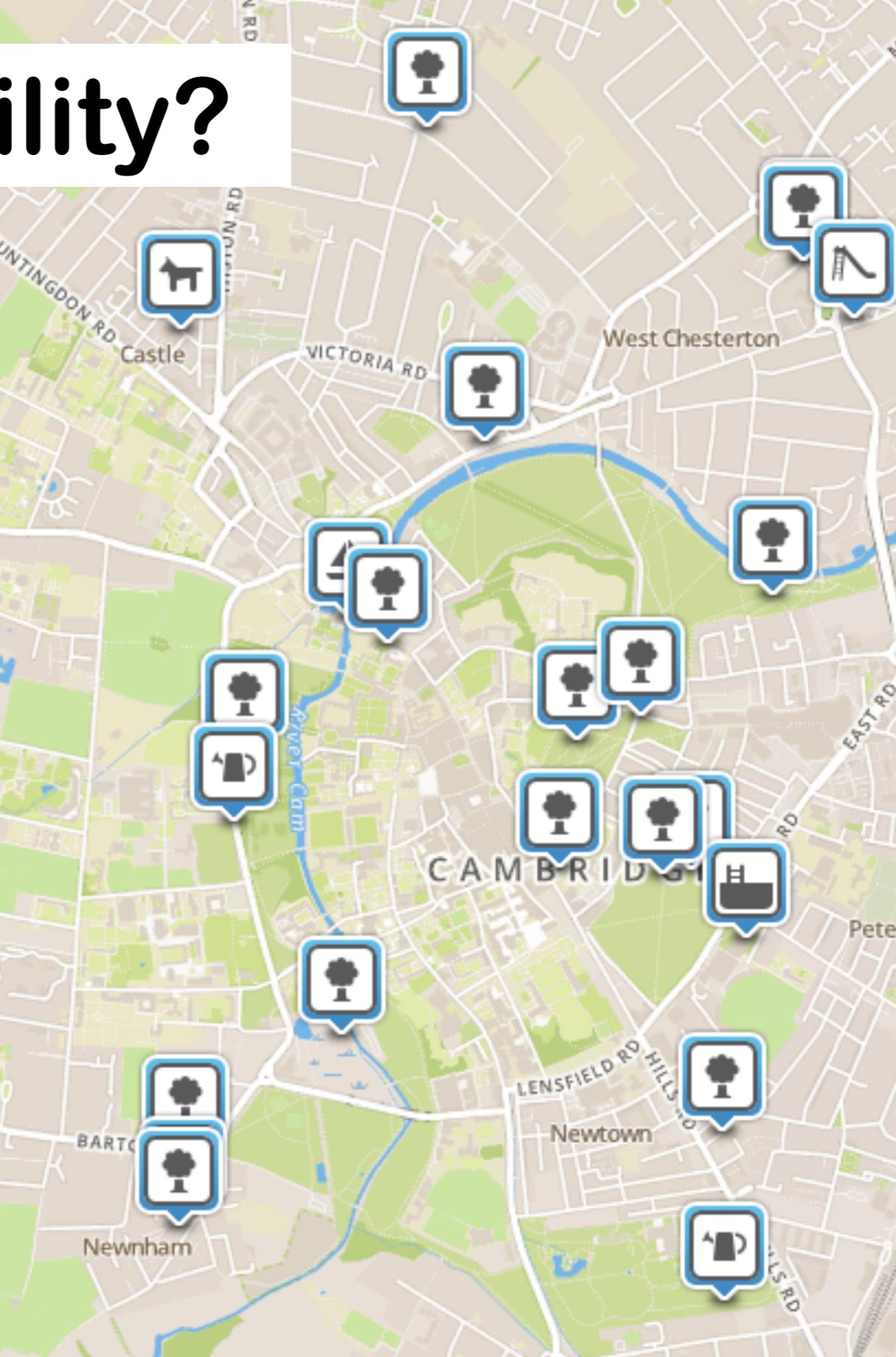


$$F_{ij} = \gamma \frac{m_i m_j}{d_{ij}^2}$$

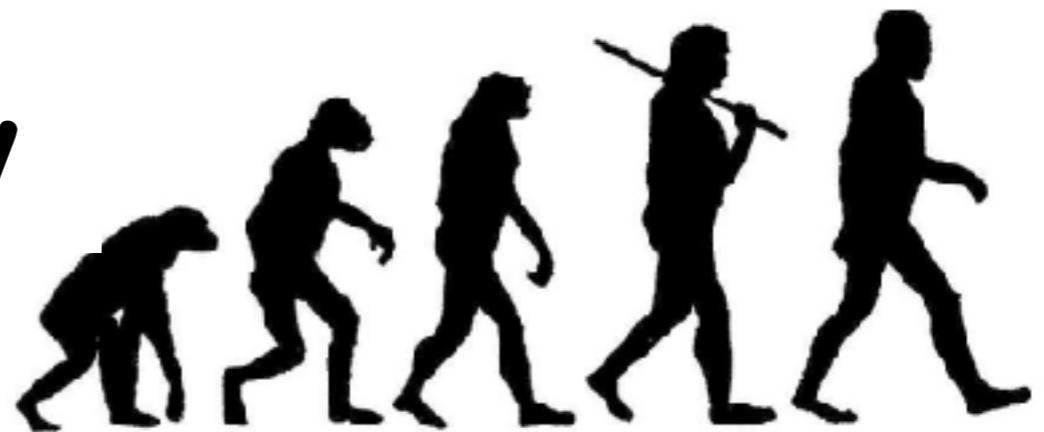
Why human mobility?

Urban planning :
understand the city and
optimise services

Mobile applications and
recommendations:
study the user and offer
services



Why human mobility



Animals have the capacity
to search and navigate
across space

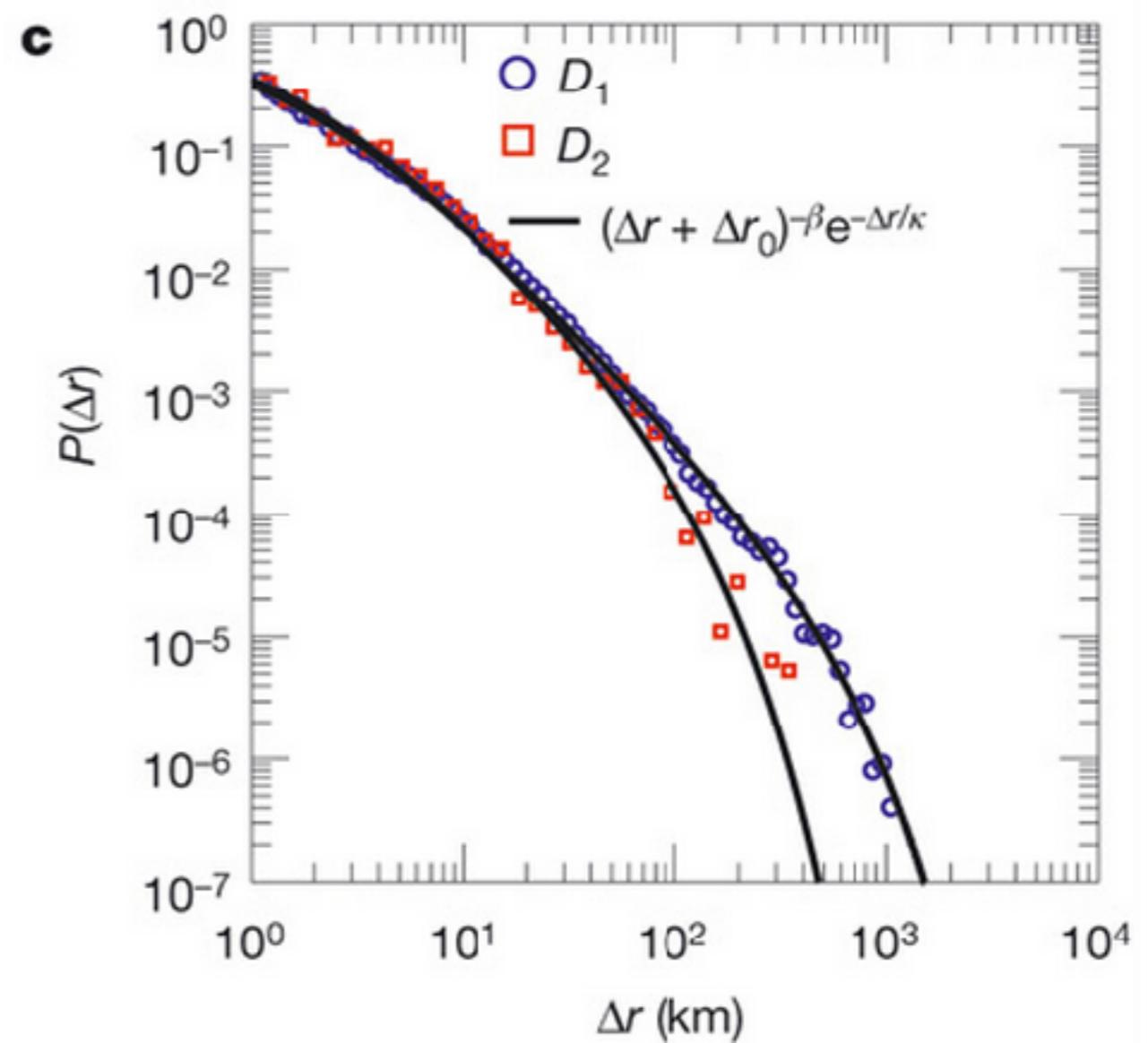
We can understand how
our brain is wired

Have we really left the
monkey ?



Cellular Datasets

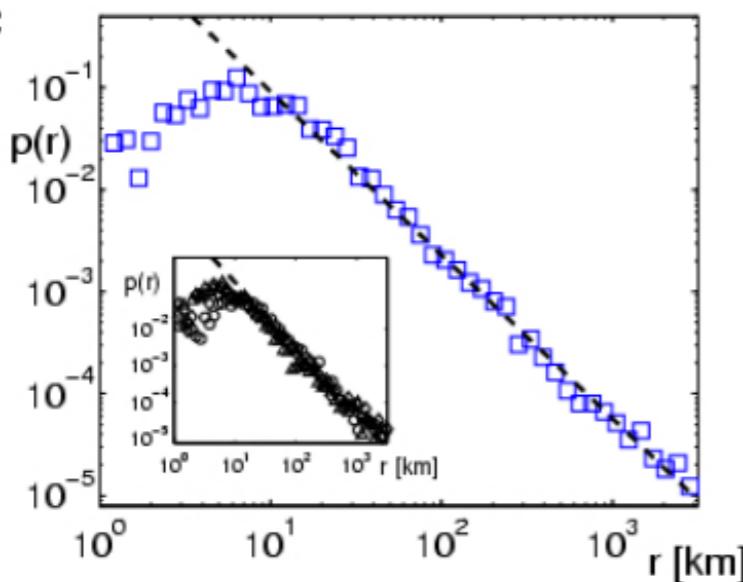
One of the first large scale studies of human movement with modern mobile datasets...



Gonzalez, Marta C., Cesar A. Hidalgo, and Albert-Laszlo Barabasi. "Understanding individual human mobility patterns." *Nature* 453.7196 (2008): 779-782.

Where's George ?

One of the most creative ways to study human movement that has used the displacement of dollar bills as a proxy to human mobility...



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Where's George?®

Please enter the Serial Number:

10 or 11 letters & digits
If the serial number has a 'star' use the * key (shift-8)

I have this bill right now: Yes No

My current Zip Code is: ?

You can enter any USA Zip or Canadian Postal Code.
If you do not know your Zip code: [Click Here](#)
International Visitors - [Click Here](#)

Continue >>>

Brockmann, Dirk, Lars Hufnagel, and Theo Geisel. "The scaling laws of human travel." *Nature* 439.7075 (2006): 462-465.

Data on human movement...

Mobile Social

VS

Cellular

GPS accuracy ~ 10 meters

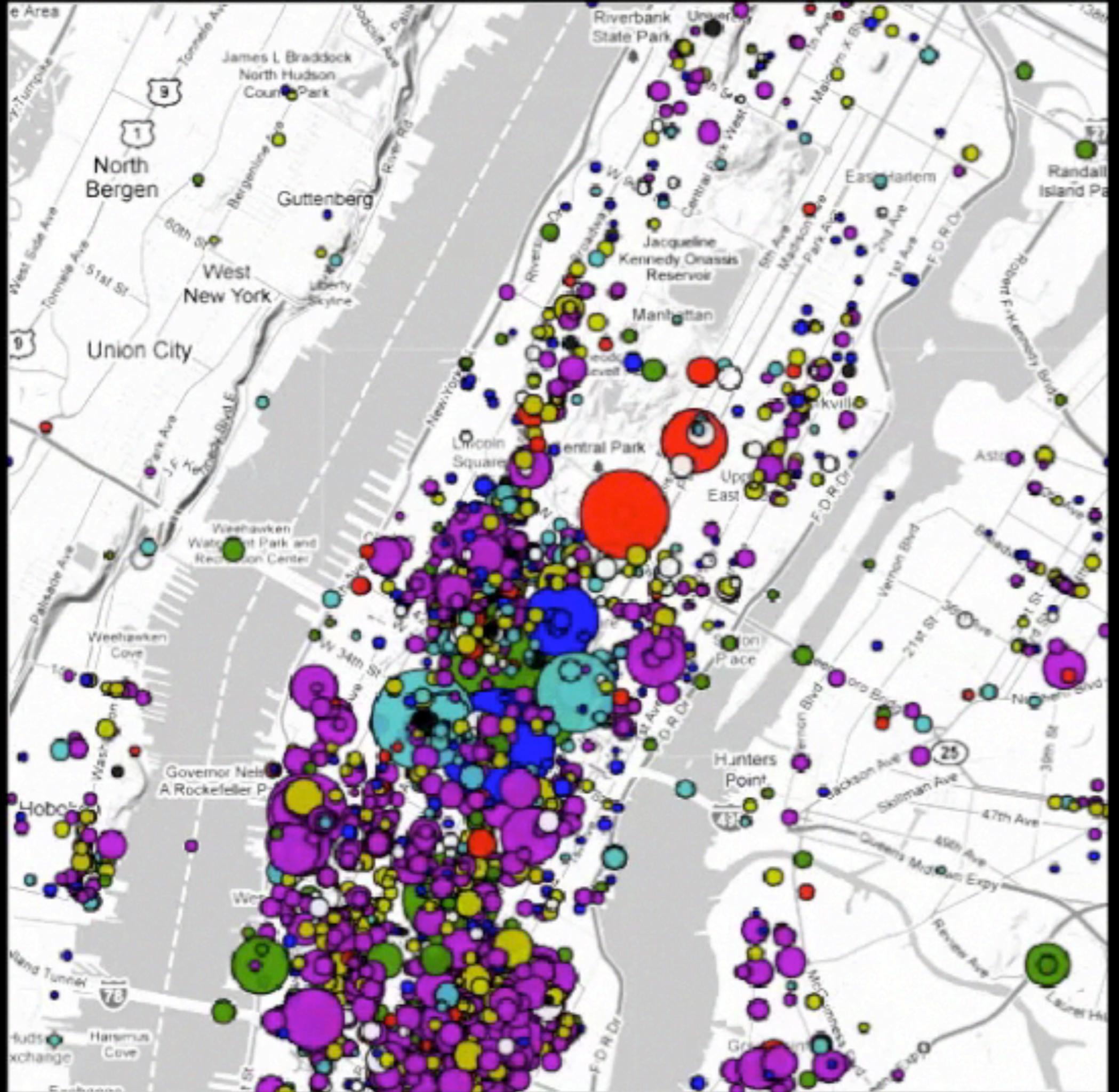
BTS Tower Accuracy ~ 1KM

Global Coverage

Country Coverage

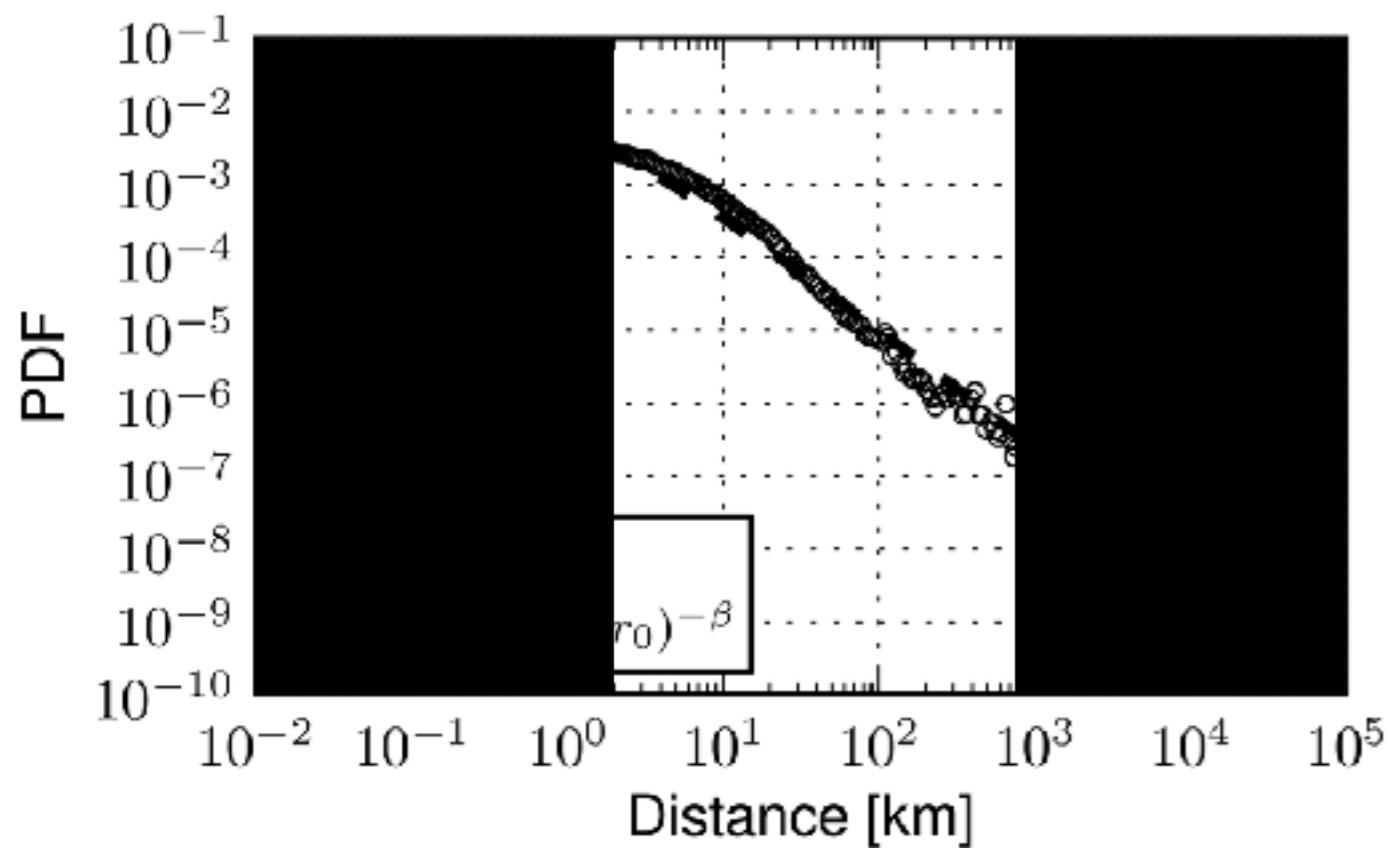
Publicly Available

Private / Corporate



Power-law tales ...

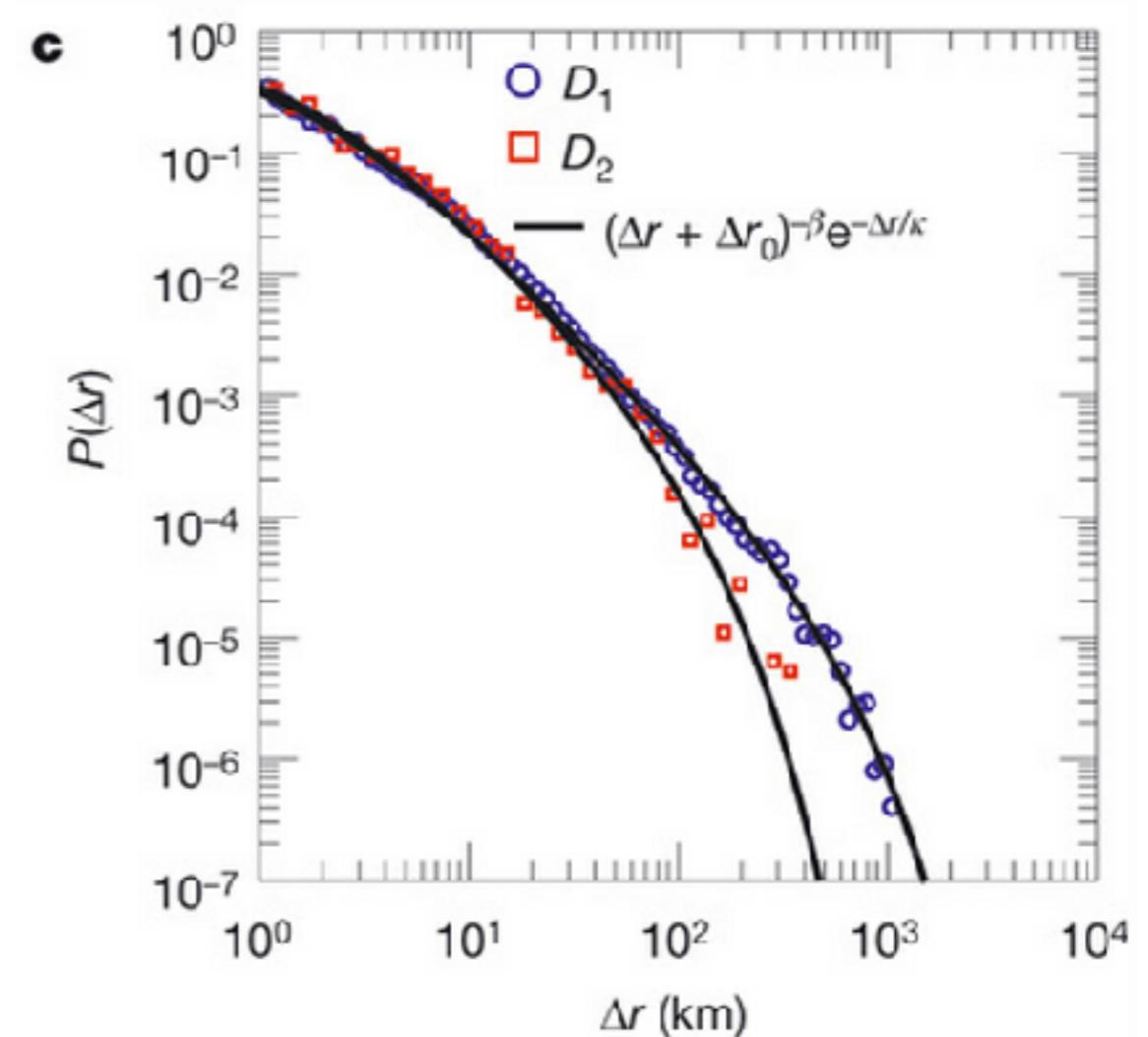
Mobile Social Network Data



$$(\Delta r + \Delta r_0)^{-\beta}$$

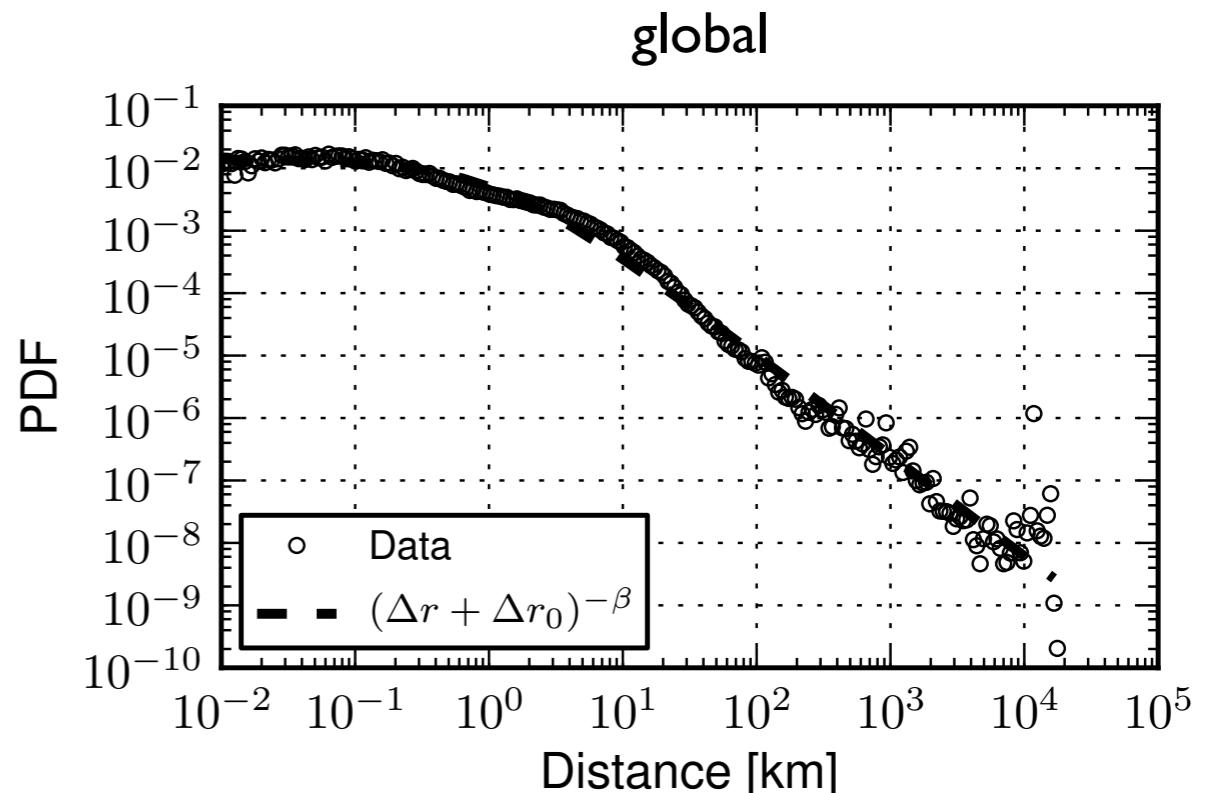
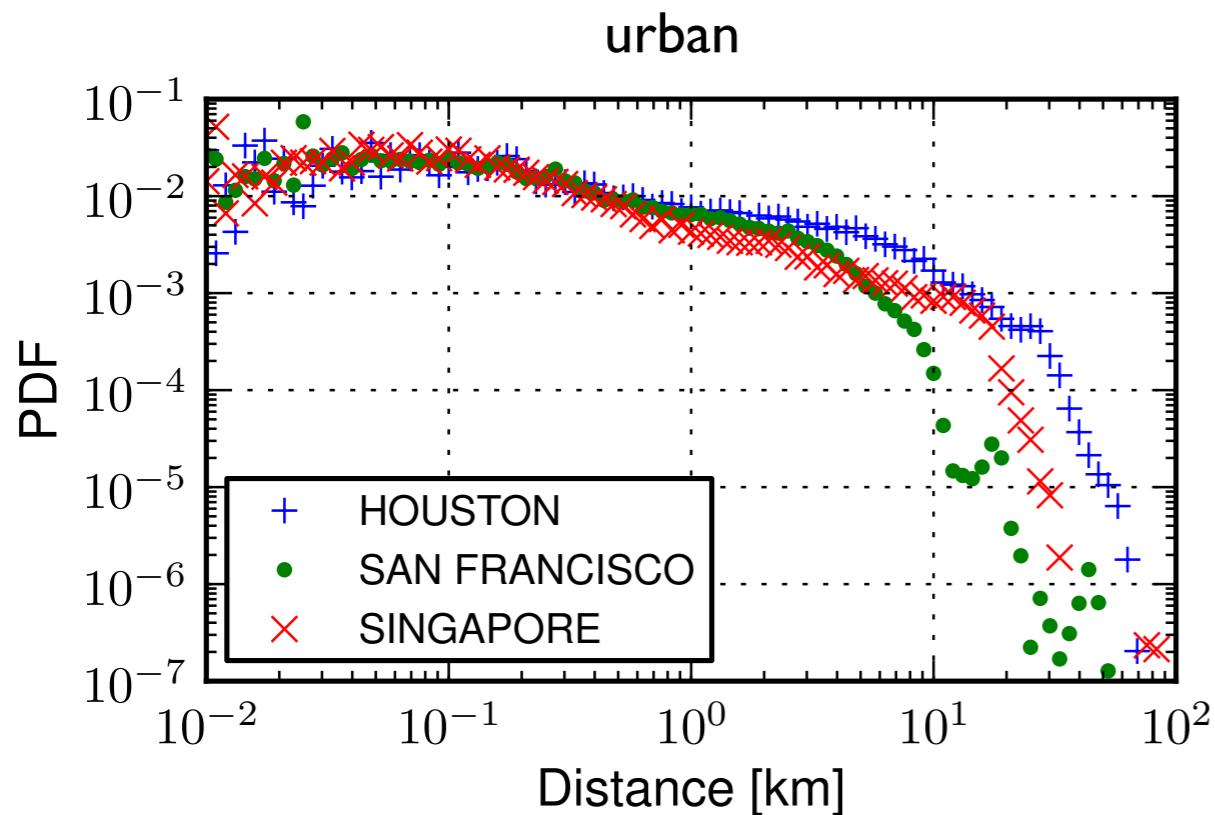
exponent $\beta = 1.50$

Nature **453**, 779-782(5 June 2008)



exponent $\beta = 1.75$

Urban vs Global mobility



Power law kicks in
at 18.42km!!!

A red arrow points upwards from the text towards the transition point on the urban mobility plot.

A tale of many cities: universal patterns in human urban mobility.

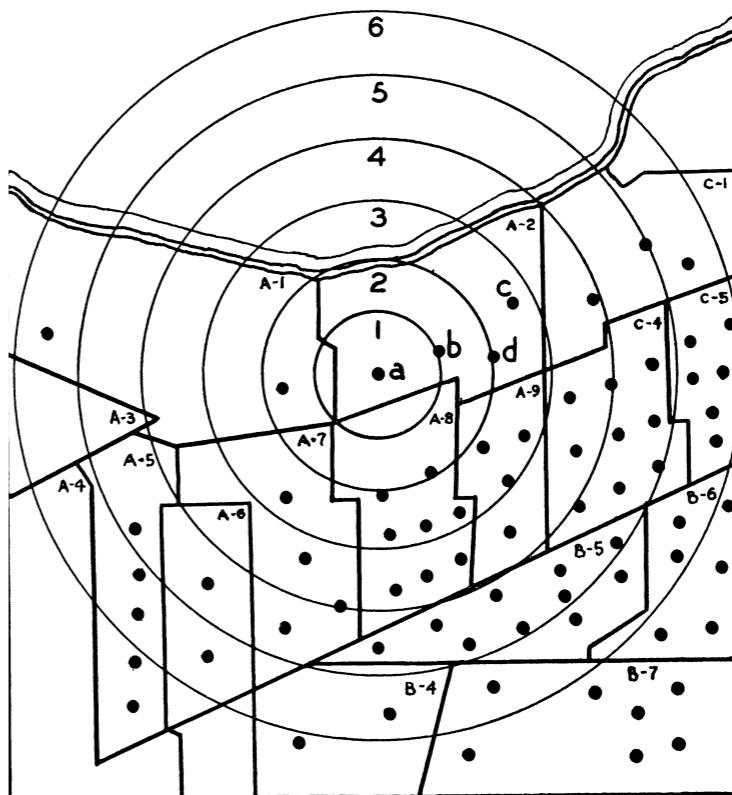
Anastasios Noulas, Salvatore Scellato, Renaud Lambiotte, Massimiliano Pontil, Cecilia Mascolo.

In PLoS ONE. PLoS ONE 7(5): e37027. doi:10.1371/journal.pone.0037027. 2012.



Samuel A. Stouffer

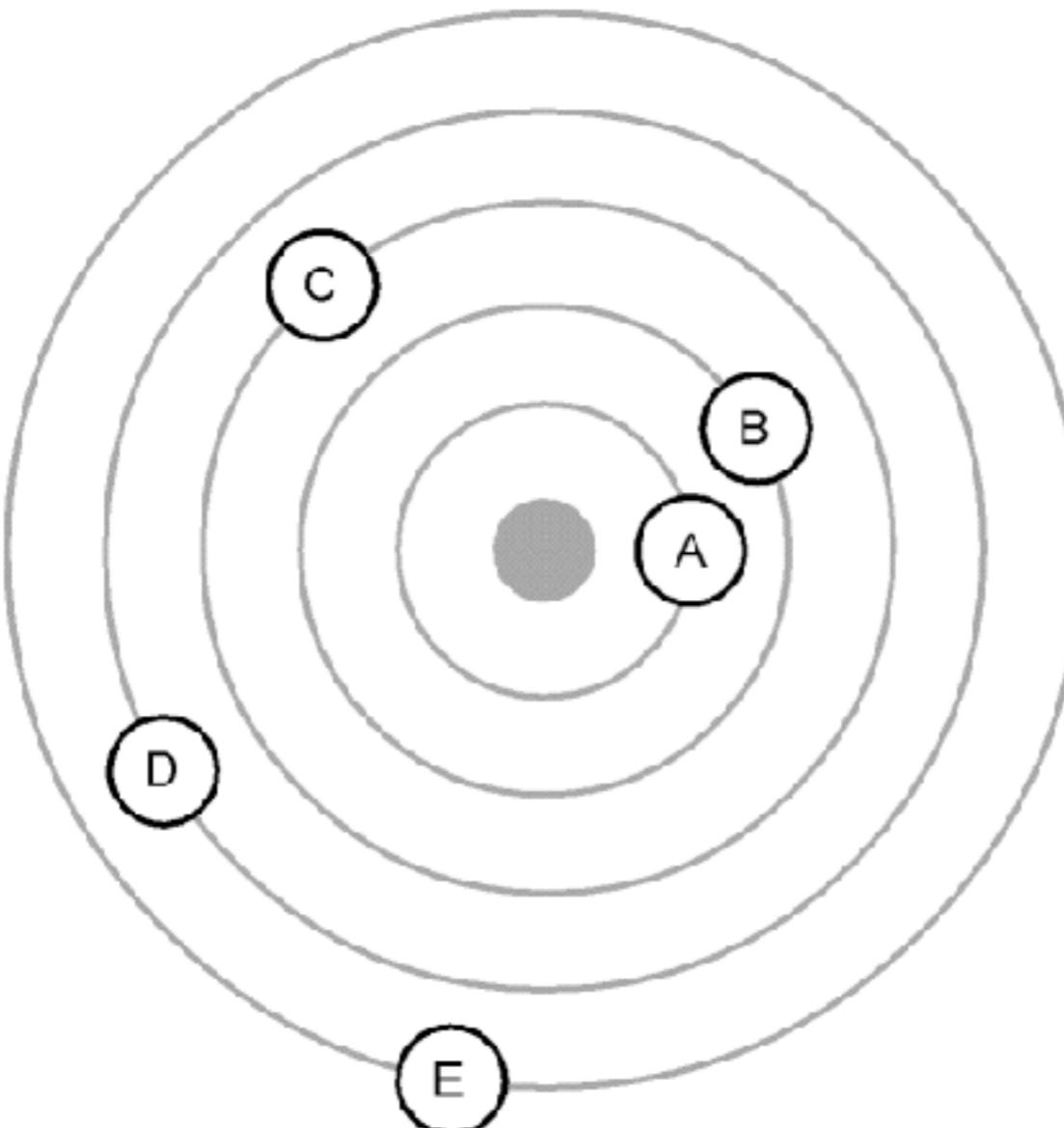
Stouffer's **law of intervening opportunities** states, "*The number of persons going a given distance is directly proportional to the number of opportunities at that distance and inversely proportional to the number of intervening opportunities.*" *



- Empirically proven using data for migrating families in the city of Cleveland.
- Inspired a host of recent works on human mobility modelling.

