



**DATA
SCIENCE**

word2vec in theory and practice with tensorflow

<https://github.com/bmtgoncalves/word2vec-and-friends/>

Bruno Gonçalves

www.bgoncalves.com



Teaching machines to read!

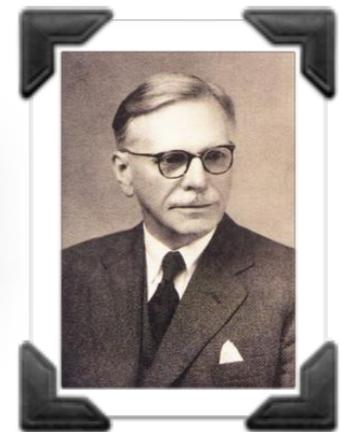
- Computers are really good at crunching numbers but not so much when it comes to words.
- Perhaps can we represent words numerically?

$$v_{\text{after}} = (0, 0, 0, 1, 0, 0, \dots)^T$$
$$v_{\text{above}} = (0, 0, 1, 0, 0, 0, \dots)^T$$

One-hot
encoding

- Can we do it in a way that preserves **semantic** information?

“You shall know a word by the company it keeps”
(J. R. Firth)



- **Words** that have similar **meanings** are used in similar **contexts** and the context in which a word is used helps us understand its meaning.

The red **house** is beautiful.

The blue **house** is old.

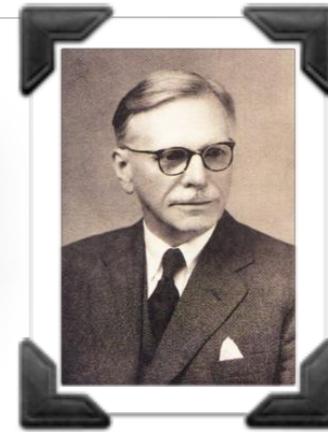
The red **car** is beautiful.

The blue **car** is old.

a	1
about	2
above	3
after	4
again	5
against	6
all	7
am	8
an	9
and	10
any	11
are	12
aren't	13
as	14
...	...

Teaching machines to read!

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- Words with similar meanings should have similar representations.
- From a word we can get some idea about the context where it might appear

_____ house _____
_____ car _____

$$\max p(C|w)$$

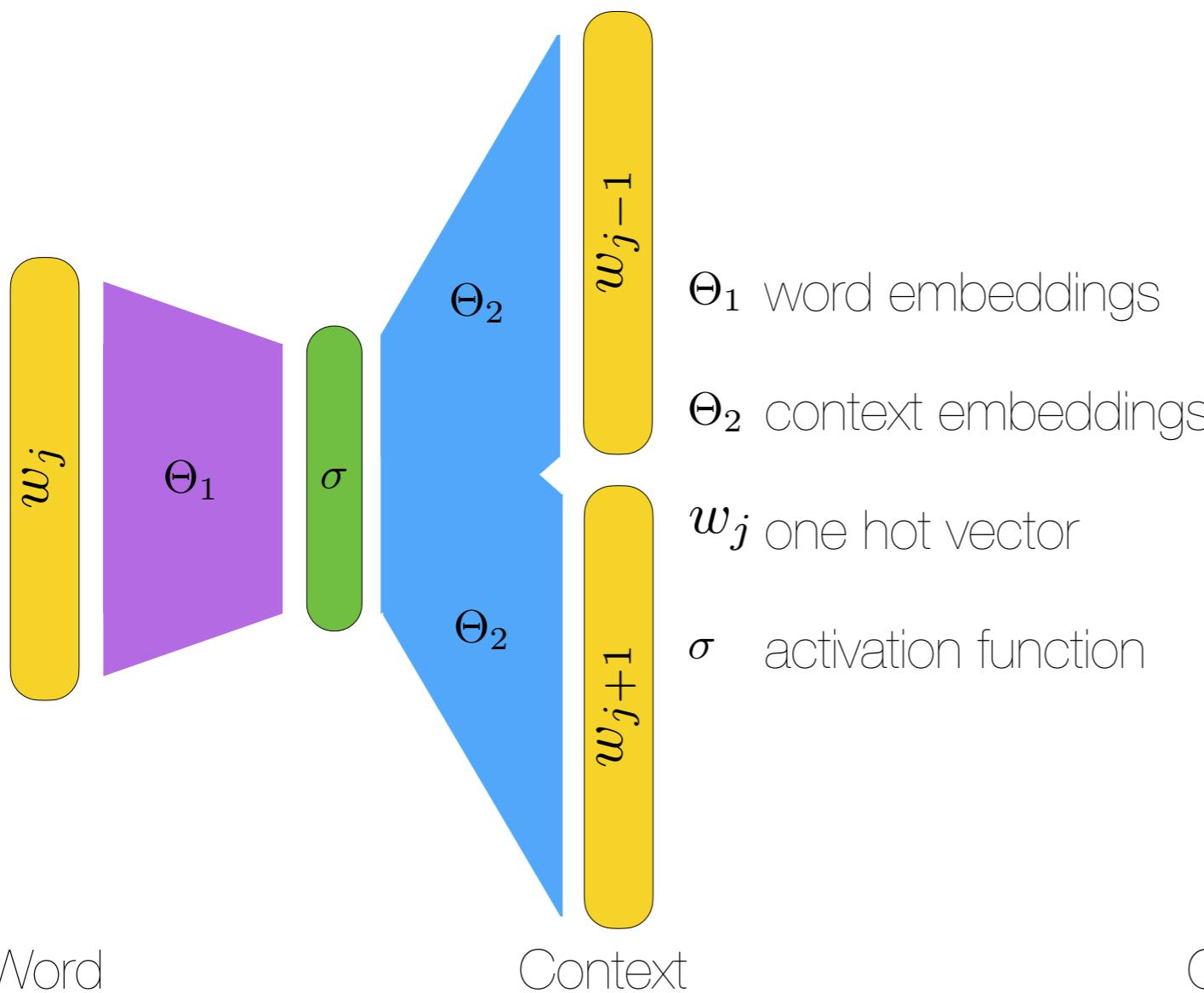
- And from the context we have some idea about possible words

The red _____ is beautiful.
The blue _____ is old.

$$\max p(w|C)$$

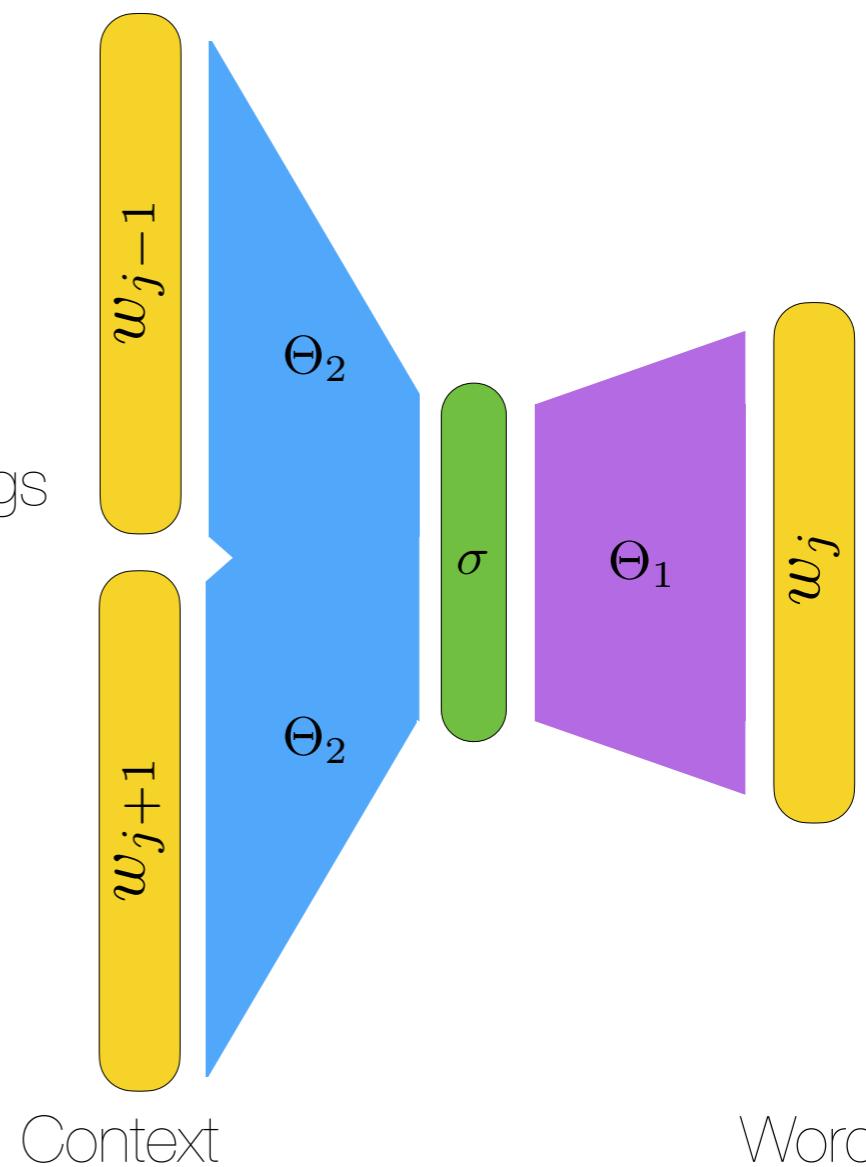
Skipgram

$$\max p(C|w)$$



Continuous Bag of Words

$$\max p(w|C)$$



Skipgram

- Let us take a better look at a simplified case with a single context word
- Words are one-hot encoded vectors $w_j = (0, 0, 1, 0, 0, 0, \dots)^T$ of length V

