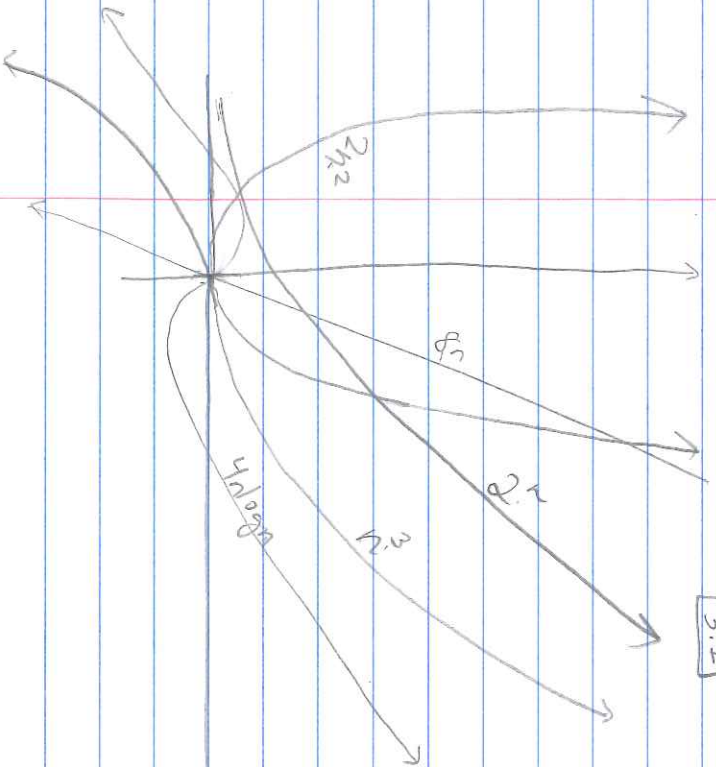


C341

Angely + Brandon

3.1



3.2

#ops A and B

 $8n \log n$  $2n^2$  $n_0$  A is better than B

lower degree

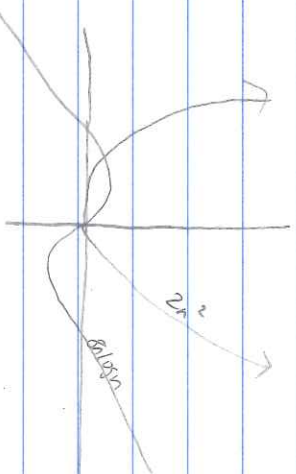
 $8n \log n = 2n^2$  $4n \log n = n^2$  $4 \log n \approx n$  $4 = n$  $\log n$ at  $n=16$ ,  $4 = \frac{16}{\log 16}$ ;  $n_0=17$  is when A

is faster in

terms of run time,

true making it

better.



3.8  $2^{10}, 2^{109n}, 3n + 100 \log n, 4n, n \log n,$   
 $4n \log n + 2n, n^2 + 10n, n^3, 2^n$   
 increase left to right

3.10

$d(n)$  is  $O(f(n))$ ,  $d(n) \leq c_1 f(n)$  for  $n \geq n_0$   
 $e(n)$  is  $O(g(n))$ ,  $e(n) \leq c_2 g(n)$

$d(n)e(n)$  is  $O(f(n)g(n))$

$d(n)e(n) \leq c_1 f(n)e(n)$

$c_1 f(n)e(n) \leq c_1 c_2 f(n)g(n)$

$d(n)e(n)$  is  $O(f(n)g(n))$  for  $n \geq \max\{n_0, n_2\}$

3.14

$O(\max\{f(n), g(n)\}) = O(f(n) + g(n))$

\* max of a set of 2 functions

should result in one function.

$f(n) + g(n) \leq 2 \max\{f(n), g(n)\}$   $n_0 > n$

if  $c=2$   $n_0=1$

by definition of big-Oh,  $f(n) + g(n)$

is in  $O(\max\{f(n), g(n)\})$

[3.17]

Angely + Brandon

$$(n+5)^5 \text{ is } O(n^5)$$

$$n^5 + 25n^4 + 250n^3 + 1250n^2 + 3125n + 3125$$

≤

$$(1 + 25 + 250 + 1250 + 3125 + 3125)n^5$$

by definition of big O

$$(n+5)^5 = O(n^5)$$

[3.18]

$$2^{n+1} \text{ is } O(2^n)$$

$$2^n \cdot 2^1 \leq c \cdot 2^n$$

$$c \geq 2 \quad n_0 = 0$$

[3.20]

$$n^2 \text{ is } \Omega(n \log n)$$

$$n^2 \geq n \log n$$

$$n \geq \log n$$

$$c \geq 0 \quad n_0 = 1$$

by definition of big Omega

[3.27]

$$O(n^3)$$

because there are 3 for loops are in

this code, you are going through  $n$  3 times.



C. 335

Since elements are disjoint, as they are unique sets, mix the 3 sets and then sort the sets. Then you can sequentially move through the structure, as it will be linear, since the majority of the time will be spent on sorting ( $O(n \log n)$ )

$$T(n) = O(n \log n)$$

$$P = O(n)$$

$$Q = O(n)$$

$$R = O(n)$$

$$S = O(n)$$

$$T = O(n)$$

$$U = O(n)$$

$$V = O(n)$$

$$W = O(n)$$

$$X = O(n)$$

$$Y = O(n)$$

$$Z = O(n)$$

Angelus + Brendon.

$$F(n) \text{ is } \boxed{\sqrt{3,49}} \left( \left( \frac{3}{2} \right)^n \right)$$

$$F(n) > c \left( \frac{3}{2} \right)^n$$

$$c = \left( \frac{2}{3} \right)^2 = \frac{4}{9}$$

$$F(n) > c \left( \frac{3}{2} \right)^n$$

$$n = 1, 2, 3.$$

$$n_0 = 2$$

n	F(n)	$\left( \frac{3}{2} \right)^n$	$c \cdot \left( \frac{3}{2} \right)^n$
0	0	1	$\frac{4}{9}$
1	1	$\frac{3}{2}$	$\frac{2}{3}$
2	1	$\frac{9}{4}$	1
3	2	$\frac{27}{8}$	$\frac{3}{2}$

Induction:  $F(k) > c \left( \frac{3}{2} \right)^k \quad k \geq n_0$

$$F(k+1) = F(k) + F(k-1)$$

$$\begin{aligned}
 & \geq c \left( \frac{3}{2} \right)^k + c \left( \frac{3}{2} \right)^{k-1} \\
 & = c \left( \frac{3}{2} + 1 \right) \left( \frac{3}{2} \right)^{k-1} \\
 & > c \left( \frac{3}{2} \right)^2 \left( \frac{3}{2} \right)^{k-1} \\
 & = c \left( \frac{3}{2} \right)^{k+1}
 \end{aligned}$$



• 4.7.2 def convert\_string(s, acc):

if (s == 1)

return acc

return convert\_string(s[1:], 10<sup>4</sup>acc + ord(s[0]) - 48)

• 4.11.1 def unique(s):

if len(s) == 1:

return True

else:

index = s[0]

rest = s[1:]

isUnique = index not in rest

storage = unique(rest)

return isUnique and storage