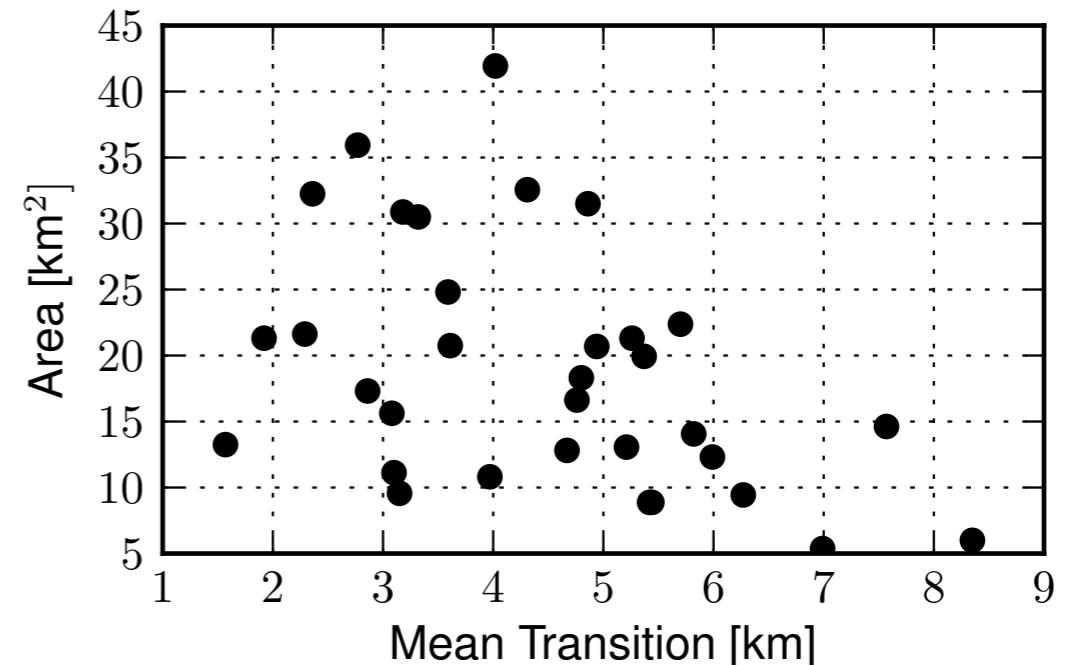
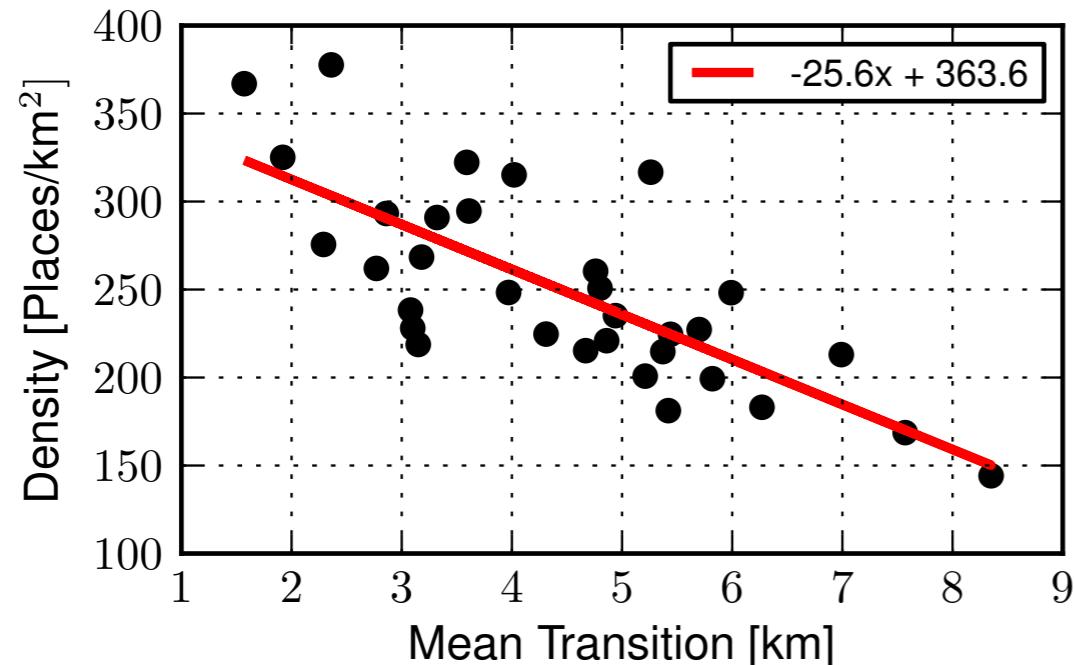
* S. Stouffer (1940) **Intervening opportunities: A theory relating mobility and distance**, American Sociological Review 5, 845-867

Rank-Distance



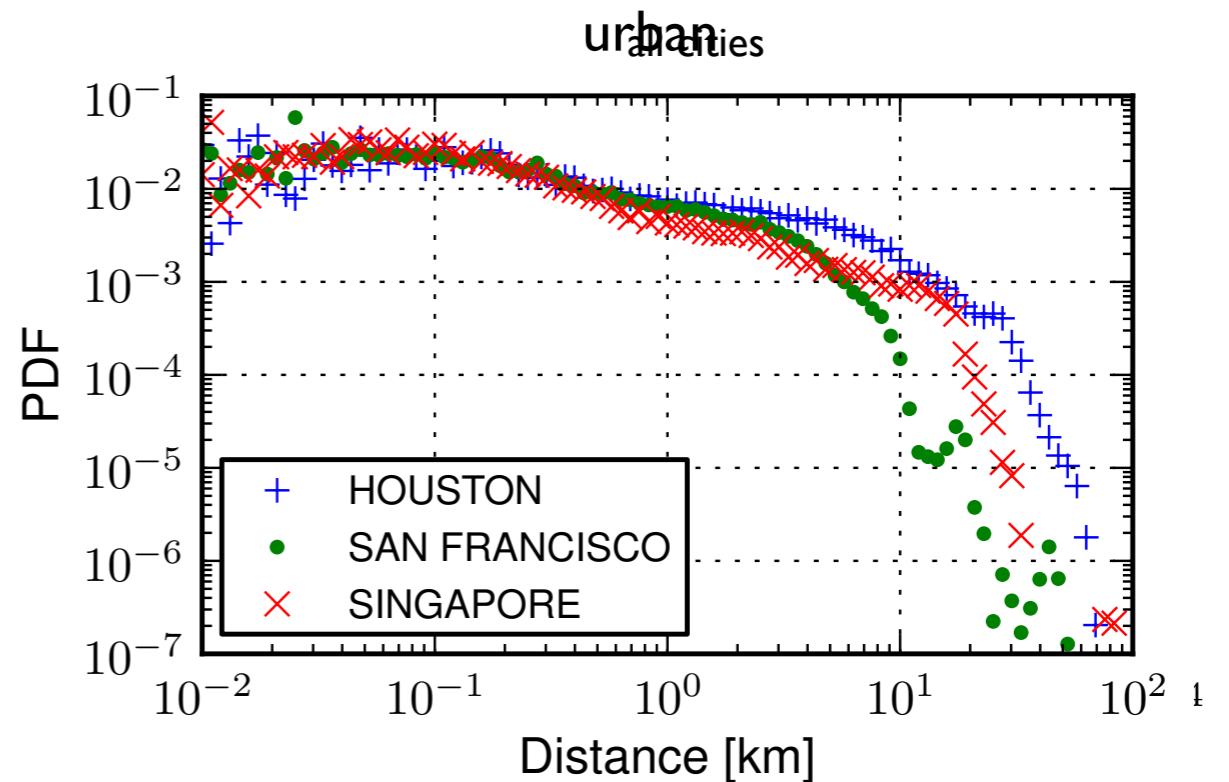
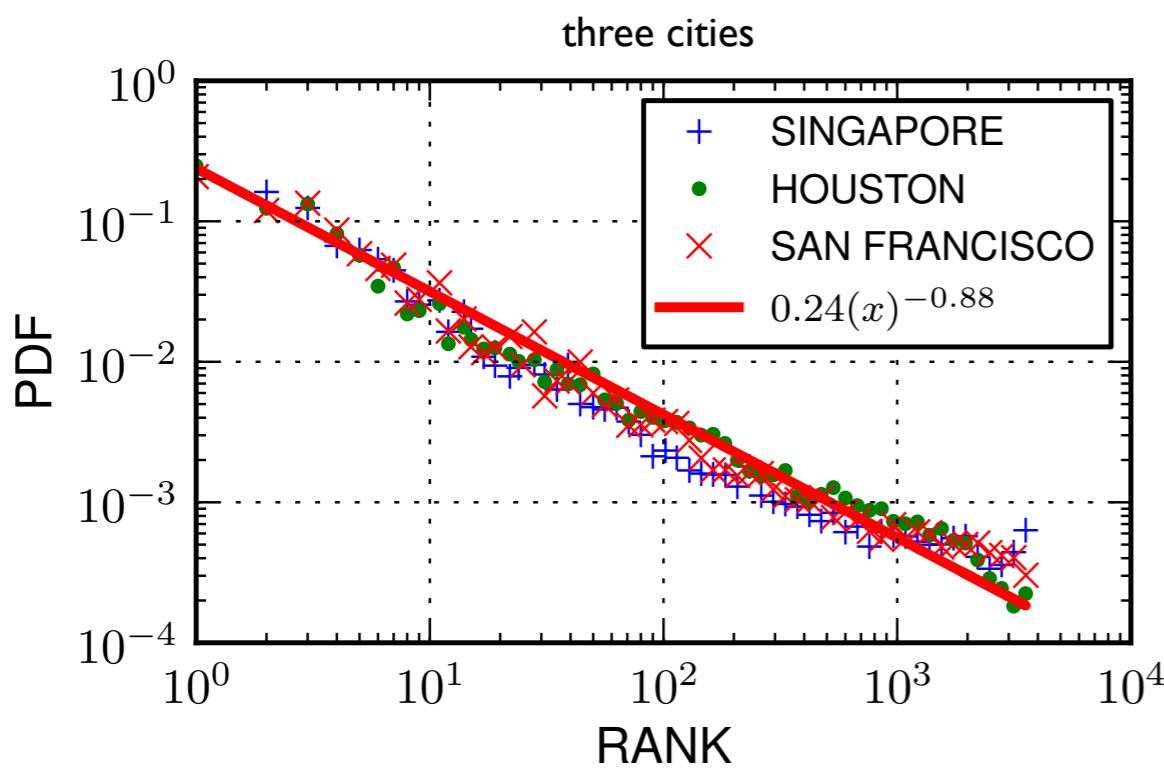
$$\text{rank}_u(v) = |\{w : d(u, w) < d(u, v)\}|$$

The importance of density



- Stouffer's Theory of Intervening Opportunities motivated us to inspect the impact of places(=opportunities) in human mobility.
- Place density by far more important than the city area size with respect to mean length of human movements ($R^2 = 0.59$ and 0.19 respectively).

Rank universality

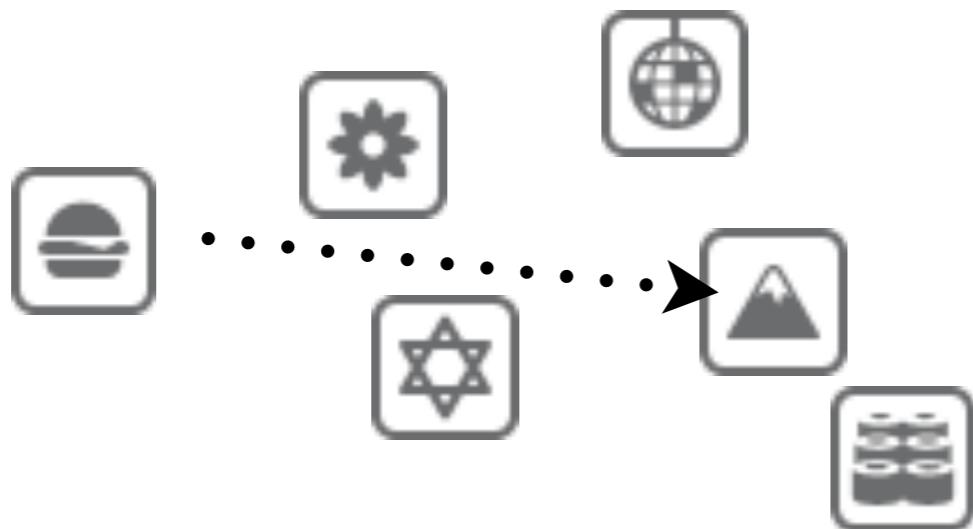


The rank of all cities collapse to a single line.

We have measured a power law exponent $\alpha = 0.84 \pm 0.07$

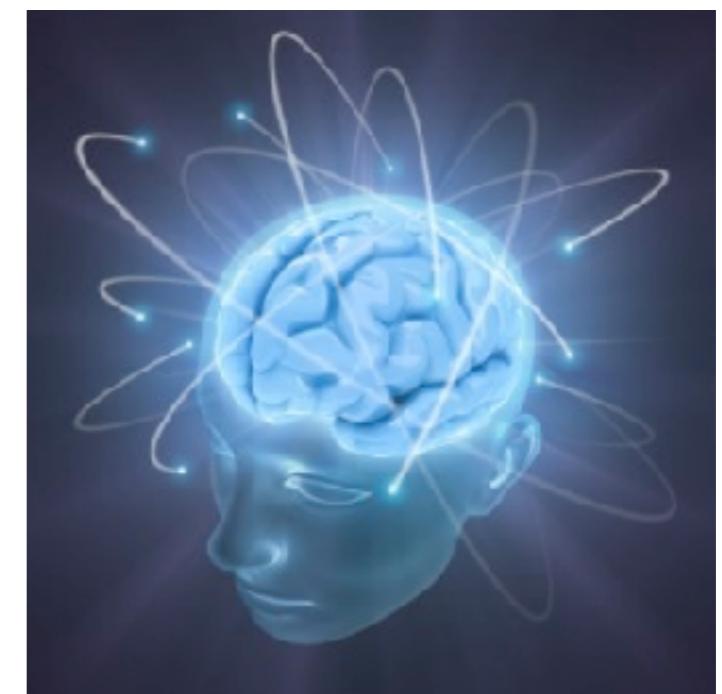
Decoupling cognition & space

soil...

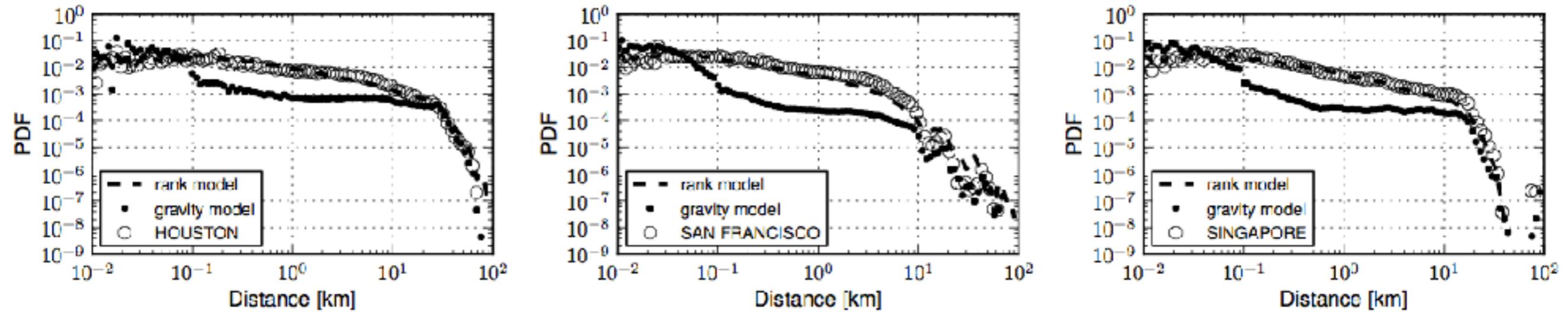


and mind!

$$Pr[u \rightarrow v] \propto \frac{1}{rank_u(v)^a}$$



Rank vs Gravity



Rank is simpler and achieves better quality fits for all cities.

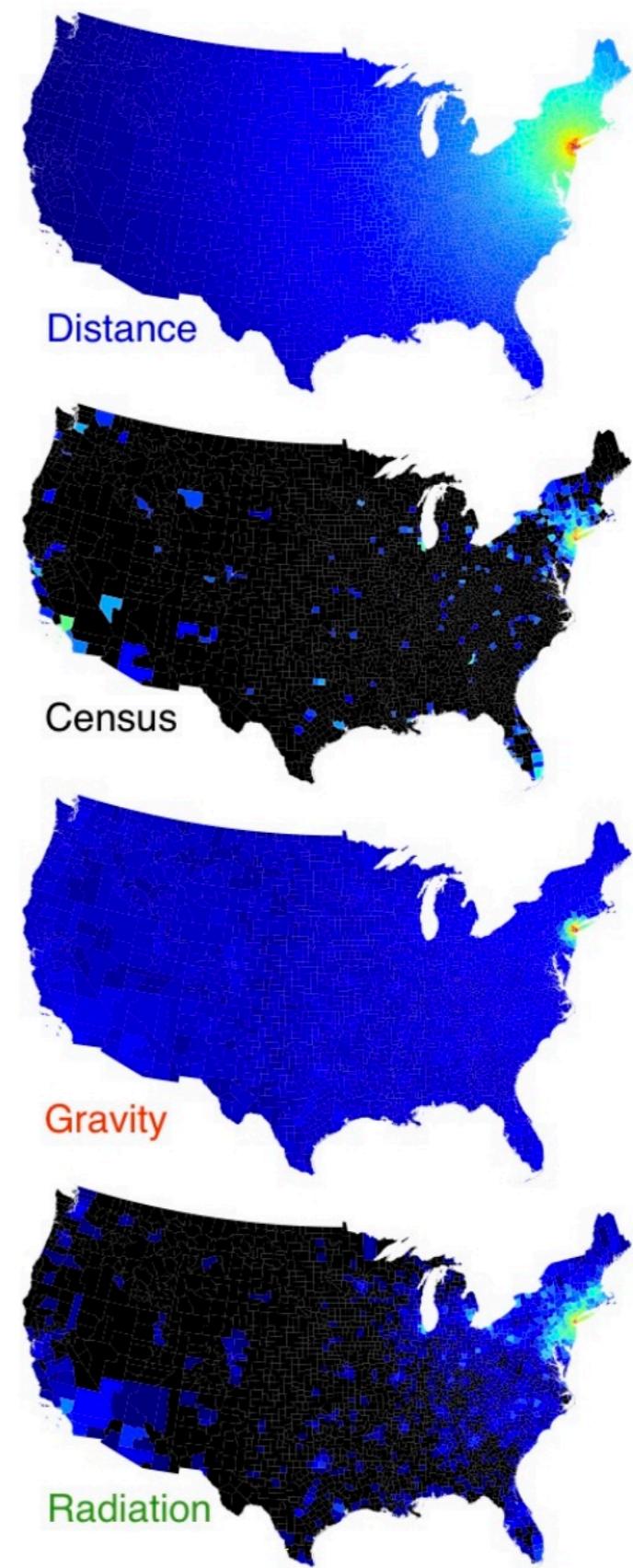
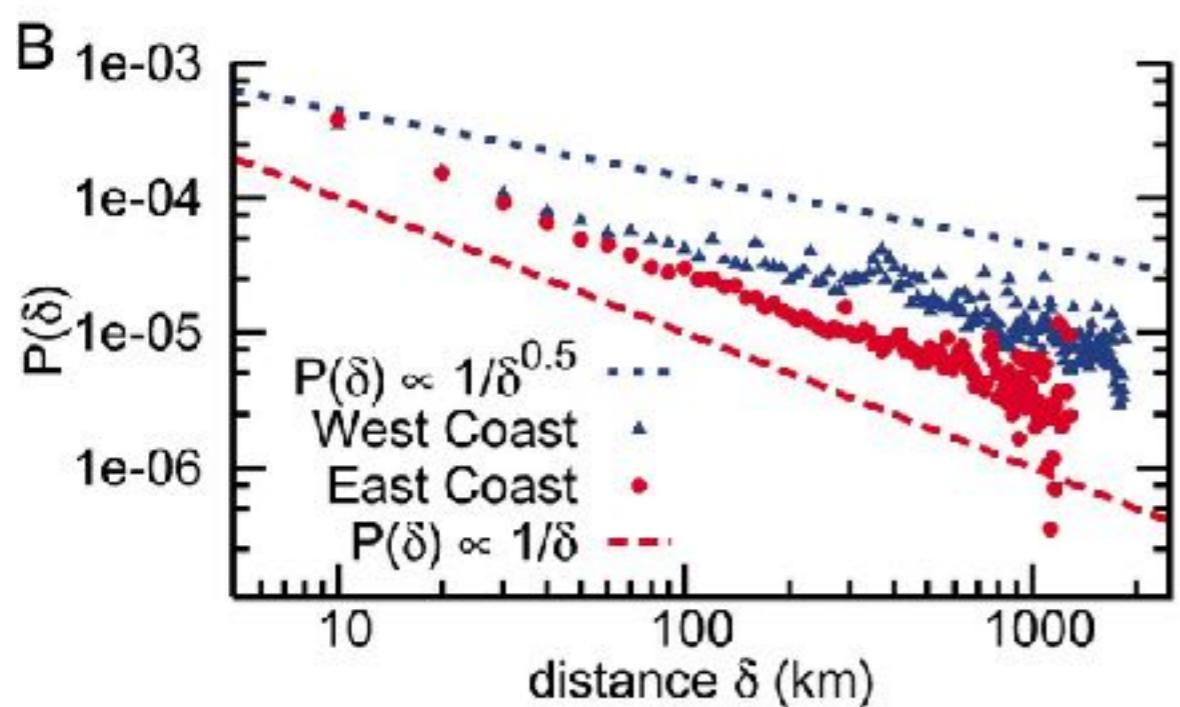
Gravity overestimates short transitions ...

A tale of many cities: universal patterns in human urban mobility.

Anastasios Noulas, Salvatore Scellato, Renaud Lambiotte, Massimiliano Pontil, Cecilia Mascolo.
In PLoS ONE. PLoS ONE 7(5): e37027. doi:10.1371/journal.pone.0037027. 2012.



Liben-Nowell, David, et al. "Geographic routing in social networks." PNAS 2005



Simini, Filippo, et al. "A universal model for mobility and migration patterns." Nature (2012)

$$\langle T_{ij} \rangle = T_i \frac{m_i n_j}{(m_i + s_{ij})(m_i + n_j + s_{ij})}$$

Abstraction Perspectives in human mobility

**complex systems
physics**

simple

**computationally
demanding
models**

complex

inter-mediate complexity,
the “undecided”!

**abstraction
level**

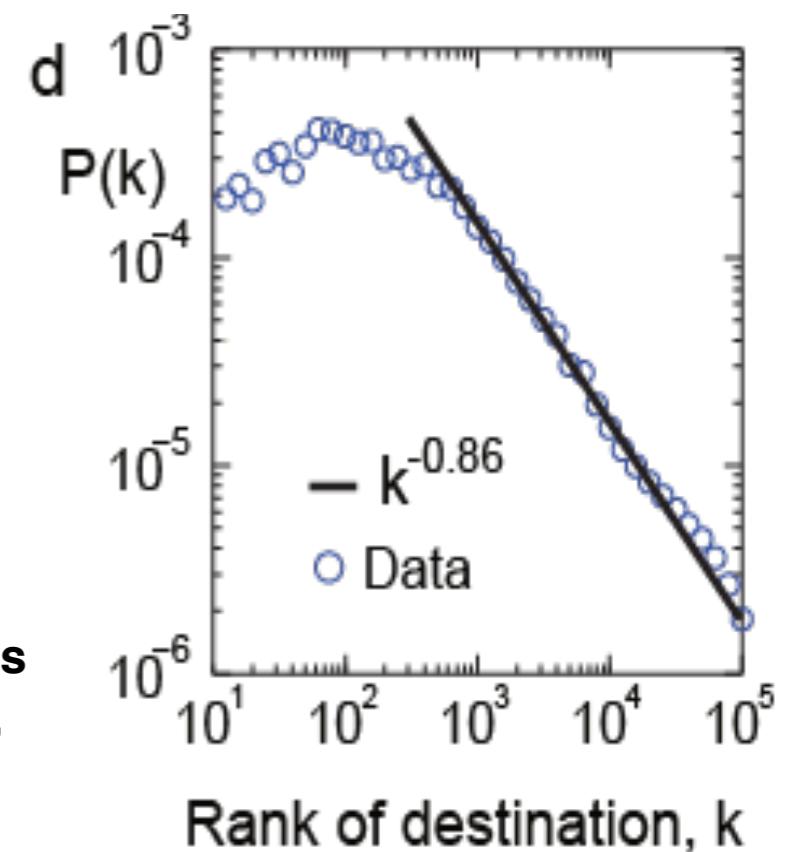
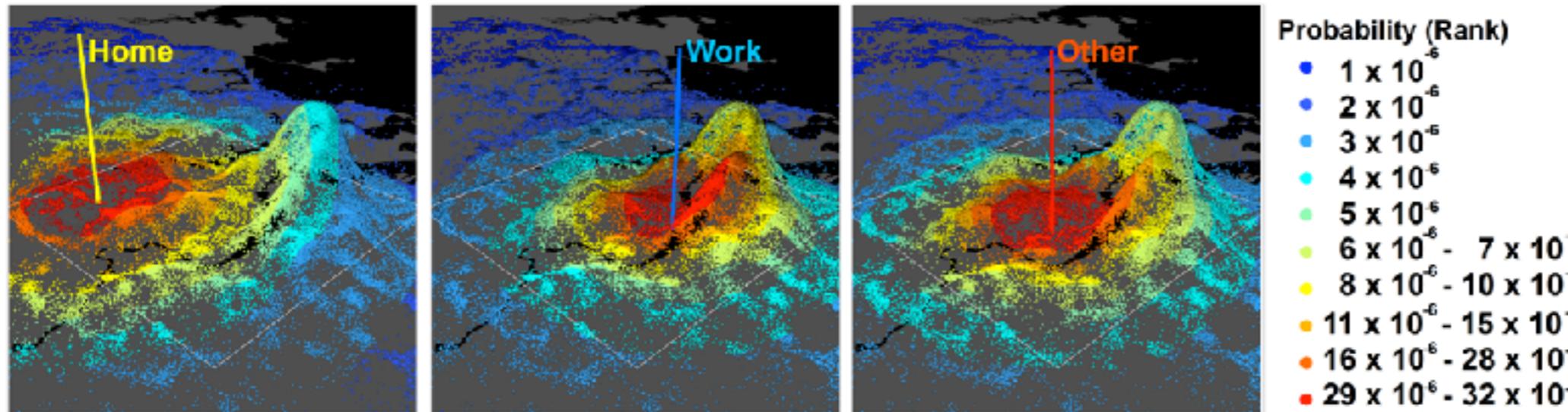
**favour
understanding**

less data

**favour
applications**

more data

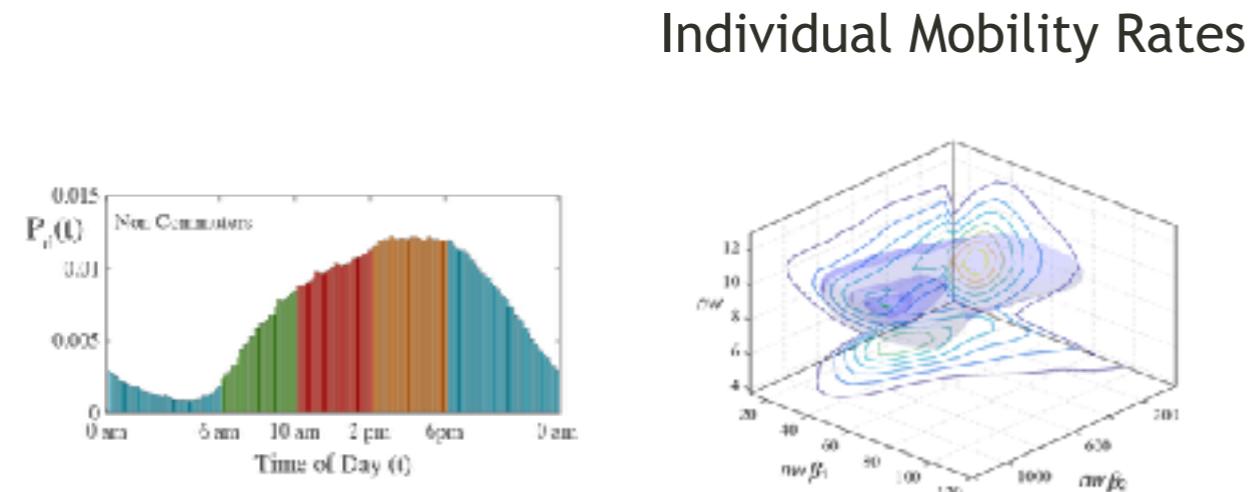
Ranking of POIs to select New Destination



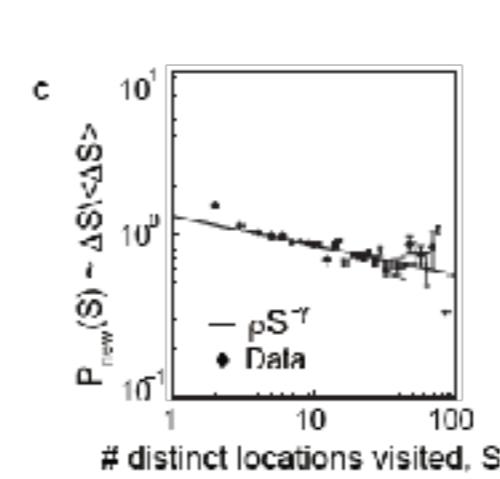
TimeGeo: a spatiotemporal framework for modeling urban mobility without surveys
Yingxiang Yang, Shan Jiang, Daniele Veneziano, Shounak Athavale, Marta C. Gonzalez,
PNAS (reviewed and resubmitted), 2016

The Model

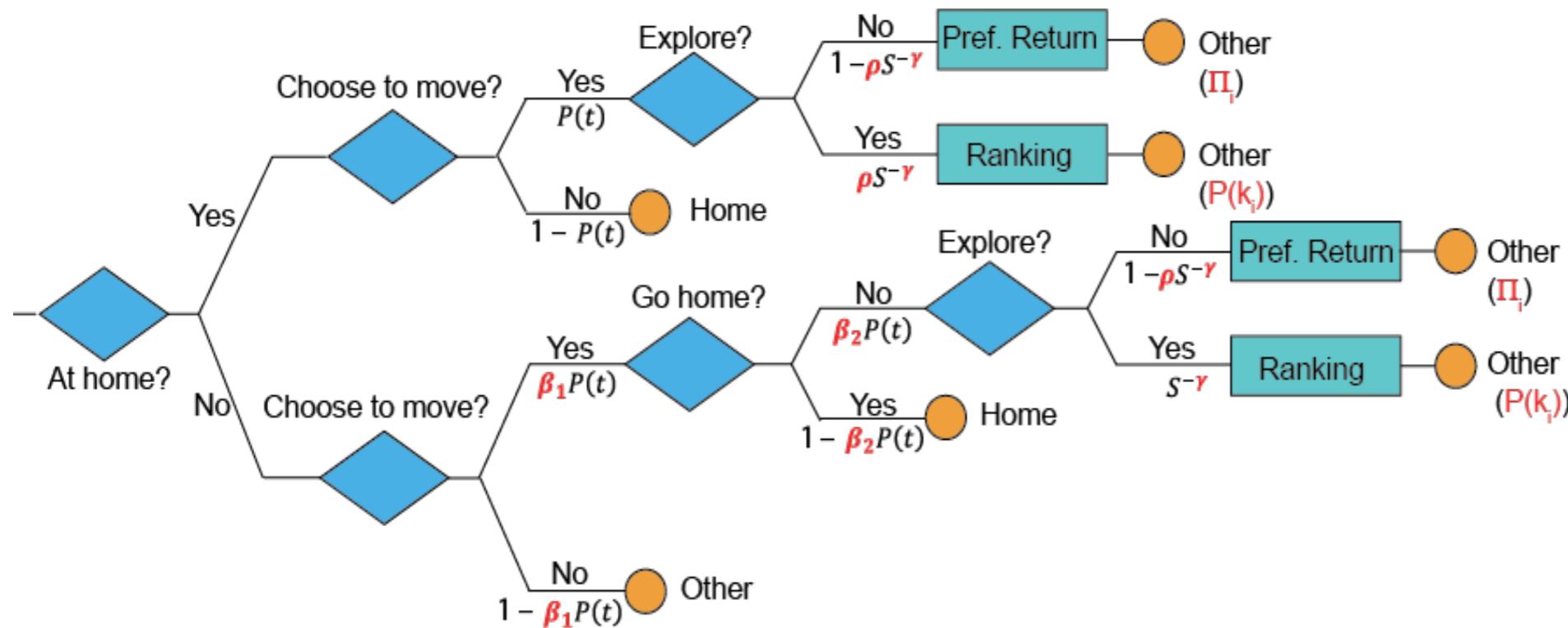
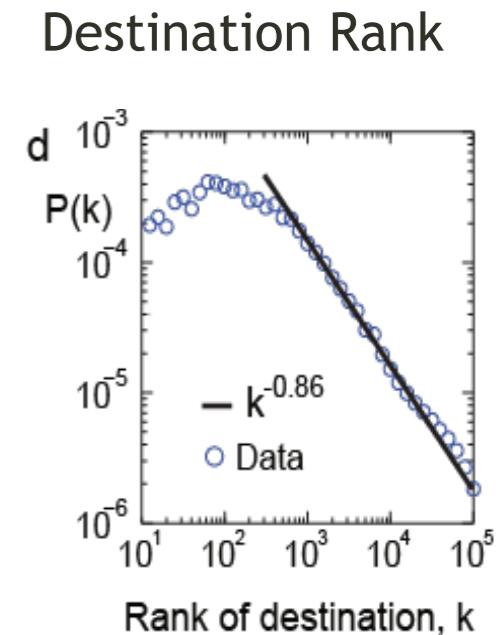
Features Extracted from data of Active Users



