Homework 3 extra credit

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We only have it in matlab. The data is collected with the arduino kit. It was collected when we walked in a straight hall way back and forth. The data collection is as fast as possible (approx 50 Hz). The time step is not exactly a constant. The state model does not handle angle wrapping, which caused some weird arifacts in the output.

To generate C code for arduino, we can use ccode function. But to prepare for the matrices in C is too tedious.

The EKF algorithm is stolen from Wikipedia.

```
function [ x_estimate, P_estimate ] = kalman_sensor_fusion(x_prev,
 u_prev, P_prev, f, F, h, H, z, Q, R)
x_predict = f(x_prev, u_prev);
P_predict = F(x_prev, u_prev) * P_prev * F(x_prev, u_prev)' + Q;
y = z - h(x predict);
S = H(x_predict) * P_predict * H(x_predict)' + R;
K = P_predict * H(x_predict)' / S;
x_estimate = x_predict + K * y;
P_estimate = (eye(size(x_prev,1)) - K * H(x_predict)) * P_predict;
end
clear variables
syms gyro_x gyro_y gyro_z psi theta phi psid thetad phid dt real
H_321 = @(theta, phi) [-sin(theta) 0 1;
    sin(phi)*cos(theta) cos(phi) 0;
    cos(phi)*cos(theta) -sin(phi) 0];
x = [psi theta phi]'; % state
u = [gyro_x gyro_y gyro_z dt]';
f_{expr} = x + (H_321(theta, phi) \setminus u(1:3, :)) * u(4, :); % state model
h_expr = eye(3) * x; % observation model
F_expr = jacobian(f_expr, x); % linearized state model
H_{expr} = jacobian(h_{expr}, x); % linearized observation model
close all
n \text{ states} = 3;
n_measurements = 3;
x_prev = [0 0 pi]';
u prev = [0 0 0 0.02]';
P_prev = eye(n_states);
```

```
Q = eye(n_states) * 1e-2;
R = eye(n measurements) * 1e-0;
data = csvread('hw3q7 2.csv',1,0);
time_stamp = data(:, 1)';
gyro_readings = data(:, 5:7)';
heading = deg2rad(data(:, 13:-1:11)');
dt = [0.02, diff(time stamp)];
z_traj = heading;
u_traj = [gyro_readings; dt];
f_fun = matlabFunction(f_expr, 'Vars', {x,u});
F_fun = matlabFunction(F_expr, 'Vars', {x,u});
h_fun = matlabFunction(h_expr, 'Vars', {x});
H_fun = matlabFunction(H_expr, 'Vars', {x});
x_traj = zeros(n_states, size(z_traj,2));
for t = 2:size(z_traj,2)
    [ x_estimate, P_estimate ] = kalman_sensor_fusion(x_prev,
 u_traj(:, t-1), P_prev, f_fun, F_fun, h_fun, H_fun, z_traj(:, t), Q,
 R);
    x traj(:, t) = x estimate;
    x_prev = x_estimate;
    P_prev = P_estimate;
end
figure()
plot(time stamp, rad2deg(x traj(1:3,:)))
xlabel('time (sec)');
ylabel ('euler angles (deg)');
title('EKF filtered headings');
legend ('yaw(psi)','pitch(theta)','roll(phi)')
figure()
plot(time stamp, rad2deg(heading))
xlabel('time (sec)');
ylabel ('euler angles (deg)');
title('raw headings from magnetometer');
legend ('yaw(psi)','pitch(theta)','roll(phi)')
```





