



# **EARTH 114: GLOBAL WARMING**

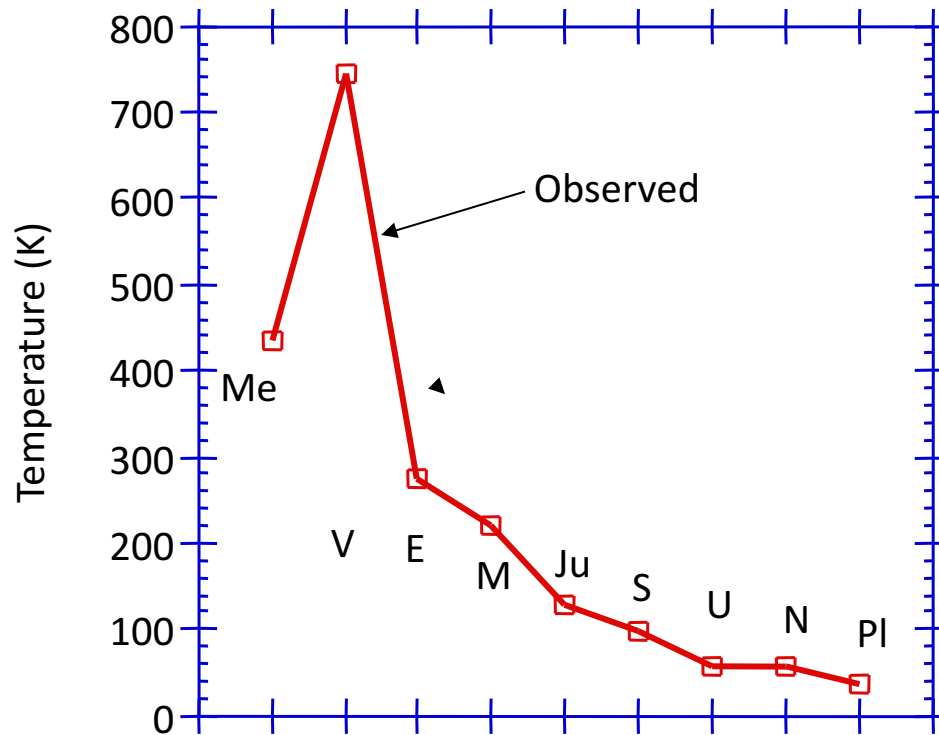
## **Lecture 2: Radiation and planetary temperature**

# *Overview*

- i. Solar energy and electromagnetic radiation– a little about light
- ii. Radiation laws– relationship between electromagnetic radiation and temperature
- iii. Planetary energy balance & the greenhouse effect– modeling planetary temperature

# *Planetary temperature*

What determines Earth's mean temperature?

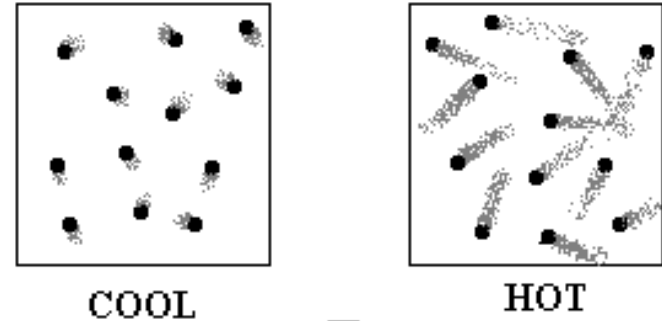


# Energy and Heat

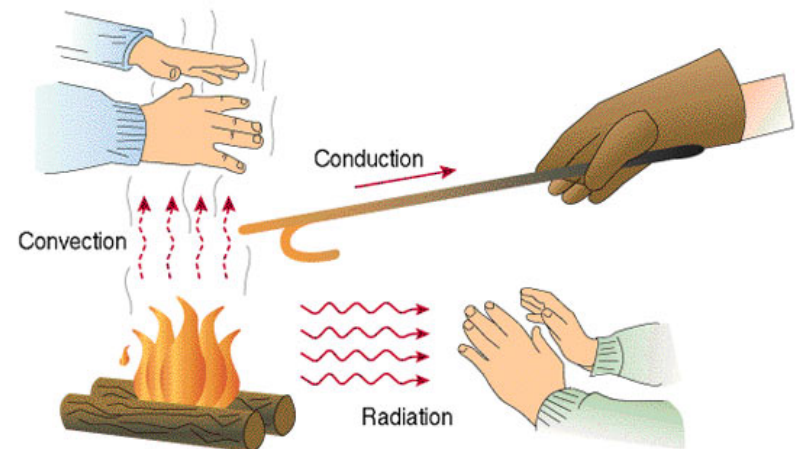
**Energy:** property responsible for work on or heating of an object.

**Heat:** Is a measure of the kinetic energy (bouncing-around energy) of atoms.

- Temperature (K, C, F) is a measure of the heat in an object.



- Heat (J) is transferred through convection, conduction, and radiation.



# *Solar energy*

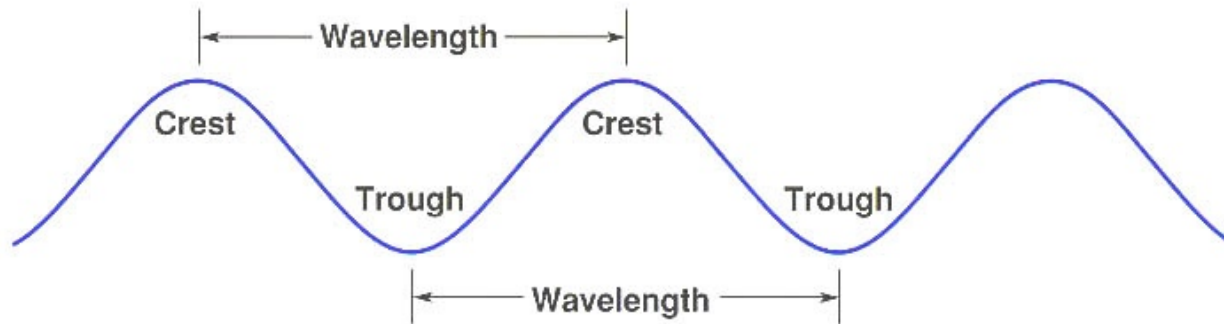
## **Solar heating:** Earth's surface is heated by the Sun

- Earth receives 99.98% of its surface energy from the Sun.
- Solar energy is created in the core of the Sun through nuclear fusion, the welding of H atoms into He atoms.
- Every second our Sun fuses ~600 million tons of H to He, converting >4 million tons of matter into energy.
- And radiates  $3.828 \times 10^{26}$  J/s to space (the Sun's luminosity).
- Some of this energy reaches Earth's surface.

# *Electromagnetic radiation*

**Electromagnetic radiation:** self-propagating waves that have electric and magnetic fields

- Induced by acceleration of electrons within atoms
- Moves through vacuum or matter at speed of light ( $c = 3 \times 10^8$  m/s)
- Characterized by wavelength ( $\lambda$ ) or frequency ( $\nu$ )