Global Trip probability



Preferential Return



Data layers need data mining

User Specific features

- historic visits
- friend check-ins
- preferred venue types



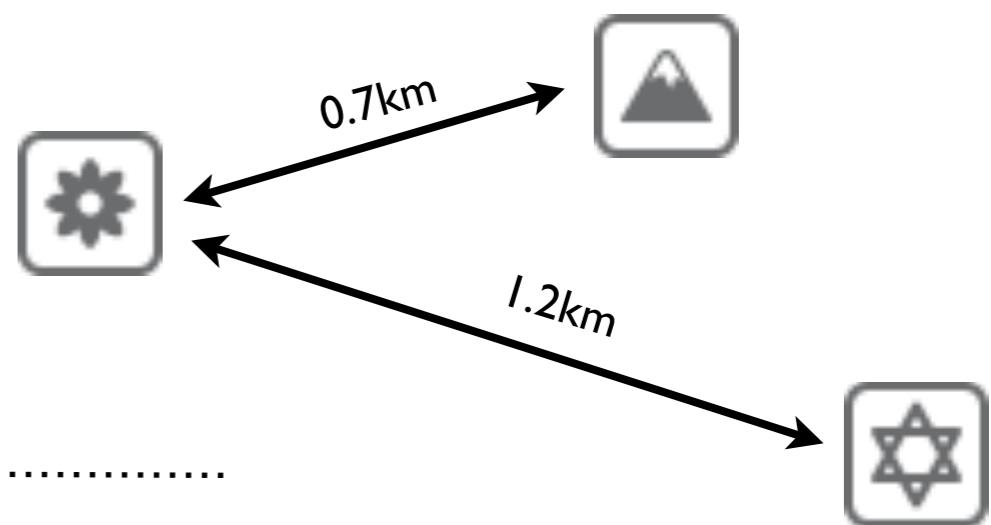
Temporal

- trending places (hour/day)
- trending place types (eg. cinema at nights)

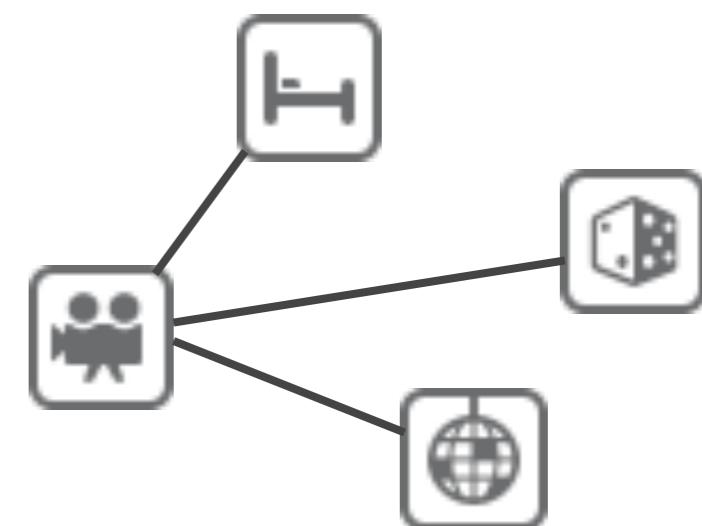


Geographic

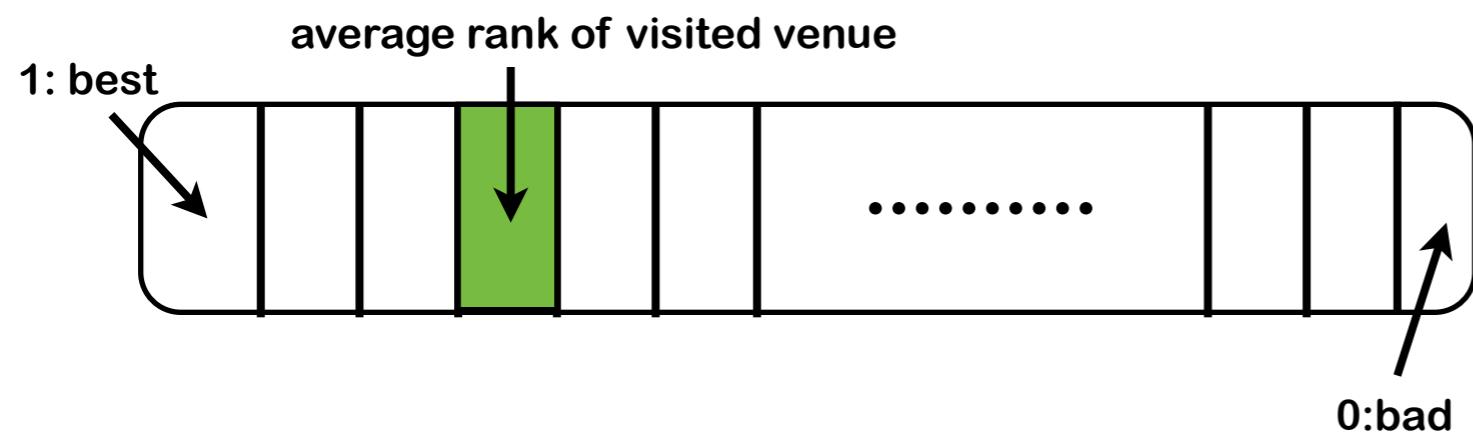
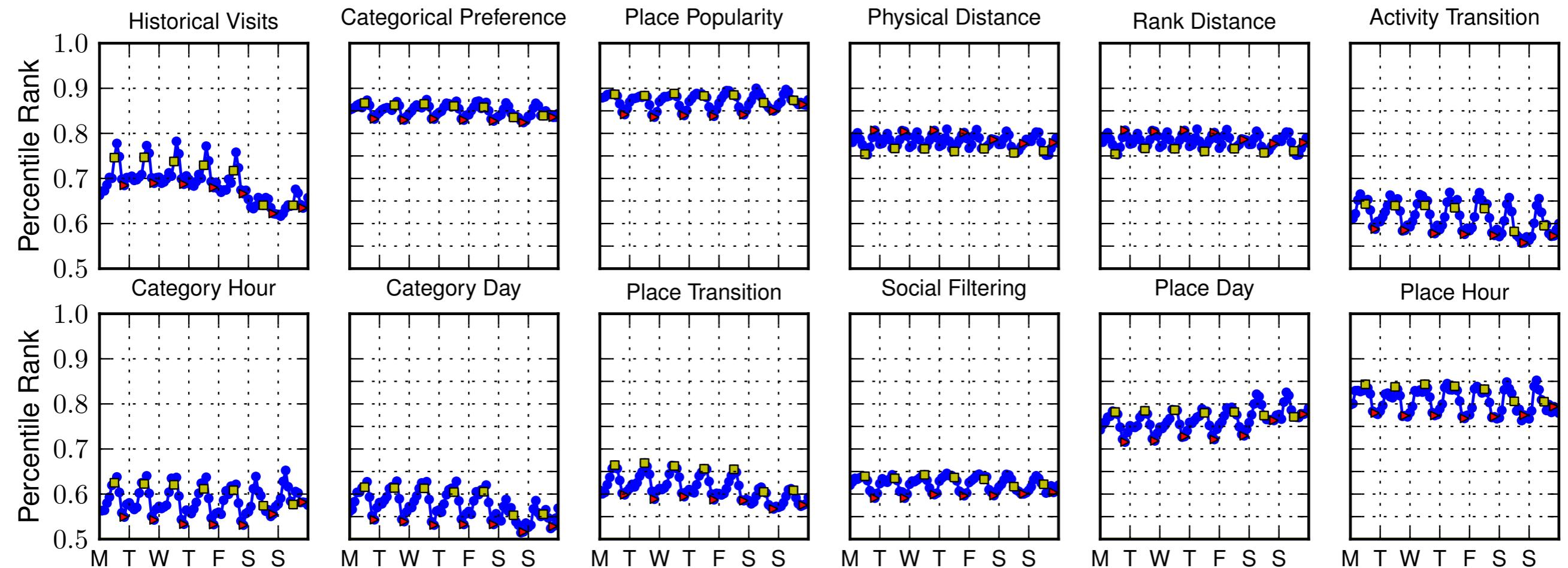
- distance and rank-distance



Place Network



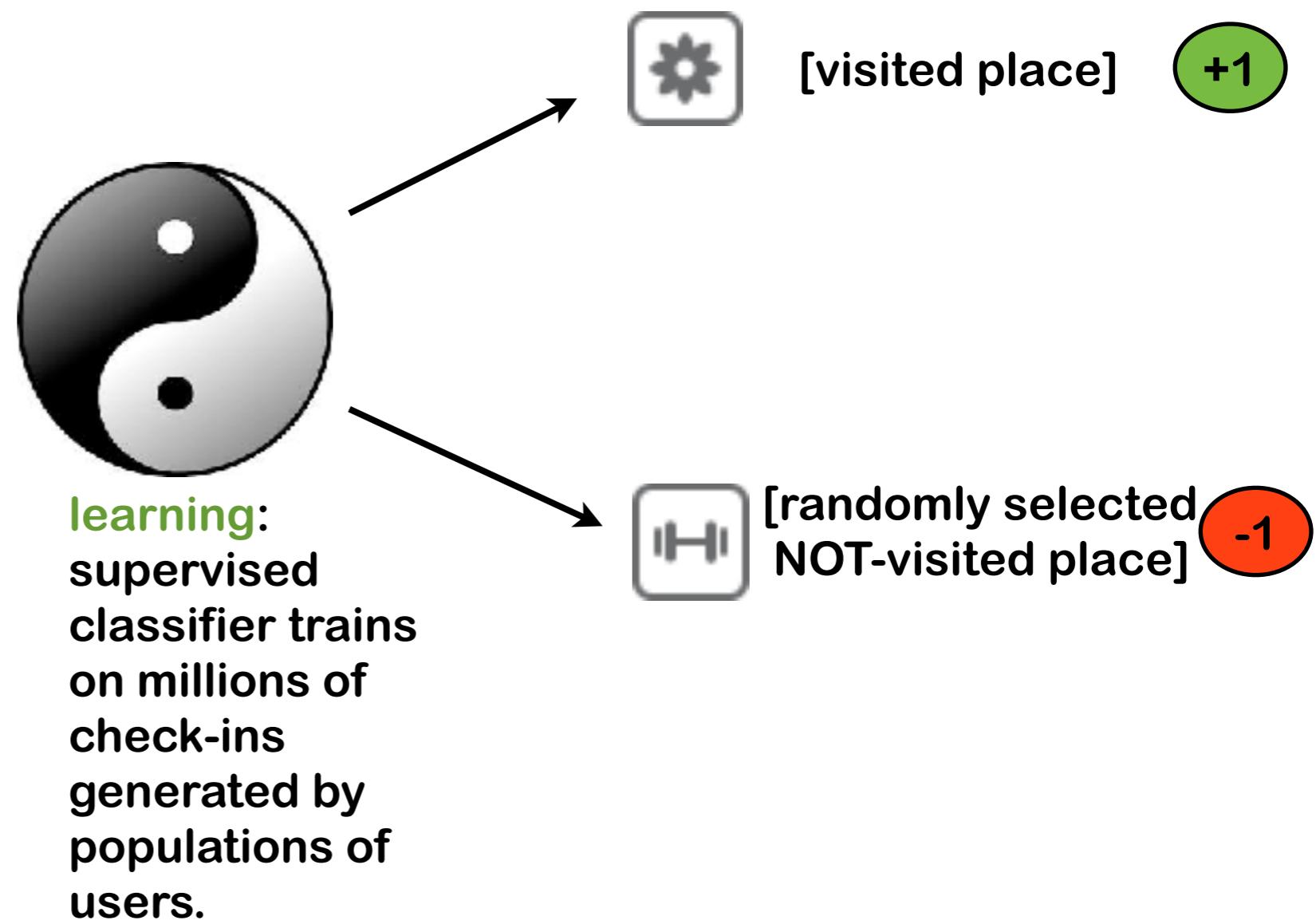
Modern data is rich



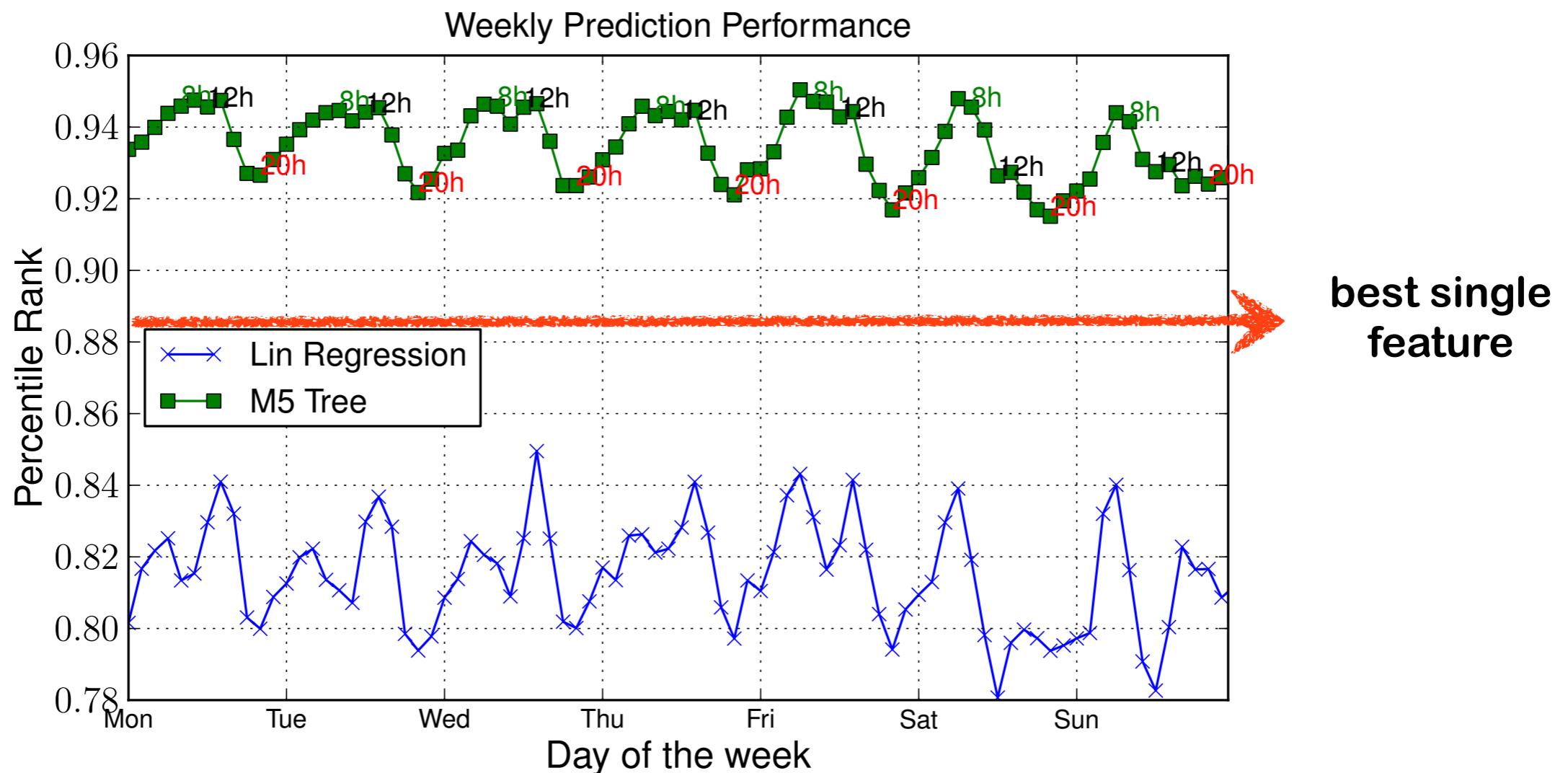
Supervised Training: teaching the good and the bad!



Key Insight: Every time little Amy checks-in she expresses a direct preference at a place and implicitly ignores all the rest!



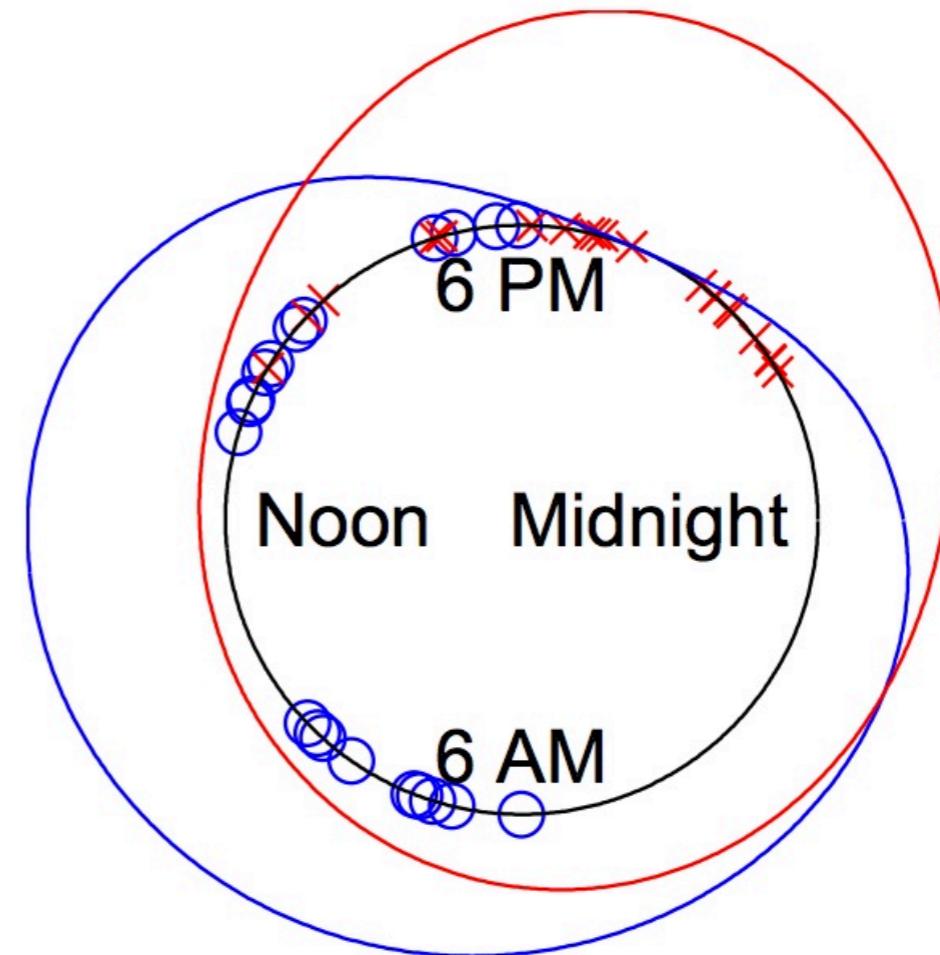
Supervised Learning Scores!



Probabilistic Models



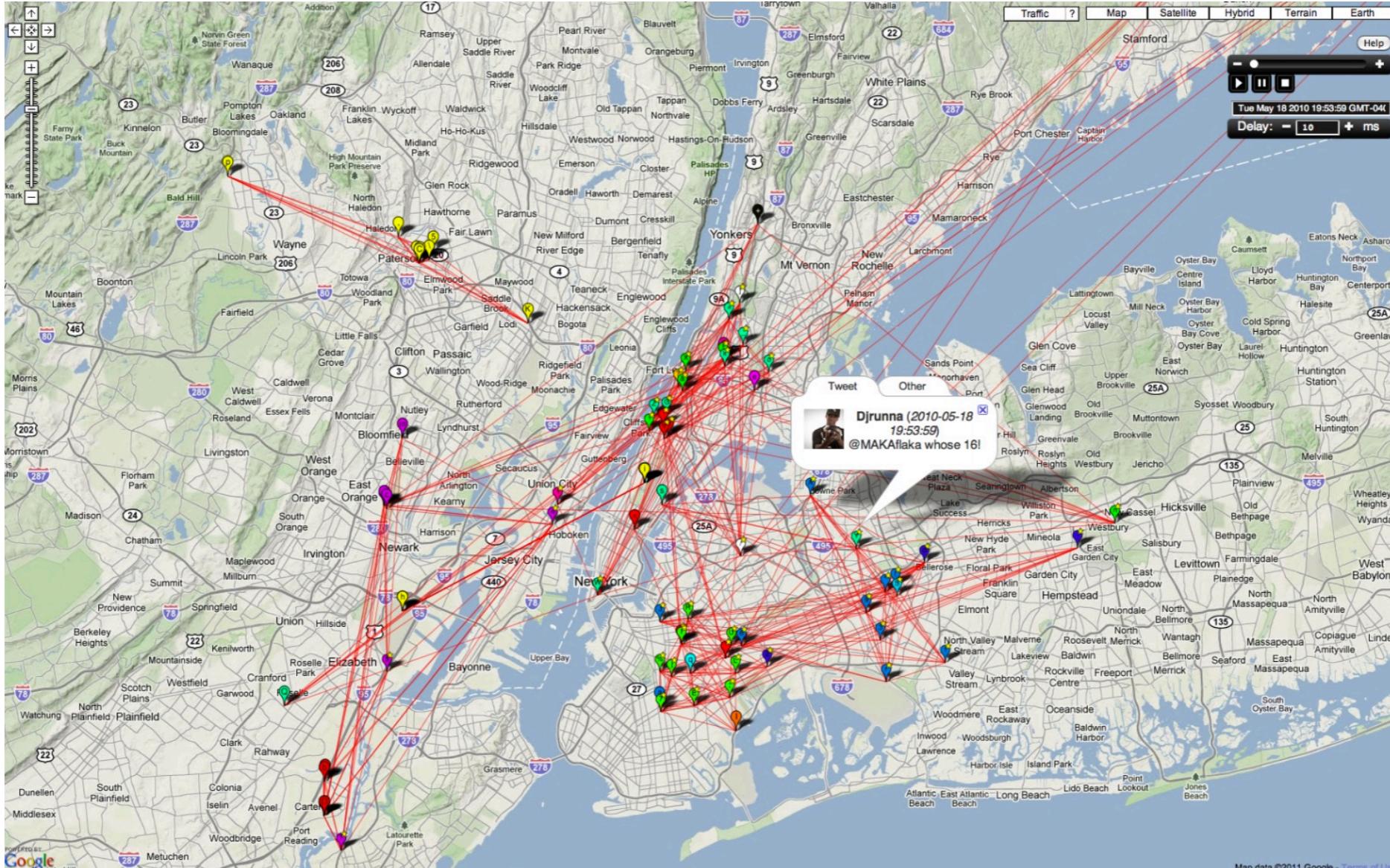
(a) Spatial model



(b) Temporal model

$$\begin{aligned} P [x(t) = x] &= P [x_u(t) = x | c_u(t) = H] \cdot P [c_u(t) = H] \\ &\quad + P [x_u(t) = x | c_u(t) = W] \cdot P [c_u(t) = W] \end{aligned}$$

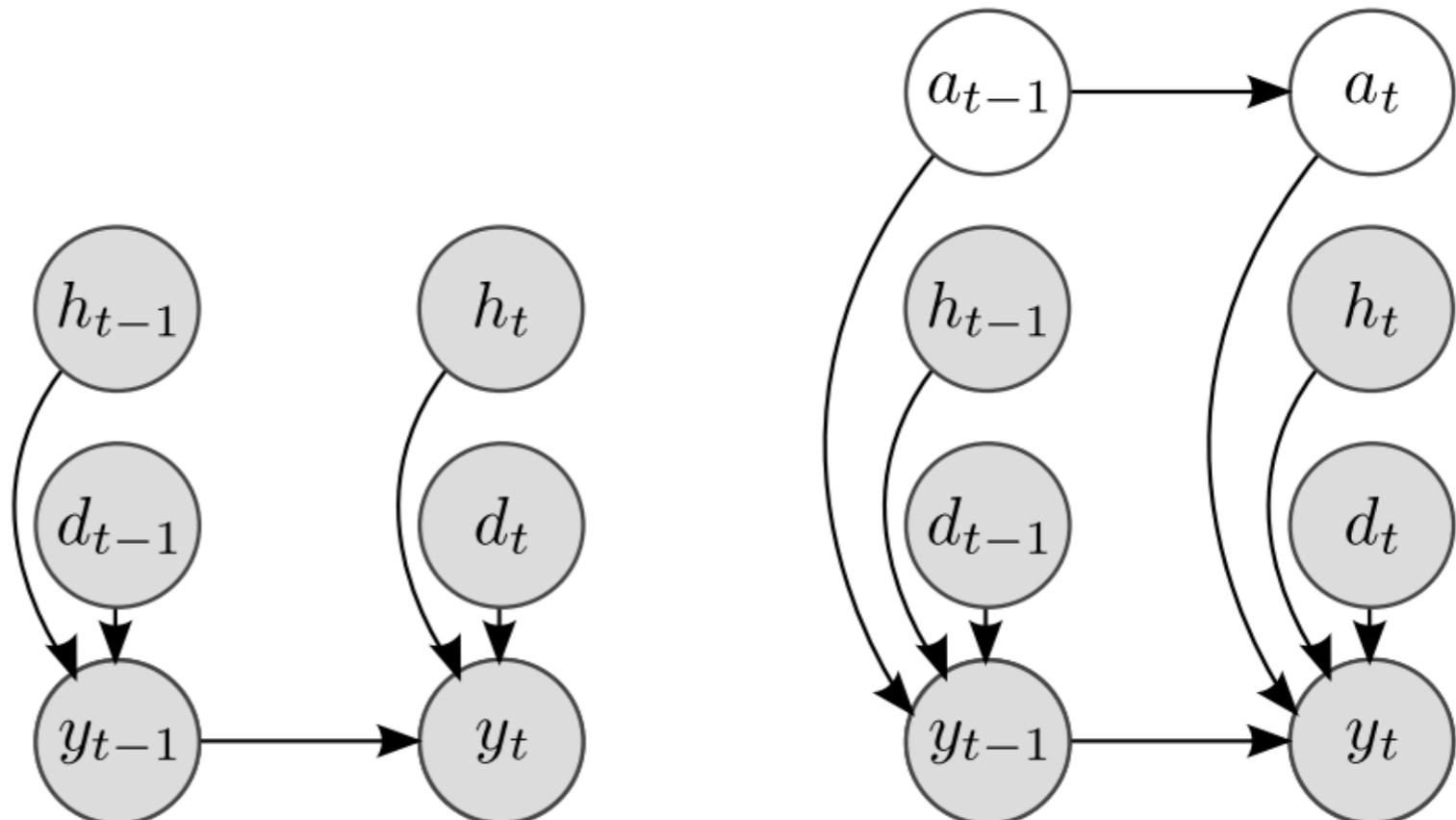
Probabilistic Models



Users with known GPS positions are noisy sensors of the location of their friends

Why not using a Markov model?

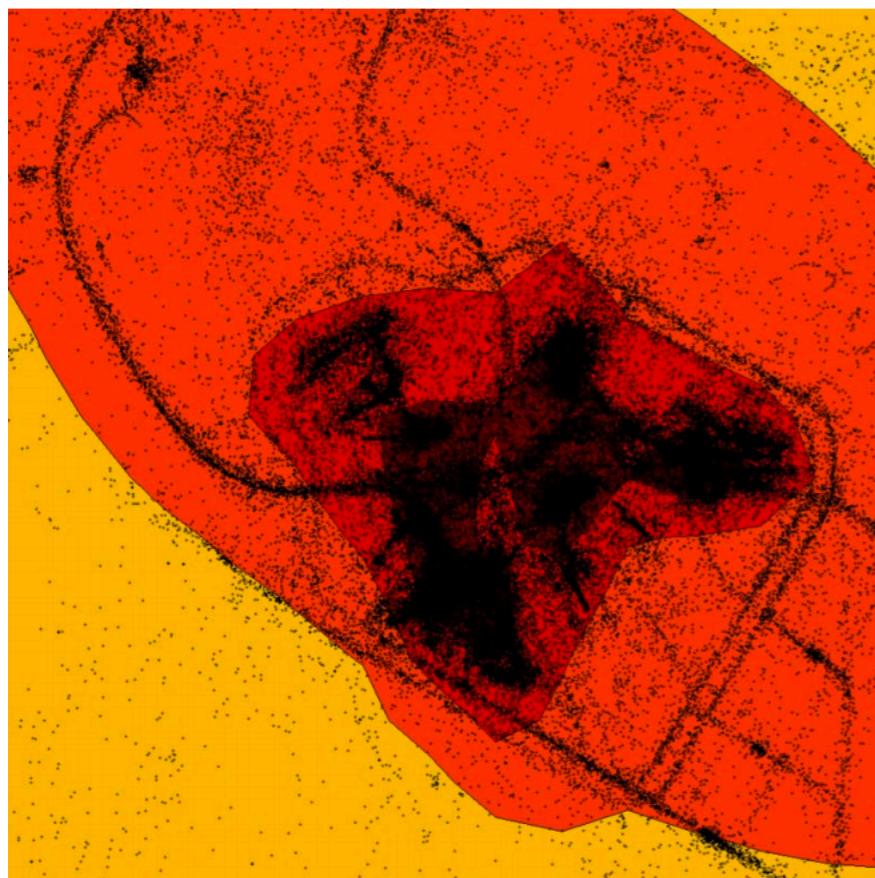
The place-network feature is a form of markov-model, but tells us only part of the truth in the prediction task.



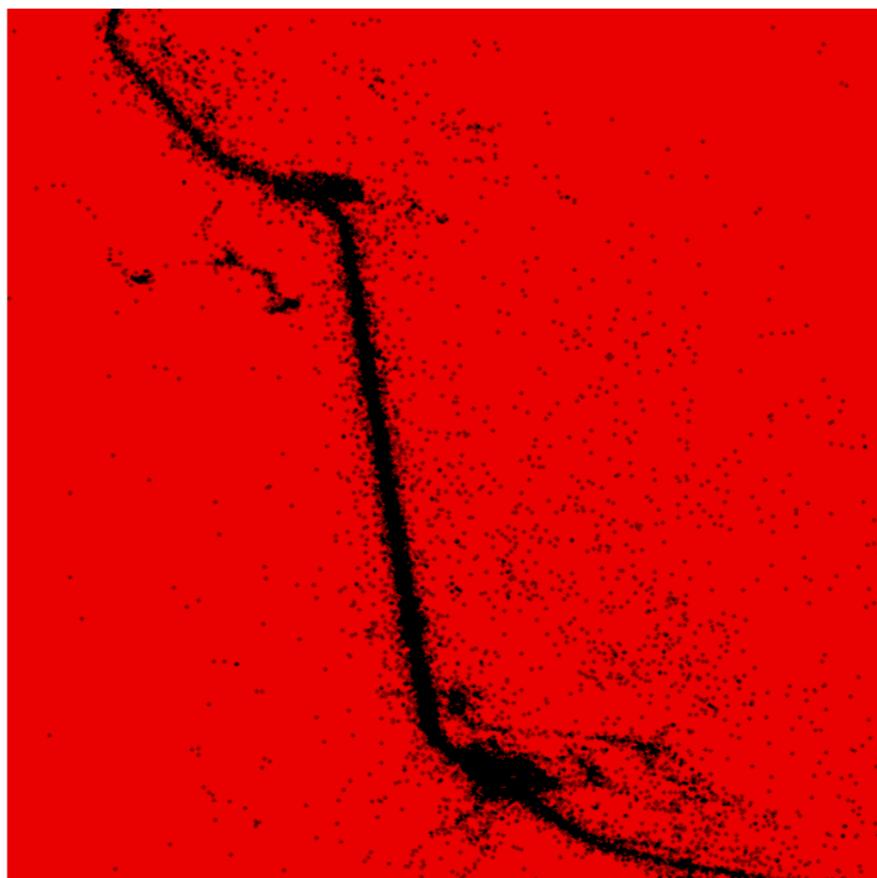
Eagle, Nathan, John A. Quinn, and Aaron Clauset. "Methodologies for continuous cellular tower data analysis." *Pervasive computing*. Springer Berlin Heidelberg, 2009. 342-353.

<http://realitycommons.media.mit.edu/pdfs/pervasive09.pdf>

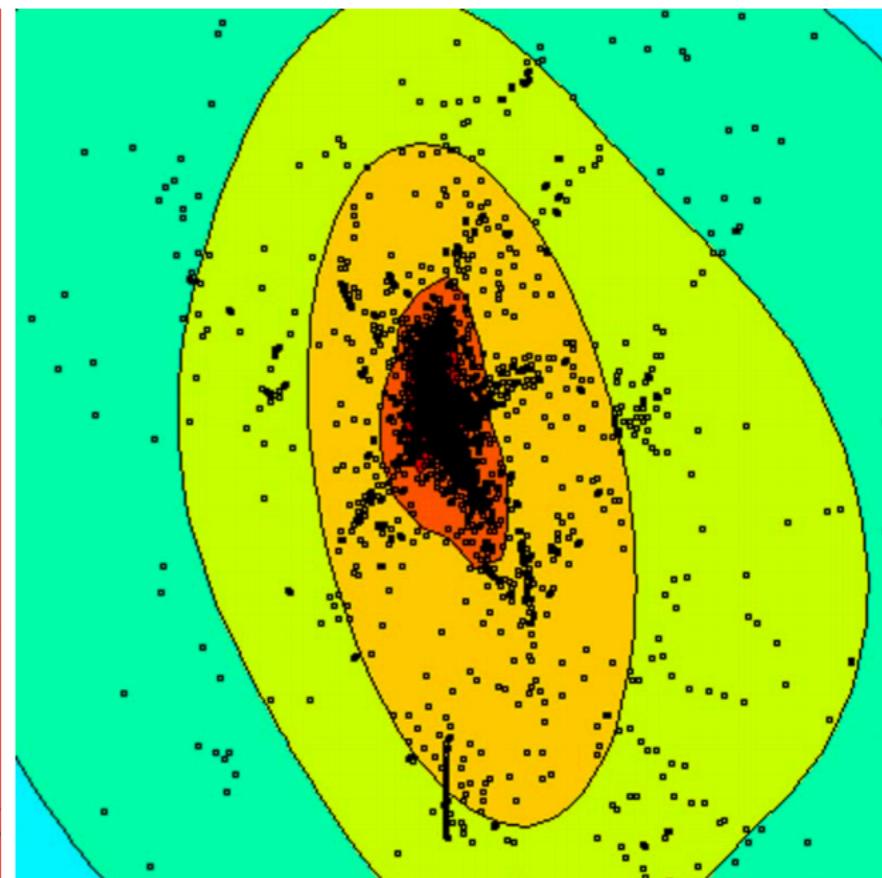
Place Shapes



(a) JFK Airport



(b) Golden Gate Bridge (close up)



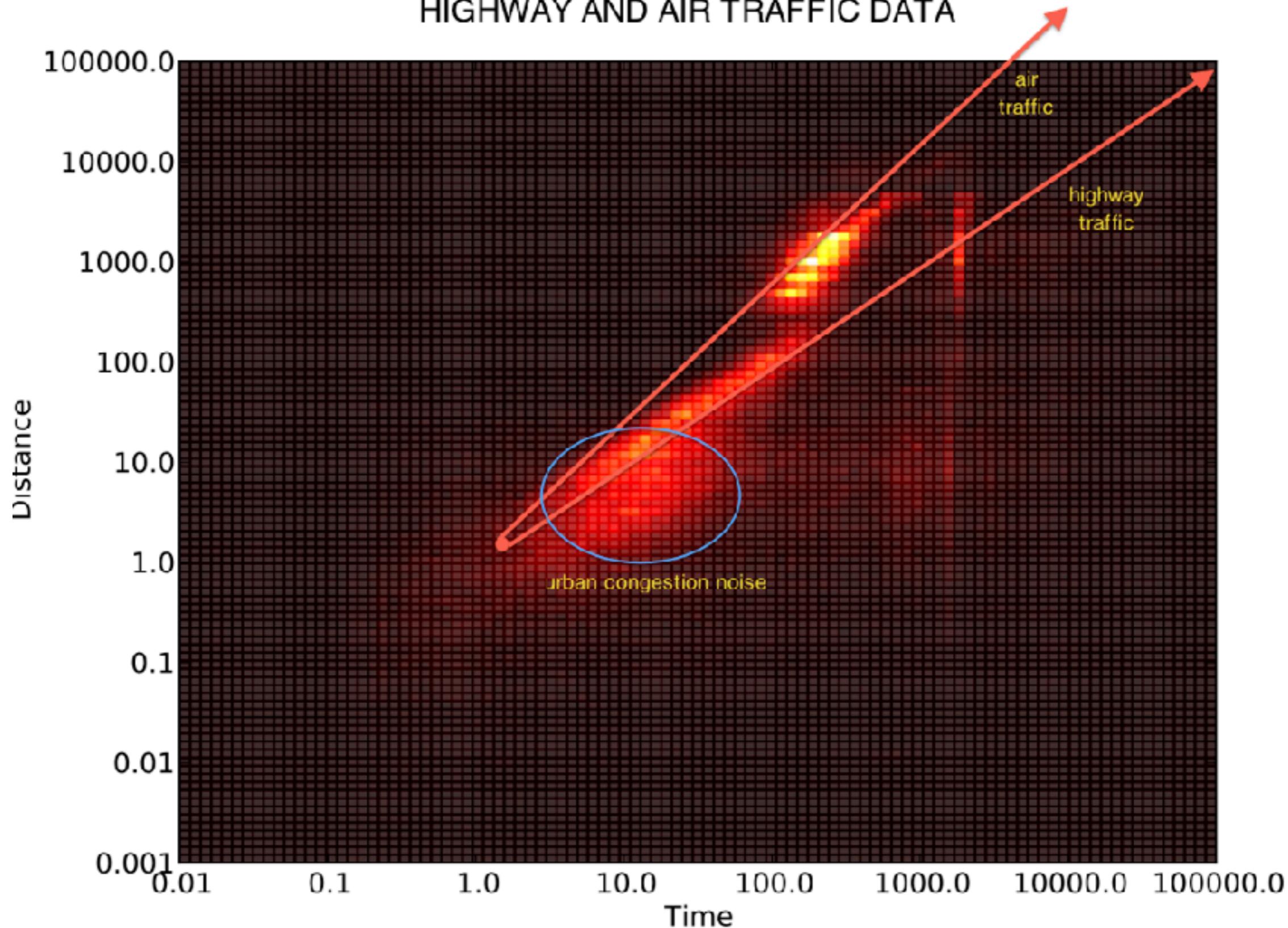
(c) The Blind Tiger

Shaw, Blake, et al. "**Learning to rank for spatiotemporal search.**" Proceedings of the sixth ACM international conference on Web search and data mining. ACM, 2013.