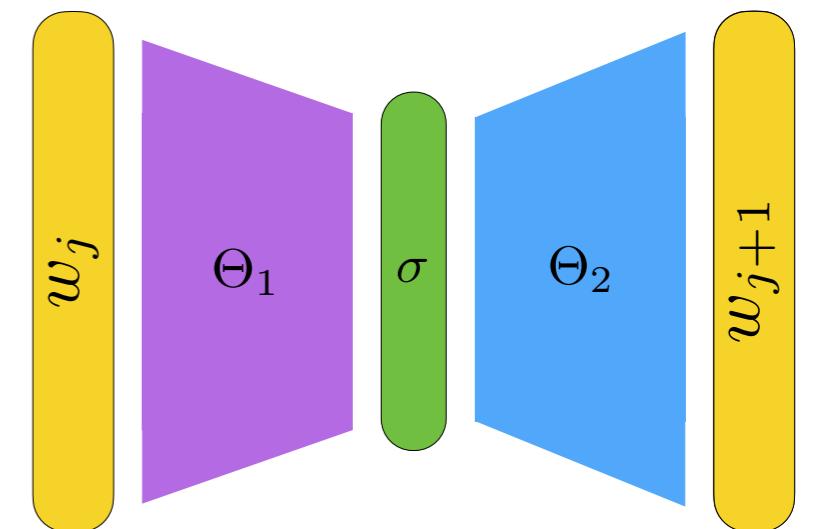
- Θ_1 is an $(M \times V)$ matrix so that when we take the product:

$$\Theta_1 \cdot w_j$$

- We are effectively selecting the j 'th column of Θ_1 :

$$v_j = \Theta_1 \cdot w_j$$

- The **linear** activation function simply passes this value along which is then multiplied by Θ_2 , a $(V \times M)$ matrix.



- Each element k of the output layer its then given by:

$$u_k^T \cdot v_j$$

- We convert these values to a normalized probability distribution by using the **softmax**

Softmax

- A standard way of converting a set of numbers to a normalized probability distribution:

$$\text{softmax}(x) = \frac{\exp(x_j)}{\sum_l \exp(x_l)}$$

- With this final ingredient we obtain:

$$p(w_k|w_j) \equiv \text{softmax}(u_k^T \cdot v_j) = \frac{\exp(u_k^T \cdot v_j)}{\sum_l \exp(u_l^T \cdot v_j)}$$

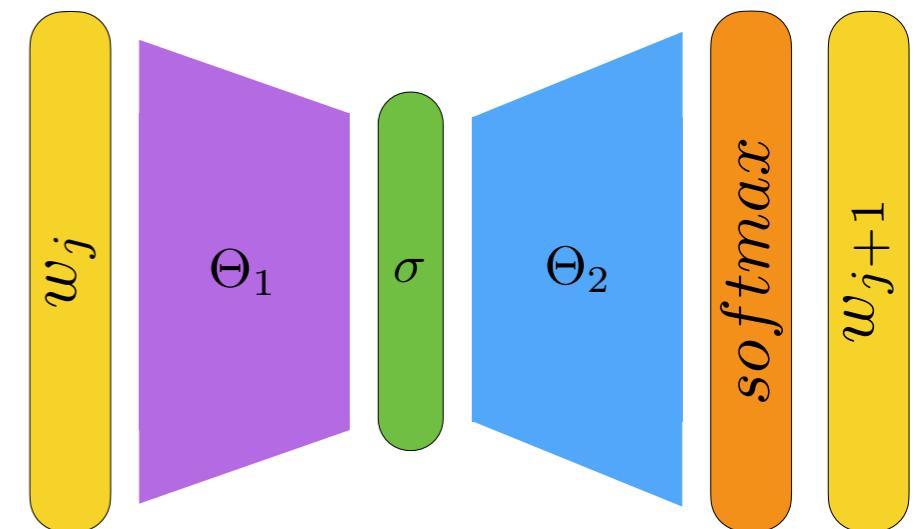
- Our goal is then to learn:

$$\Theta_1 \quad \Theta_2$$

- so that we can predict what the next word is likely to be using:

$$p(w_{j+1}|w_j)$$

- But how can we quantify how far we are from the correct answer? Our error measure shouldn't be just binary (right or wrong)...



Cross-Entropy

- First we have to recall that what we are, in effect, comparing two probability distributions:

$$p(w_k|w_j)$$

- and the one-hot encoding of the context:

$$w_{j+1} = (0, 0, 0, 1, 0, 0, \dots)^T$$

- The Cross Entropy measures the distance, in number of bits, between two probability distributions \mathbf{p} and \mathbf{q} :

$$H(p, q) = - \sum_k p_k \log q_k$$

- In our case, this becomes:

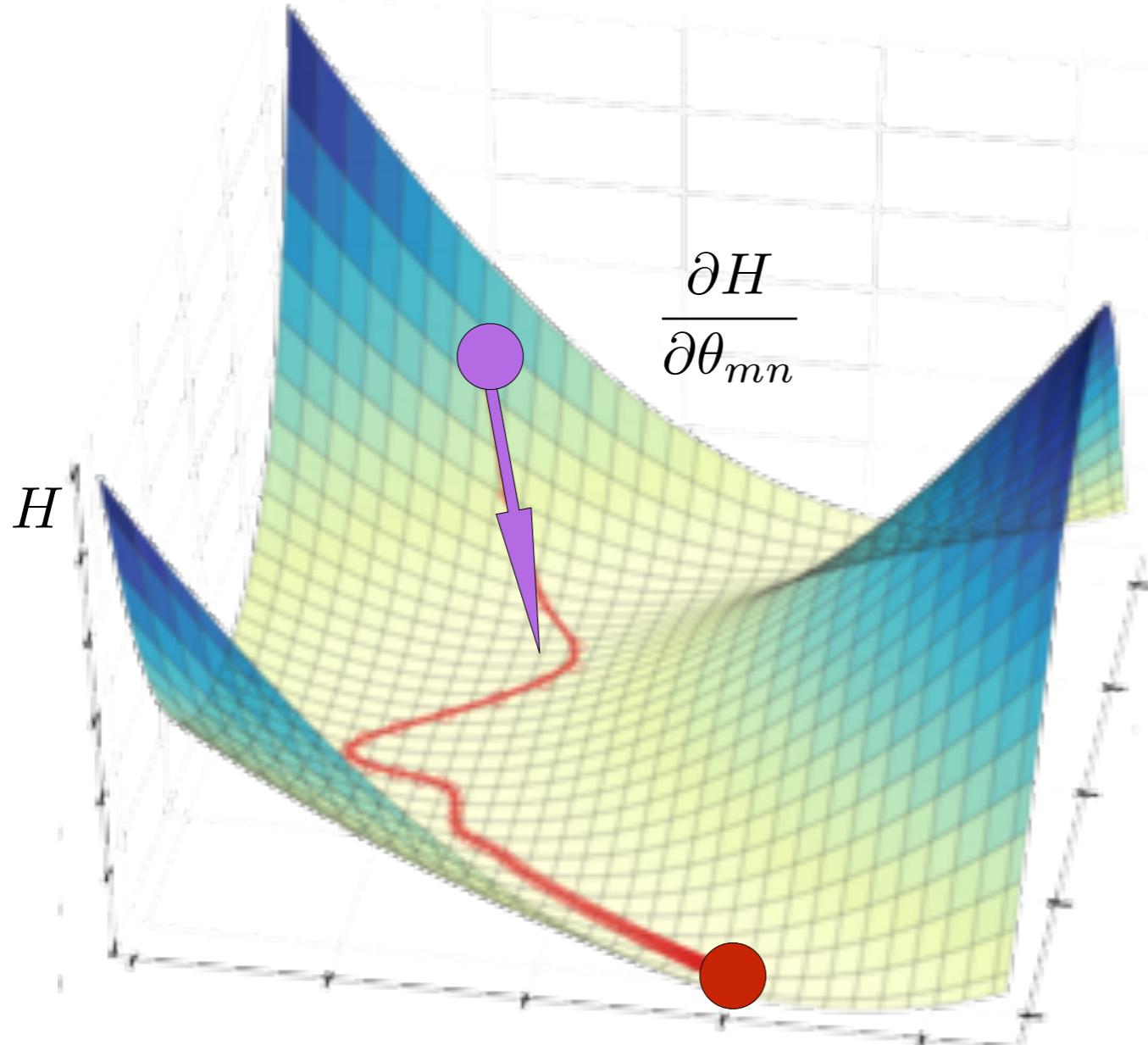
$$H[w_{j+1}, p(w_k|w_j)] = - \sum_k w_{j+1}^k \log p(w_k|w_j)$$