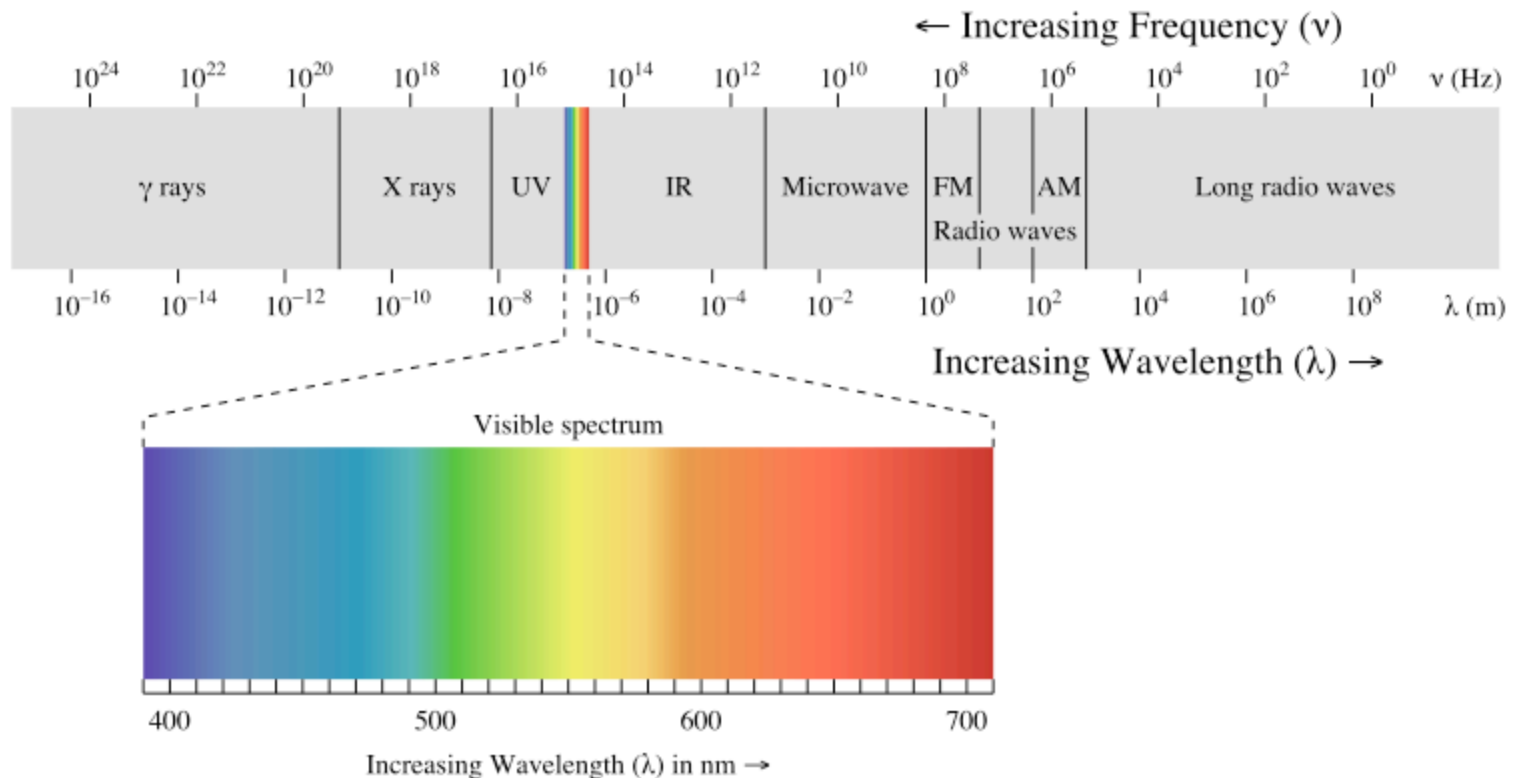


- Frequency is inversely proportional to wavelength:

$$\nu = \frac{c}{\lambda}$$

# *Electromagnetic spectrum*

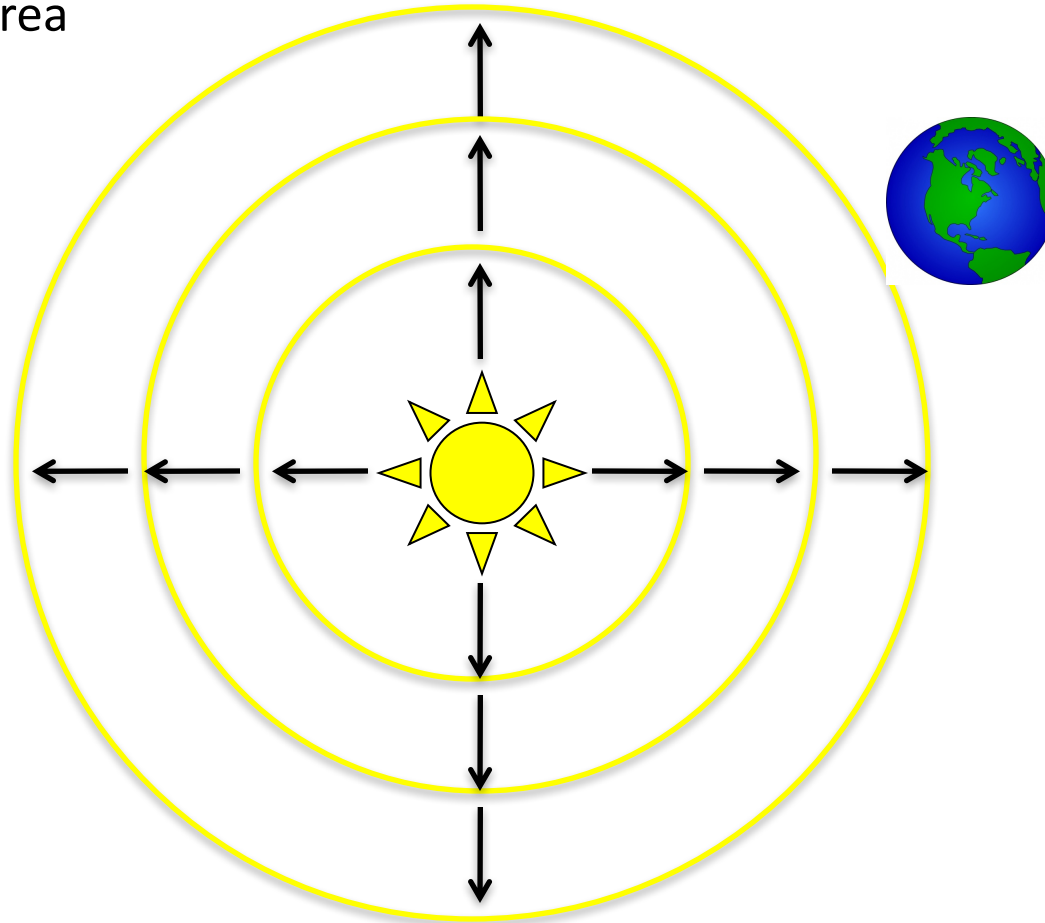
**Electromagnetic spectrum:** full range of electromagnetic radiation



# *Inverse square law*

**Newton's inverse square law:** solar flux is inversely proportional to the square of the distance from Sun

- As energy moves away from Sun, it is spread over a greater and greater area





# *Inverse square law*

**Newton's inverse square law:** solar flux is inversely proportional to the square of the distance from Sun

- As energy moves away from Sun, it is spread over a greater and greater area
- Spread over the area of a sphere,  $4\pi r^2$ , where r is distance from the Sun
- Solar flux is the luminosity divided by the sphere of incidence:

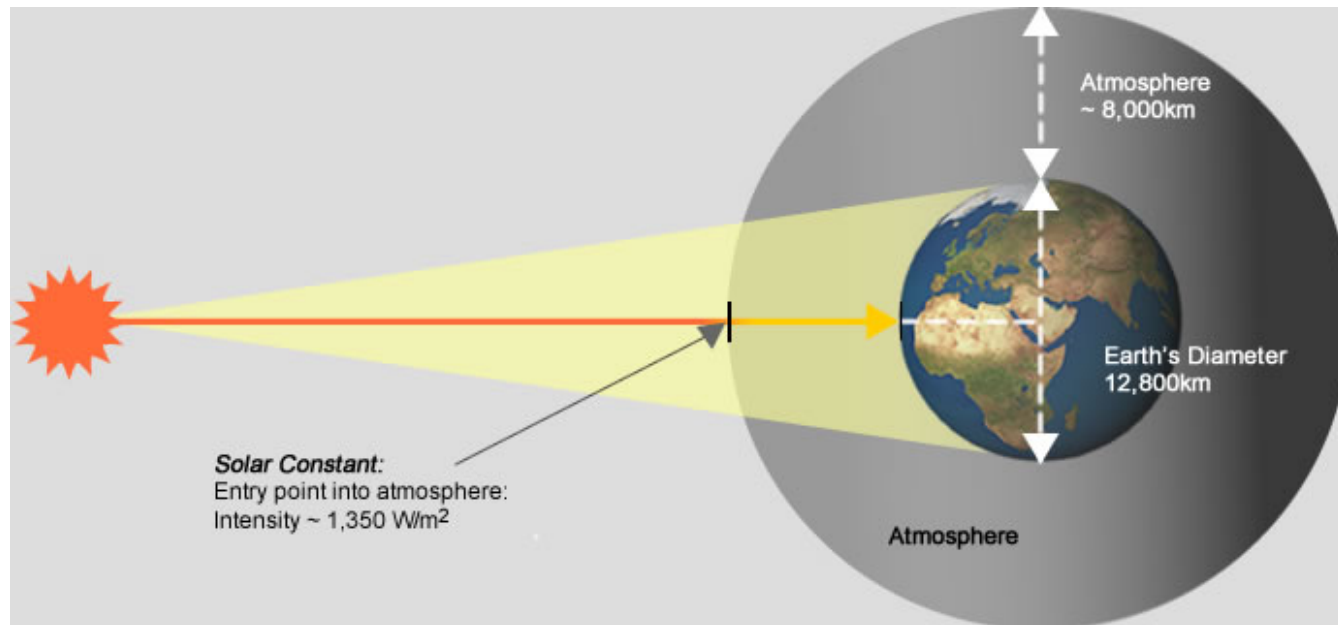
$$S = \frac{L}{4\pi r^2}$$

- What is Earth's solar flux ( $S_0$ )?
  - $L = 3.839 \times 10^{26} \text{ W}$
  - $r_0 = 1.496 \times 10^{11} \text{ m}$