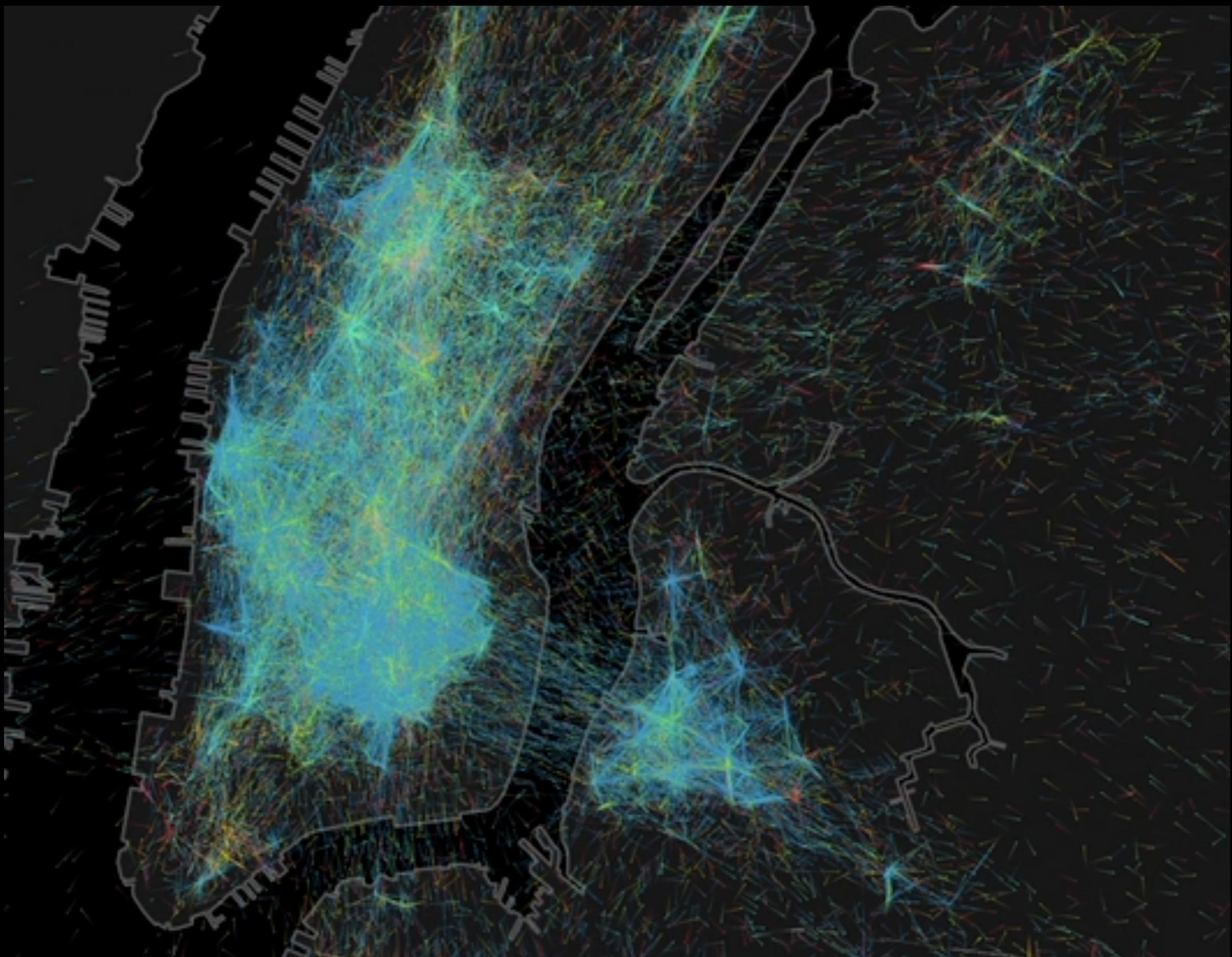


HIGHWAY AND AIR TRAFFIC DATA

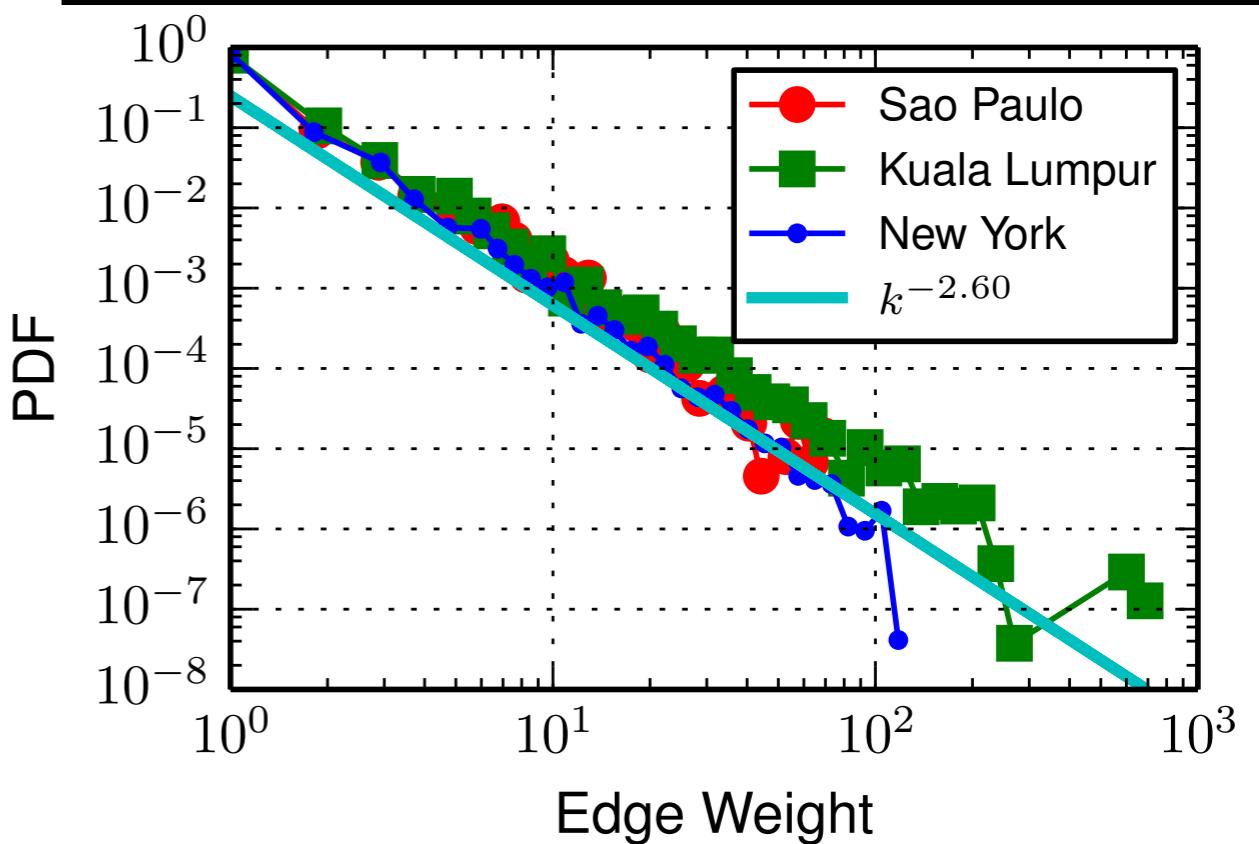
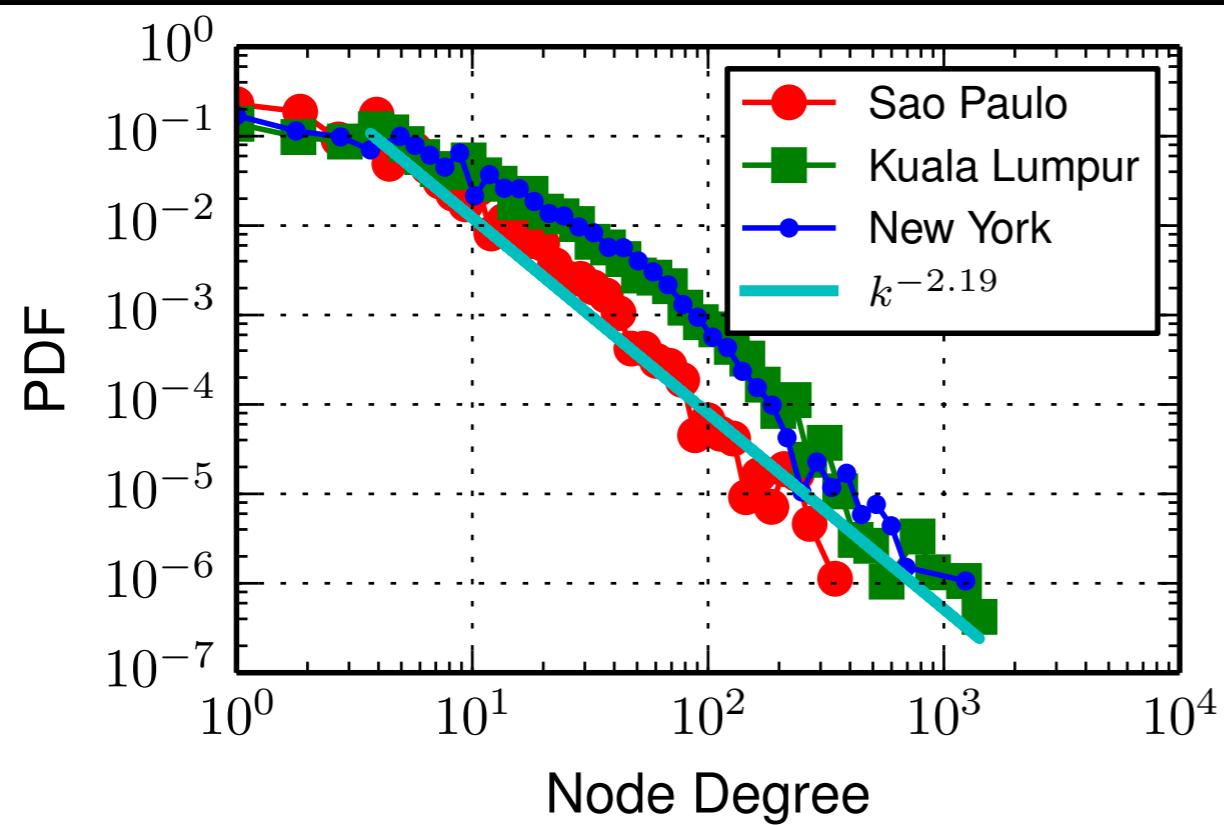


FOURSQUARE CHECK-INS
SHOW THE PULSE OF
TOKYO

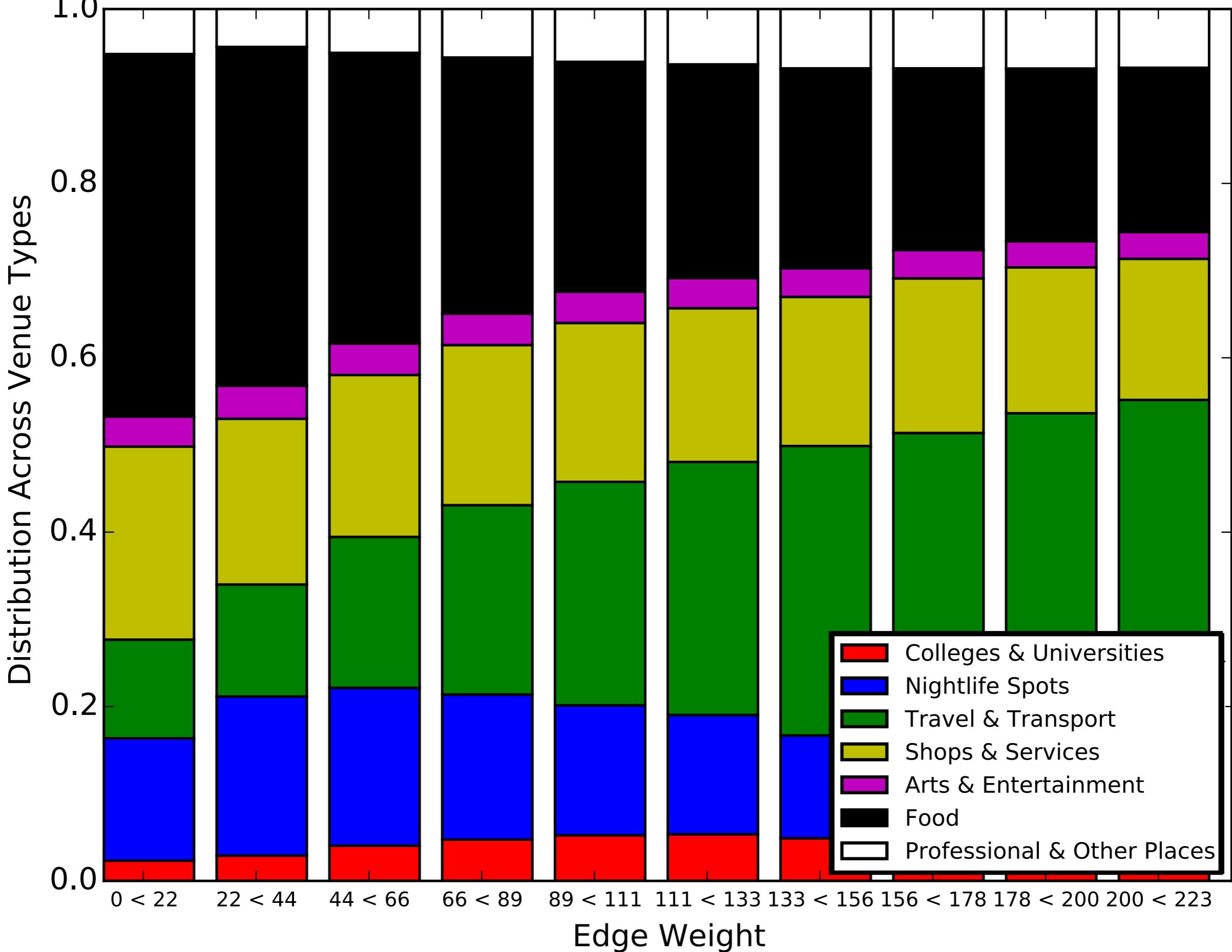
New York City



11-12PM



New York



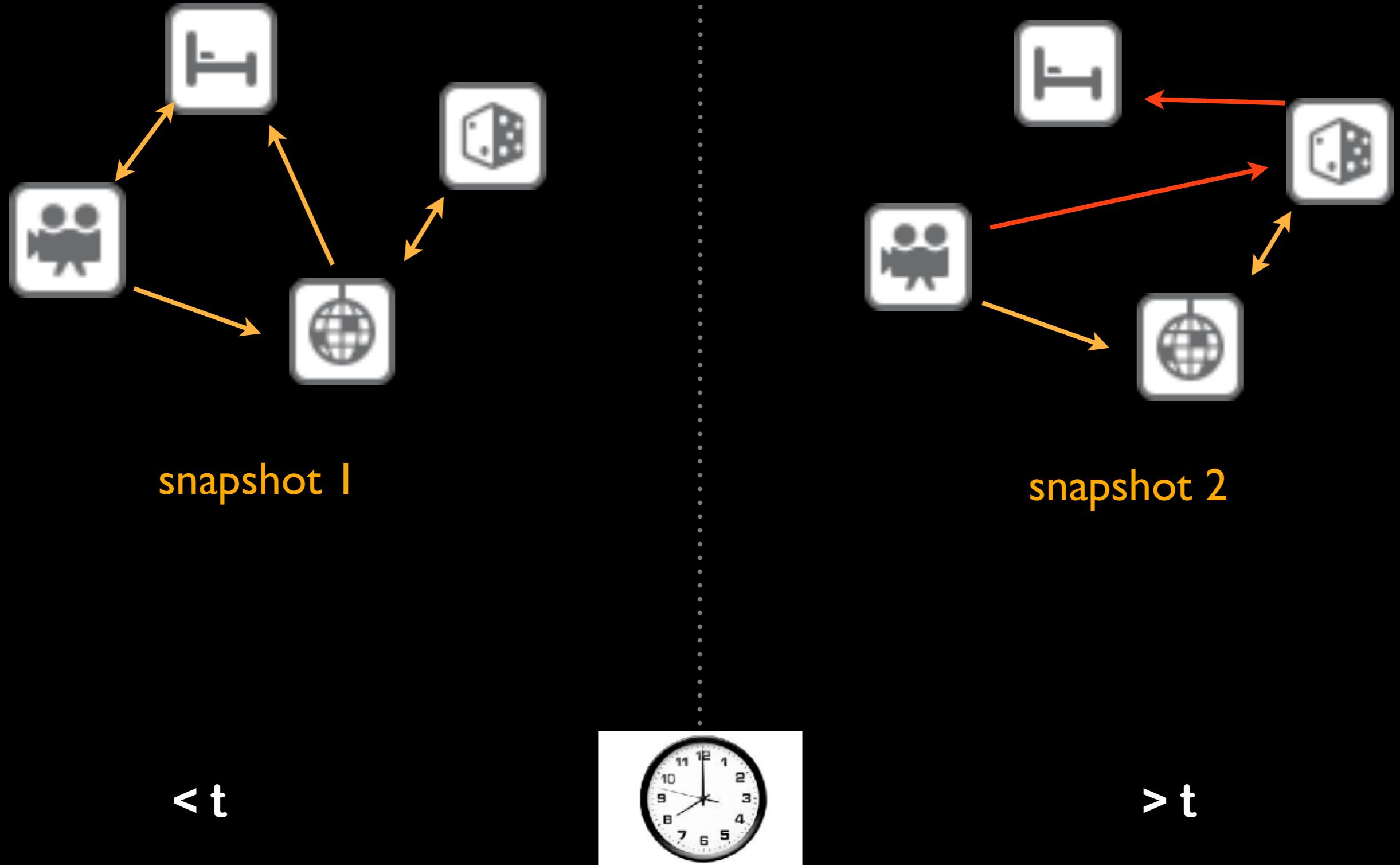
City	$ V $	$ E $	C	C_r	D	D_r	d	d_r	$\langle k \rangle$	r
Saint Petersburg	9292	278099	0.20	0.08	5.83	5.91	3.30	3.25	42.57	-0.05
Moscow	8962	168945	0.19	0.07	6.25	6.00	3.21	3.37	30.96	-0.05
Sao Paulo	8643	66110	0.17	0.04	6.83	6.25	3.67	3.68	18.01	-0.05
New York	8156	145671	0.18	0.07	5.91	5.25	3.12	3.14	40.99	-0.07
Kuala Lumpur	7656	56035	0.19	0.05	6.41	6.00	3.45	3.43	23.93	-0.06
Istanbul	7389	60790	0.14	0.02	10.00	7.50	4.66	4.20	10.50	+0.05
Tokyo	7327	36627	0.23	0.07	7.58	7.16	3.79	3.79	10.40	-0.09
Bangkok	6986	33827	0.15	0.04	7.41	6.58	3.88	3.74	15.58	-0.00
Singapore	6825	30384	0.14	0.02	8.08	7.08	4.02	3.89	14.95	-0.00
Jakarta	4645	10776	0.08	0.00	10.83	9.25	5.45	5.07	5.84	+0.05

	network	n	r
real-world networks	physics coauthorship ^a	52 909	0.363
	biology coauthorship ^a	1 520 251	0.127
	mathematics coauthorship ^b	253 339	0.120
	film actor collaborations ^c	449 913	0.208
	company directors ^d	7 673	0.276
	Internet ^e	10 697	-0.189
	World-Wide Web ^f	269 504	-0.065
	protein interactions ^g	2 115	-0.156
	neural network ^h	307	-0.163
	food web ⁱ	92	-0.276
models	random graph ^u		0
	Callaway <i>et al.</i> ^v		$\delta/(1 + 2\delta)$
	Barabási and Albert ^w		0

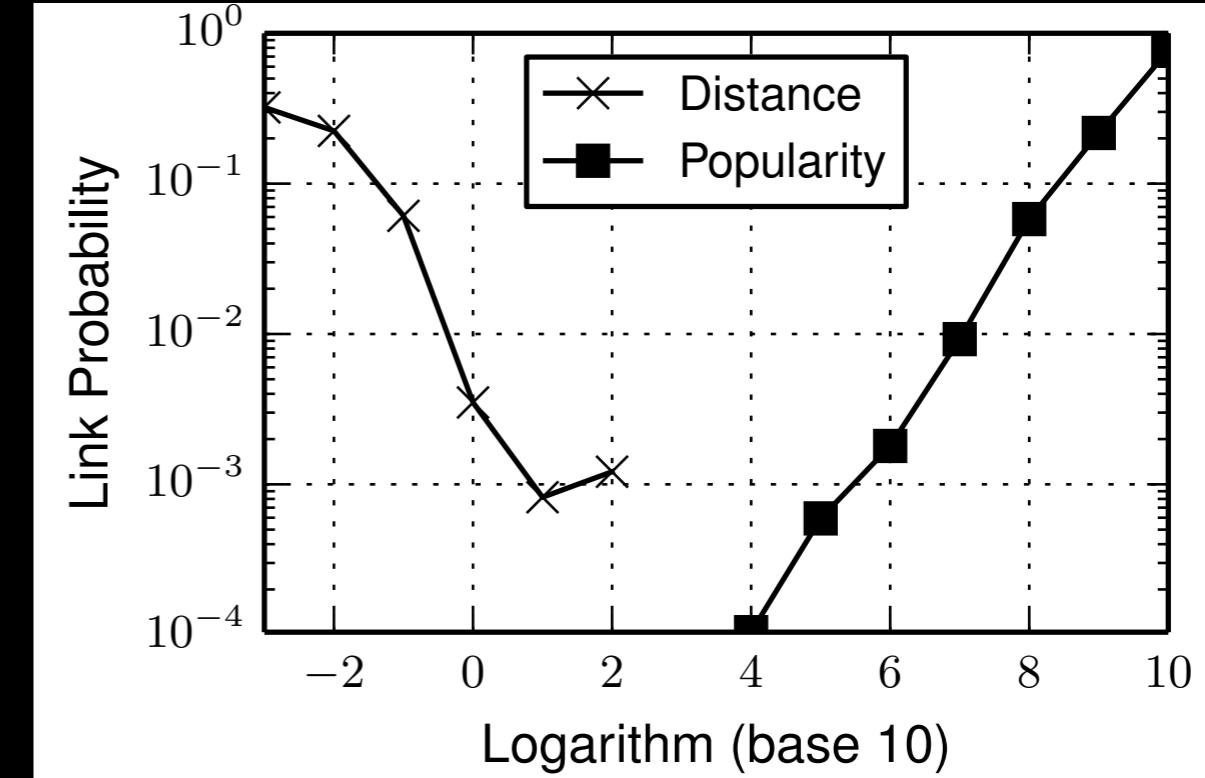
place networks tend to be dissasortative and in that sense fundamentally different to social networks.

Place Networks

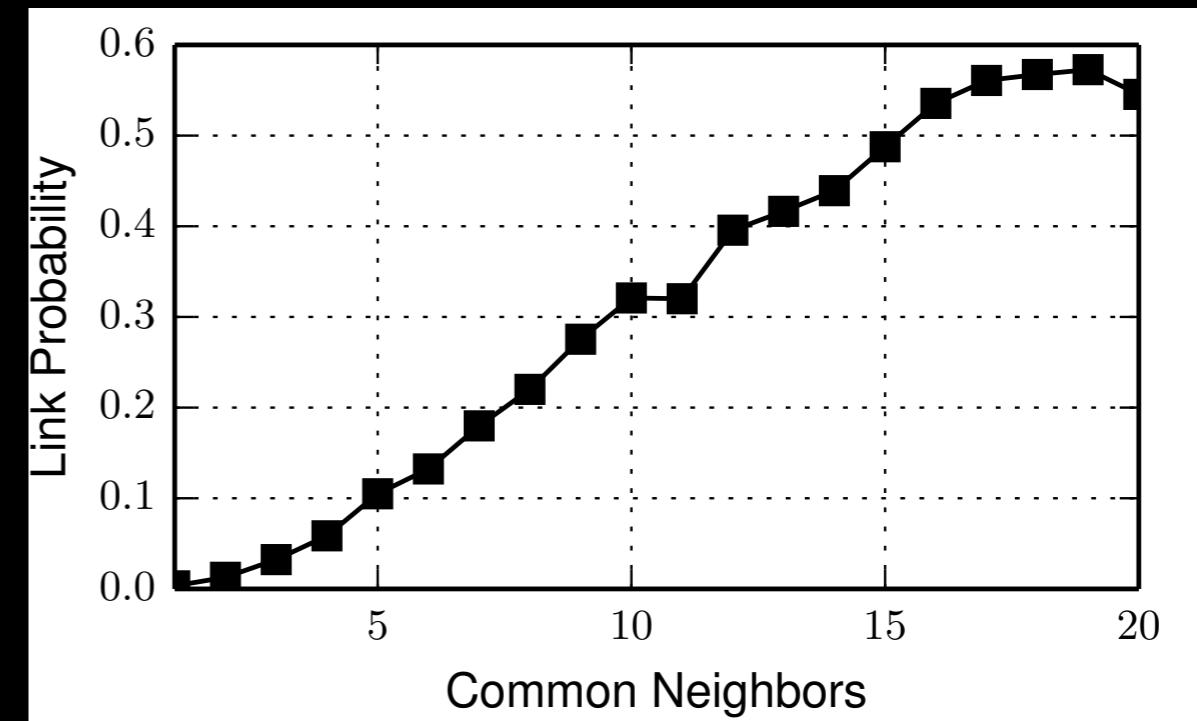
~75% New Links
~5% New Places



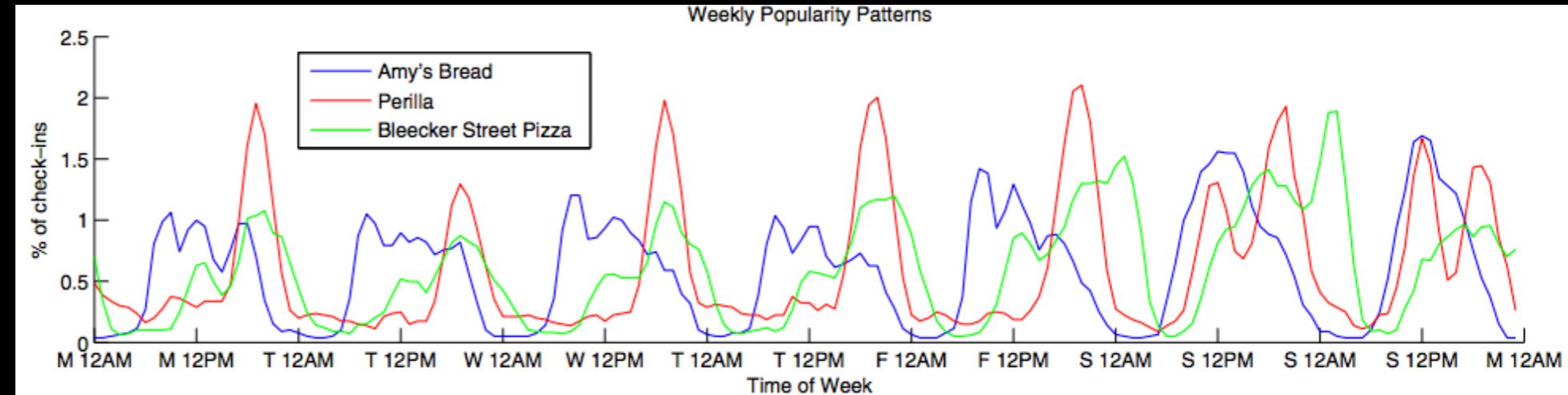
**human
mobility**



**network
form**

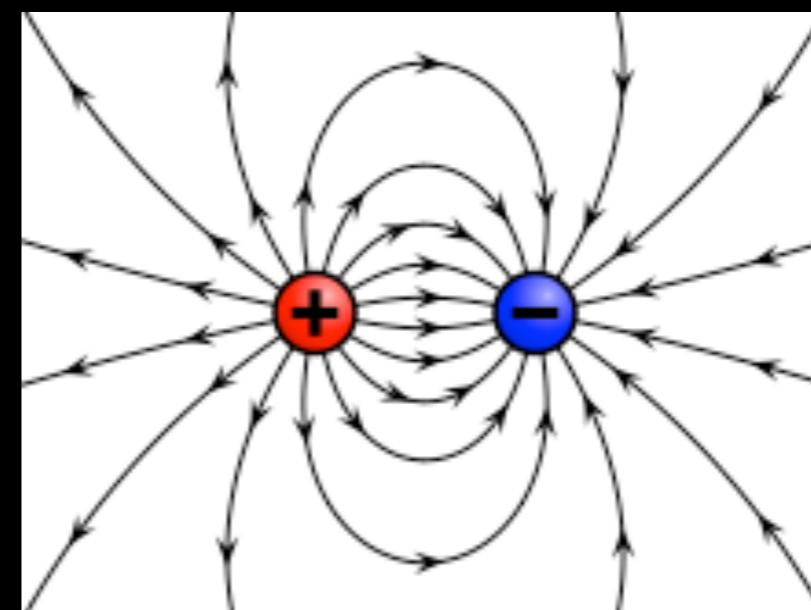


time
signal



Shaw et al. WSDM'13

place
polarity



CLASSIC GRAVITY

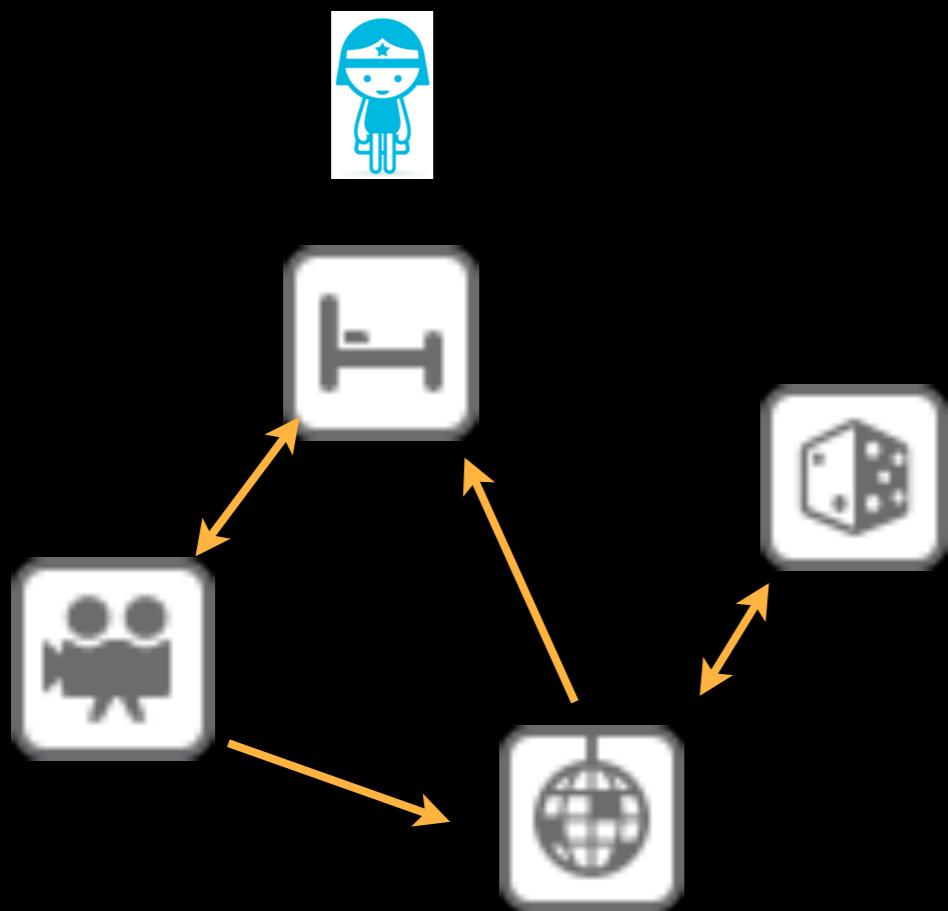
$$\frac{c_i c_j}{d(i, j)^\beta}$$

DYNAMIC GRAVITY

$$\frac{a_{ij} \sum_{\tau=1}^T c_i(\tau)^+ c_j(\tau)^-}{d(i, j)^\beta}$$

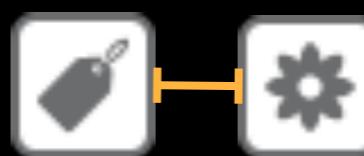
The “heavy-weights”