- So it's clear that the only non zero term is the one that corresponds to the "hot" element of w_{j+1}

$$H = - \log p(w_{j+1}|w_j)$$

- This is our Error function. But how can we use this to update the values of Θ_1 and Θ_2 ?

Gradient Descent



- Find the gradient for each training batch
 - Take a step **downhill** along the direction of the gradient
- $$\theta_{mn} \leftarrow \theta_{mn} - \alpha \frac{\partial H}{\partial \theta_{mn}}$$
- where α is the step size.
 - Repeat until "convergence".

Chain-rule

- How can we calculate

$$\frac{\partial H}{\partial \theta_{mn}} = \frac{\partial}{\partial \theta_{mn}} \log p(w_{j+1} | w_j) \quad \theta_{mn} = \left\{ \theta_{mn}^{(1)}, \theta_{mn}^{(2)} \right\}$$

- we rewrite:

$$\frac{\partial H}{\partial \theta_{mn}} = \frac{\partial}{\partial \theta_{mn}} \log \frac{\exp(u_k^T \cdot v_j)}{\sum_l \exp(u_l^T \cdot v_j)}$$

- and expand:

$$\frac{\partial H}{\partial \theta_{mn}} = \frac{\partial}{\partial \theta_{mn}} \left[u_k^T \cdot v_j - \log \sum_l \exp(u_l^T \cdot v_j) \right]$$

- Then we can rewrite:

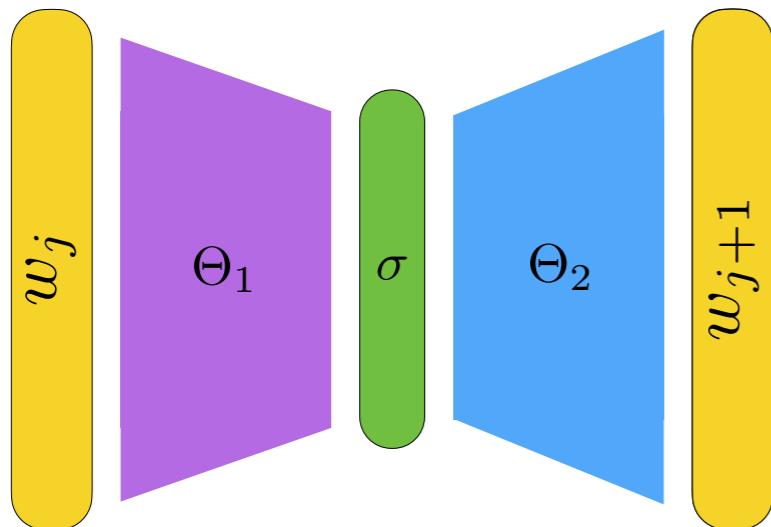
$$u_k^T \cdot v_j = \sum_q \theta_{kq}^{(2)} \theta_{qj}^{(1)}$$

- and apply the chain rule:

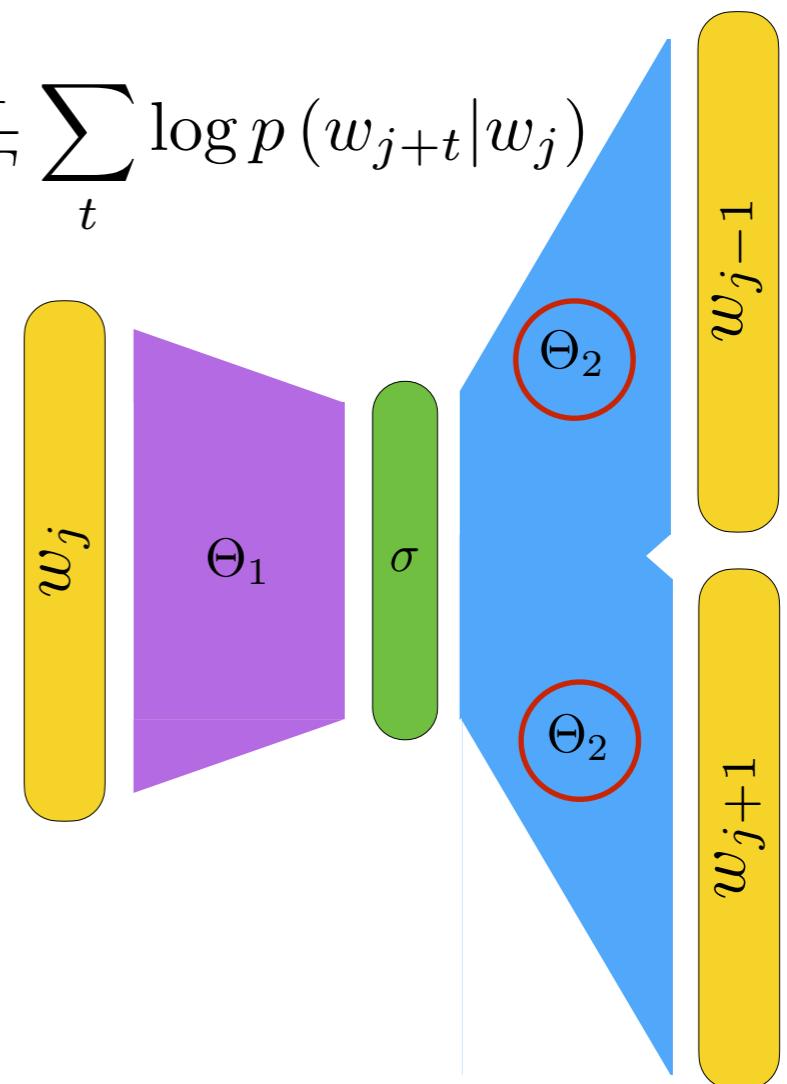
$$\frac{\partial f(g(x))}{\partial x} = \frac{\partial f(g(x))}{\partial g(x)} \frac{\partial g(x)}{\partial x}$$

SkipGram with Larger Contexts

$$H = -\log p(w_{j+1}|w_j)$$



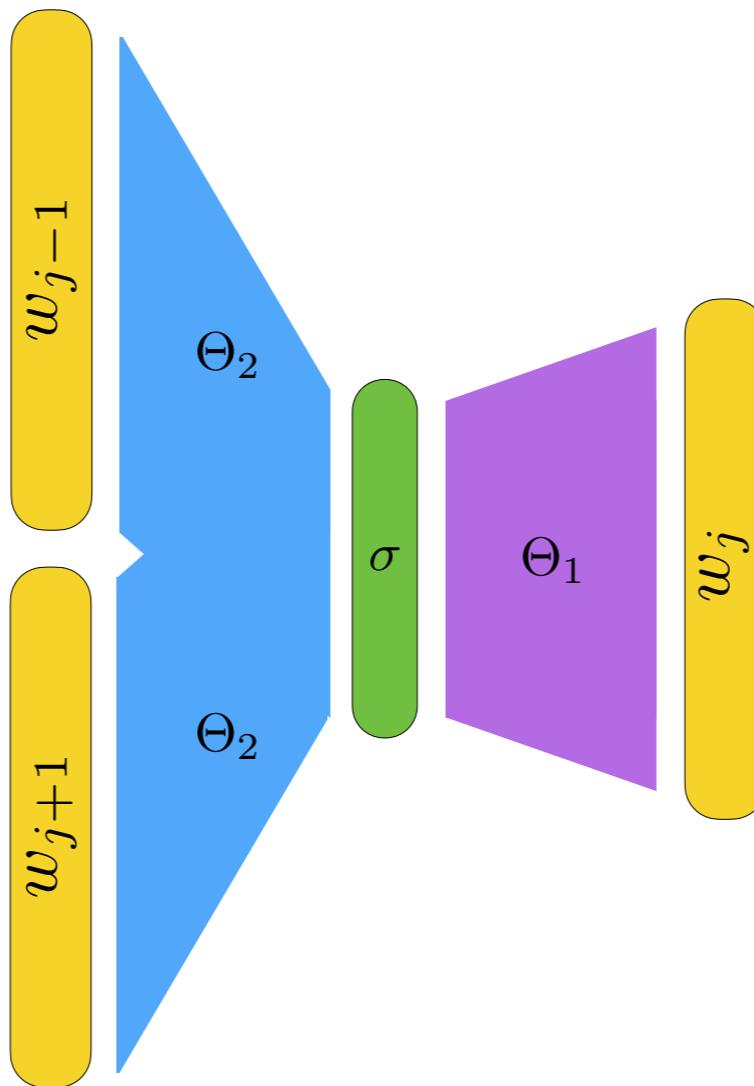
$$H = -\frac{1}{T} \sum_t \log p(w_{j+t}|w_j)$$