# Solar flux

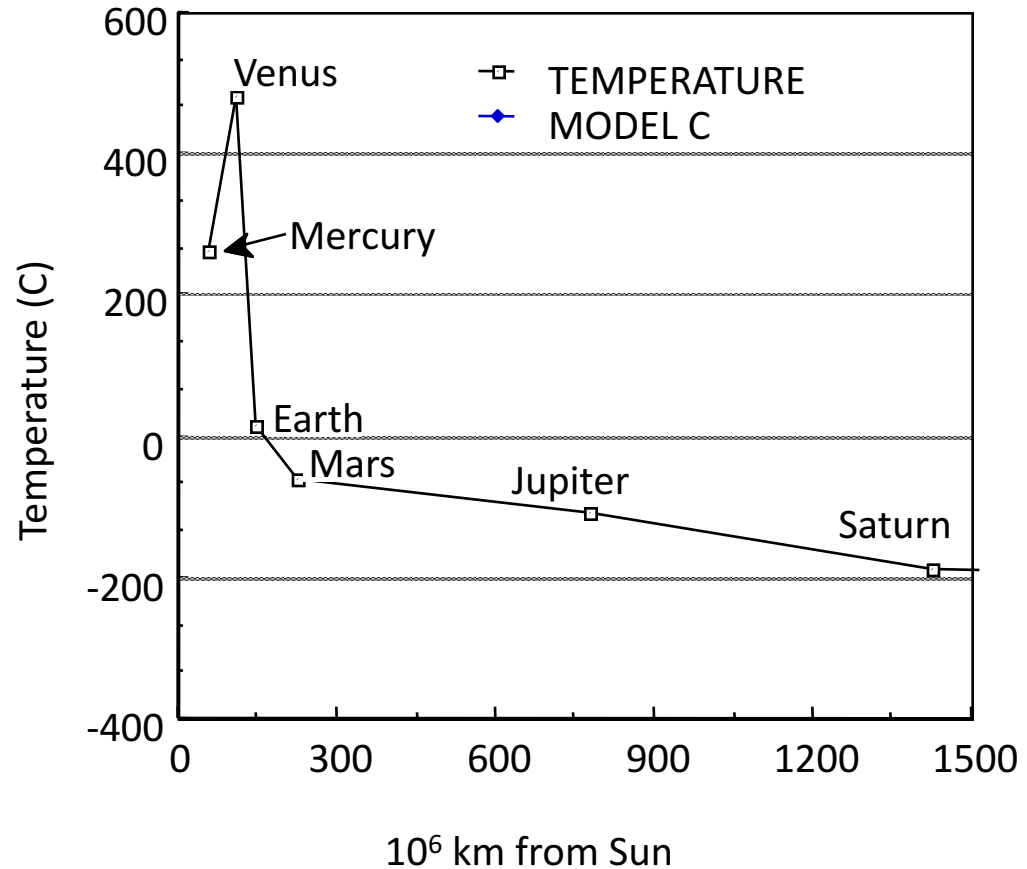
**Solar flux:** amount of solar energy that reaches a unit area of surface per unit time

- Solar flux is measured in units of  $\text{Js}^{-1}\text{m}^{-2}$  or  $\text{Wm}^{-2}$
- $S_0 = 1367 \text{ Wm}^{-2}$  – equivalent to  $\sim 13\ 100 \text{ W}$  light bulbs illuminating a square meter



# *Inverse square law model*

Is planetary temperature explained by distance from the Sun?



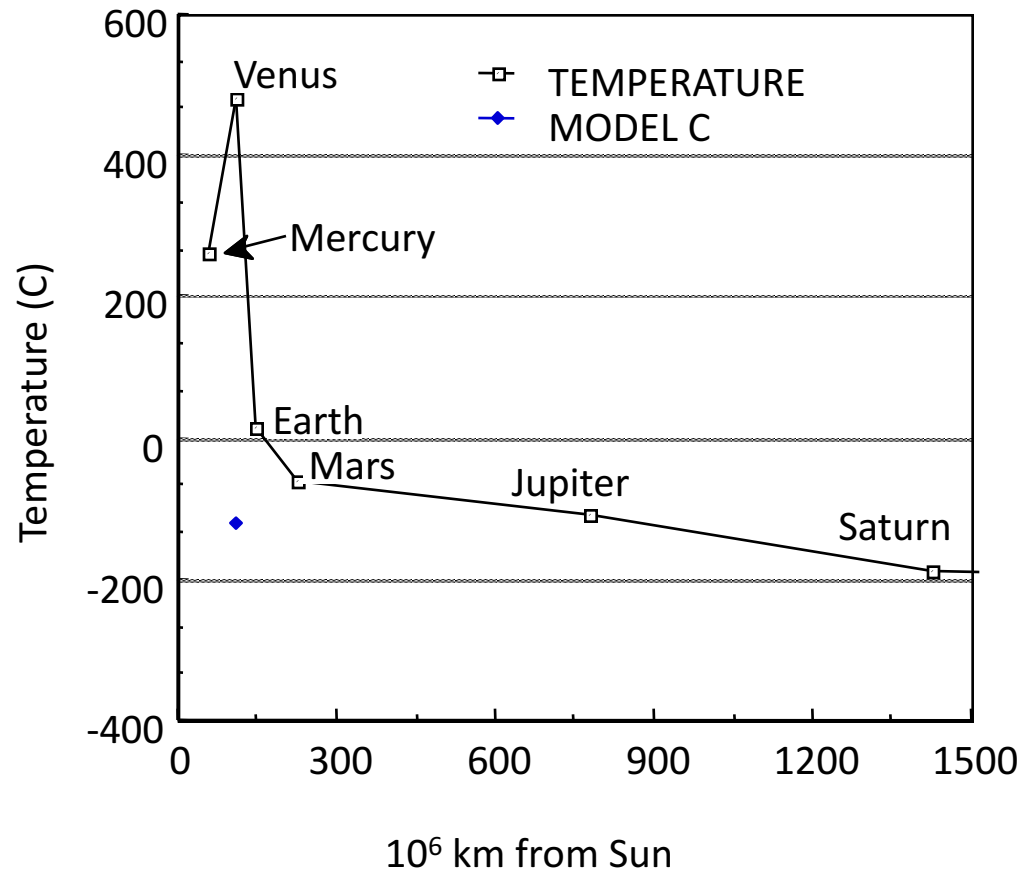
# *Inverse square law model*

Is planetary temperature explained by distance from the Sun?

Mercury's temperature = 539 K, Venus is about 2x as far away from the Sun.

Using the inverse square law, we estimate that Venus should receive  $\frac{1}{4}$  as much solar radiation.

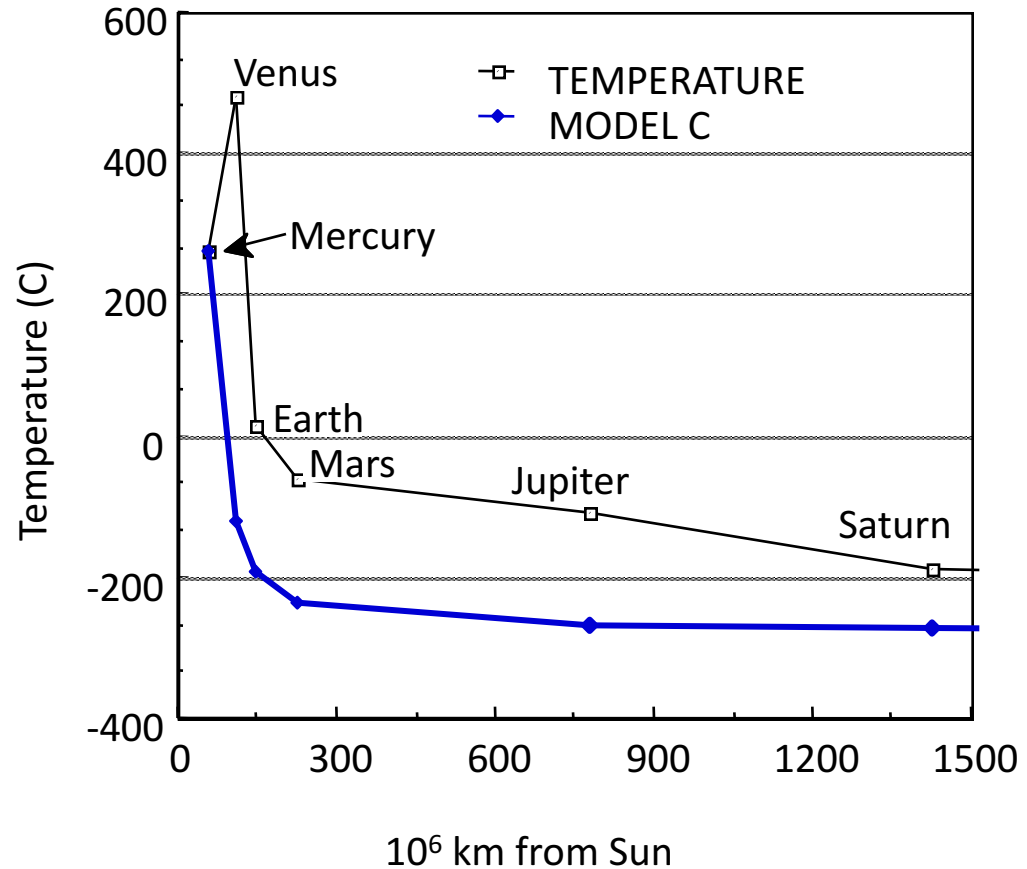
Venus' temperatures would be 539 K ( $\frac{1}{4}$ ) = 135 K or -138 C.



# *Inverse square law model*

Is planetary temperature explained by distance from the Sun?