PLACE RANK

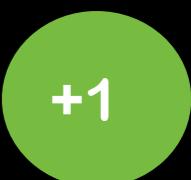


random walk with restart

SUPERVISED LEARNING FOR LINK PREDICTION



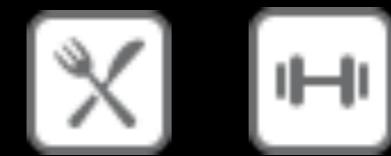
connected pair



train algorithm
on binary labels



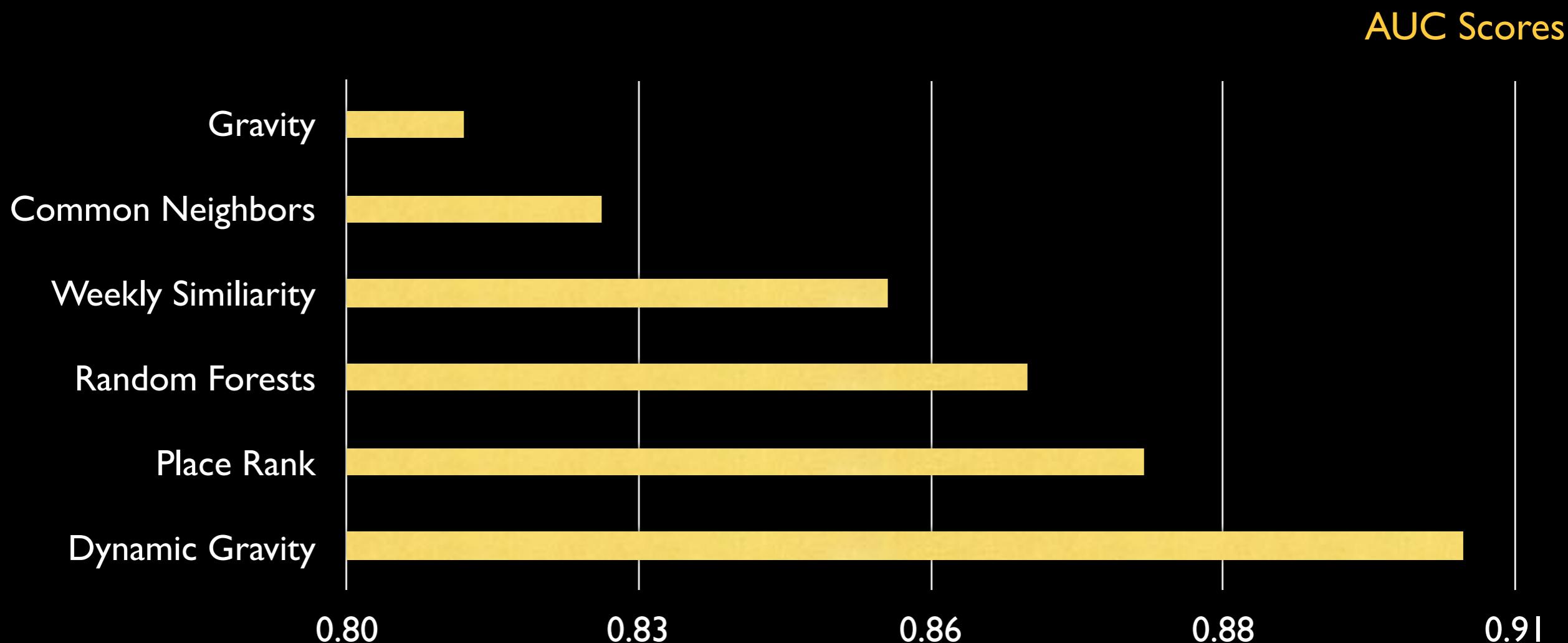
rank millions
of place
pairs



disconnected pair



Dynamic Gravity model offers best results across 100 cities



Domain knowledge + simplicity wins

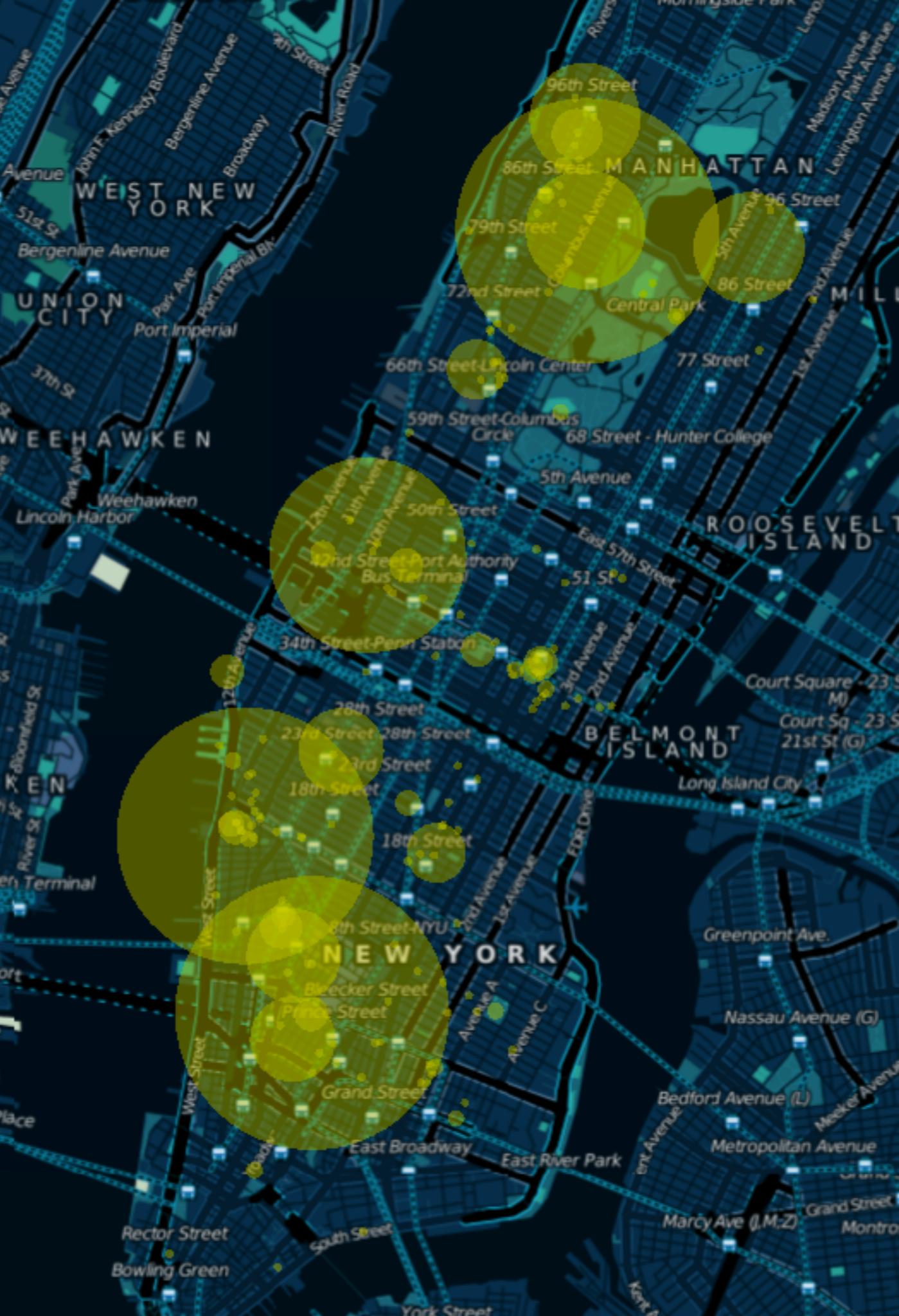
Dynamic gravity also works well in informal tests we have done on CDR

Cities

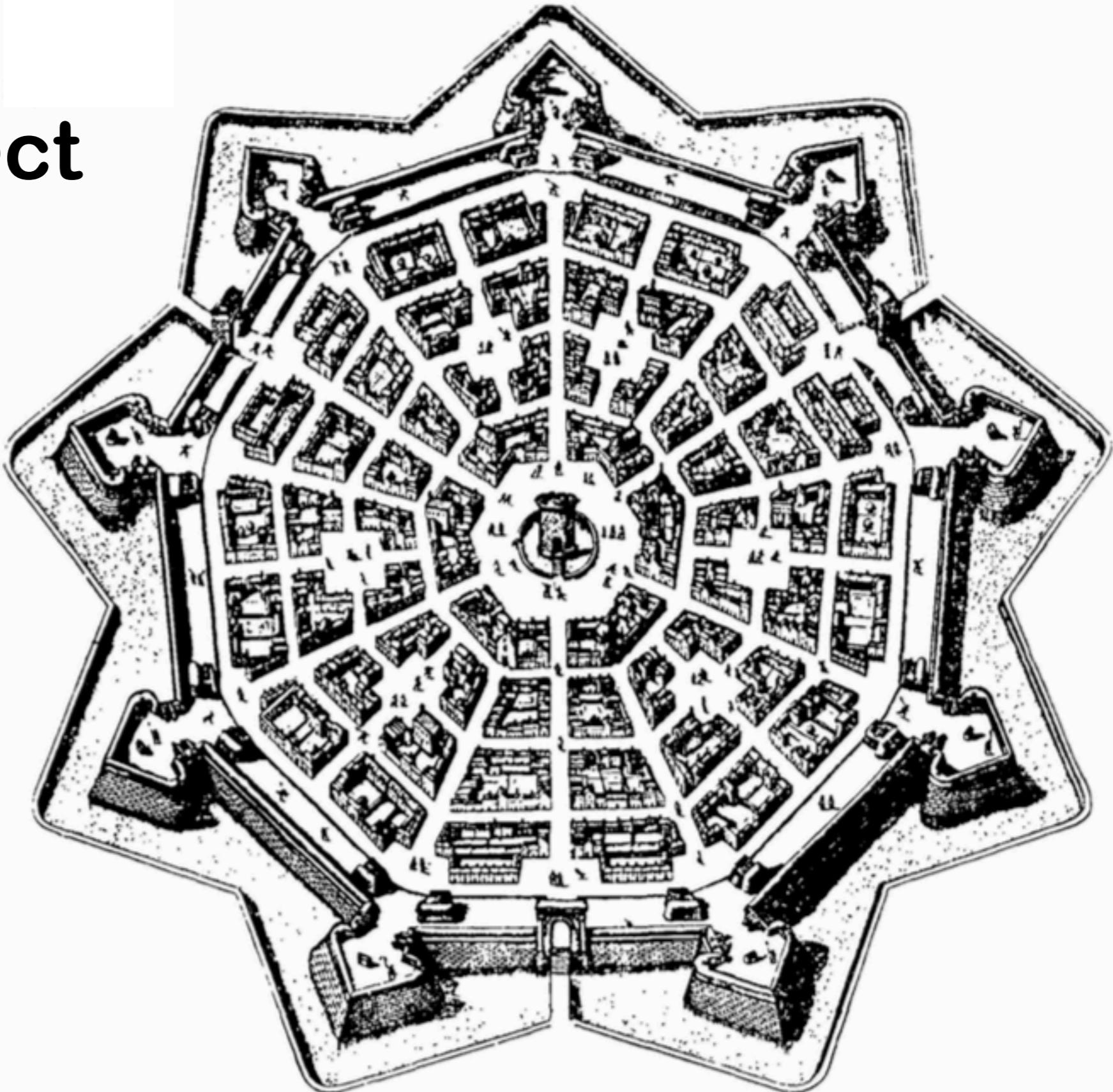
54% of total population in cities as of 2014

That's up from 34% in 1960.

Of course, most of the data discussed previously is generated in urban environments.



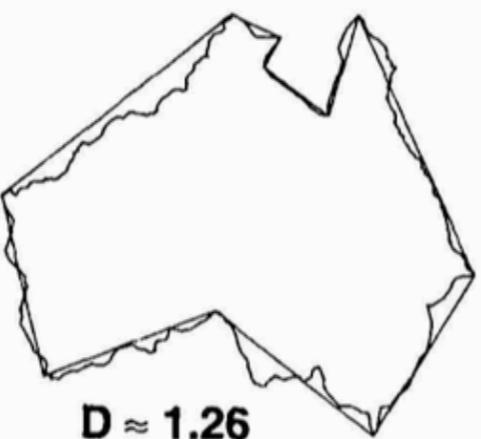
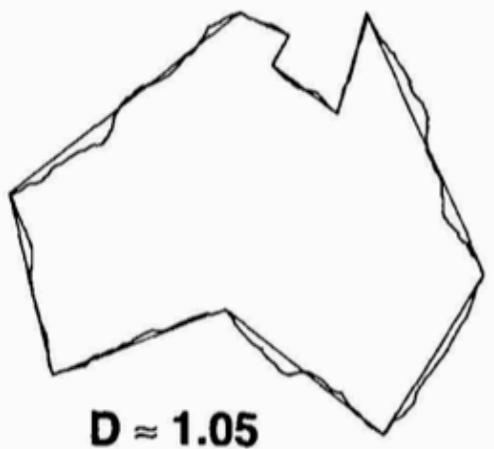
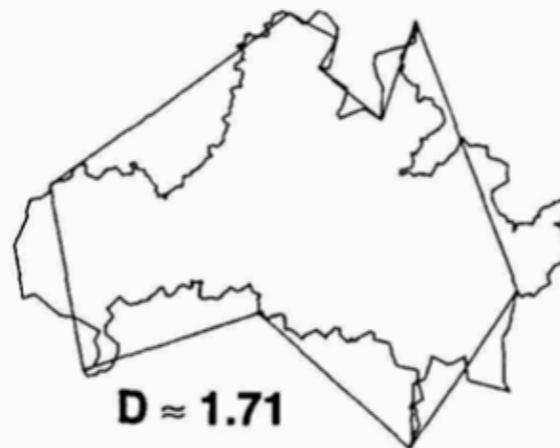
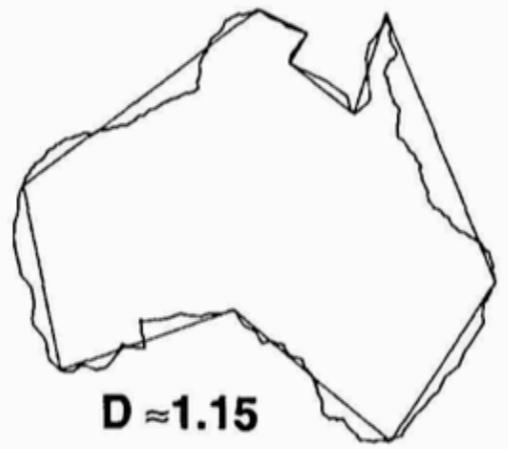
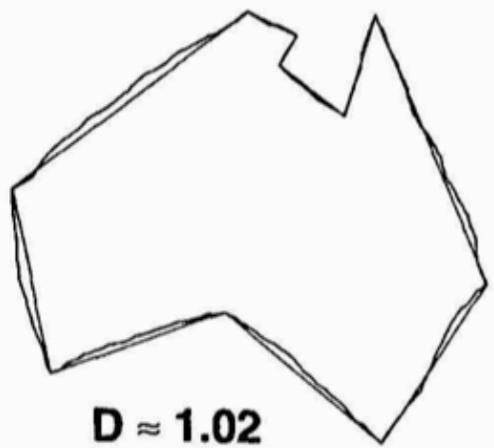
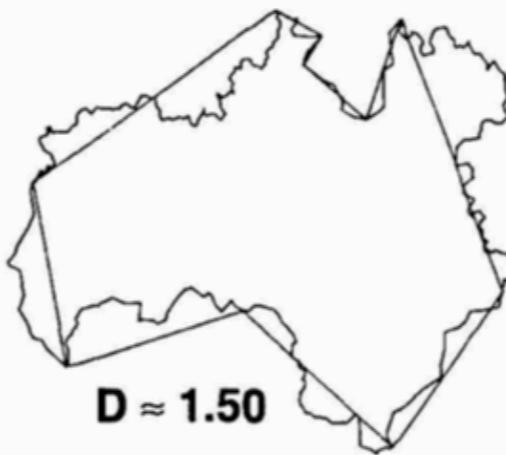
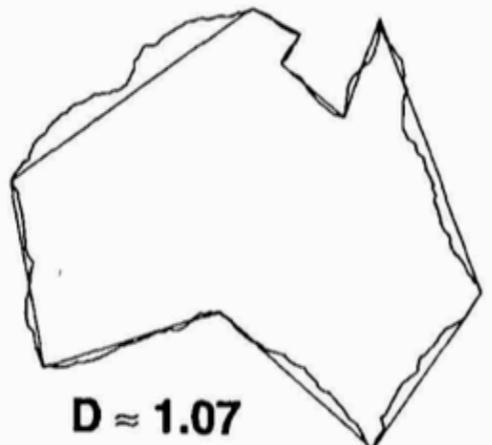
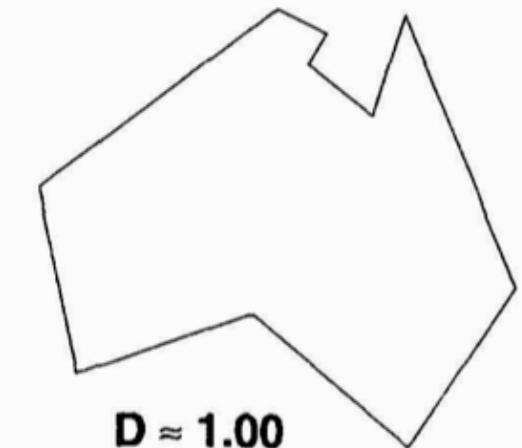
The City as a geometric object



Source:
Michael Batty
www.fractalcities.org

Figure 1.4. Ideal cities of the Renaissance: (a) from Vitruvius; (b) Palma Nuova after Scamozzi (from Morris, 1979).

Fractal Cities



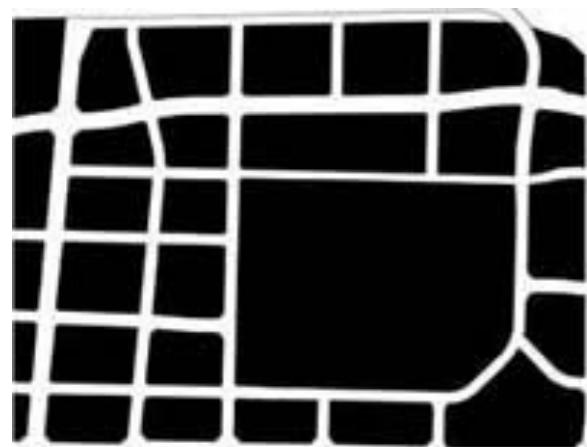
Self similarity

Length depends
on the unit of
measurement

Fractal properties
beyond shapes?
“The city within the
city”.

Country	The World Factbook ^[3]		World Resources Institute ^[2]		Land area km ² (TWI) ^[4]	Coast/area ratio (m/km ²)	
	#	km	#	km		(TWI)	(WRI)
						(TWI)	(WRI)
World ^[Note 2]	—	1,162,306	—	1,634,701	148,940,000	7.80	11.
other ^[Note 3]	—	356,000					
Canada	1	202,080	1	265,523	9,984,670	20.2	26.
Indonesia	2	54,716	4	95,181	1,811,569	30.2	52.
Greenland ^[Note 4]	—	44,087			2,166,086	20.4	
Russia	3	37,653	3	110,310	16,377,742	2.30	6.7.
Philippines	4	36,289	8	33,900	298,170	122	11.
Japan	5	29,751	12	29,020	364,485	81.6	79.
Australia	6	25,760	6	66,530	7,682,300	3.35	8.6.
Norway	7	25,148 ^[Note 5]	7	53,199	304,282	82.6	17.
United States	8	19,924	2	133,312	9,161,966	2.17	14.
Antarctica	—	17,968			14,000,000	1.28	
New Zealand	9	15,134	17	17,209	267,710 ^[5]	56.5	64.
China	10	14,500	11	30,017	9,569,901	1.52	3.1.
Greece	11	13,676	19	15,147	131,957	104	11.
United Kingdom	12	12,429	16	19,717	241,930	51.4	81.
Mexico	13	9,330	14	23,761	1,943,945	4.80	12.
Italy	14	7,600	28	9,226	204,140	25.8	21.

Urban Morphology



MISSISSAUGA



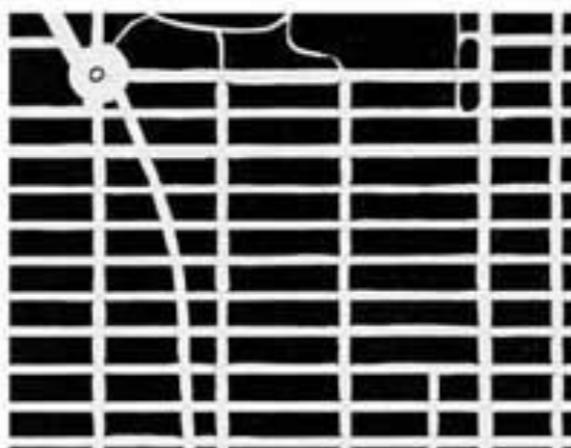
LONDON



ROME



BARCELONA



NEW YORK



COPENHAGEN



PARIS



SAN FRANCISCO



TORONTO

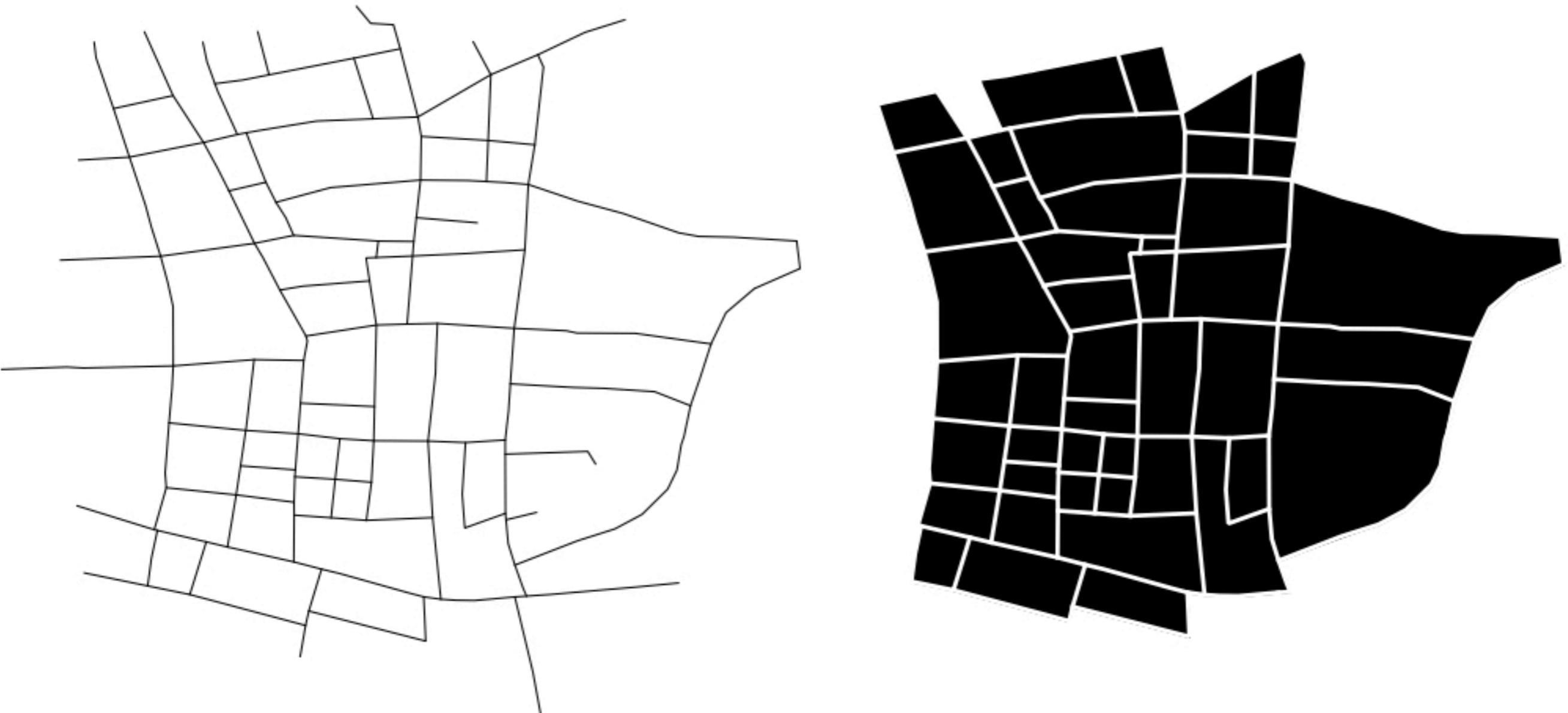
<http://urbagram.stdio-london.com/v1/show/Network>

<https://nextcity.org/daily/entry/city-street-grid-maps-visualize-density>

Connecting the Fractal City.

<http://zeta.math.utsa.edu/~yxk833/connecting.html>

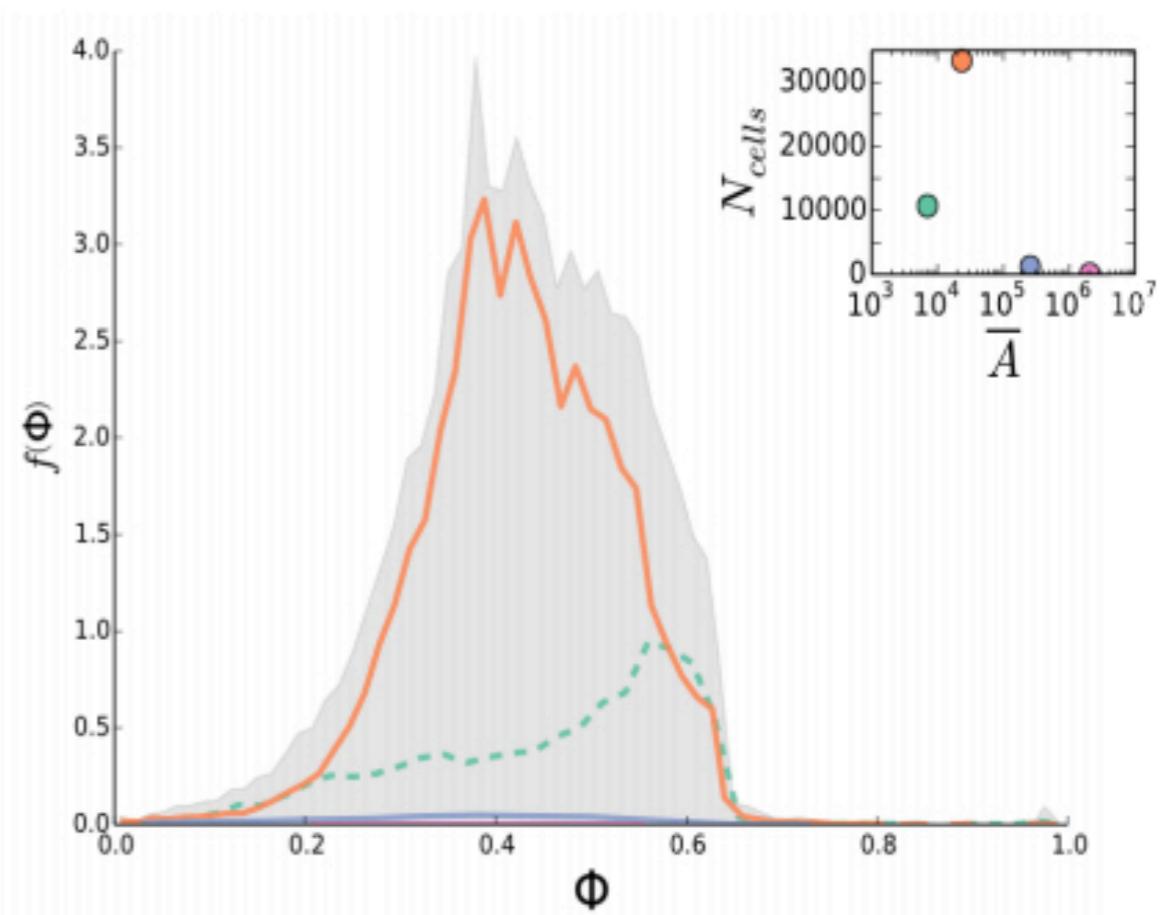
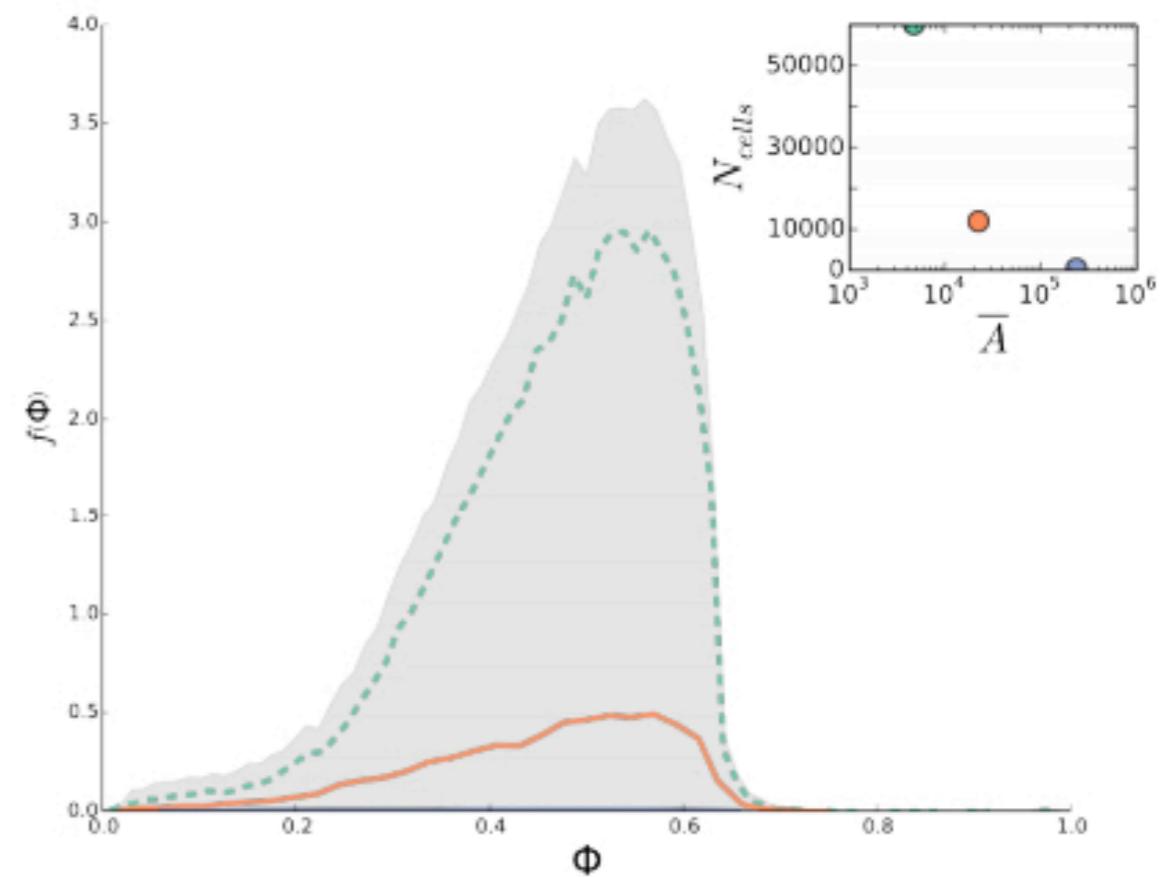
Extracting land patches