- Use the same Θ_2 for all context words.
- Use the average of cross entropy.
- word order is not important (the average does not change).

Continuous Bag of Words

- The process is essentially the same

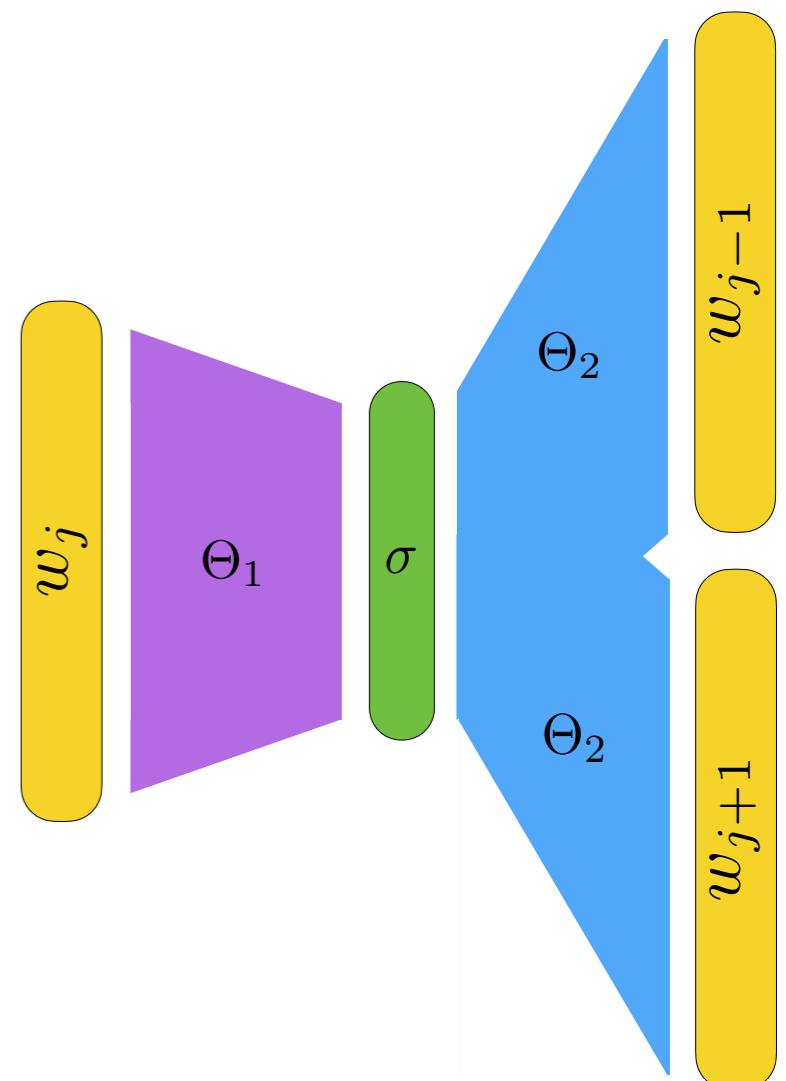


Variations

- Hierarchical Softmax:
 - Approximate the softmax using a binary tree
 - Reduce the number of calculations per training example from V to $\log_2 V$ and increase performance by orders of magnitude.
- Negative Sampling:
 - Under sample the most frequent words by removing them from the text before generating the contexts
 - Similar idea to removing stop-words — very frequent words are less informative.
 - Effectively makes the window larger, increasing the amount of information available for context

Comments

- **word2vec**, even in its original formulation is actually a family of algorithms using various combinations of:
 - Skip-gram, CBOW
 - Hierarchical Softmax, Negative Sampling
- The output of this neural network is deterministic:
 - If two words appear in the same context ("blue" vs "red", for e.g.), they will have similar internal representations in Θ_1 and Θ_2
 - Θ_1 and Θ_2 are vector embeddings of the input words and the context words respectively
- Words that are too rare are also removed.
- The original implementation had a dynamic window size:
 - for each word in the corpus a window size k' is sampled uniformly between 1 and k



Online resources

- C - <https://code.google.com/archive/p/word2vec/> (the original one)
- Python/tensorflow - <https://www.tensorflow.org/tutorials/word2vec>
 - Both a minimalist and an efficient versions are available in the tutorial
- Python/gensim - <https://radimrehurek.com/gensim/models/word2vec.html>
- Pretrained embeddings:
 - **90** languages, trained using wikipedia: <https://github.com/facebookresearch/fastText/blob/master/pretrained-vectors.md>



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Analogies

- The embedding of each word is a function of the context it appears in:

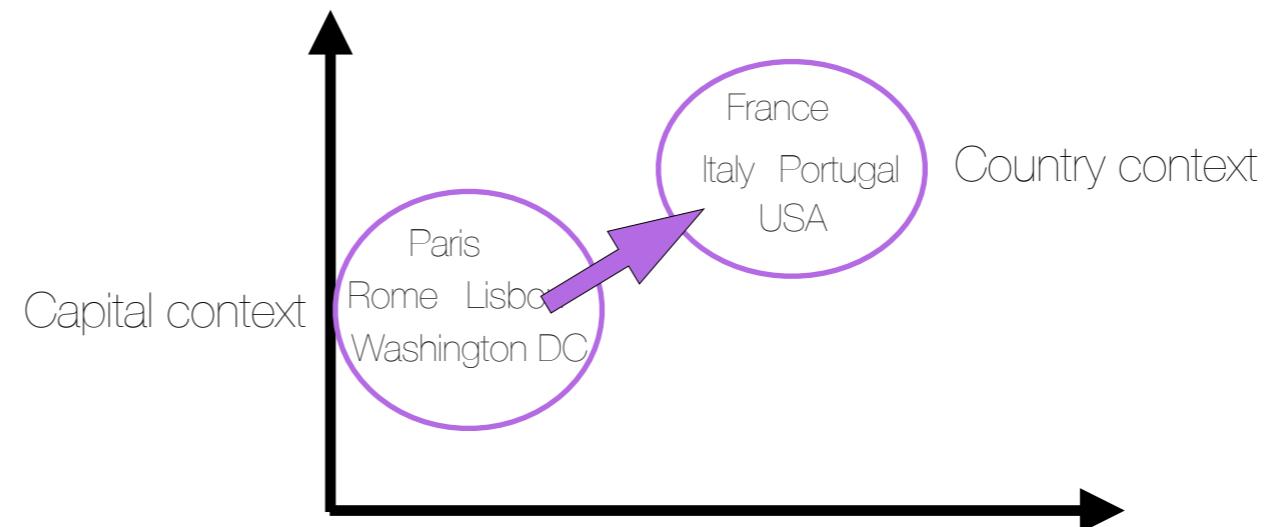
$$\sigma(\text{red}) = f(\text{context}(\text{red}))$$

- words that appear in similar contexts will have similar embeddings:

$$\text{context}(\text{red}) \approx \text{context}(\text{blue}) \implies \sigma(\text{red}) \approx \sigma(\text{blue})$$