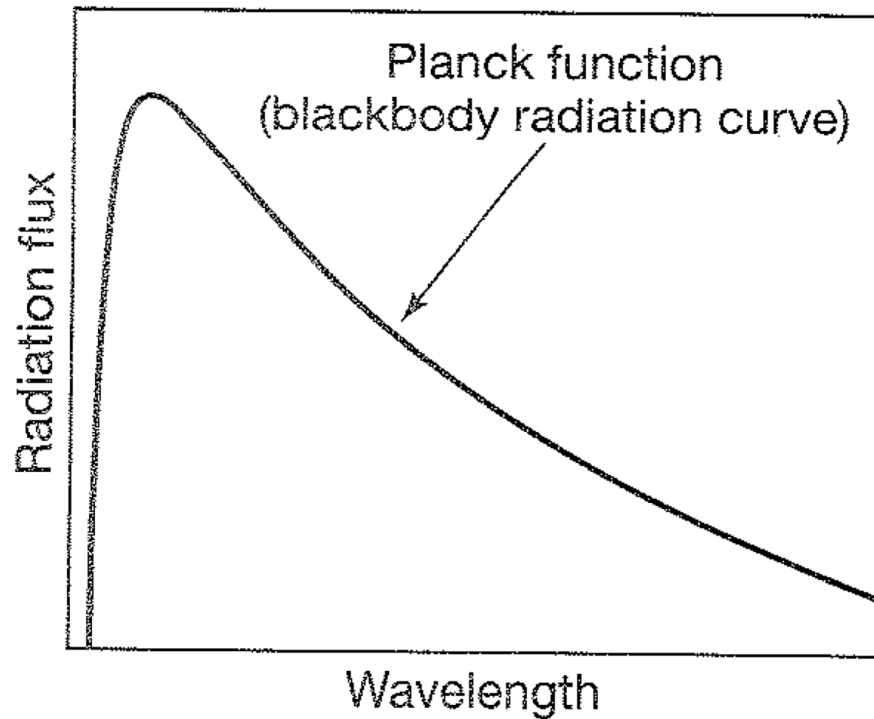
Distance from the Sun does a poor job of estimating planetary temperatures.



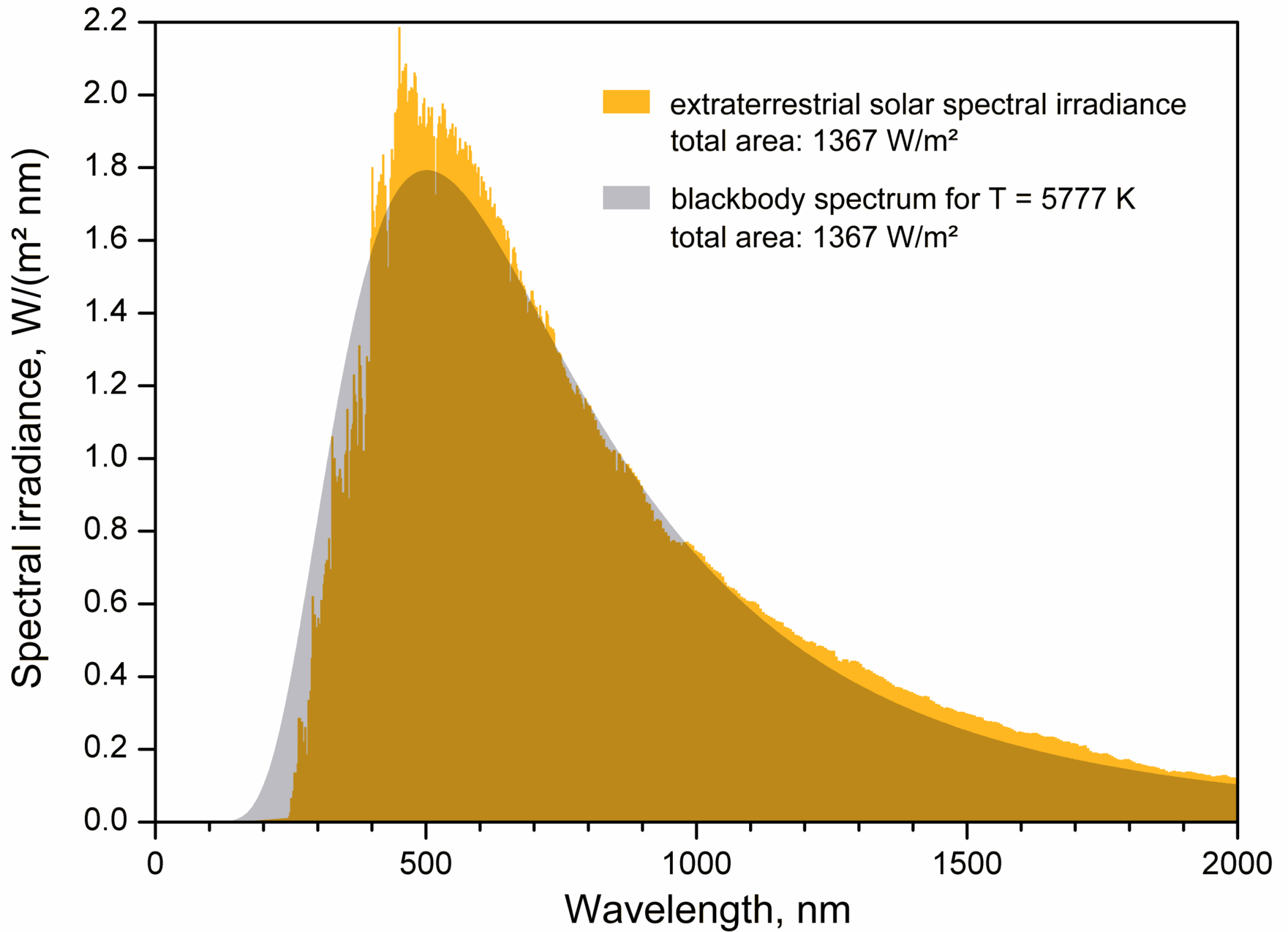
# *Planck's function*

**Planck's law of black body radiation:** describes the electromagnetic radiation of a black body in thermal equilibrium.

Relates radiation flux to wavelength at equilibrium T



(a)



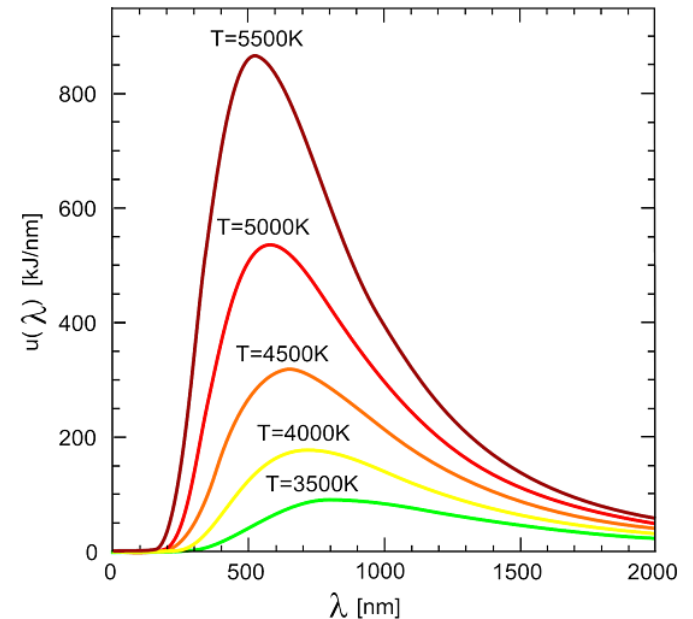
# Wien's law

**Wien Law:** the peak electromagnetic radiation is inversely related to the temperature of a black body

A hot body will radiate at shorter peak wavelengths than a cold one:

$$\lambda_{\max} = B/T$$

where  $B=0.0029$  K m is Wien's constant

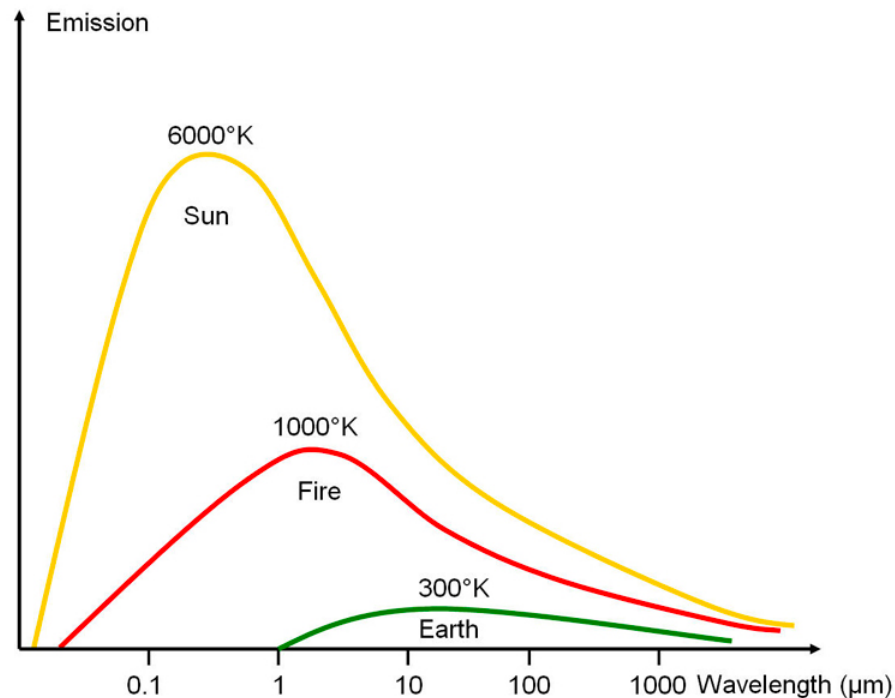




# Wien's law

**Wien Law:** the peak electromagnetic radiation is inversely related to the temperature of a black body

- Sun – radiates in the shortwave (visible) spectra
- Earth – radiates in the longwave (ir) spectra



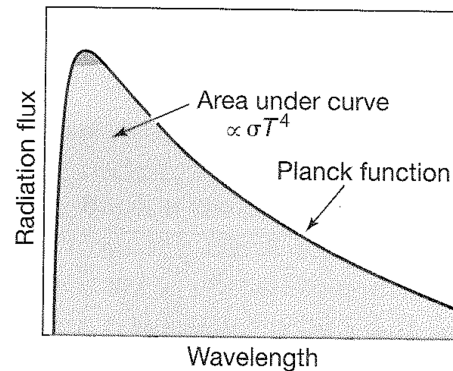
# Stefan-Boltzmann law

**Stefan-Boltzmann law:** the total energy emitted by an object is proportional to its temperature:

$$I = \sigma T^4$$

where  $\sigma = 5.67e-8 \text{ Wm}^{-2}\text{K}^{-4}$ . Note that  $I$  is an energy flux (energy per time per area)! Units =  $\text{Wm}^{-2} = \text{Jm}^{-2}\text{s}^{-1}$ .