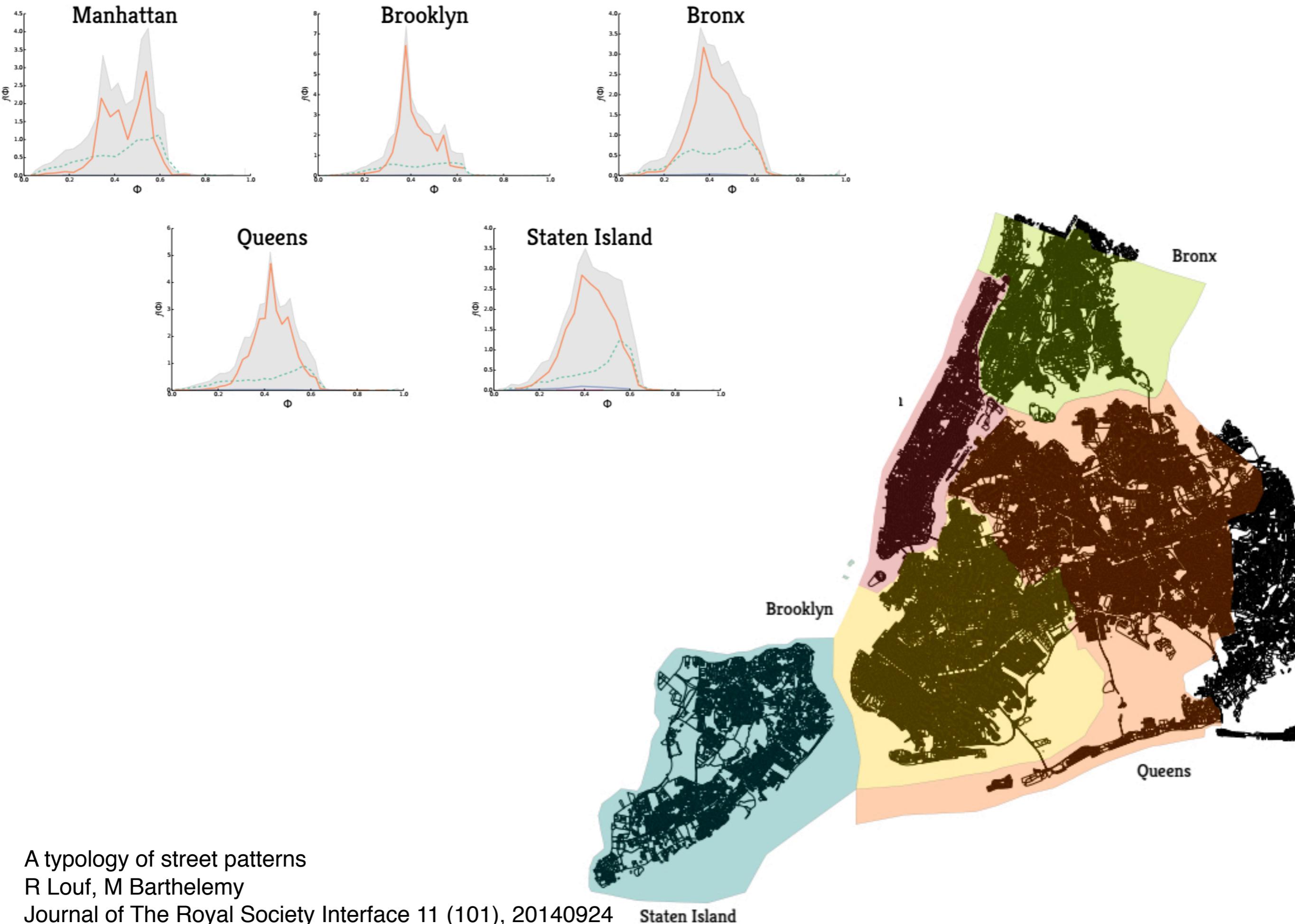


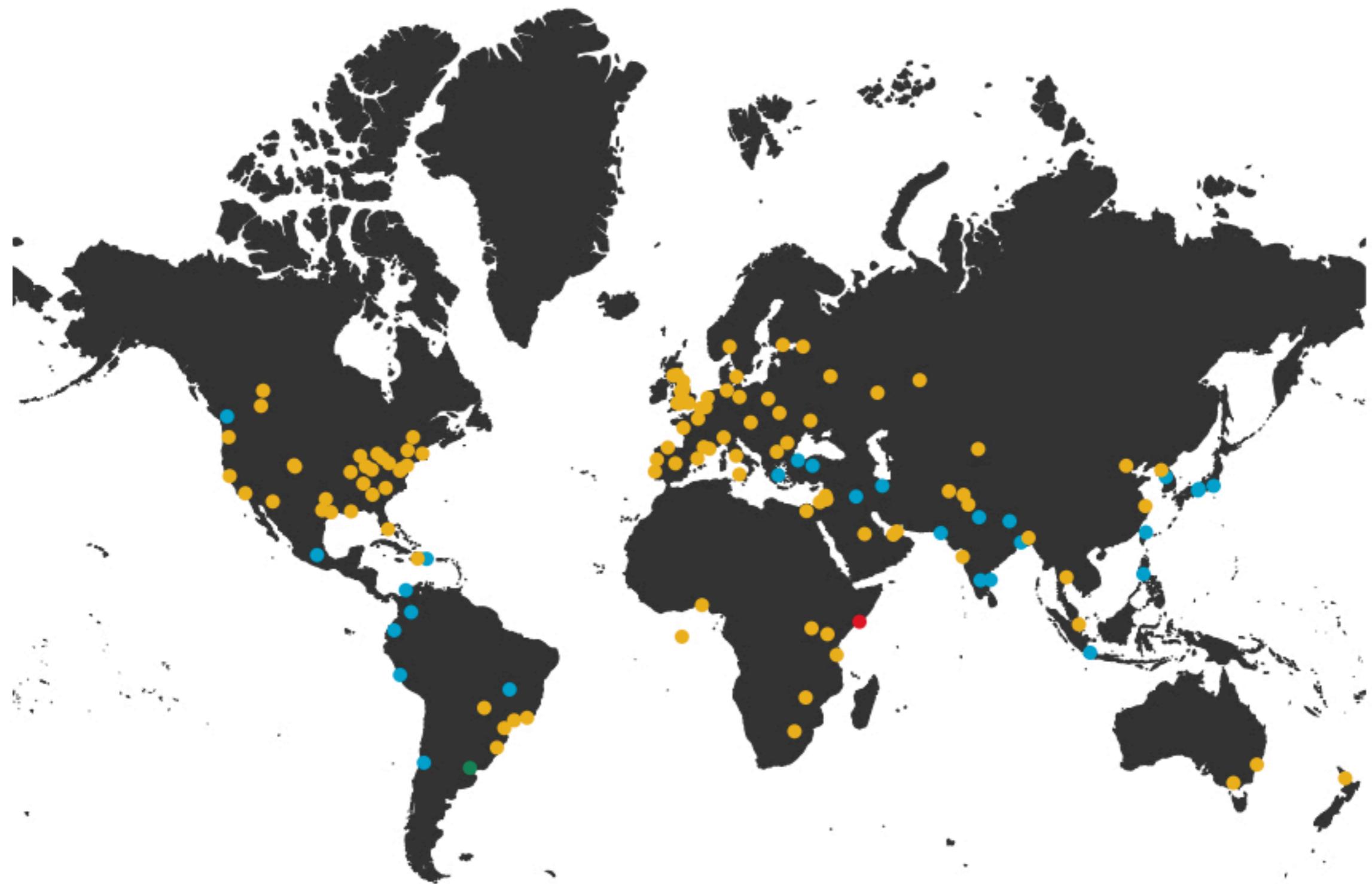
A typology of street patterns

R Louf, M Barthelemy

Journal of The Royal Society Interface 11 (101), 20140924







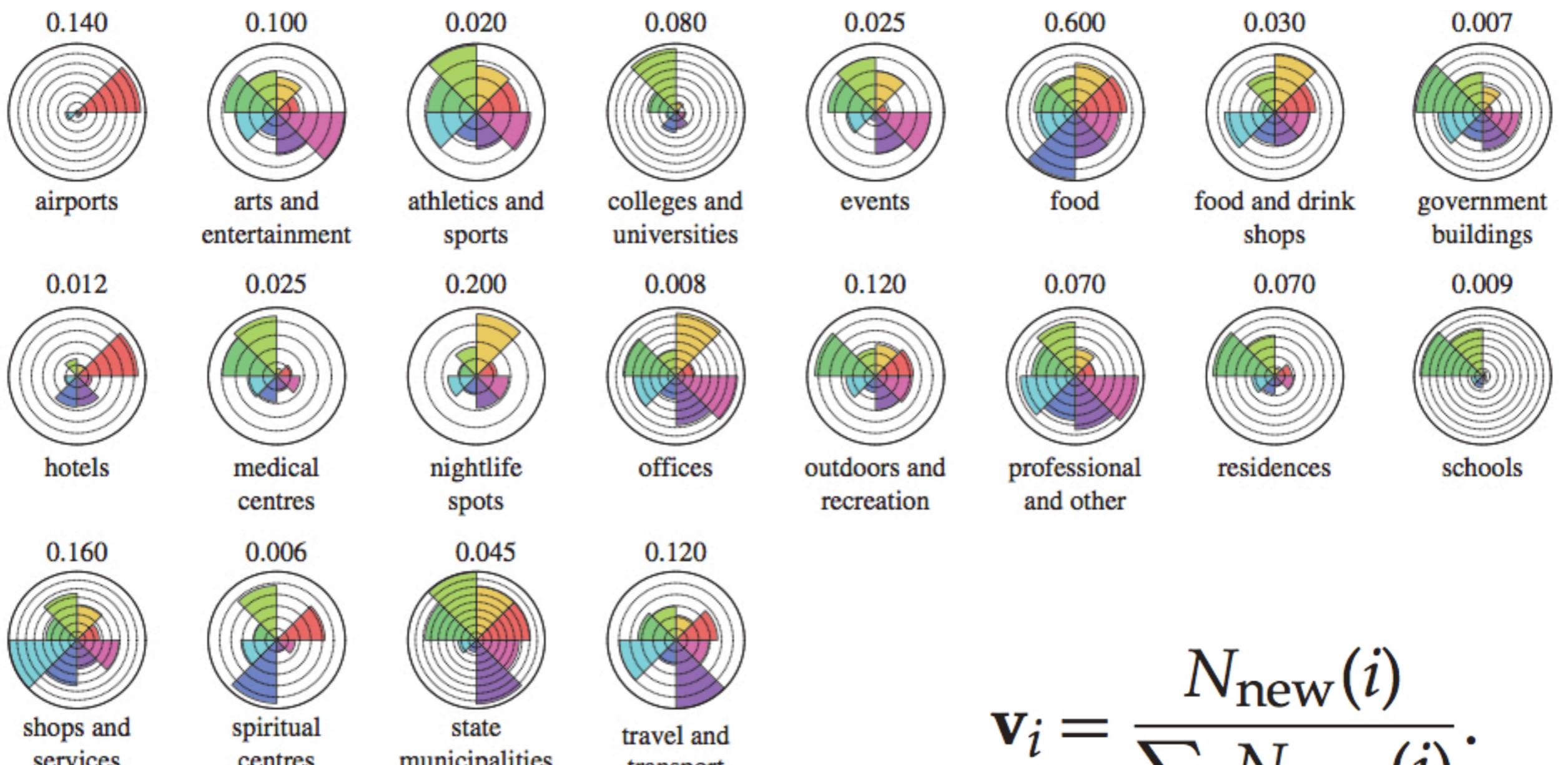
A typology of street patterns

R Louf, M Barthelemy

Journal of The Royal Society Interface 11 (101), 20140924



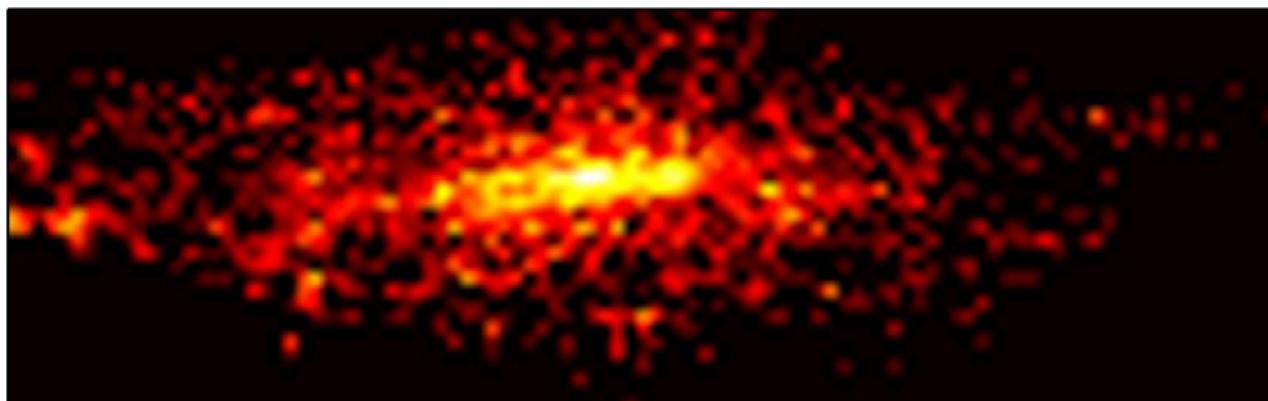
no.	MPD (km)	cities
1	10 996	Dubai, Borough of Queens
2	5800	Athens, Brooklyn, Bucharest, Portland, Sofia
3	5250	Belo Horizonte, Coyoacán, Curitiba, Fortaleza, Gent, Manaus, Porto Alegre
4	4924	Adana, Ankara, Bursa, Denizli, Eskişehir, İstanbul, İzmir, Lima, Santiago, Trabzon
5	5887	Charlotte, Chiba, Columbus, Houston, Indianapolis, Jacksonville, Kiev, Moscow, Nashville, Orlando, Osaka, Phoenix, Raleigh, Saint Petersburg, San Antonio, San Jose, Yokohama
6	3537	Bandung, Bangkok, Chiang Mai, George Town, Hong Kong, Jakarta, Kuala Lumpur, Makati City, Medan, Petaling Jaya, Pineda, Quezon City, Seoul, Shah Alam, Singapore, Surabaya, Tokyo, Toronto, Yogyakarta
7	5790	Amsterdam, Barcelona, Berlin, Bogotá, Boston, Brussels, Budapest, Buenos Aires, Copenhagen, Helsinki, London, Madrid, Milano, Paris, Prague, Recife, Riga, Riyadh, Sydney, Tampa
8	4276	Antwerpen, Atlanta, Austin, Brasília, Chicago, Dallas, Denver, Las Vegas, Los Angeles, Mexico City, Milwaukee, Minneapolis, New York, Philadelphia, Rio de Janeiro, San Diego, San Francisco, São Paulo, Seattle, Washington DC



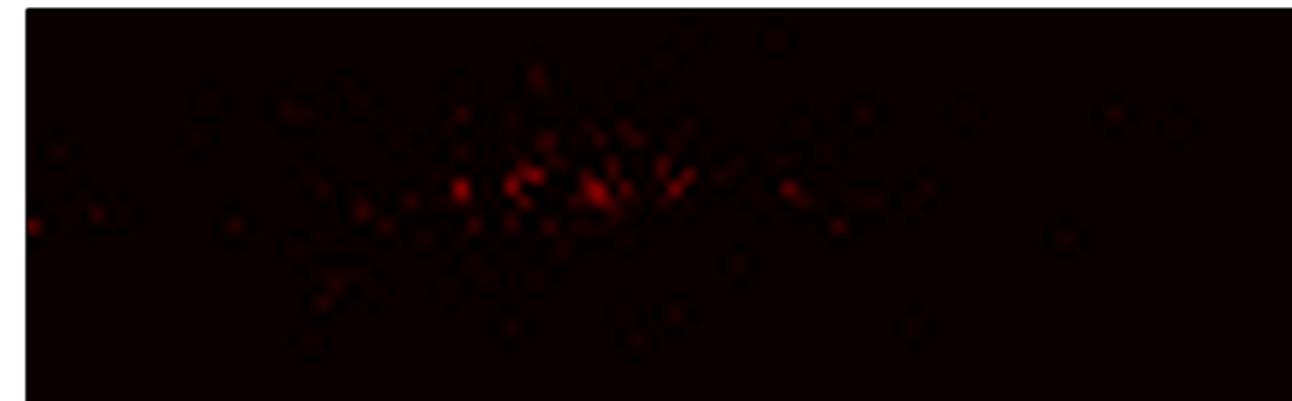
$$\mathbf{v}_i = \frac{N_{\text{new}}(i)}{\sum_i N_{\text{new}}(i)}.$$

Tracking the birth of places [London 2010-2014]

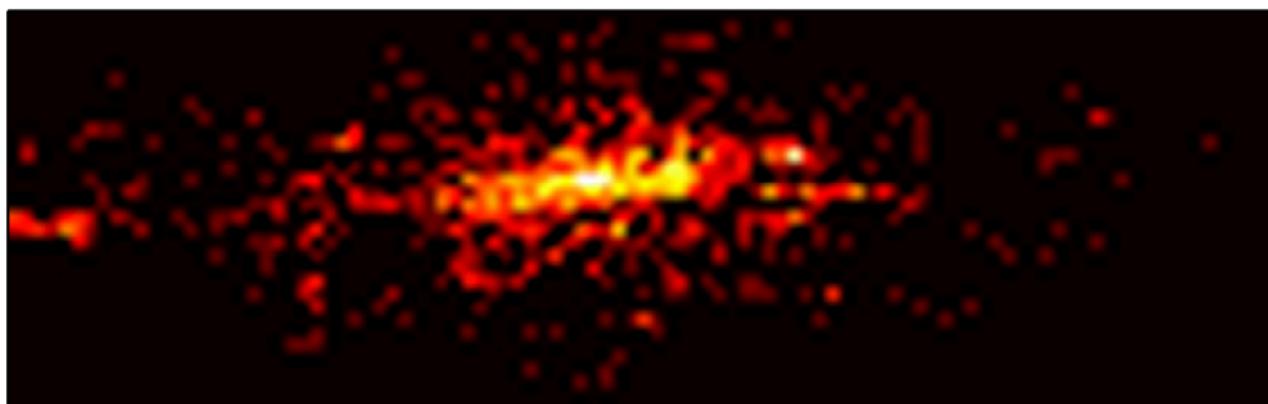
existing places



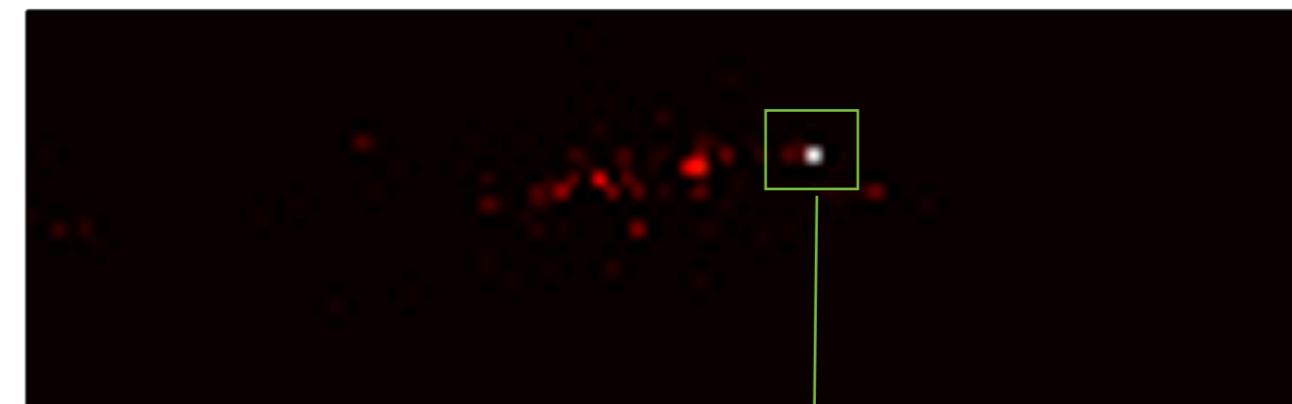
less than expected



new places



more than expected

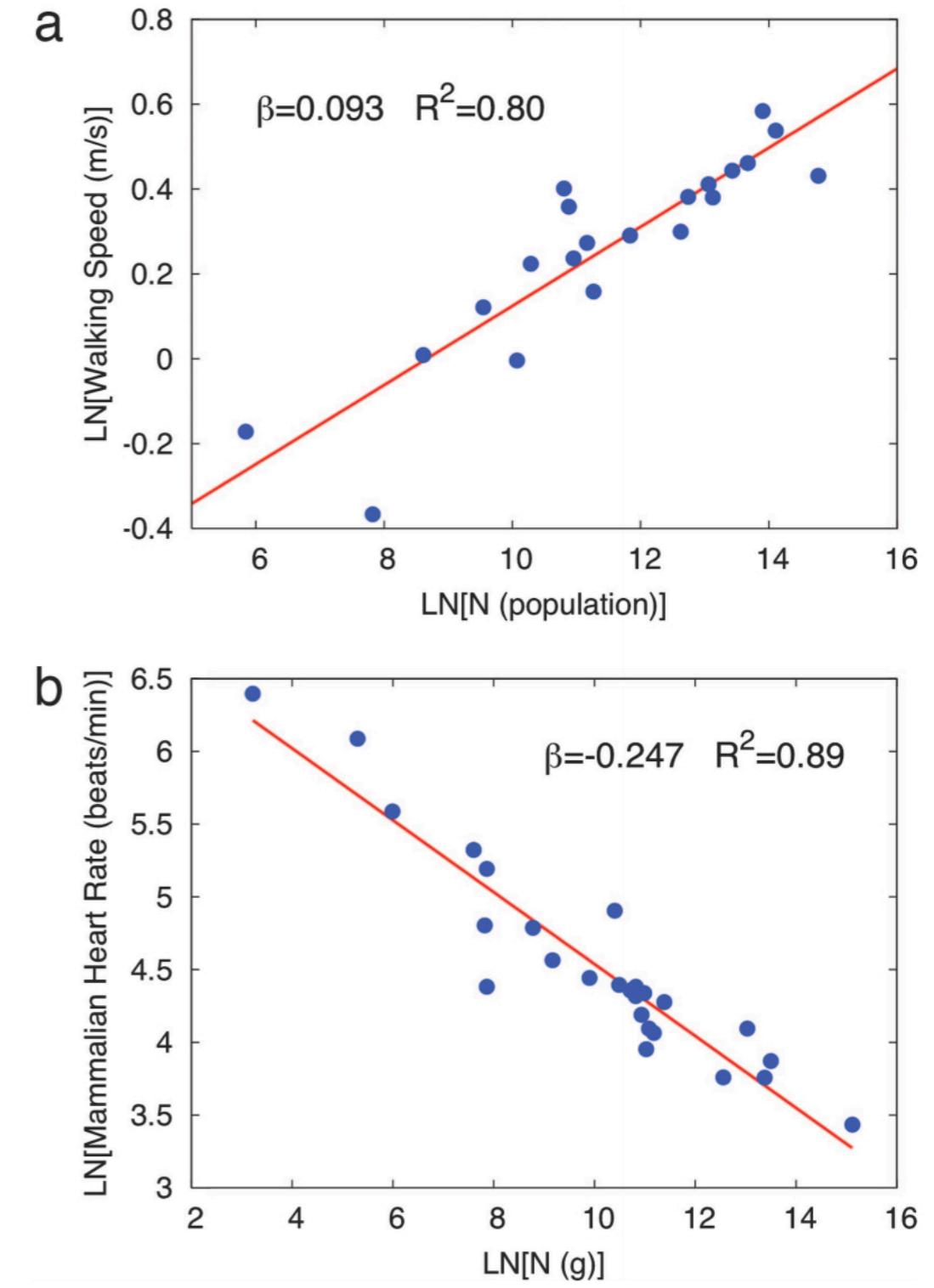
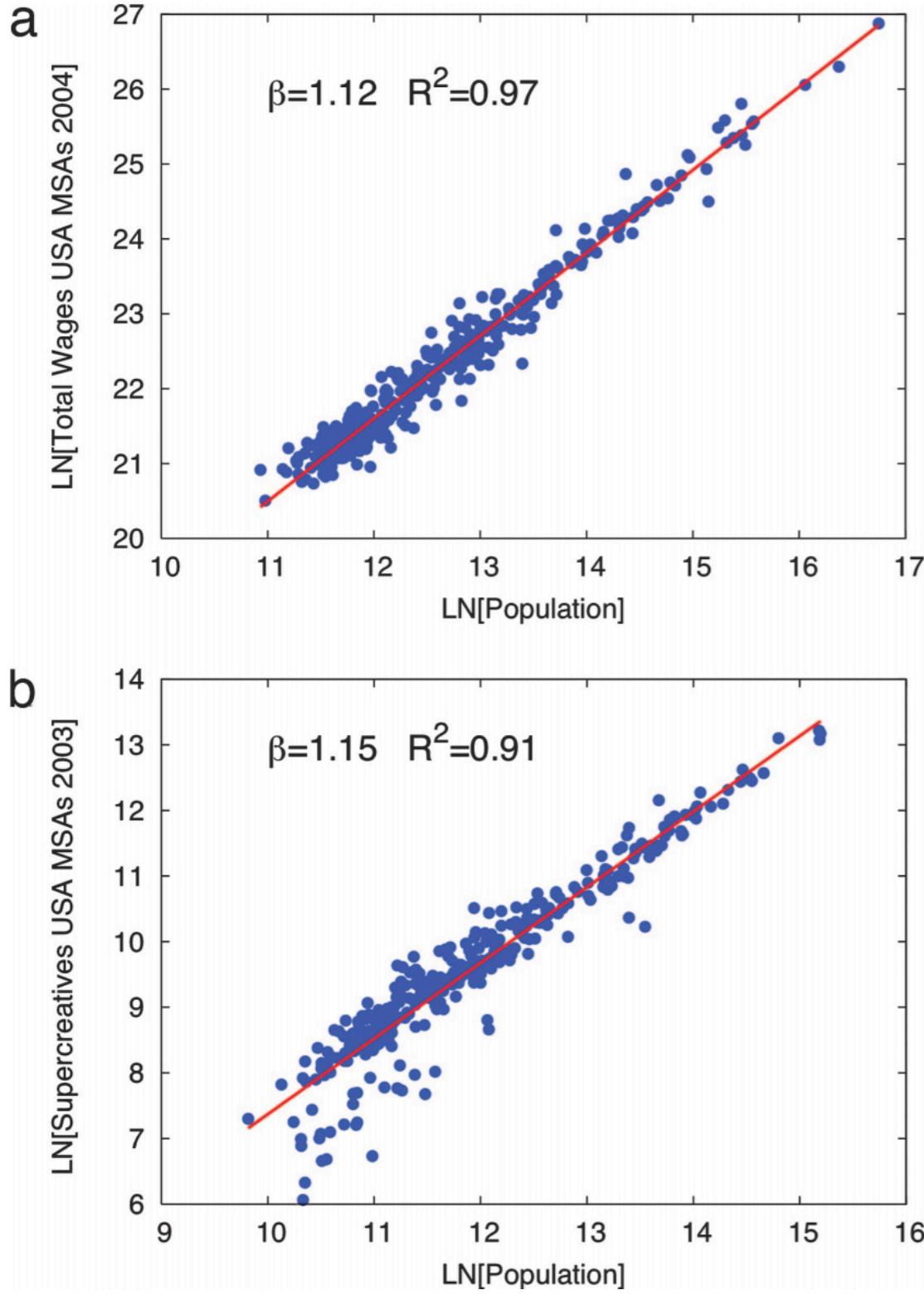


Stratford: Olympic Village

$$n_{i,j}^{\text{null}} = \frac{n_{i,j}^{\text{existing}} n_{i,j}^{\text{new}}}{n^{\text{existing}}}$$

$$v_{i,j} = n_{i,j}^{\text{null}} - n_{i,j}^{\text{new}}$$

Tracking Urban Activity Growth Globally with Big Location Data
M Daggitt, A Noulas, B Shaw, C Mascolo
Royal Society Open Science

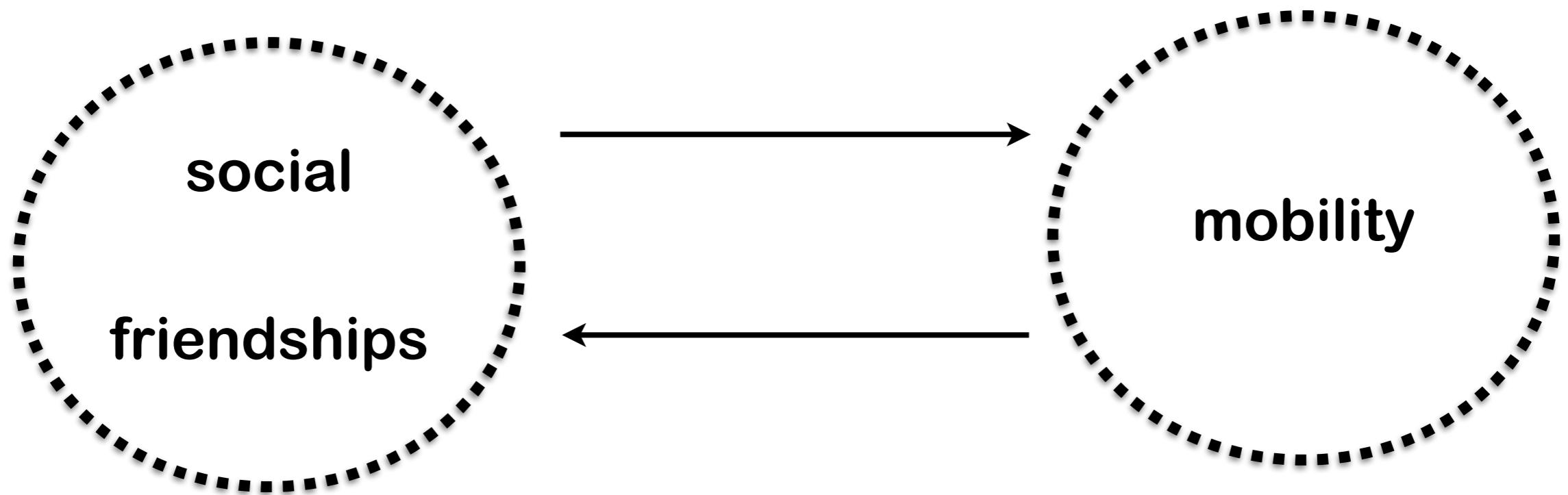


Growth, innovation, scaling, and the pace of life in cities
<http://www.pnas.org/content/104/17/7301.long>

Table 1. Scaling exponents for urban indicators vs. city size

Y	β	95% CI	Adj-R ²	Observations	Country–year
New patents	1.27	[1.25,1.29]	0.72	331	U.S. 2001
Inventors	1.25	[1.22,1.27]	0.76	331	U.S. 2001
Private R&D employment	1.34	[1.29,1.39]	0.92	266	U.S. 2002
"Supercreative" employment	1.15	[1.11,1.18]	0.89	287	U.S. 2003
R&D establishments	1.19	[1.14,1.22]	0.77	287	U.S. 1997
R&D employment	1.26	[1.18,1.43]	0.93	295	China 2002
Total wages	1.12	[1.09,1.13]	0.96	361	U.S. 2002
Total bank deposits	1.08	[1.03,1.11]	0.91	267	U.S. 1996
GDP	1.15	[1.06,1.23]	0.96	295	China 2002
GDP	1.26	[1.09,1.46]	0.64	196	EU 1999–2003
GDP	1.13	[1.03,1.23]	0.94	37	Germany 2003
Total electrical consumption	1.07	[1.03,1.11]	0.88	392	Germany 2002
New AIDS cases	1.23	[1.18,1.29]	0.76	93	U.S. 2002–2003
Serious crimes	1.16	[1.11, 1.18]	0.89	287	U.S. 2003
Total housing	1.00	[0.99,1.01]	0.99	316	U.S. 1990
Total employment	1.01	[0.99,1.02]	0.98	331	U.S. 2001
Household electrical consumption	1.00	[0.94,1.06]	0.88	377	Germany 2002
Household electrical consumption	1.05	[0.89,1.22]	0.91	295	China 2002
Household water consumption	1.01	[0.89,1.11]	0.96	295	China 2002
Gasoline stations	0.77	[0.74,0.81]	0.93	318	U.S. 2001
Gasoline sales	0.79	[0.73,0.80]	0.94	318	U.S. 2001
Length of electrical cables	0.87	[0.82,0.92]	0.75	380	Germany 2002
Road surface	0.83	[0.74,0.92]	0.87	29	Germany 2002

Reflections of two processes



“[Cities] differ from towns and suburbs in basic ways, and one of these is that cities are, by definition, full of strangers”

-Jane Jacobs,



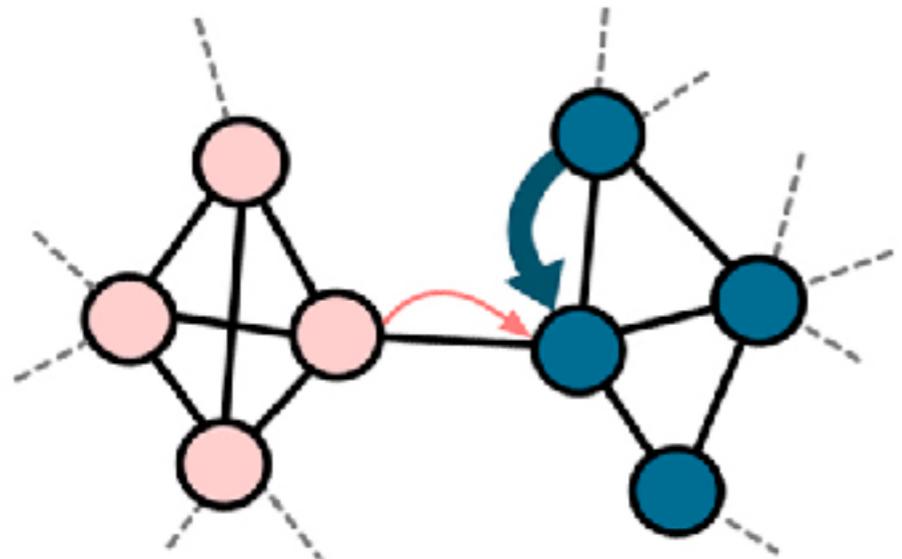
Most common non-British
Nationalities by London borough
Data: UK Census 2011
Photo: Yanko Tihov, 2015

1961

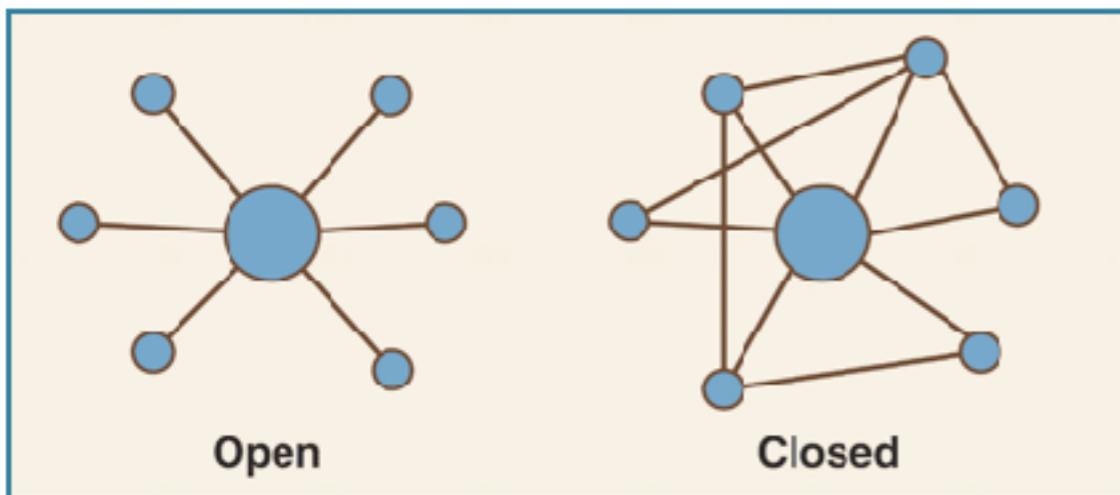


Hristova, Desislava, et al. "Measuring Urban Social Diversity Using Interconnected Geo-Social Networks." Proceedings of the 25th International Conference on World Wide Web. International World Wide Web Conferences Steering Committee, 2016.