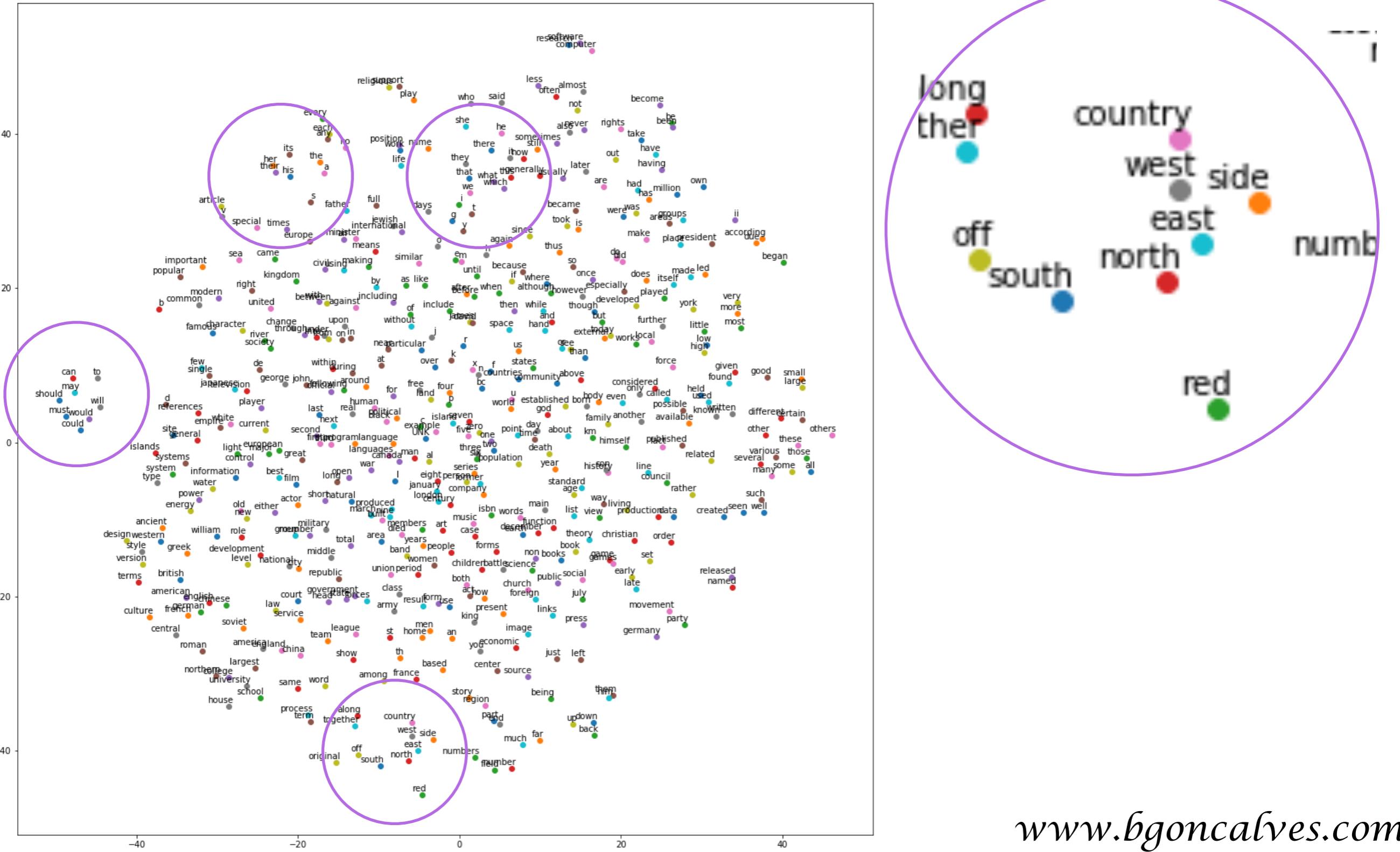
- "Distributional hypothesis" in linguistics

Geometrical relations
between contexts imply
semantic relations
between words!



$$\sigma(\text{France}) - \sigma(\text{Paris}) + \sigma(\text{Rome}) = \sigma(\text{Italy})$$

Visualization



Linguistic Change

WWW'15, 625 (2015)

Statistically Significant Detection of Linguistic Change

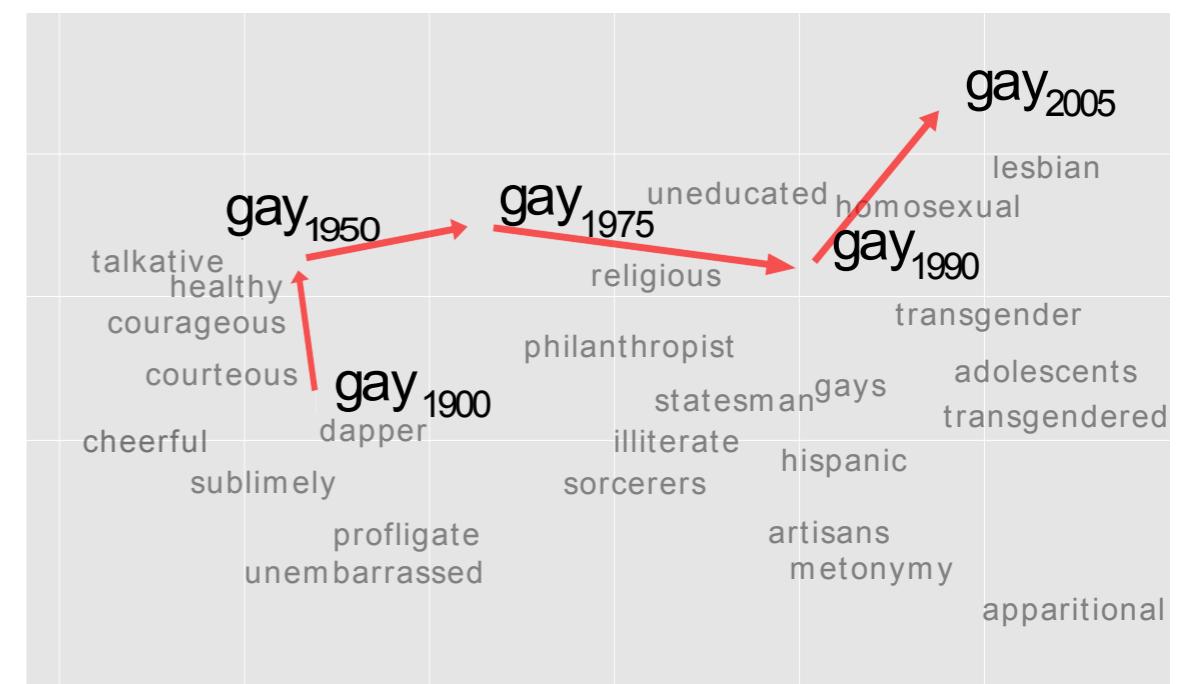
Vivek Kulkarni
Stony Brook University, USA
vvkulkarni@cs.stonybrook.edu

Bryan Perozzi
Stony Brook University, USA
bperozzi@cs.stonybrook.edu

Rami Al-Rfou
Stony Brook University, USA
ralrfou@cs.stonybrook.edu

Steven Skiena
Stony Brook University, USA
skiena@cs.stonybrook.edu

- Train word embeddings for different years using Google Books
- Independently trained embeddings differ by an arbitrary rotation
- Align the different embeddings for different years
- Track the way in which the meaning of words shifted over time!



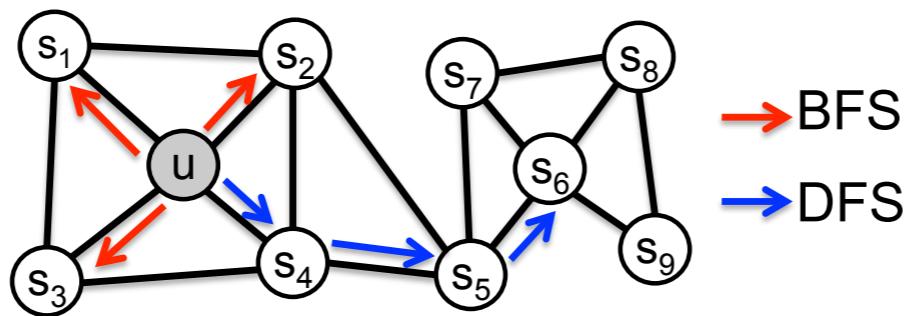
node2vec: Scalable Feature Learning for Networks

Aditya Grover
Stanford University
adityag@cs.stanford.edu

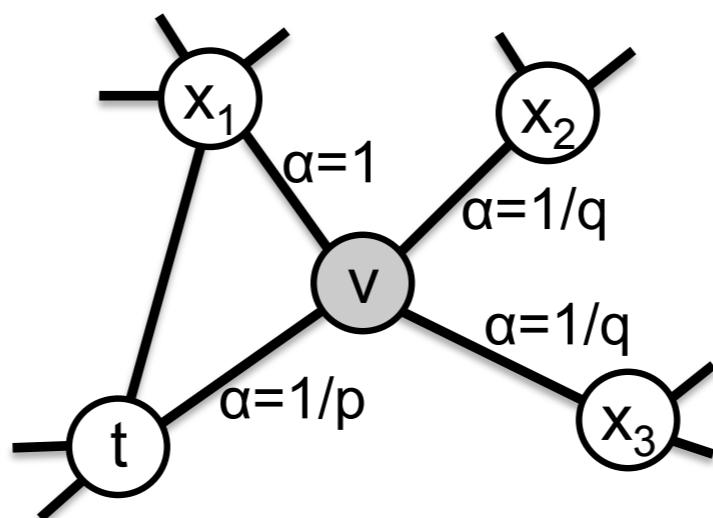
Jure Leskovec
Stanford University
jure@cs.stanford.edu

- You can generate a graph out of a sequence of words by assigning a node to each word and connecting the words within their neighbors through edges.
- With this representation, a piece of text is a walk through the network. Then perhaps we can invert the process? Use walks through a network to generate a sequence of nodes that can be used to train node embeddings?
- node embeddings should capture **features** of the network structure and allow for detection of similarities between nodes.