Stefan-Boltzmann Law is derived by integrating Planck's Function.



(c)



# *Radiation characteristics*

	<b>T</b> <b>(K)</b>	$\lambda_{\max}$ <b>(<math>\mu\text{m}</math>)</b>	<b>region in</b> <b>spectrum</b>	<b>F</b> <b>(W/m<sup>2</sup>)</b>
<b>Sun</b>	6000			
<b>Earth</b>	300			

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# *Radiation characteristics*

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<b>Sun</b>	6000	0.5	visible	
<b>Earth</b>	300	10	infrared	

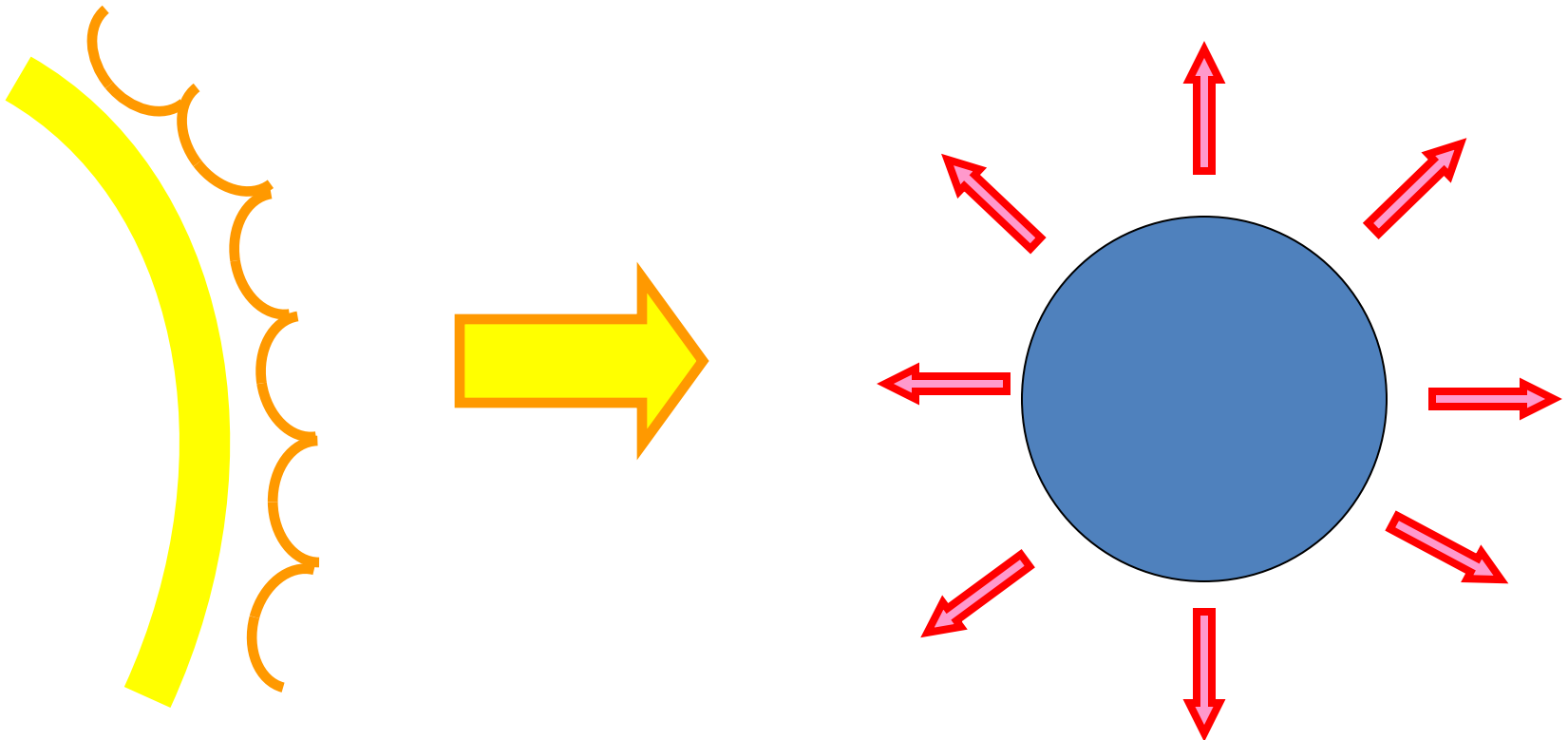
# *Radiation characteristics*

	<b>T</b> <b>(K)</b>	$\lambda_{\max}$ <b>(<math>\mu\text{m}</math>)</b>	<b>region in</b> <b>spectrum</b>	<b>F</b> <b>(W/m<sup>2</sup>)</b>
<b>Sun</b>	6000	0.5	visible	$7 \times 10^7$
<b>Earth</b>	300	10	infrared	460

# *Planetary energy balance*

**Radiative equilibrium:** assumes energy balance, incoming radiation equals outgoing radiation

- If incoming and outgoing radiation are not in balance, Earth's temperature will rise or fall.



# *Earth's radiative temperature*

Let's calculate the radiative equilibrium temperature for Earth!

- Start from our equation for radiative equilibrium:

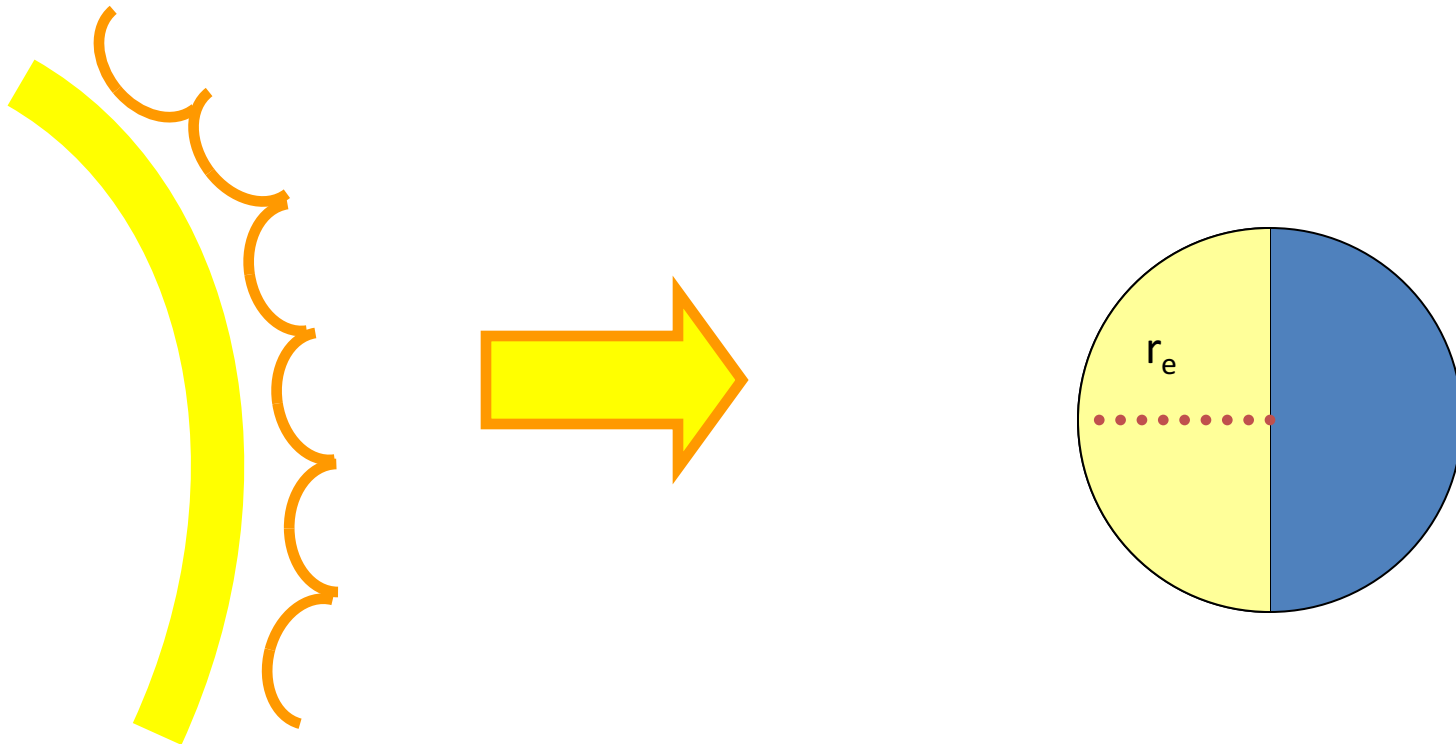
$$\text{Incoming Radiation} = \text{Outgoing Radiation}$$

- Write equation for Incoming Radiation
- Write equation for Outgoing Radiation
- Solve