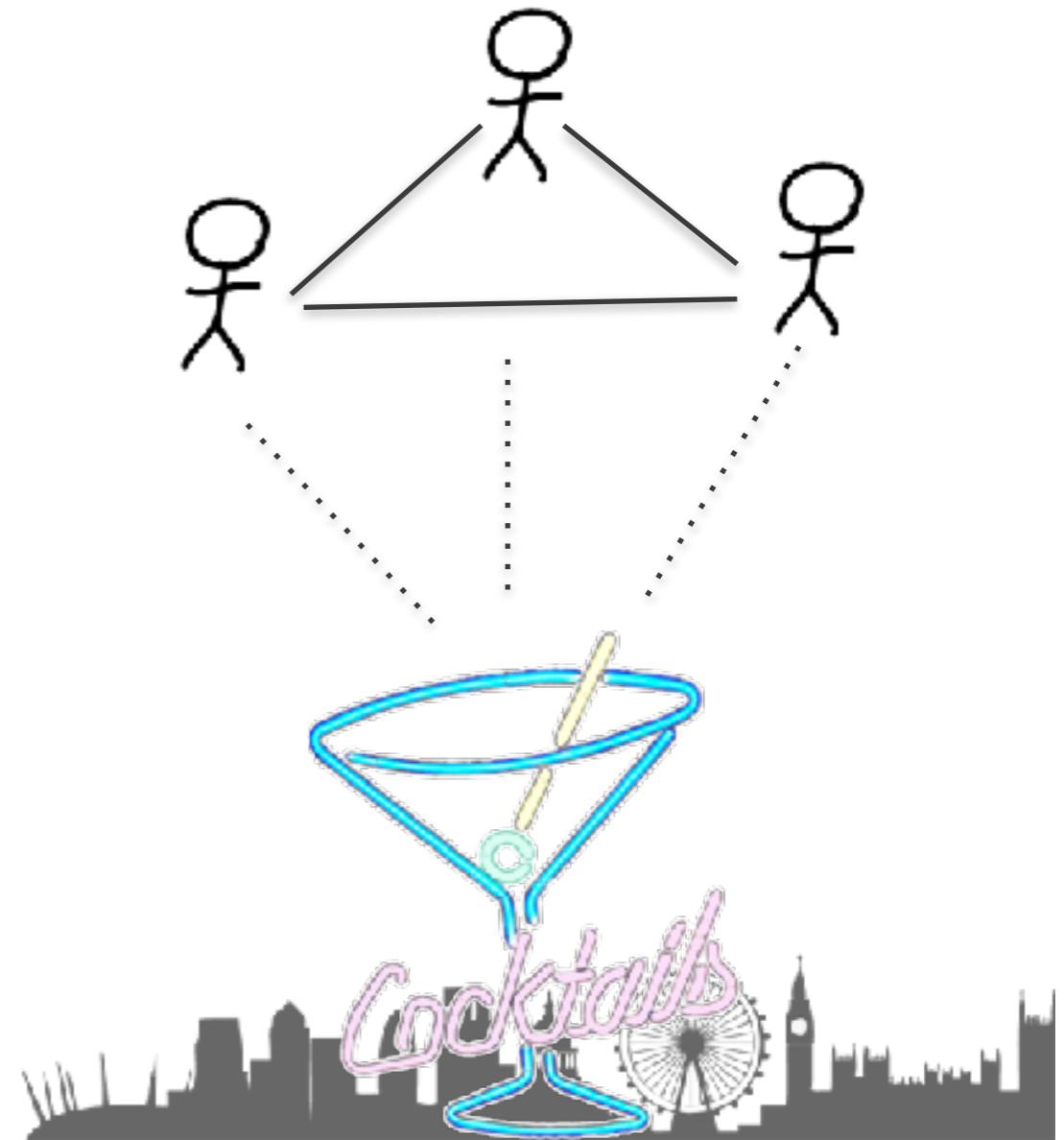
Strangers & Social Capital



Bridging vs Bonding



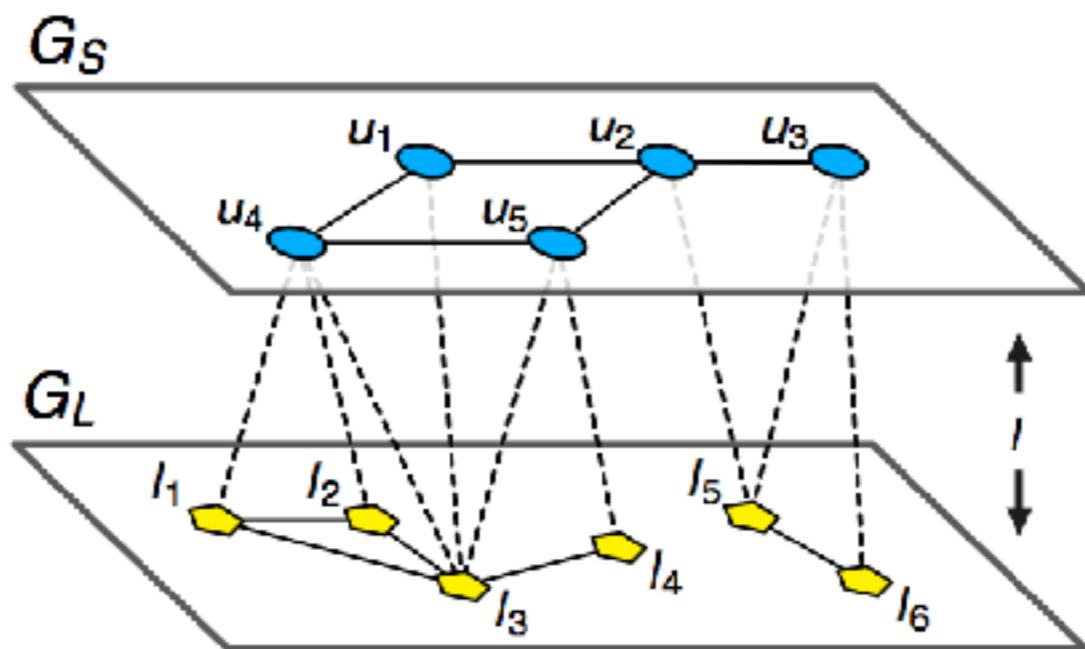
Social Brokerage



Geo-Social Brokerage

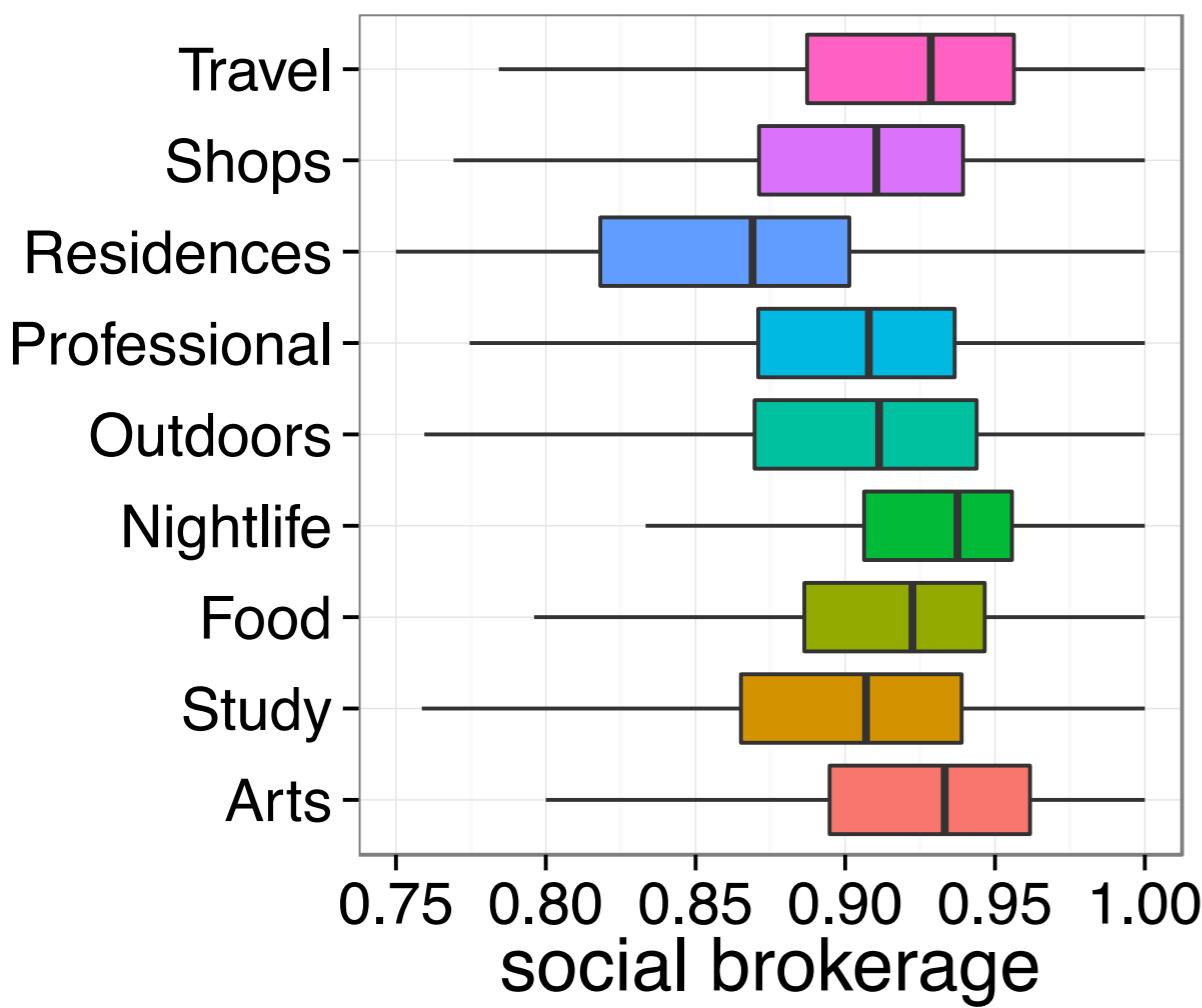
Geo-Social Interconnected Network

(a)



Social Brokerage of Places

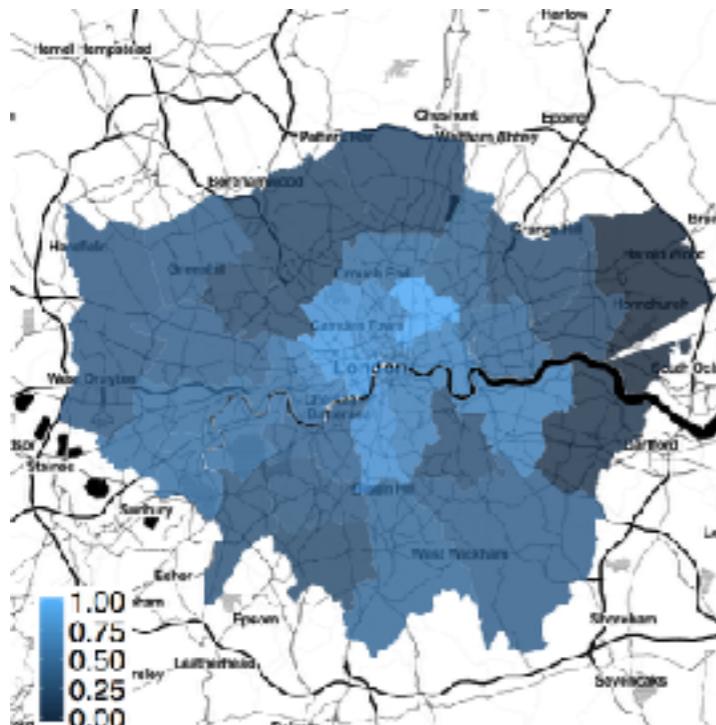
$$B(l) = |N_S^h(l)| - \frac{\sum_{u,v \in N_S^h(l)} e_{u,v}}{|N_S^h(l)|}$$



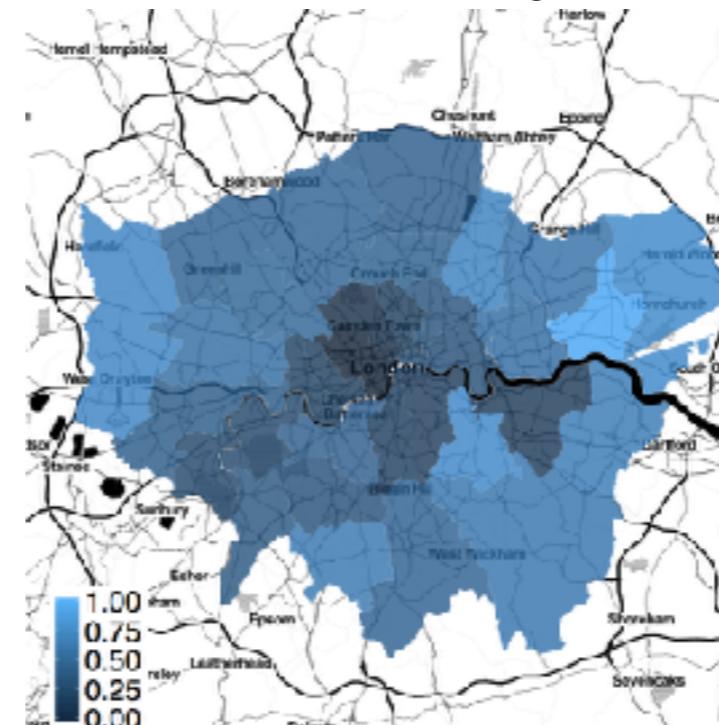
Category	Bridging role	Bonding role
Travel	Motel	B&B
Shops	Mall	Laundry
Residences	Apartment Building	Home
Professional	Courthouse	Emergency Room
Outdoors	Bridge	Vineyard
Nightlife	Gay Bar	Strip Club
Food	Dumplings	Fried Chicken
Study	Bookstore	Classroom
Arts	Art Museum	Football

Urban Diversity

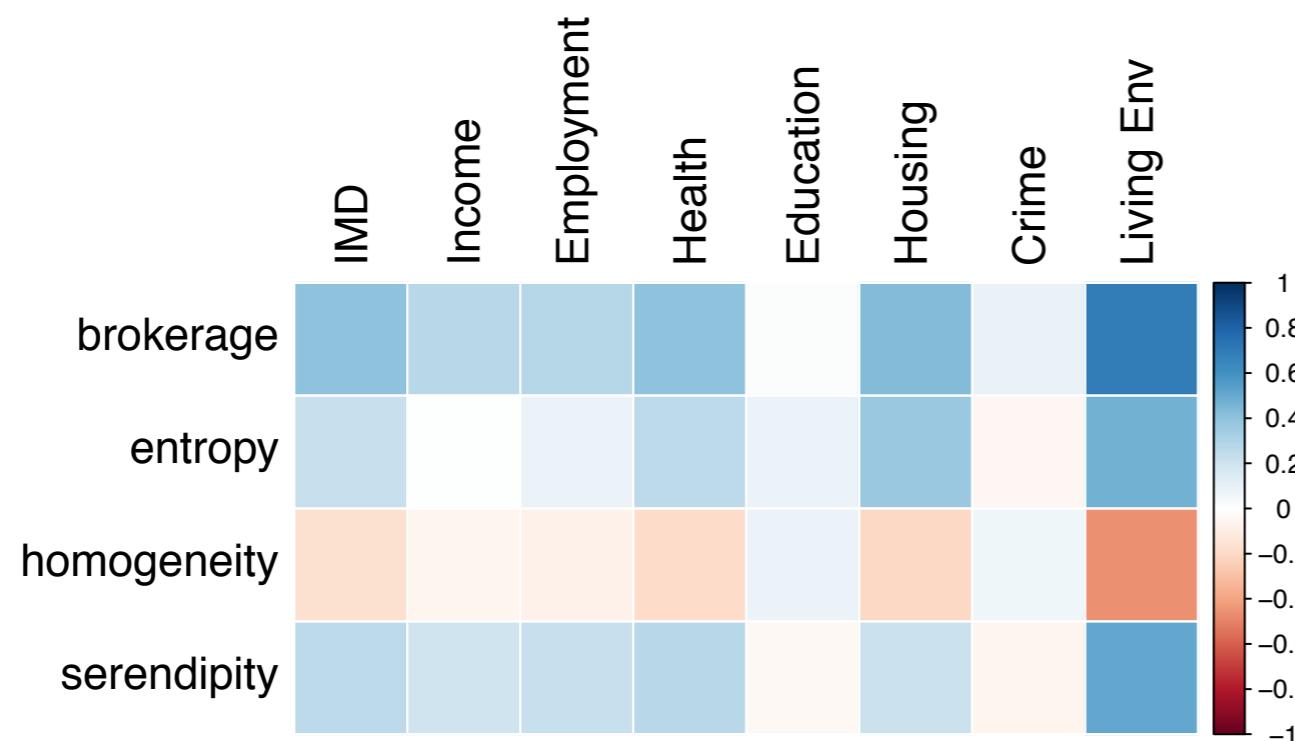
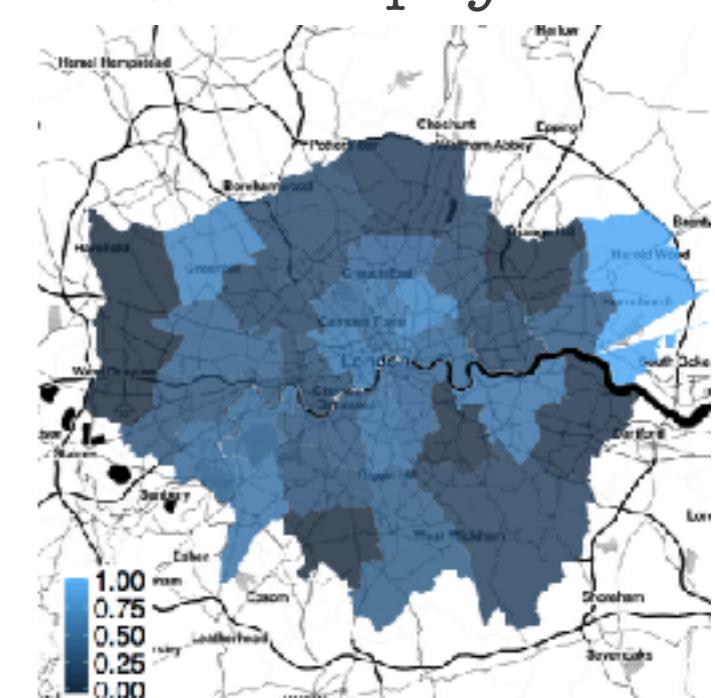
Brokerage



Homogeneity

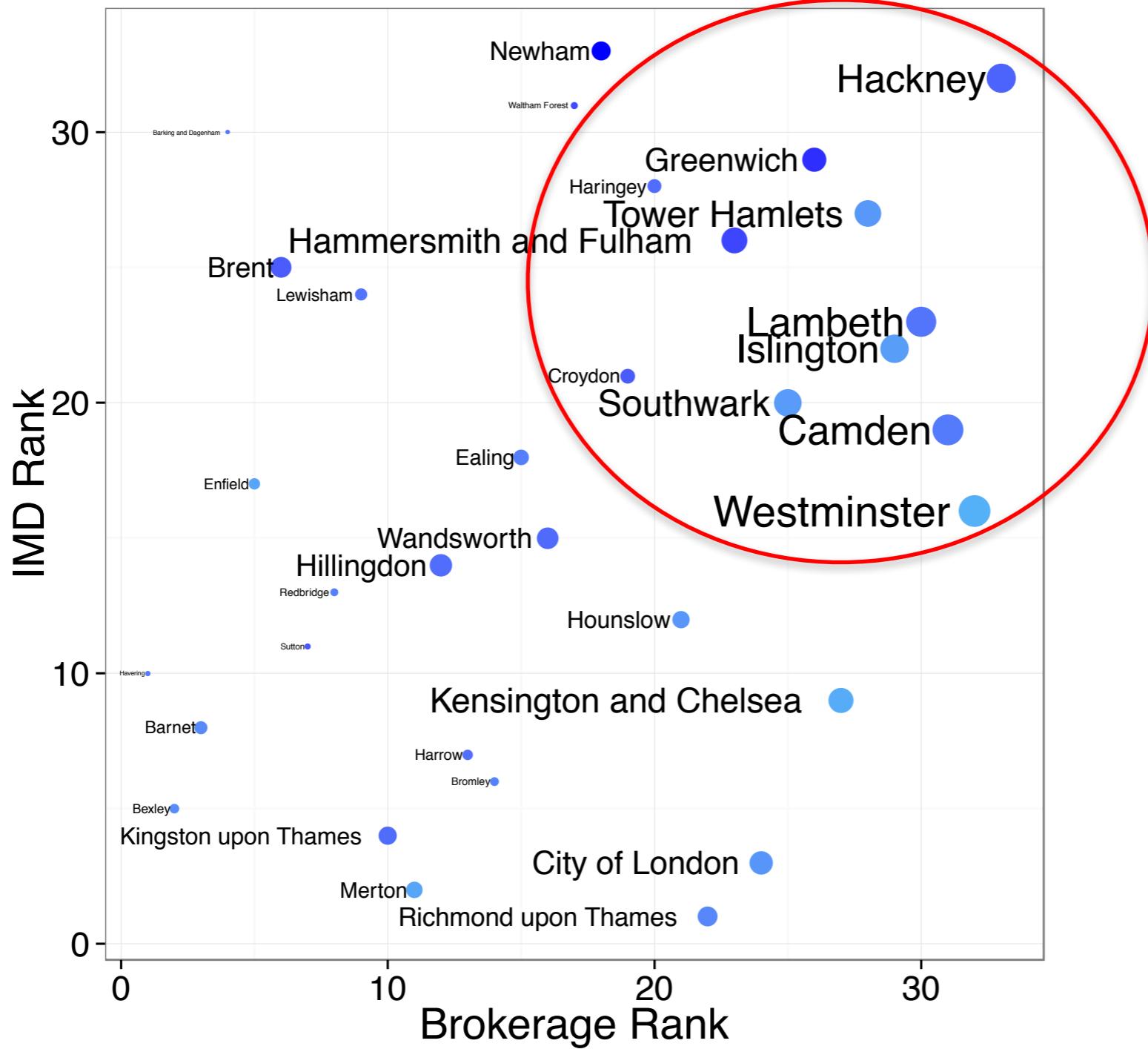


Serendipity



Deprivation is higher
in areas with higher
urban social diversity.

Diversity and Deprivation



Hackney, 2011

Population: 246K

Age: 25-34

Avg. House Price: £326K

2nd most deprived

Hackney, 2016

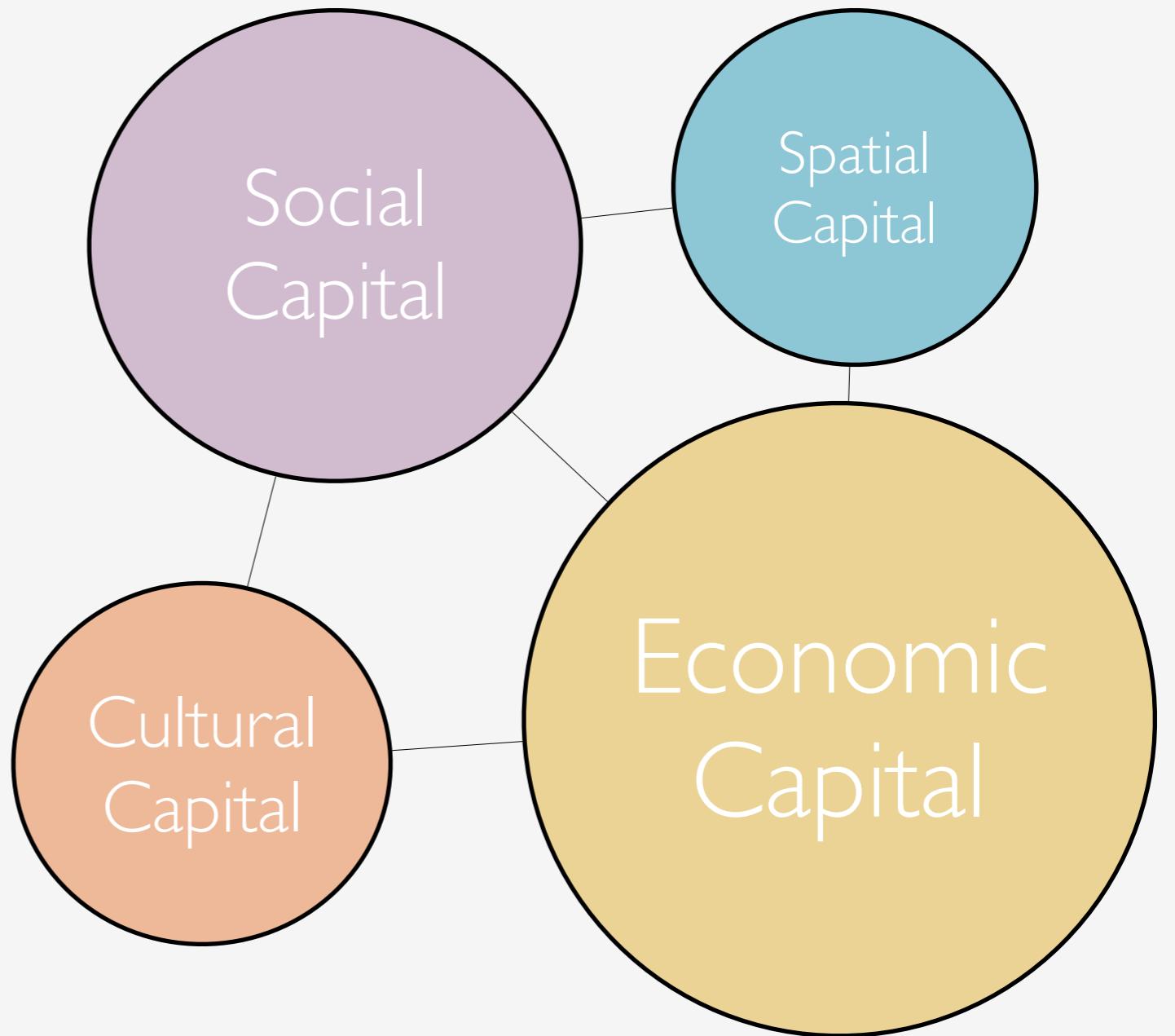
Population: 263K

Age: 25-34

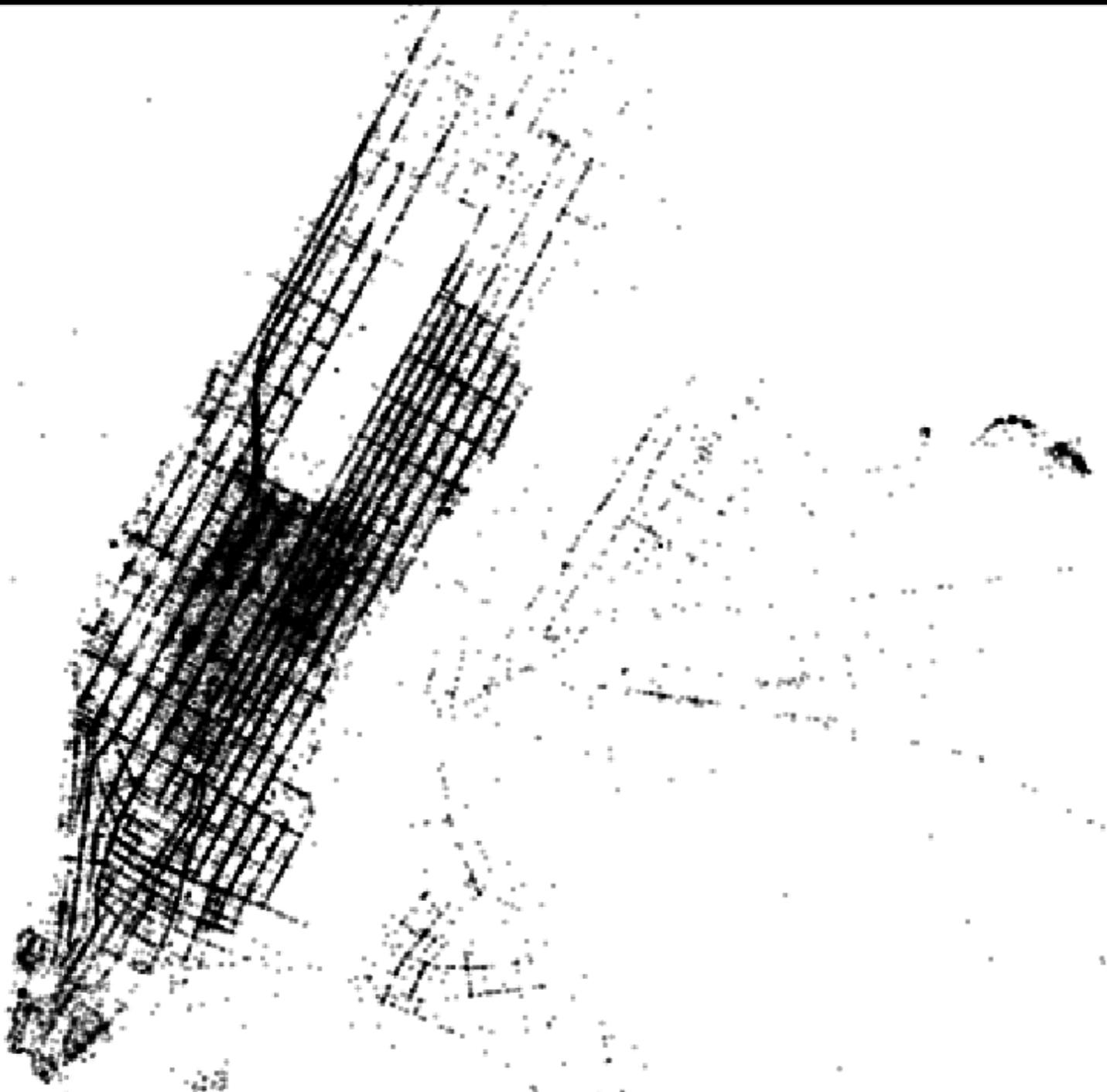
Avg. House Price: £546K

11th most deprived

Forms of Urban Capital



THE NEW YORK CITY TAXI DATASET



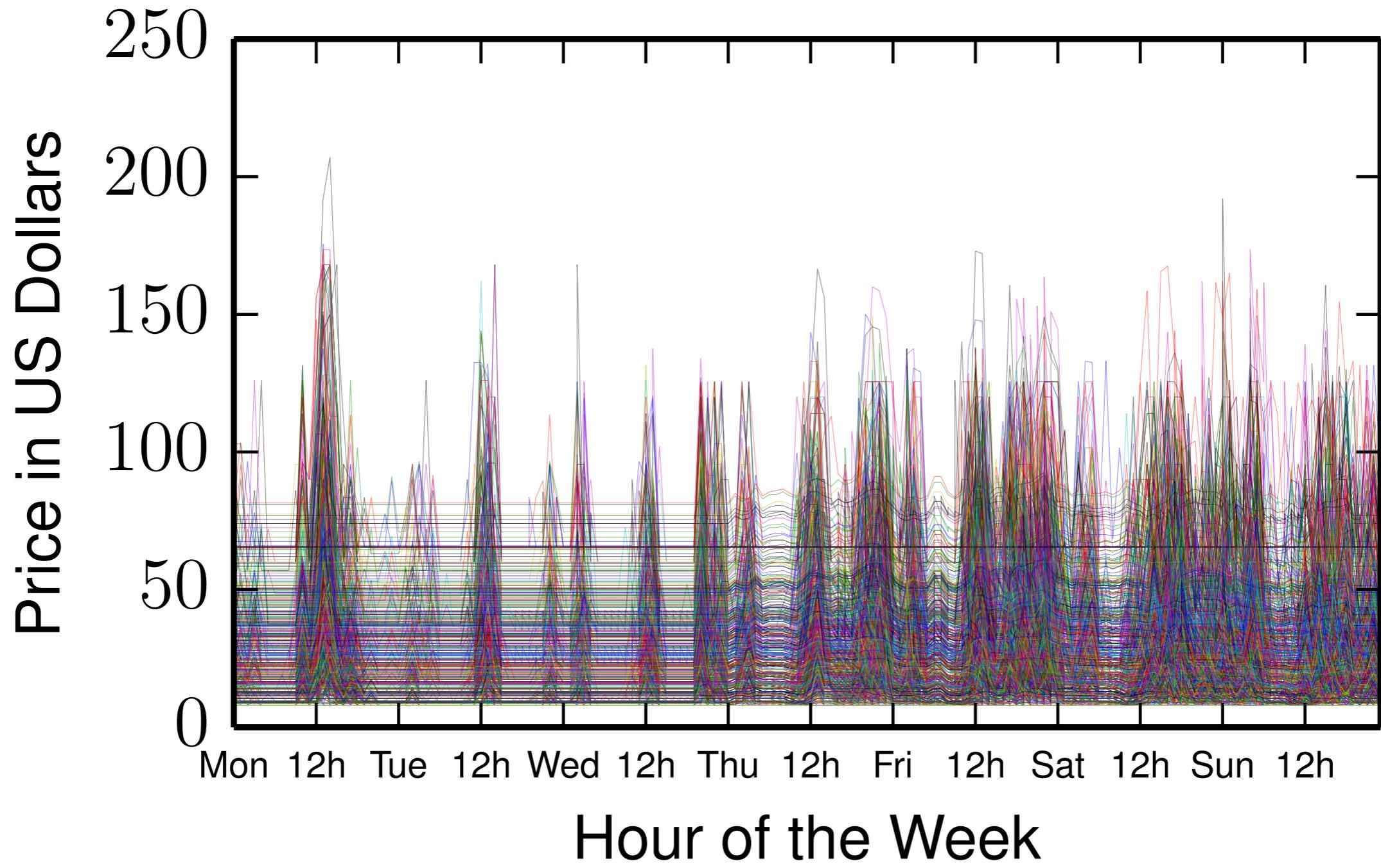
FOILing NYC's Taxi Trip Data

Freedom of Information Law

2013 Trip Data, 11GB, zipped!

2013 Fare Data, 7.7GB

**Idea: Uber Vs Yellow Taxi
Price Comparison.**





OpenStreetCab

Carrier 11:51 PM Carrier 11:51 PM Carrier 11:51 PM Carrier 11:51 PM Carrier 11:51 PM



OpenStreetCab
London

→



OpenStreetCab
New York

Place in New York

Destination

Place in New York

Uber or Yellow

Take a Yellow cab!

Uber	\$83
Yellow cab	\$63
Saving	\$20

The above prices are estimates. Paid more?
Send us your feedback!

Share **Feedback**

Take Uber!

Uber	£8
Black cab	£13
Saving	£5

The above prices are estimates. Paid more?
Send us your feedback!

