

Fig. S8. Model simulation of disorientation. In the simulation, birds could transition between an undisturbed migratory state and a disoriented state. (a) Parameterizations of the distance-dependent disorientation probability f (Equation 1). a is the probability of disorientation. (b) Parameterizations of the angular Von Mises distribution g (Equation 2) for the case of uniform ( $\kappa = 0$ ), moderate ( $\kappa = 0.2$ ) and weak ( $\kappa = 0.1$ ) directed flight towards ALAN for birds in the disoriented state.  $\kappa$  is the concentration parameter for disoriented flight, determining the extent to which birds fly towards ALAN when disoriented. When  $\kappa = 0$ , birds' flight paths follow a random walk; when  $\kappa > 0$ , birds fly toward the lights, with larger  $\kappa$  implying a more directed flight towards the light source.