- The features depends strongly on the way in which the network is traversed
- Generate the contexts for each node using Breath First Search and Depth First Search



- Perform a biased Random Walk



- BFS - Explores only limited neighborhoods. Suitable for structural equivalences
- DFS - Freely explores neighborhoods and covers homophiles communities
- By modifying the parameter of the model it can interpolate between the BFS and DFS extremes

dna2vec: Consistent vector representations of variable-length k-mers

Patrick Ng
ppn3@cs.cornell.edu

- Separate the genome into long non-overlapping DNA fragments.
- Convert long DNA fragments into overlapping **variable** length k-mers
- Train embeddings of each k-mer using **Gensim** implementation of SkipGram.
 - Summing embeddings is related to concatenating **k-mers**
 - Cosine similarity of k-mer embeddings reproduces a biologically motivated similarity score (Needleman-Wunsch) that is used to align nucleotides



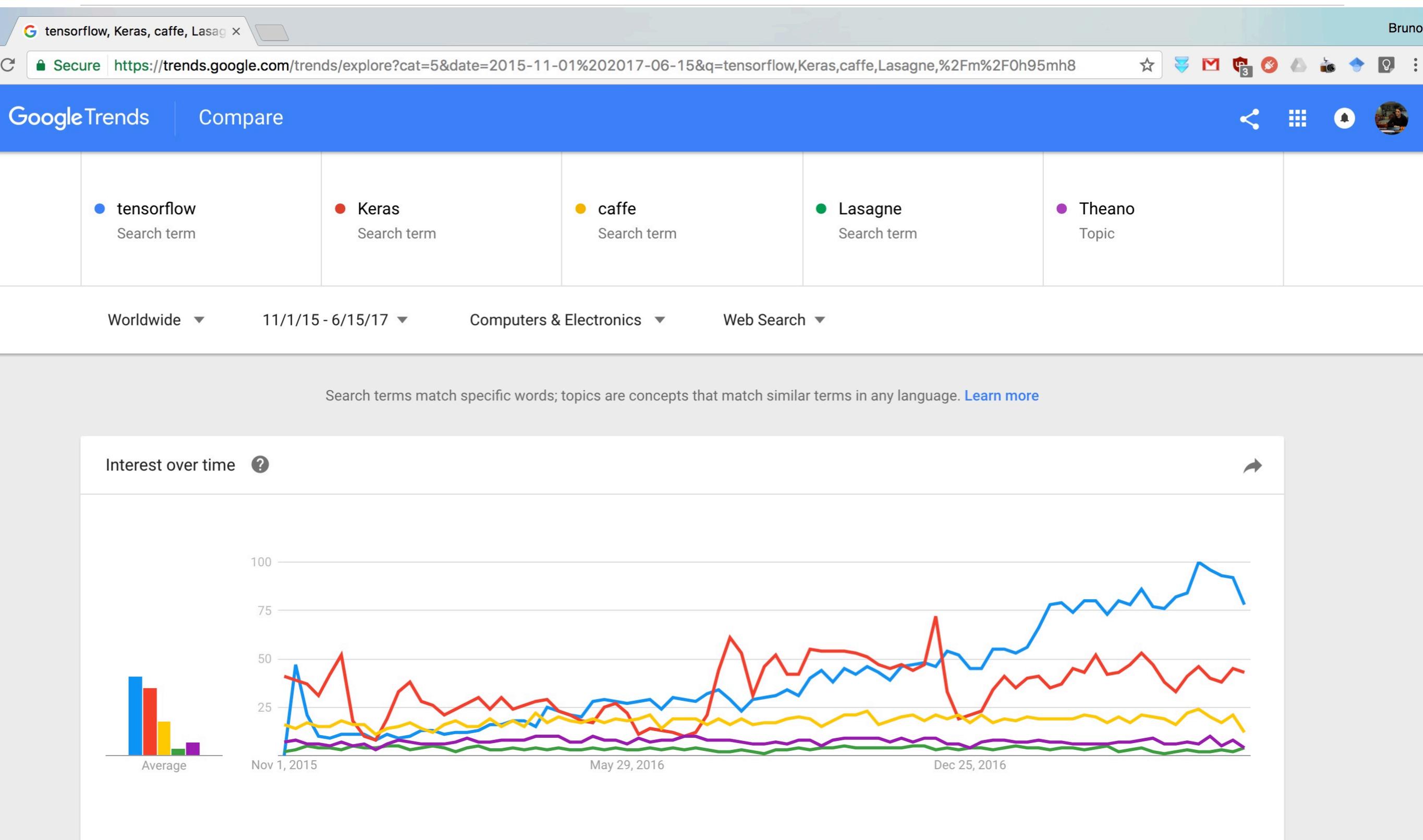
TensorFlow

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TensorFlow

Tensorflow



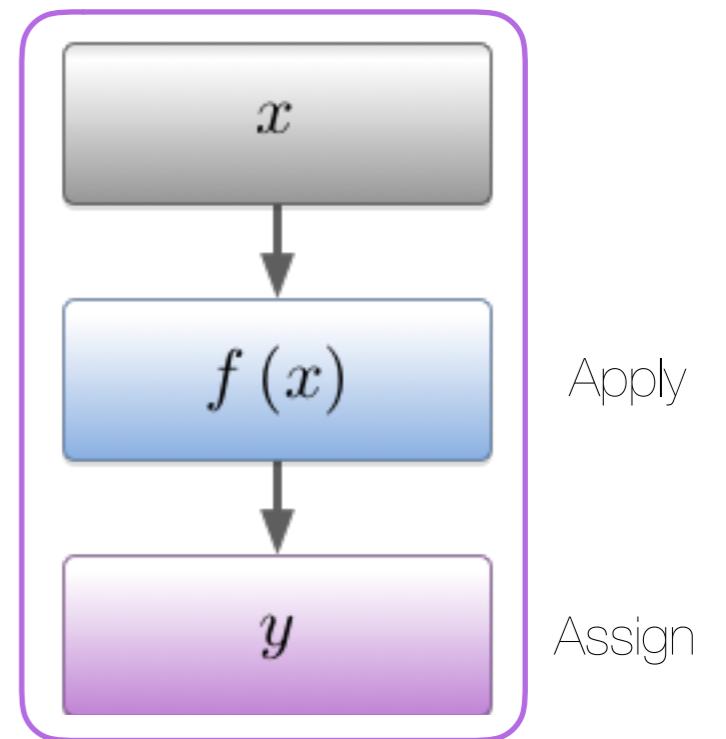
A diversion...

- Let's imagine I want to perform these calculations:

$$y = f(x)$$

$$z = g(y)$$

- for some given x .
- To calculate z we must follow a certain sequence of operations.
- Which can be shortened if we are interested in just the value of y
- In **Tensorflow**, this is called a **Computational Graph** and it's the most fundamental concept to understand
- Data, in the form of **tensors**, **flows** through the graph from inputs to outputs
- Tensorflow**, is, essentially, a way of defining arbitrary computational graphs in a way that can be automatically distributed and optimized.