Share **Feedback**

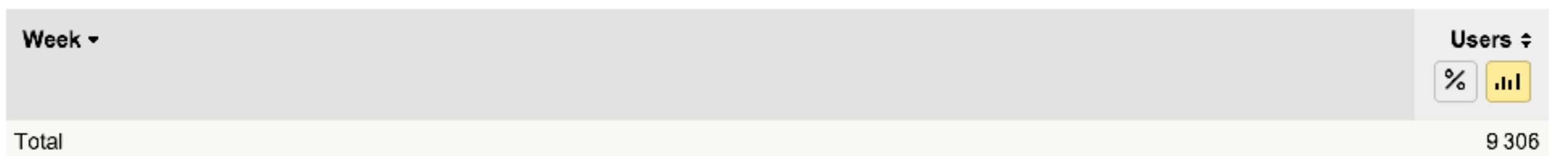
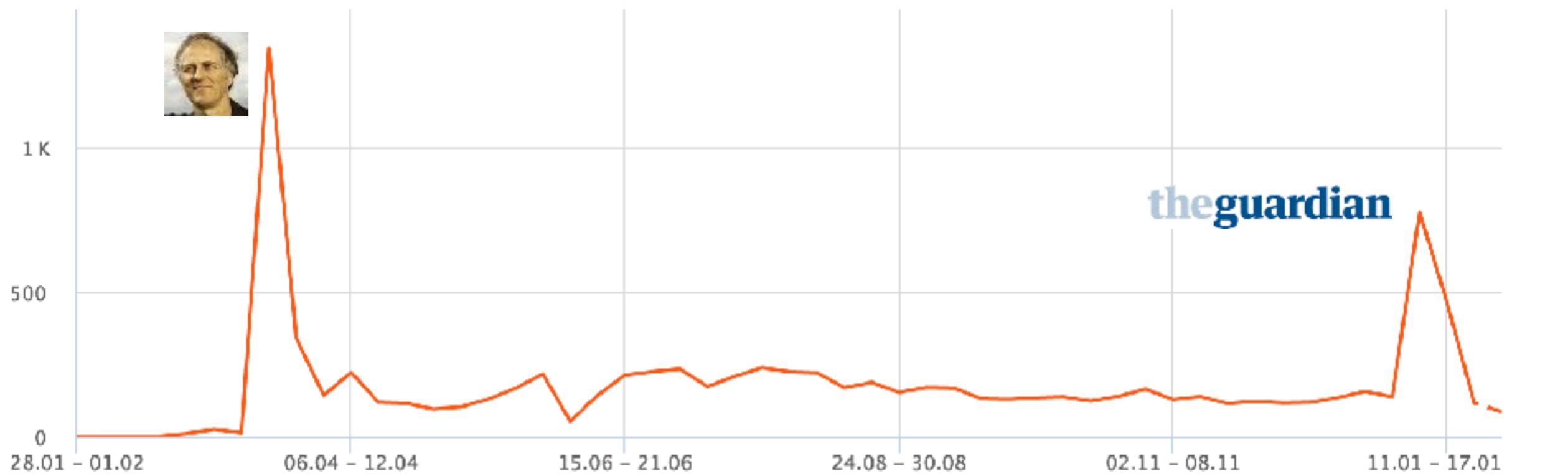
Designed by **SquareMatters**
www.squarematters.net

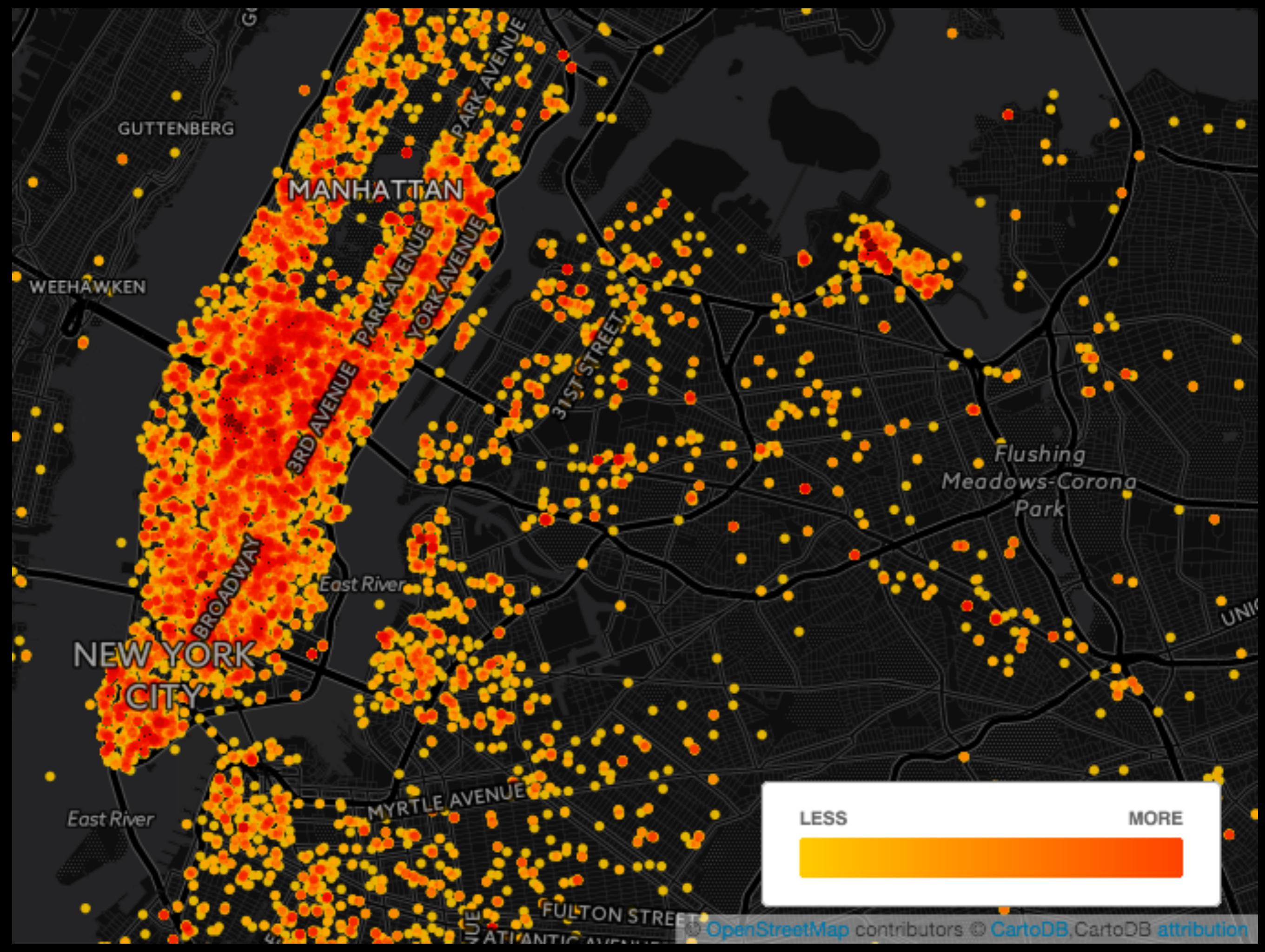
City Choice

← Go Back

← Go Back

And later on



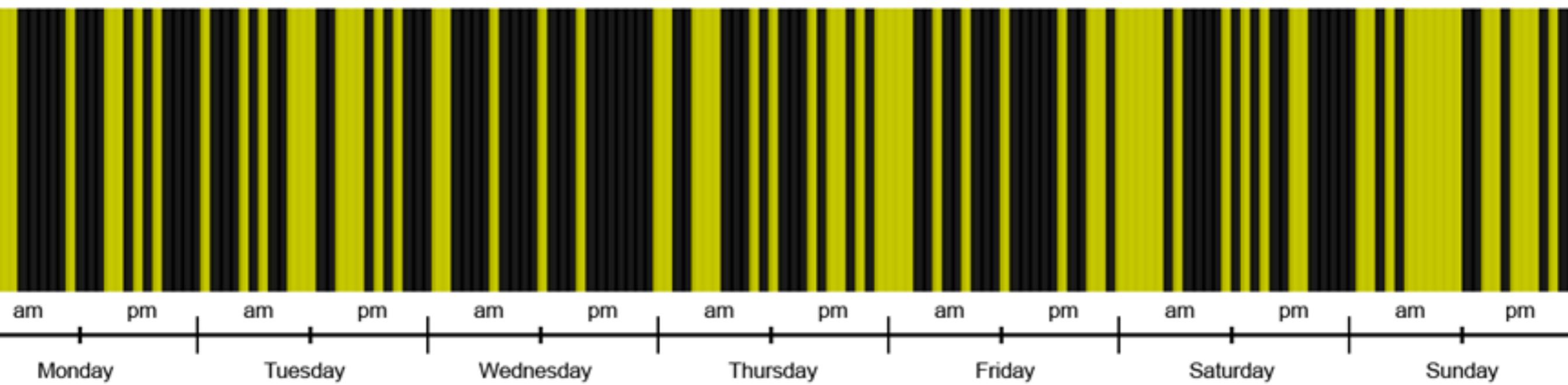


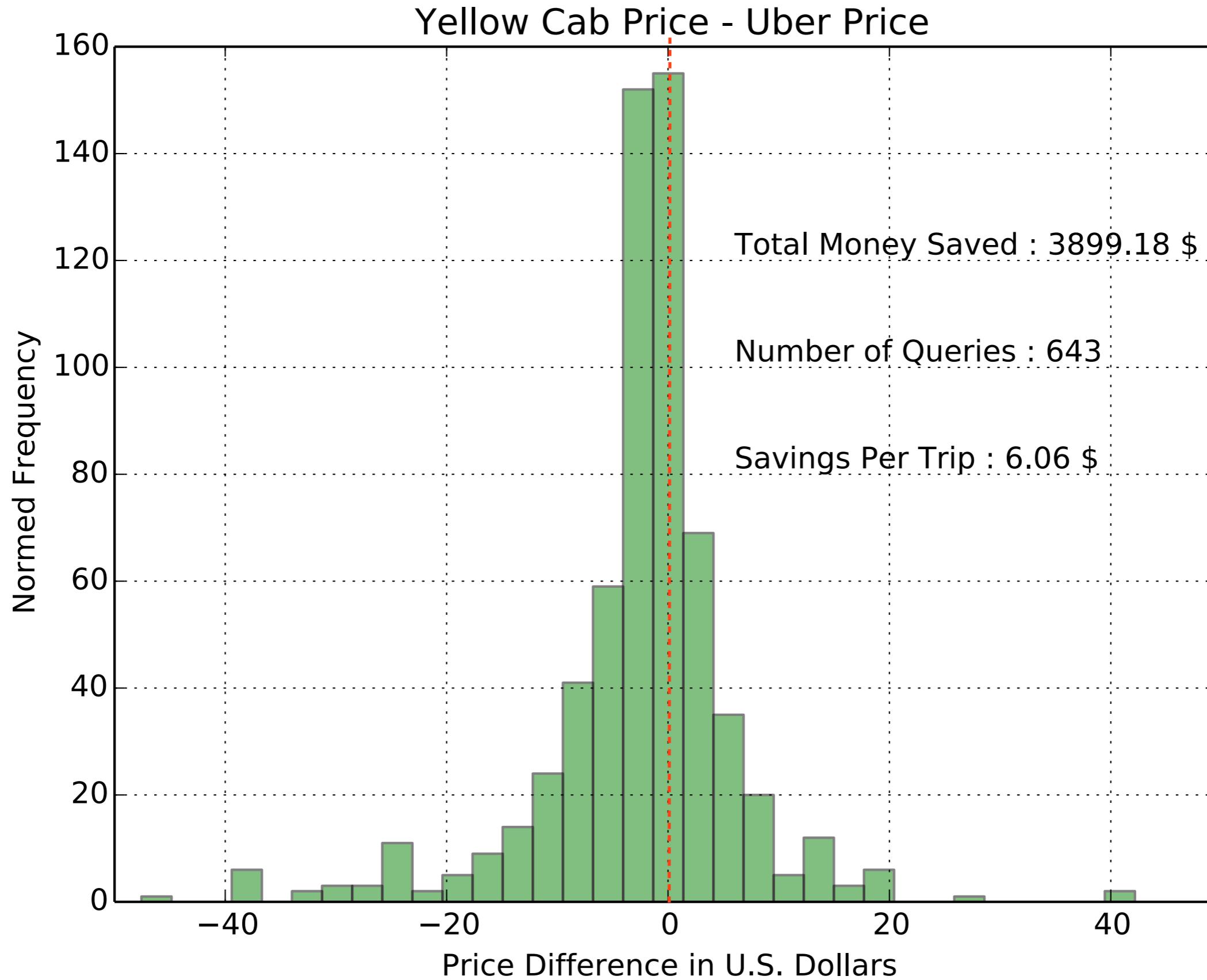
LESS

MORE

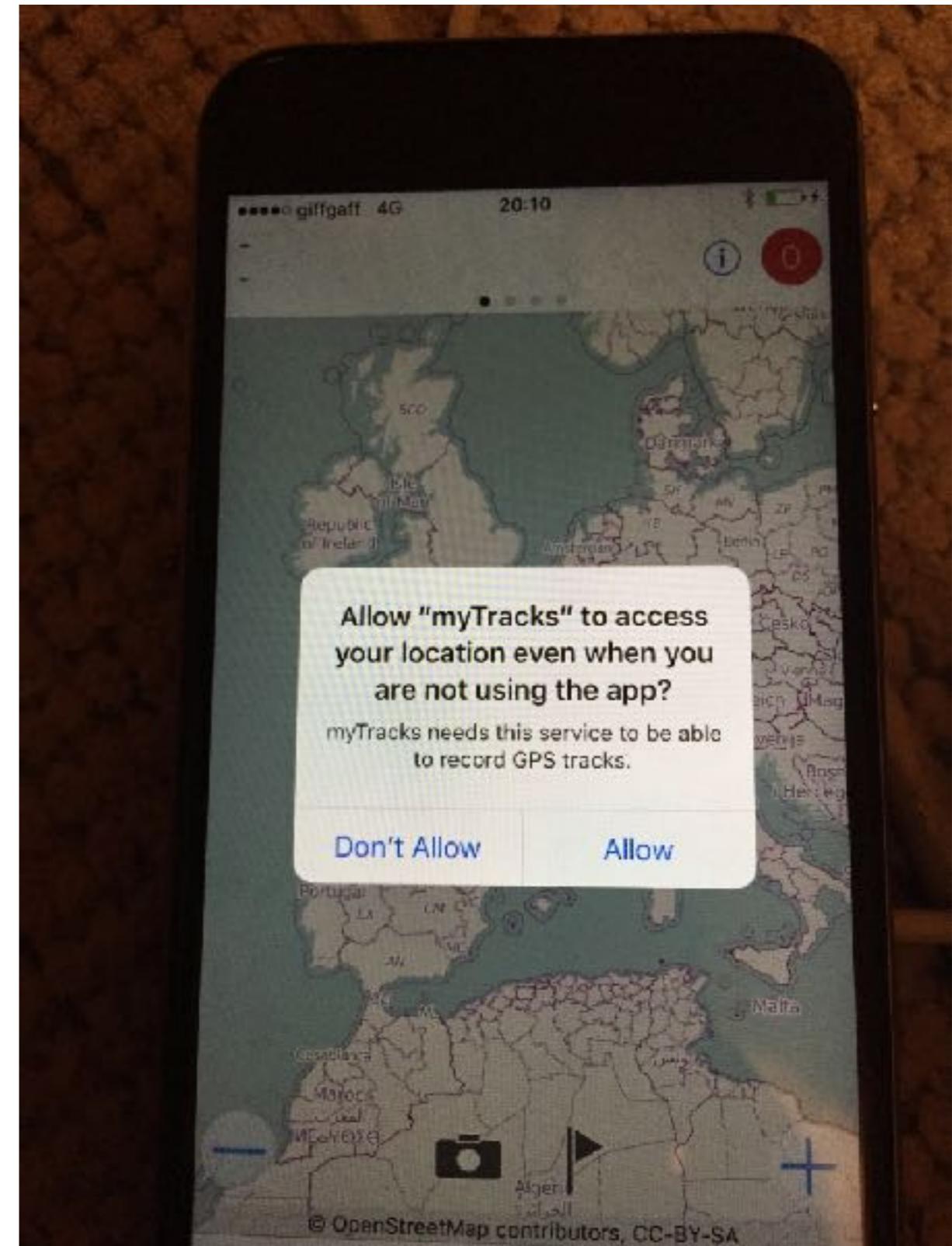
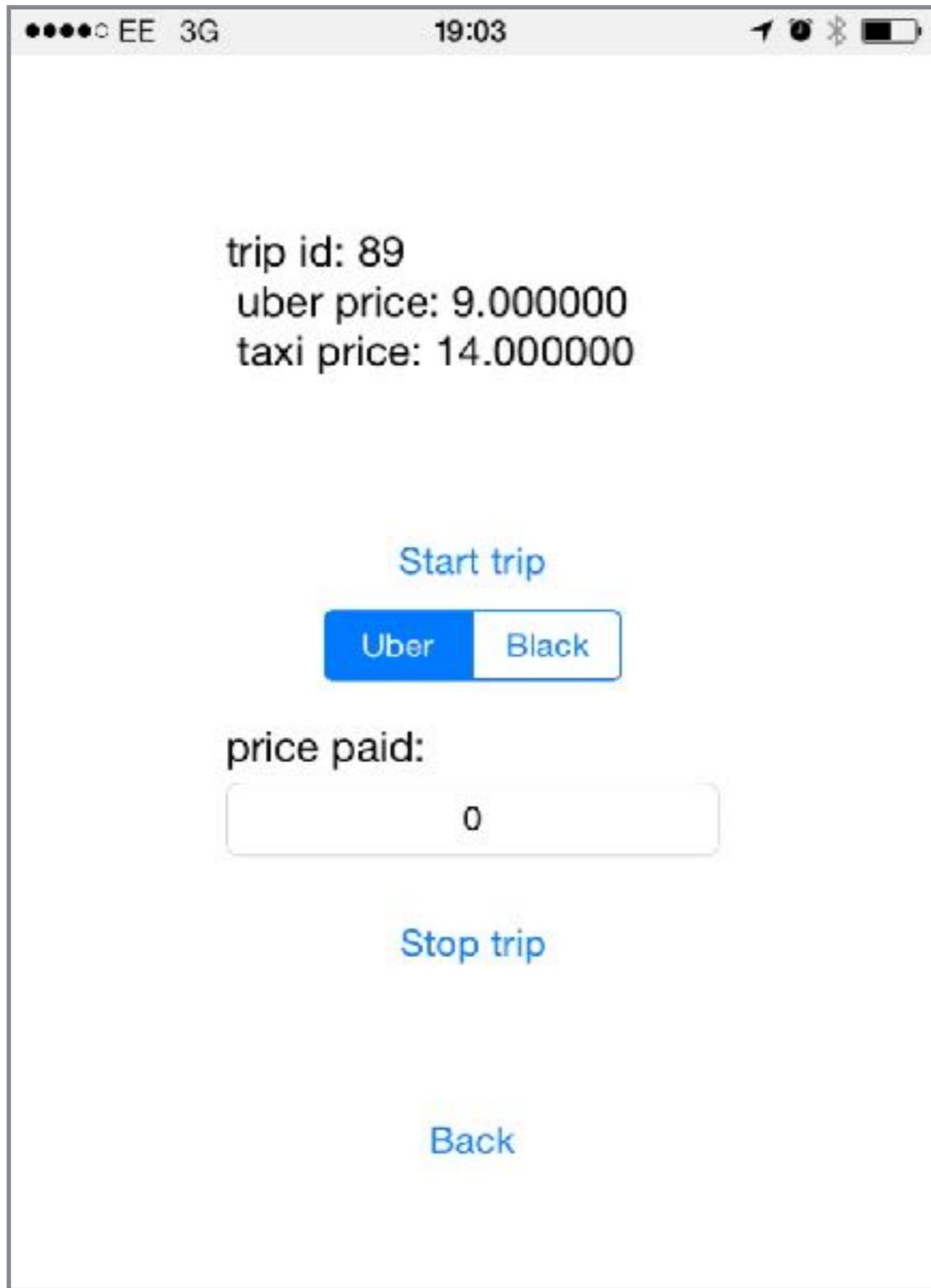
> 5K only in New York (~8K downloaded the app)

> 14000 search queries generated





ROUTE TRACKING



University College London NW11 1H2

109 Camden
Road

UCL

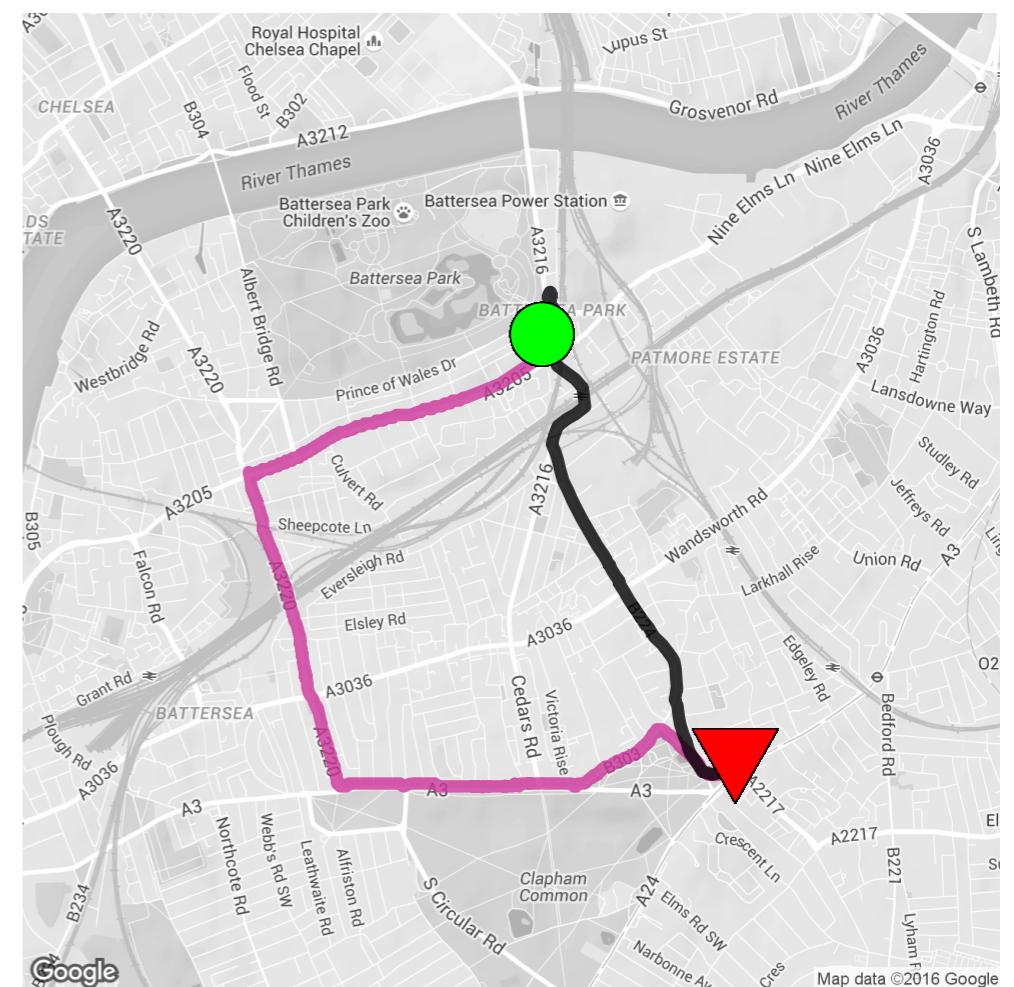
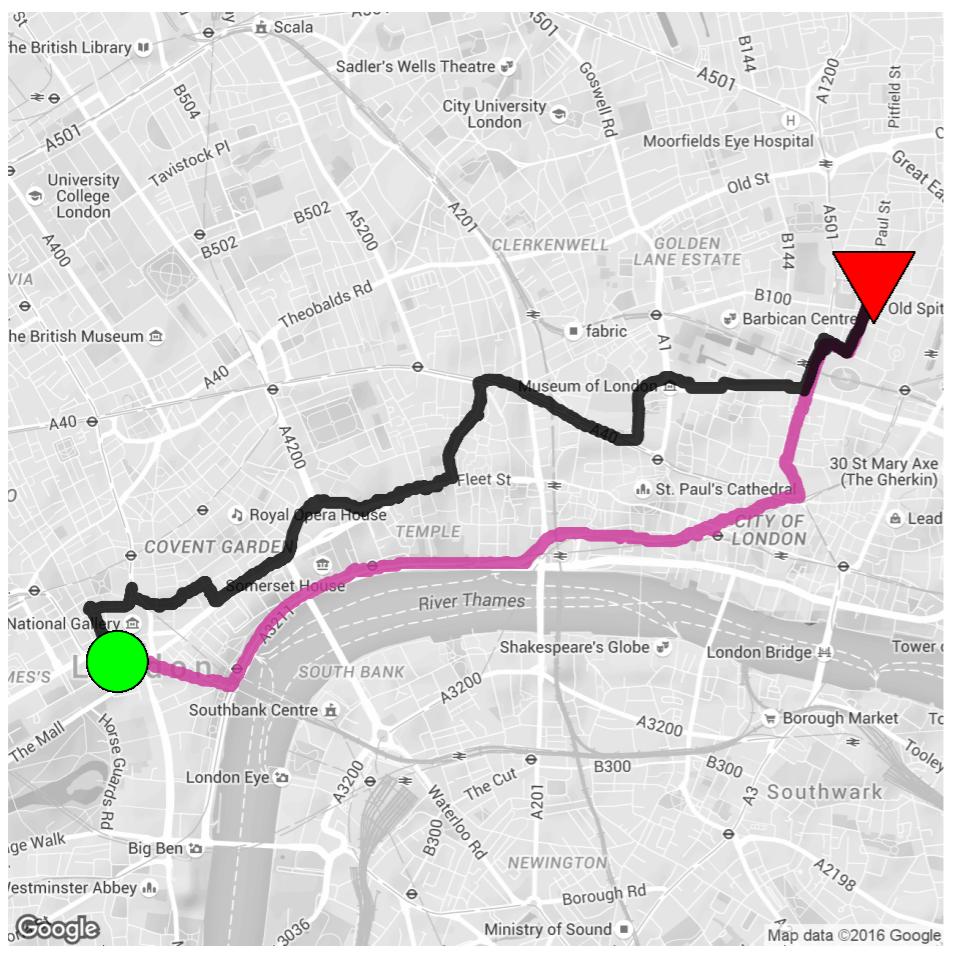
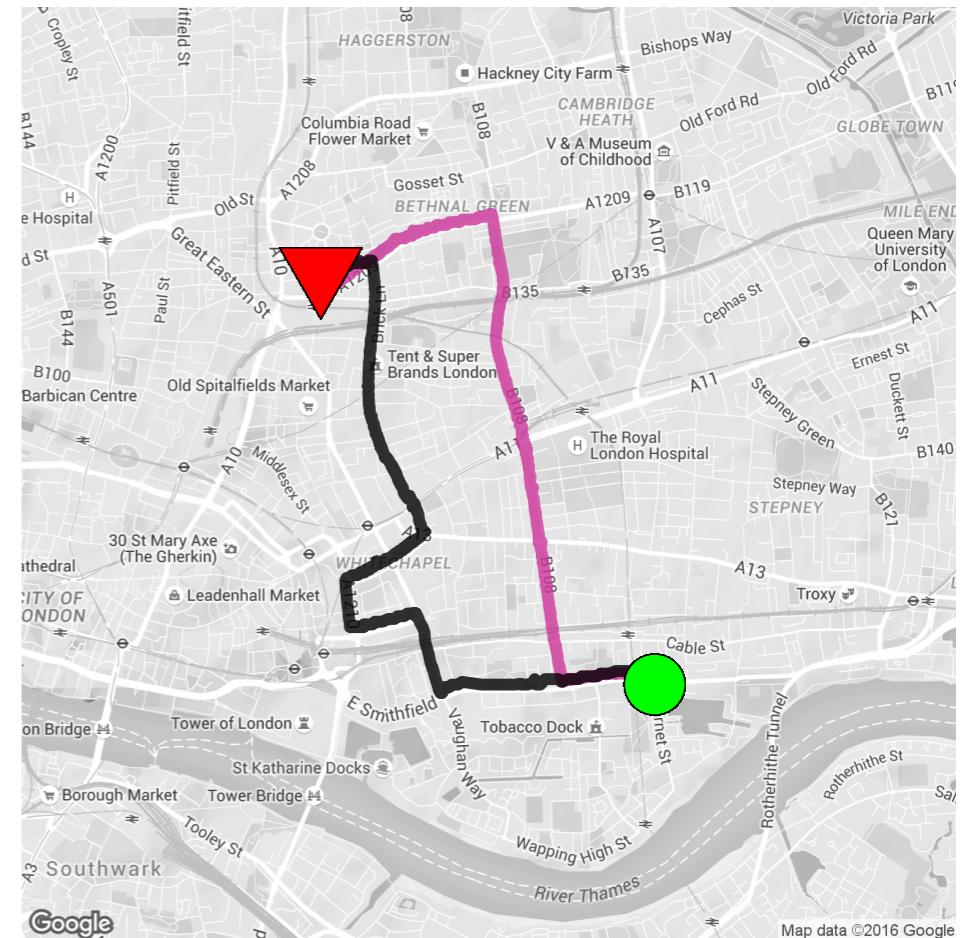
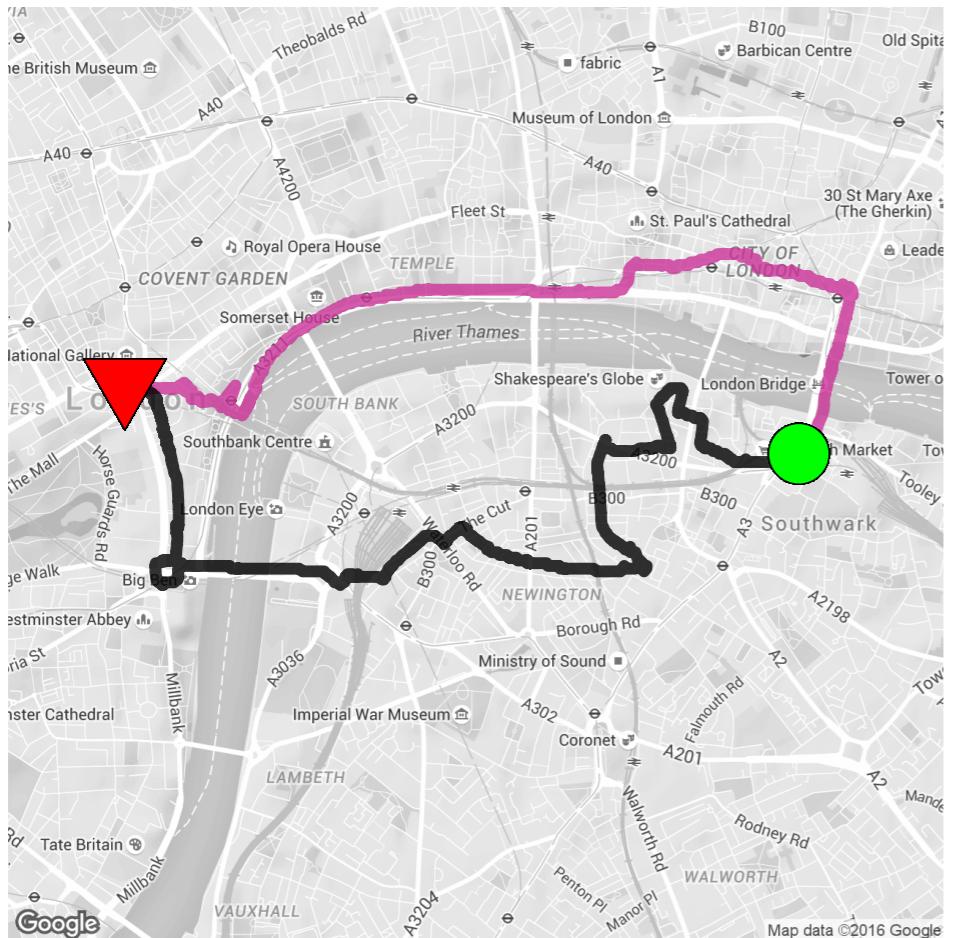


⌚ 12:00



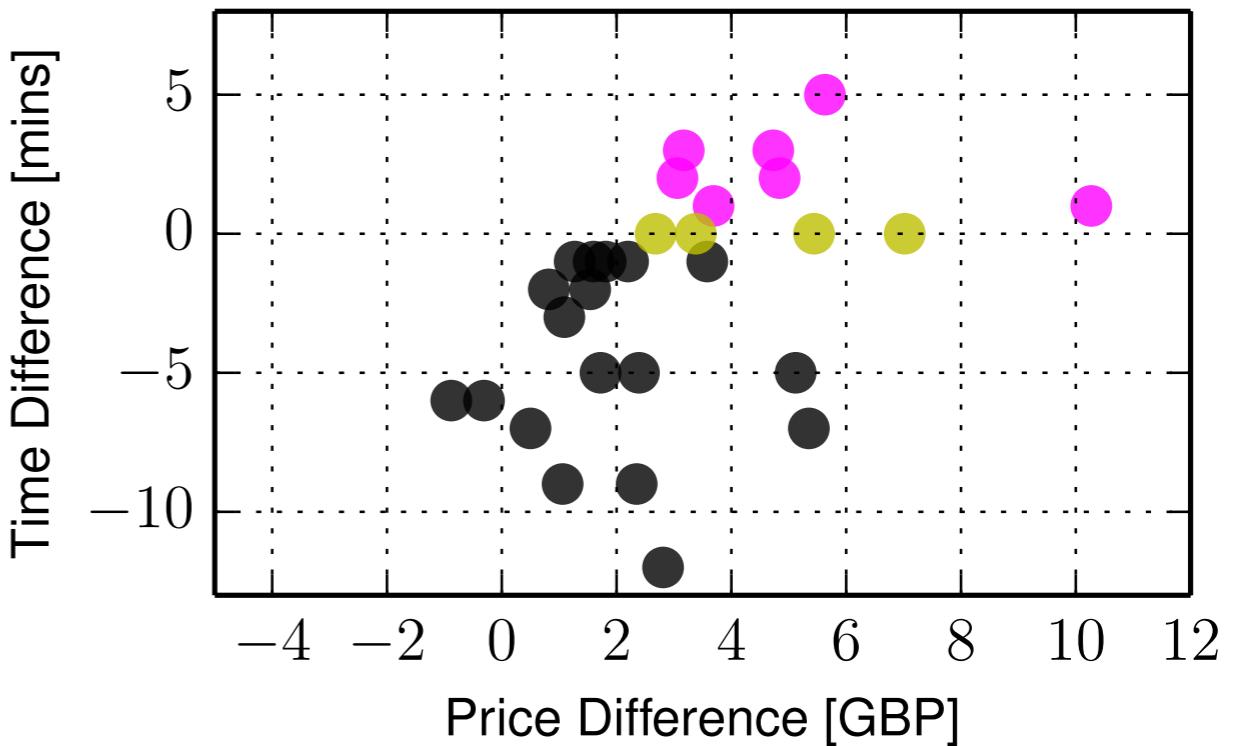
2016/02/22
Monday



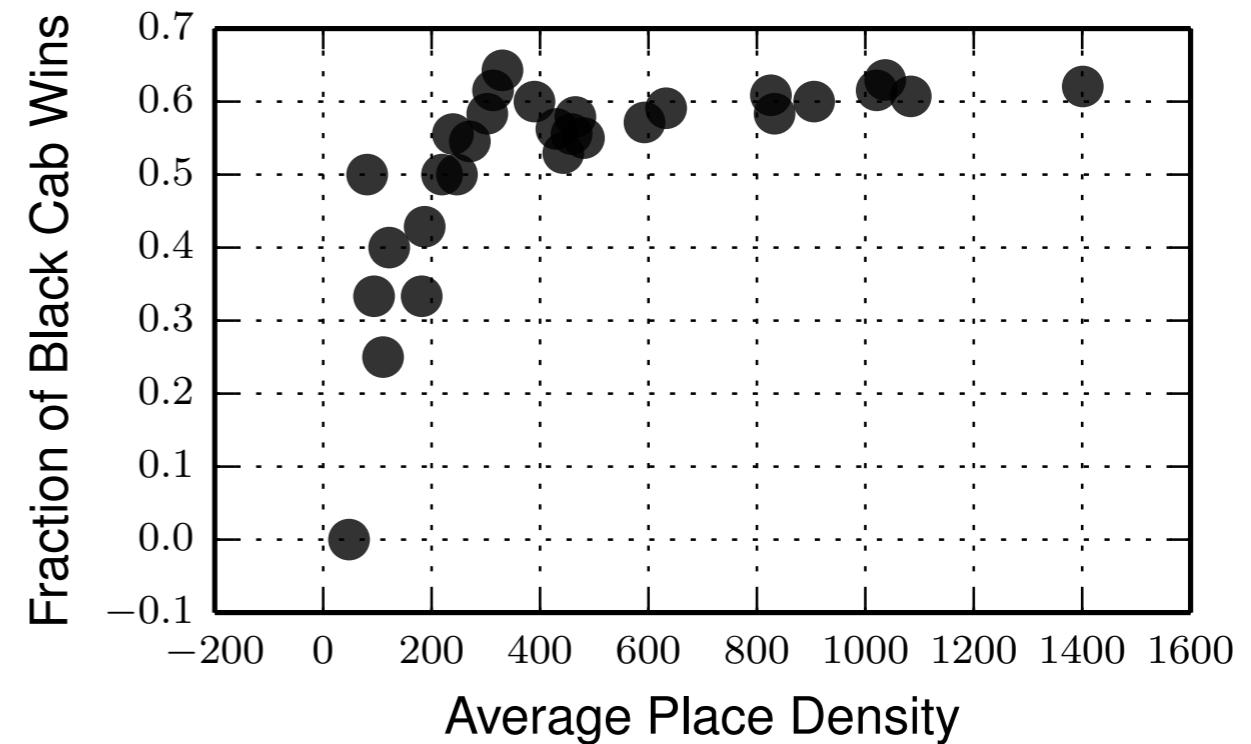


URBAN COMPLEXITY & PERFORMANCE

- Uber faster
- Black Cab faster
- Journey duration tie



$$Trip_Density = \frac{1}{|T|} \frac{\sum_{i=1}^{|T|} P(x = \text{lng}_i, y = \text{lat}_i, r = 200m)}{\pi r^2}$$



Taxi Sharing/Pooling



Combine k trips



<http://hubcab.org/>

Santi, Paolo, et al. "Quantifying the benefits of vehicle pooling with shareability networks." Proceedings of the National Academy of Sciences 111.37 (2014): 13290-13294.

THANK YOU

@taslanous

