

Exam 3 Review - Solutions

1. A block with a mass of 2 kg hangs from a rope that is attached to a pulley of mass 3 kg and radius .5 m. Attached to the other end of the rope is a block resting on a frictionless surface with a mass of 1.5 kg. You pull away from the pulley on the block lying on the surface with a force of 115 N. What is the acceleration of the blocks?

Diagram of the pulley system showing forces on blocks  $m_1$  and  $m_2$ , and the pulley  $m_3$ .

For  $m_1$ :

	x	y
$F_N$	$\emptyset$	$F_N$
$F_g$	$\emptyset$	$-F_g$
$F_{T_1}$	$F_{T_1}$	$\emptyset$
$F_P$	$-115N$	$\emptyset$
$\Sigma F$	$ma$	$\emptyset$

$\Sigma F_x = F_{T_1} - 115N = m_1 a$   
 $F_{T_1} = 115N + m_1 a$

For  $m_2$ :

	x	y
$F_g$	$\emptyset$	$-F_g$
$F_{T_2}$	$\emptyset$	$F_{T_2}$
$\Sigma F$	$\emptyset$	$ma$

$\Sigma F_y = -F_g + F_{T_2} = m_2 a$   
 $F_{T_2} = m_2 a + F_g$

For pulley  $m_3$ :

$\Sigma \tau = I \alpha$   
 $CW (-) \quad CCW (+)$   
 $\tau_1 = F_{T_1} r \sin 90^\circ$   
 $\tau_1 = (115N + m_1 a) r$   
 $\tau_2 = -(m_2 a + F_g) r$   
 $\Sigma \tau = (115N + m_1 a) r - (m_2 a + F_g) r$   
 $I \alpha = (115N + m_1 a) r - (m_2 a + F_g) r$   
 $I \frac{a}{r} = (115N + m_1 a) r - (m_2 a + F_g) r$   
 $I \Rightarrow \text{pulley} = \frac{1}{2} m r^2$   
 $\frac{1}{2} m_3 r^2 \frac{a}{r} = (115N + m_1 a) r - (m_2 a + m_2 g) r$   
 $\frac{1}{2} m_3 a = 115N + m_1 a - m_2 a - m_2 g$   
 $\frac{1}{2} m_3 a - m_1 a + m_2 a = 115N - m_2 g$   
 $a (\frac{1}{2} m_3 - m_1 + m_2) = 115N - m_2 g$   
 $a = \frac{115N - m_2 g}{(\frac{1}{2} m_3 - m_1 + m_2)} = \frac{115N - (2kg \cdot 9.8 \frac{m}{s^2})}{(\frac{1}{2} (3kg) - 1.5kg + 2kg)}$   
 $a = \frac{95.4N}{2} = 47.7 \frac{m}{s^2}$

2. A block with a mass of 2 kg is attached to a spring and stretched 60 cm from equilibrium. The spring has a constant  $k = 200 \text{ N/m}$ . At  $t=0$  s, the block is released from rest.
- What is the max speed?
  - At what time  $t$  does max speed occur? 1st occur
  - If the block is 30 cm from equilibrium, what is its speed?

a)  $\frac{1}{2} k A^2 = \frac{1}{2} m v^2$   
 $\sqrt{\frac{200 \frac{N}{m} (.6m)^2}{2kg}} = v = 6 \frac{m}{s}$

b)  $T = 2\pi \sqrt{\frac{m}{k}} = 2\pi \sqrt{\frac{2kg}{200 \frac{N}{m}}} = .63s$   
Max speed  $\rightarrow \frac{1}{4} T \rightarrow \frac{1}{4} (.63s) = .1575s$

c) before after  
 $\frac{1}{2} k A^2 = \frac{1}{2} k x^2 + \frac{1}{2} m v^2$   
 $\sqrt{\frac{k A^2 - k x^2}{m}} = v = 5.2 \frac{m}{s}$

3. In a thermally insulated container, .5 kg of ice at  $-20^\circ C$  is combined with .8 kg of water at an unknown temperature.
- If all of the ice melts, leaving the container to be filled only with water at  $10^\circ C$ , then what is the initial temperature of the .8 kg of water?
  - What is the entropy change of the ice-water system?

Diagram showing the process of ice melting and mixing with water.

	ice as water	ice as water	water	water
Q	$Q_1$	$Q_2$	$Q_3$	$Q_4$
state	ice	ice as water	water	water
temp	$-20^\circ C$	$0^\circ C$	$10^\circ C$	$?^\circ C < 72.4^\circ C$
m	$m_i$	$m_i$	$m_w$	
type	SH	LH	SH	
#	$C_i$	$L_f$	$C_w$	
+/-	+	+	-	

a)  $\Delta Q = 0 = Q_1 + Q_2 + Q_3$   
 $m_i C_i \Delta t + L_f m_i - m_w C_w \Delta t = 0$   
 $(.5kg)(2.10)(20) + (334)(.5kg) - .8kg(4.186)(\Delta t) = 0$   
 $|\Delta t| = 62.4^\circ C$   
So initial temp water is  
 $\Delta t + 10^\circ C = 72.4^\circ C$

b)  $\Delta S_{LH} = \frac{mL}{T}$   $\Delta S_{SH} = mc \ln\left(\frac{T_{Hot}}{T_{Cold}}\right)$   
 $\Delta S_{system} = m_{ice} (C_{ice}) \ln\left(\frac{273K}{253K}\right) + \frac{L_f m_{ice}}{273K} + m_{ice} C_w \ln\left(\frac{283K}{273K}\right) - m_w C_w \ln\left(\frac{345.4K}{283K}\right)$   
 $= .0799 + .612 + .075 - .667$   
 $\Delta S_{system} \sim .1 \frac{KJ}{K}$