Computational Graphs

- If we use base functions, tensorflow knows how to automatically calculate the respective gradients

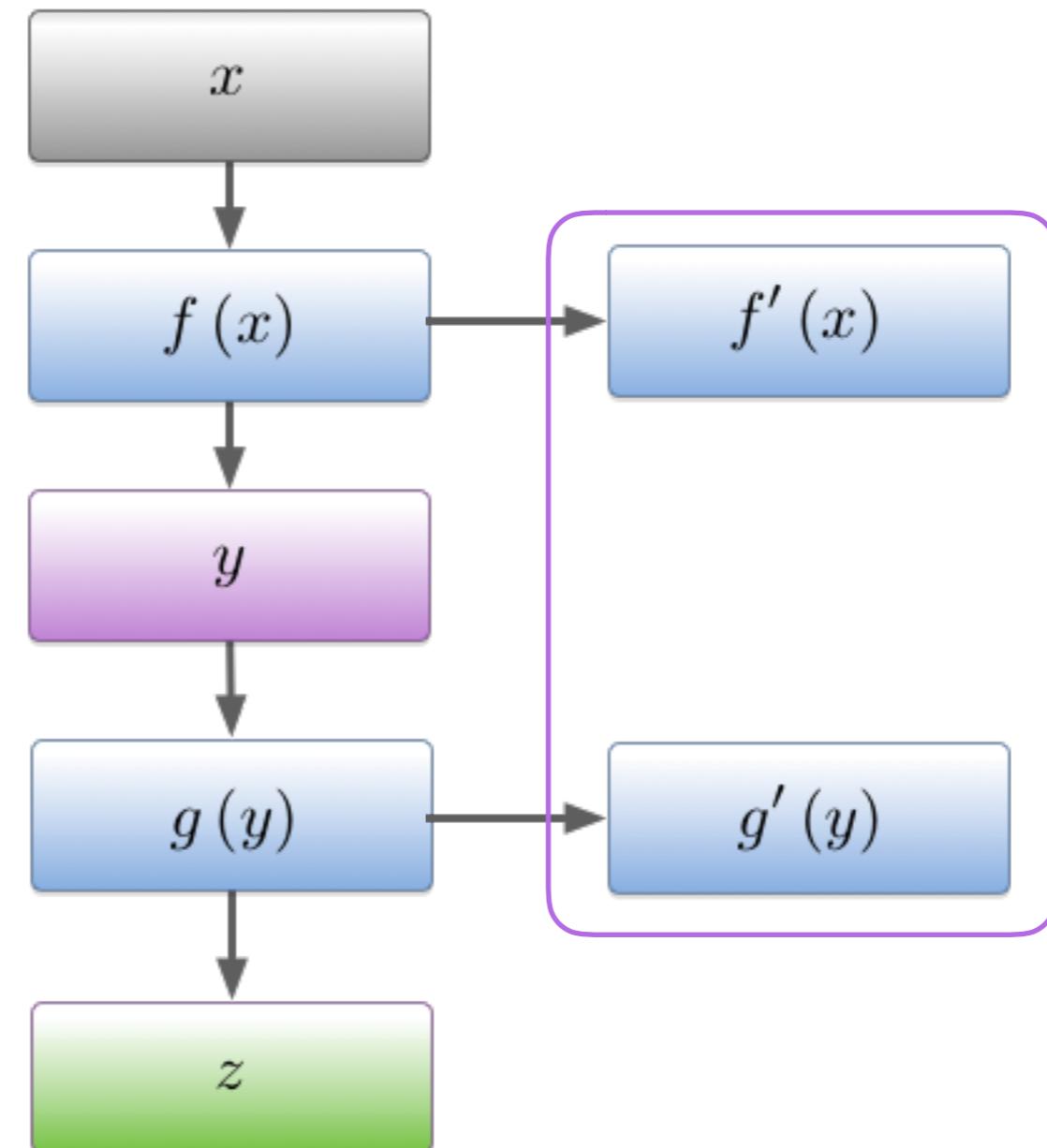
- Automatic BackProp

- Graphs can have multiple outputs

- Predictions

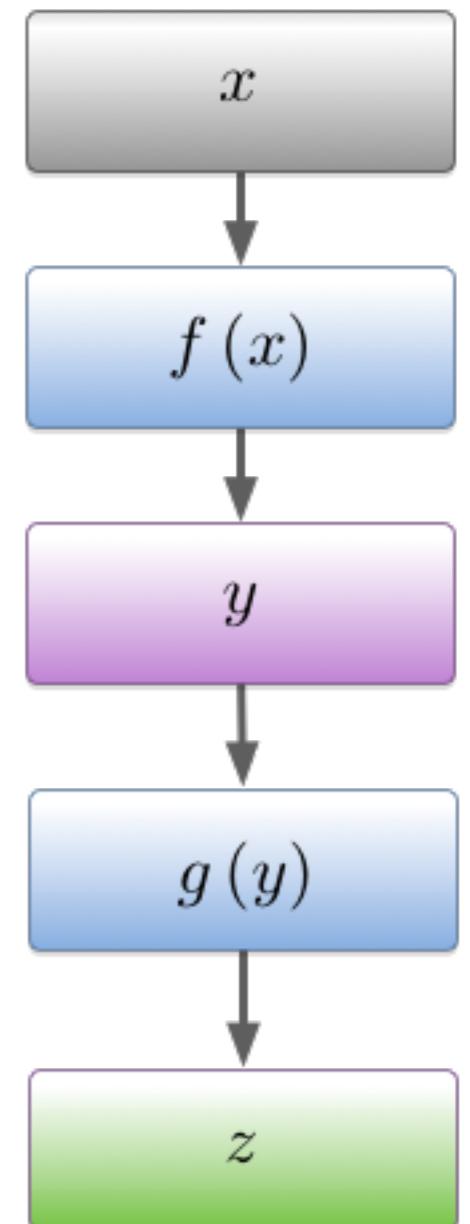
- Cost functions

- etc...



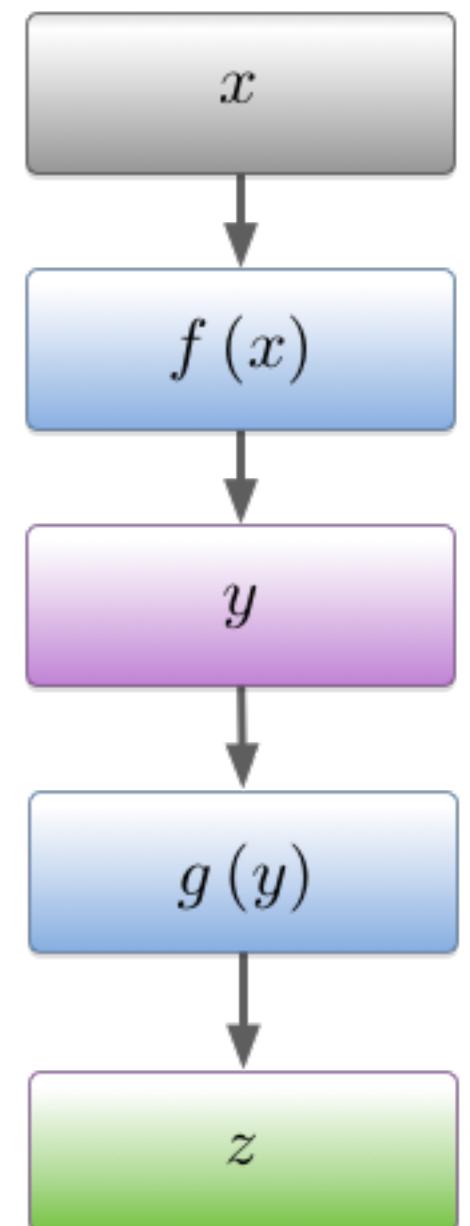
Sessions

- After we have defined the computational graph, we can start using it to make calculations
- All computations must take place within a "session" that defines the values of all required input values



Sessions

- After we have defined the computational graph, we can start using it to make calculations
- All computations must take place within a "session" that defines the values of all **required** input values
- Which values are required for a specific computation depend on what part of the graph is actually being executed.
- When you request the value of a specific output, tensorflow determines what is the specific **subgraph** that must be executed and what are the required input values.
- For optimization purposes, it can also execute independent parts of the graph in different devices (CPUs, GPUs, TPUs, etc) at the same time.