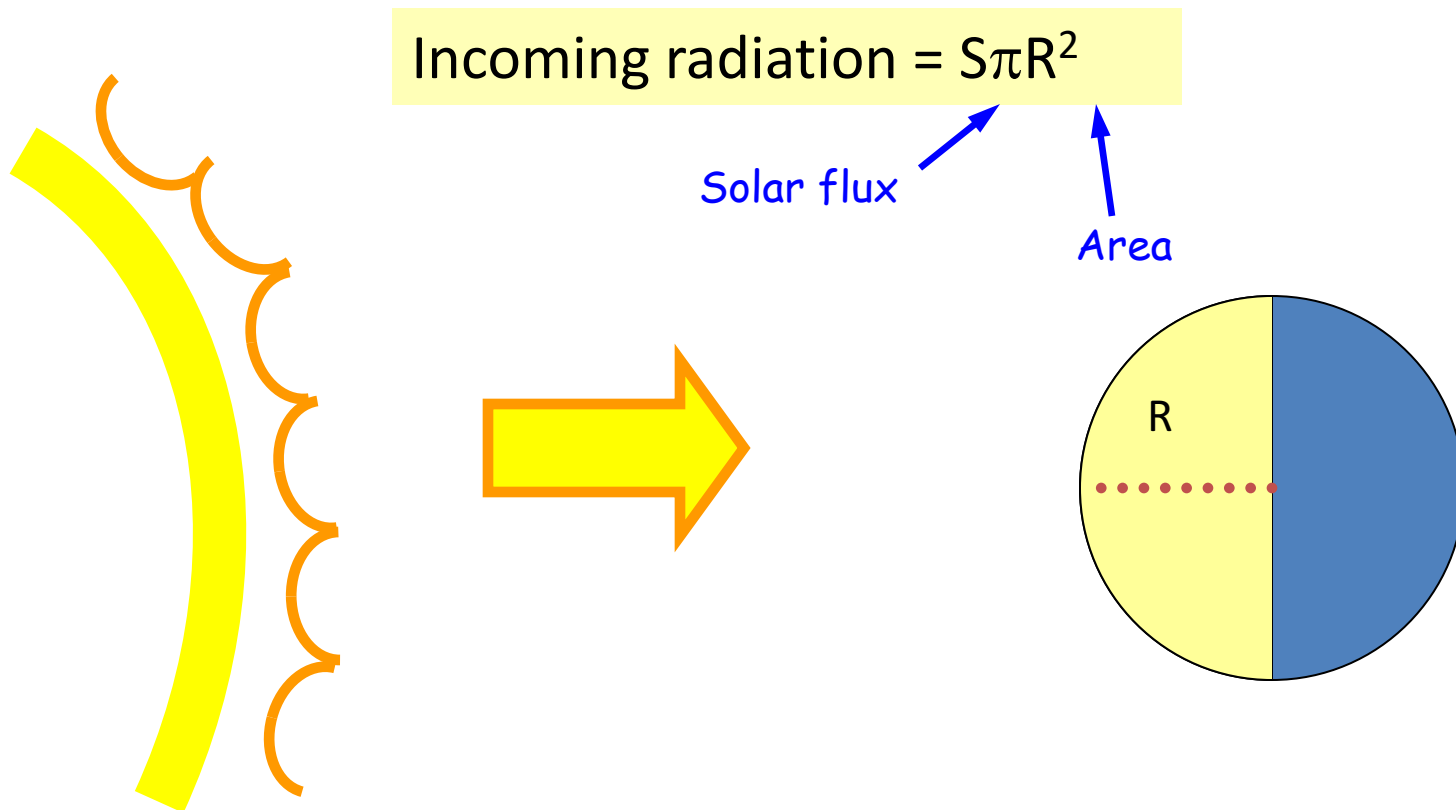
# *Earth's radiative temperature*

**Incoming radiation:** energy received from the Sun



# *Earth's radiative temperature*

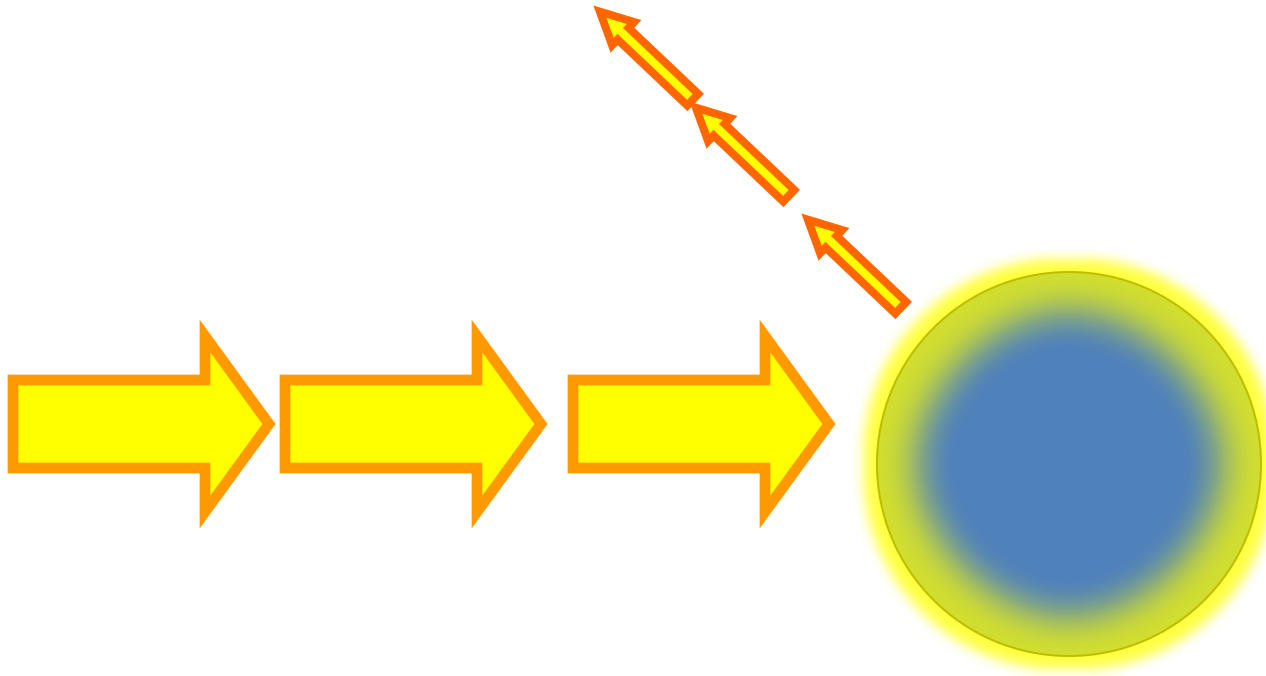
**Incoming radiation:** energy received from the Sun (S) covers the area of a circle defined by the radius of the Earth (R)



# *Albedo*

**Albedo:** measure of visible light reflection

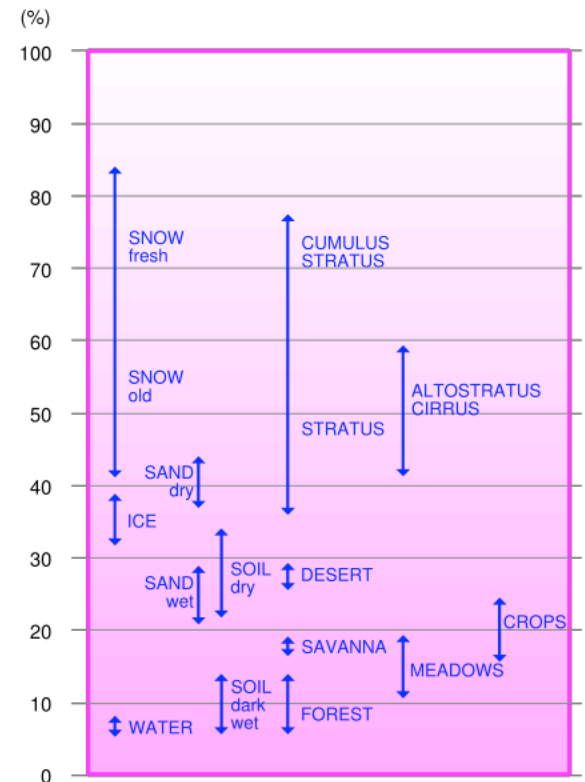
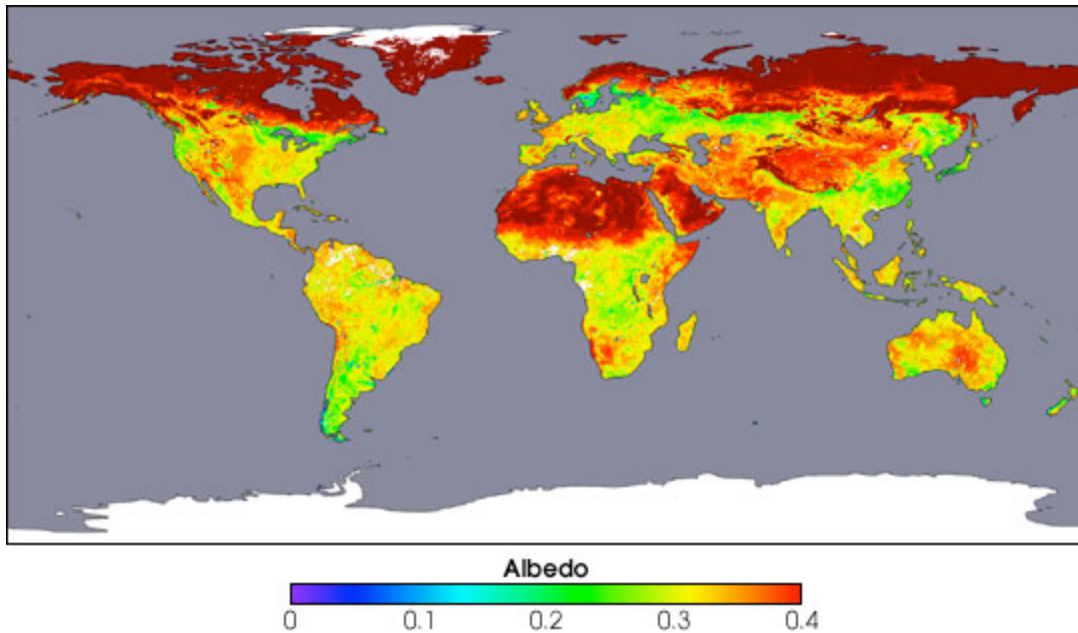
- Some of the incoming visible radiation is not absorbed, it is reflected