A basic Tensorflow program

$$z = c * (x + y)$$

```

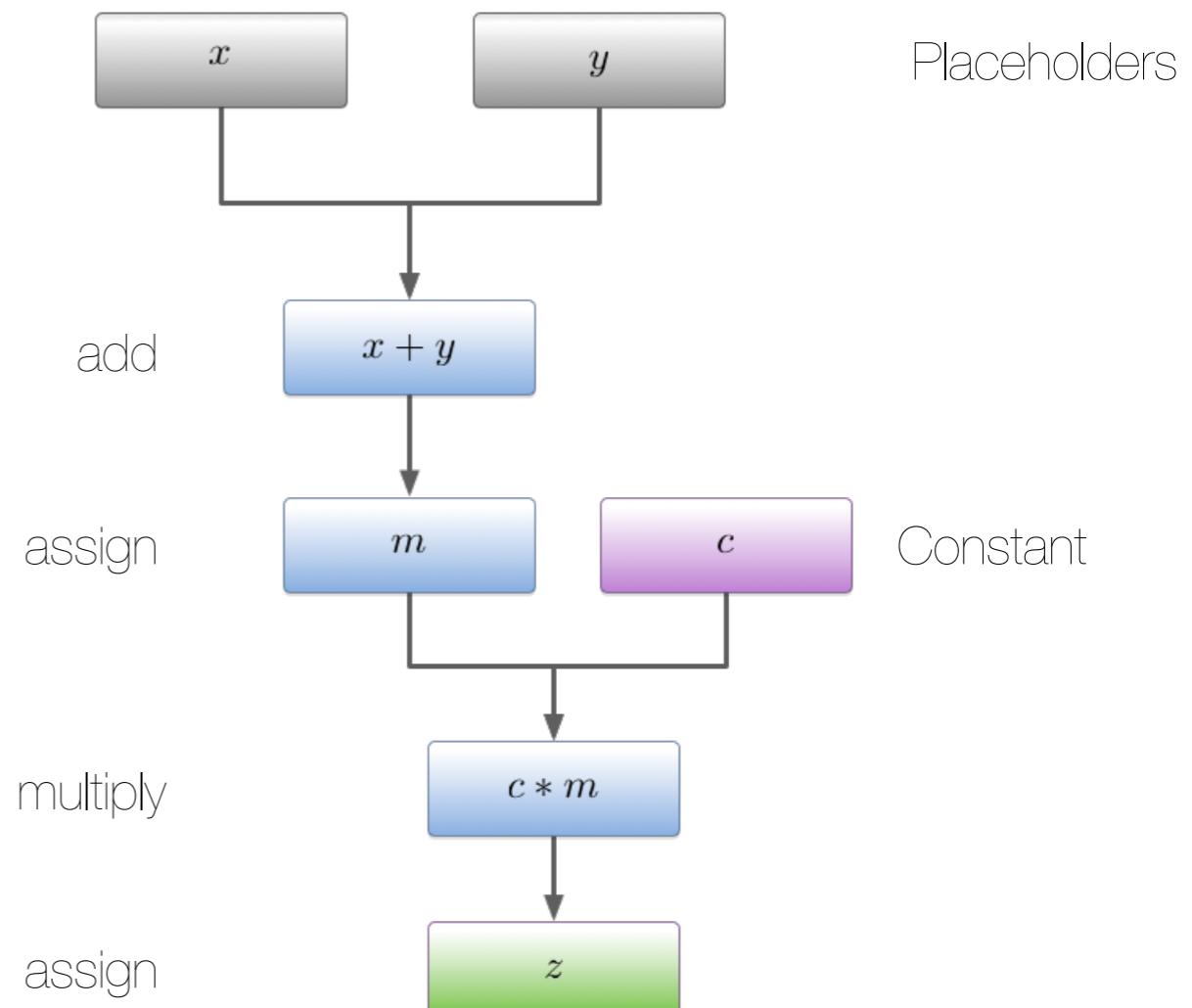
import tensorflow as tf

x = tf.placeholder(tf.float32)
y = tf.placeholder(tf.float32)
c = tf.constant(3.)

m = tf.add(x, y)
z = tf.multiply(m, c)

with tf.Session() as sess:
    output = sess.run(z, feed_dict={x: 1., y: 2.})
    print("Output value is:", output)

```



A basic Tensorflow program

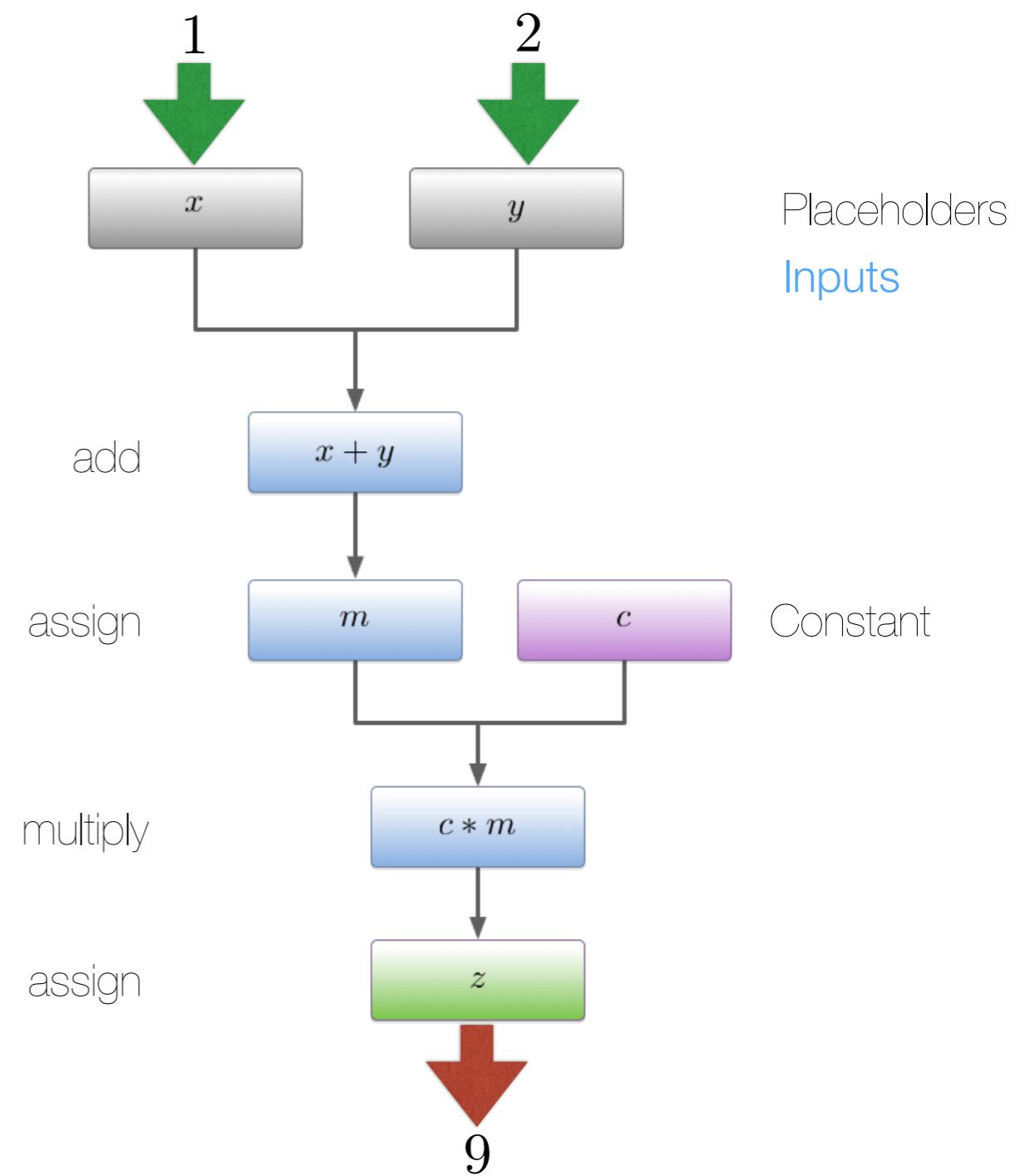
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Linear Regression

```
import numpy as np
import matplotlib.pyplot as plt
import tensorflow as tf

learning_rate = 0.01
N = 100
N_steps = 300

# Training Data
train_X = np.linspace(-10, 10, N)
train_Y = 2*train_X + 3 + 5*np.random.random(N)

# Computational Graph
X = tf.placeholder("float")
Y = tf.placeholder("float")

W = tf.Variable(np.random.randn(), name="weight")
b = tf.Variable(np.random.randn(), name="bias")
y = tf.add(tf.multiply(X, W), b)

cost = tf.reduce_mean(tf.pow(y-Y, 2))
optimizer = tf.train.GradientDescentOptimizer(learning_rate).minimize(cost)
init = tf.global_variables_initializer()

with tf.Session() as sess:
    sess.run(init)

    for step in range(N_steps):
        sess.run(optimizer, feed_dict={X: train_X, Y: train_Y})
        cost_val, W_val, b_val = sess.run([cost, W, b], feed_dict={X: train_X, Y:train_Y})
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$$y = W * x + b$$

$$cost = \frac{1}{N} \sum_i (y_i - Y_i)^2$$

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Jupyter Notebook

Deep Learning...