# Albedo

**Albedo:** measure of visible light reflection

- Some of the incoming radiation is not absorbed, it is reflected
- Expressed as a fraction of the total incident radiation
- Varies from 0 (no reflection) to 1 (complete reflection)

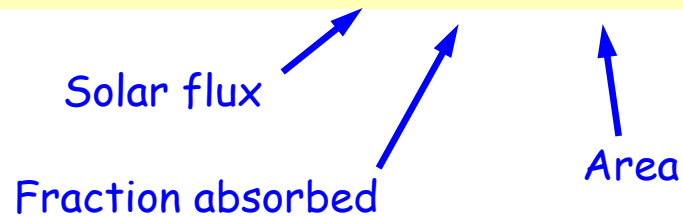


# *Earth's radiative temperature*

**Incoming radiation:** energy received from the Sun

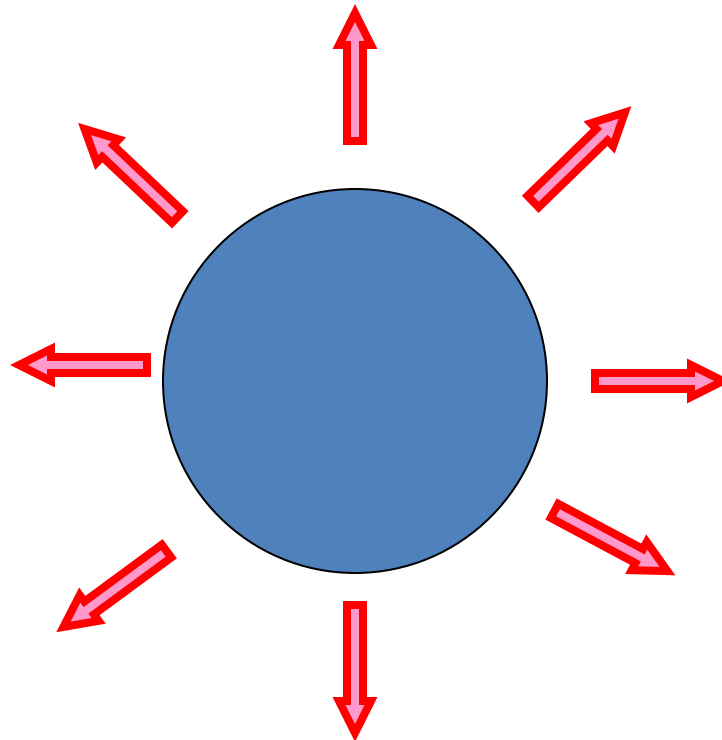
- Fraction of incoming radiation that is absorbed is  $(1 - \alpha)$

$$\text{Incoming radiation} = S(1-\alpha)\pi R^2$$



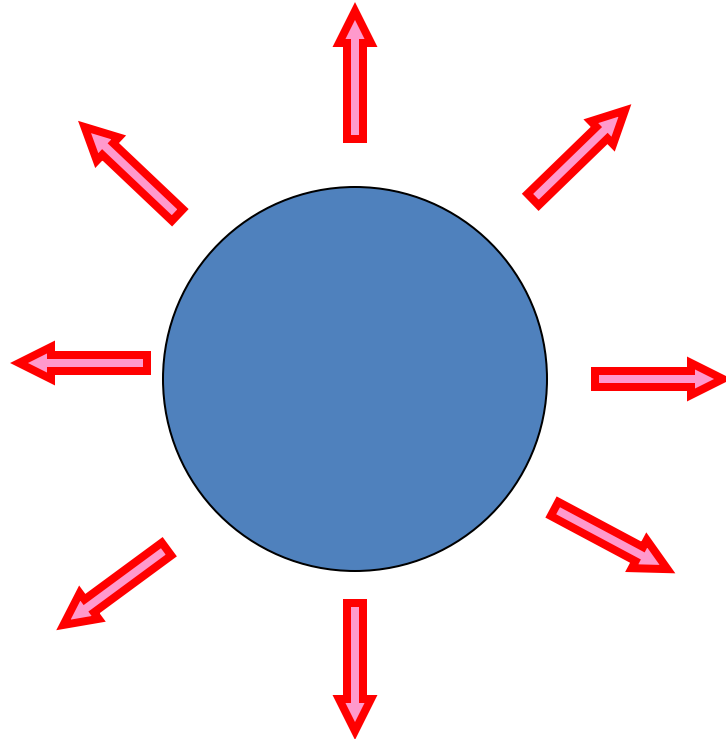
# *Earth's radiative temperature*

**Outgoing radiation:** energy emitted by planet



# *Earth's radiative temperature*

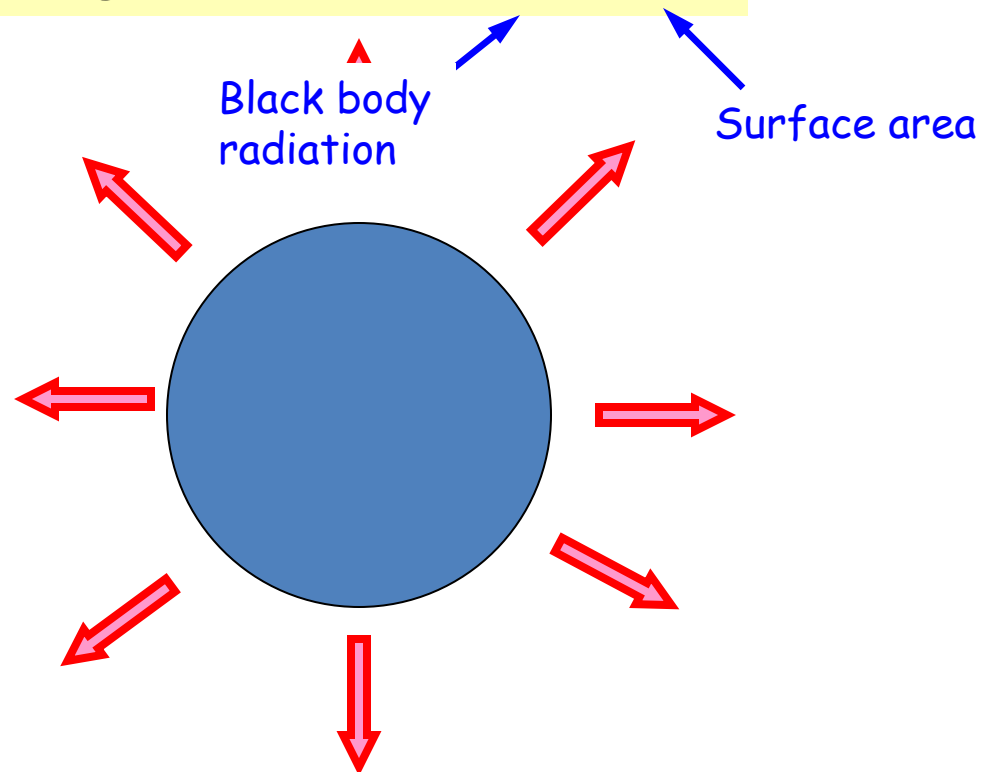
**Outgoing radiation:** energy emitted by planet is equal to its black body radiation over its surface area



# *Earth's radiative temperature*

**Outgoing radiation:** energy emitted by planet is equal to its black body radiation over its surface area

$$\text{Outgoing radiation} = \sigma T^4 4\pi R^2$$





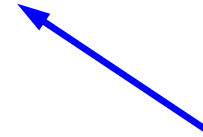
# *Earth's radiative temperature*

- Radiative equilibrium model for planet:

Incoming solar radiation



$$S(1-\alpha)\pi R^2 = \sigma T^4 4\pi R^2$$



Outgoing black-body radiation

- Solve for T to estimate planetary temperature

# *Earth's radiative temperature*

- Radiative equilibrium model for planet:

$$S(1-\alpha)\pi R^2 = \sigma T^4 4\pi R^2$$

- Solve for T to estimate planetary temperature

$$\cancel{S(1-\alpha)\pi R^2} = \cancel{\sigma T^4 4\pi R^2}$$

$$\sigma T^4 4 = S(1-\alpha)$$

$$T^4 = S(1-\alpha) / 4\sigma$$

$$T = (S(1-\alpha) / 4\sigma)^{1/4}$$

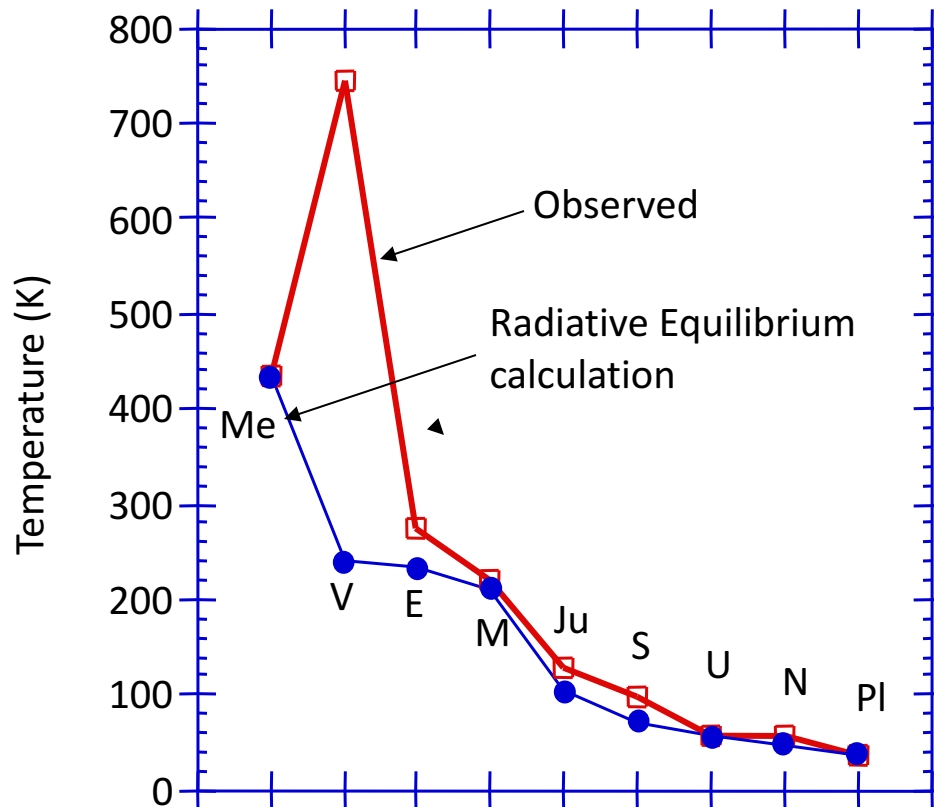
where  $S = 1367 \text{ Wm}^{-2}$ ,  $\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2}\text{K}^{-4}$ , and  $\alpha = 0.3$ .

*Earth's radiative temperature*

**255 K**

# *Planetary radiative temperature*

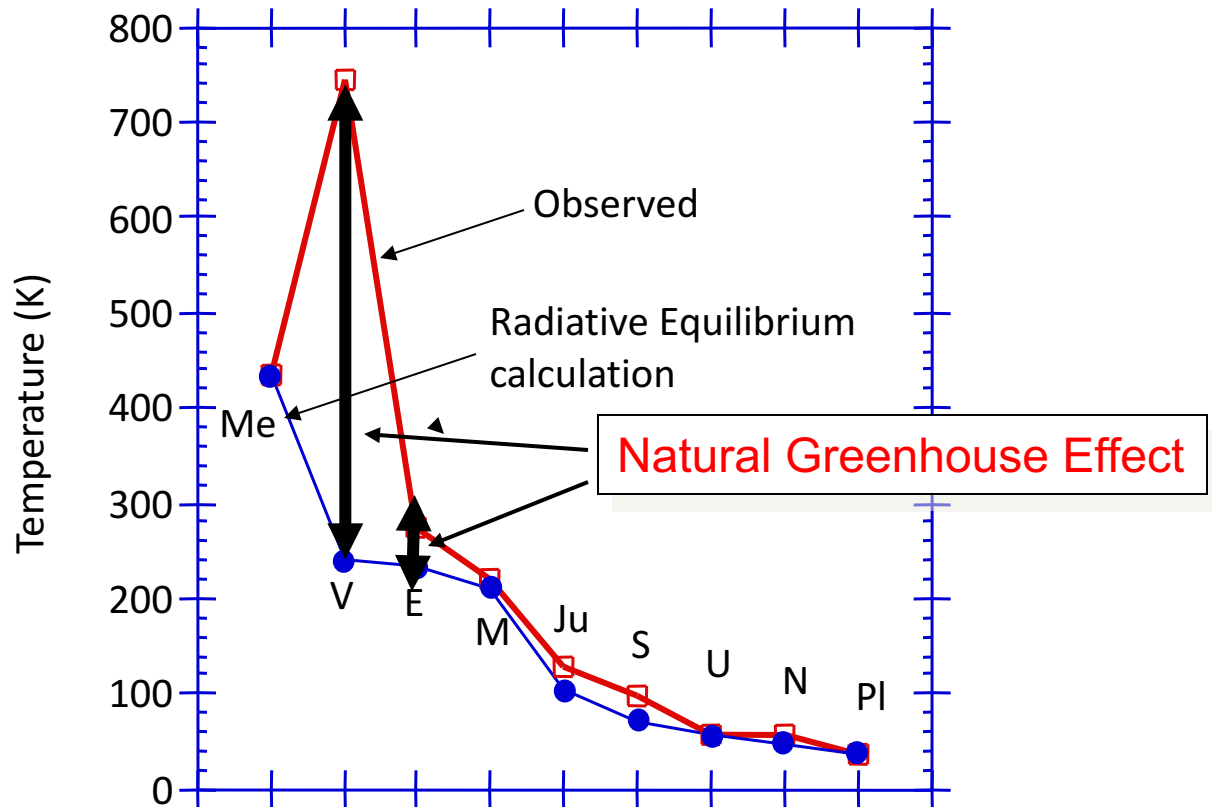
Can we use the radiative equilibrium model to predict planetary temperature?





# Where did we go wrong?

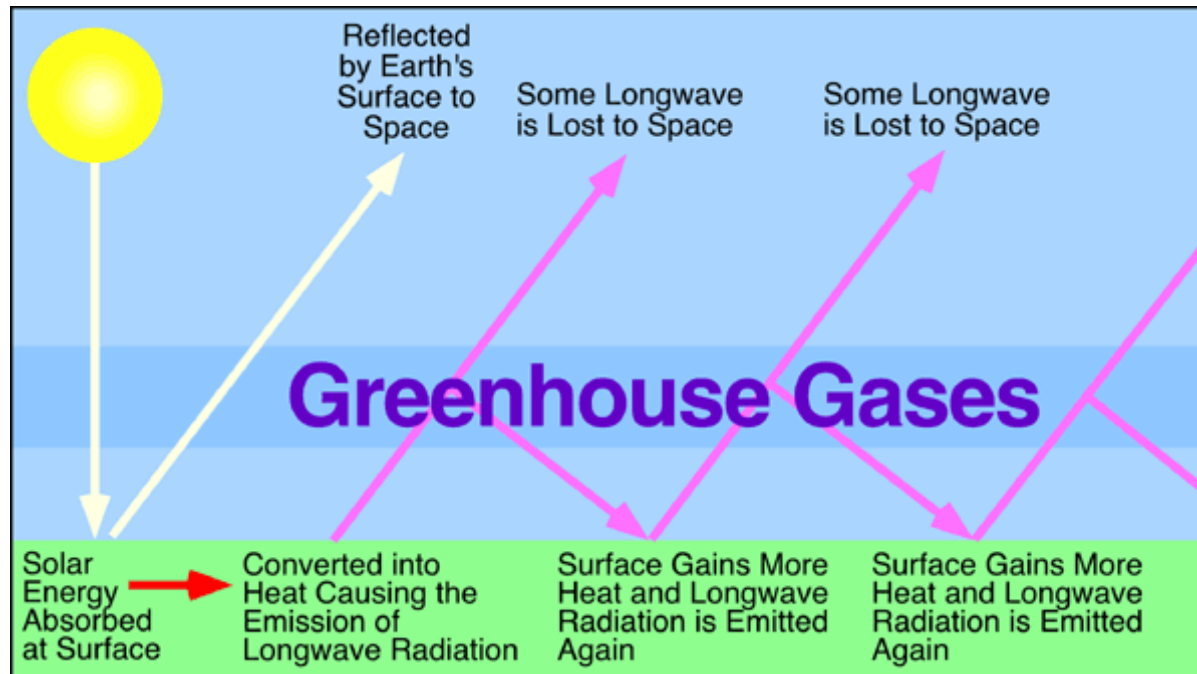
**Greenhouse effect:** not all radiation emitted by the surface escapes to space. Some is absorbed by gases in the atmosphere (greenhouse gases) and re-emitted back to the surface



# Greenhouse effect

**Greenhouse effect:** traps heat in the lower atmosphere causing warming.

- Atmosphere is almost **transparent** to solar (shortwave) radiation!
- Greenhouse gases absorb infrared (longwave radiation) and re-emit radiation in all directions



# *Summary*

- i. Earth receives its energy from the Sun in the form of electromagnetic radiation. Electromagnetic radiation varies by wavelength with warmer objects emitting more energy at shorter wavelengths.
- ii. Earth's global temperature is determined by its energy budget, the difference between the incoming and outgoing energy.
- iii. The greenhouse effect exists because gases in our atmosphere are transparent to shortwave radiation, but absorb longwave radiation. The greenhouse effect reduces the amount of outgoing energy, increasing Earth's temperature.