



EARTH 114: GLOBAL WARMING

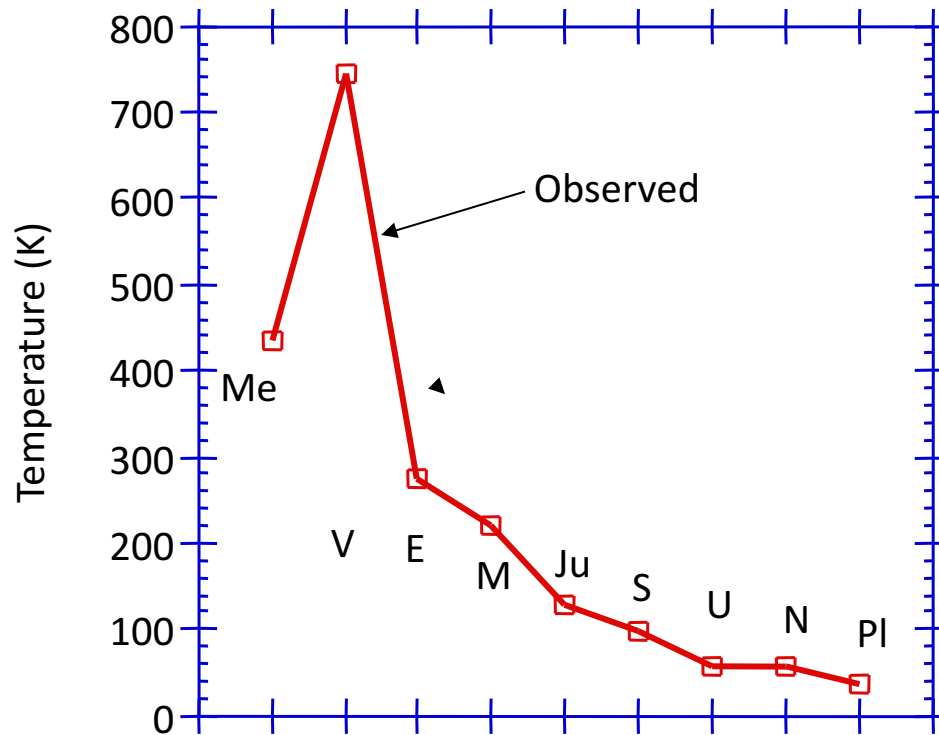
Lecture 2: Radiation and planetary temperature

Overview

- i. Solar energy and electromagnetic radiation– a little about light
- ii. Radiation laws– relationship between electromagnetic radiation and temperature
- iii. Planetary energy balance & the greenhouse effect– modeling planetary temperature

Planetary temperature

What determines Earth's mean temperature?

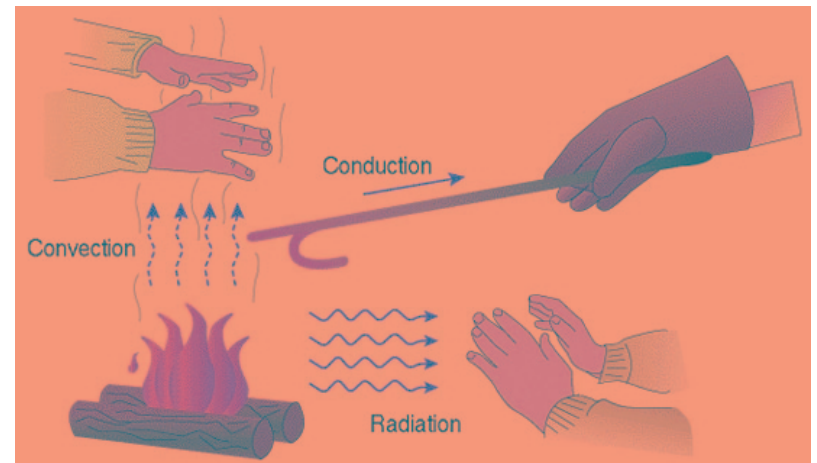
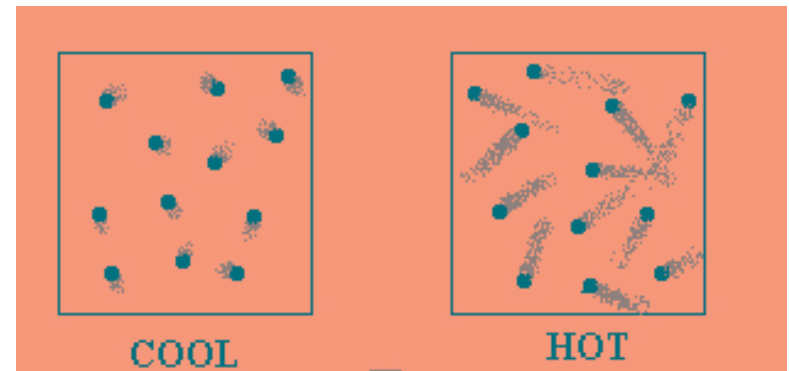


Energy and Heat

Energy: property responsible for work on or heating of an object.

Heat: Is a measure of the kinetic energy (bouncing-around energy) of atoms.

- Temperature (K, C, F) is a measure of the heat in an object.
- Heat (J) is transferred through convection, conduction, and radiation.



Solar energy

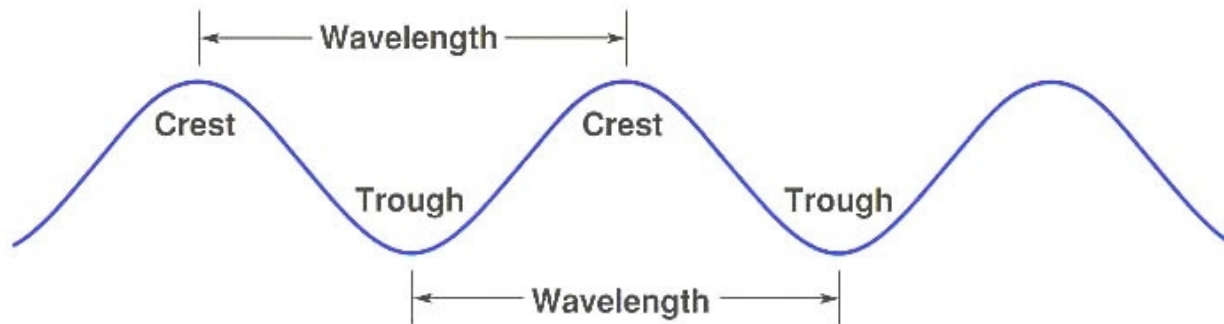
Solar heating: Earth's surface is heated by the Sun

- Earth receives 99.98% of its surface energy from the Sun.
- Solar energy is created in the core of the Sun through nuclear fusion, the welding of H atoms into He atoms.
- Every second our Sun fuses ~600 million tons of H to He, converting >4 million tons of matter into energy.
- And radiates 3.828×10^{26} J/s to space (the Sun's luminosity).
- Some of this energy reaches Earth's surface.

Electromagnetic radiation

Electromagnetic radiation: self-propagating waves that have electric and magnetic fields

- Induced by acceleration of electrons within atoms
- Moves through vacuum or matter at speed of light ($c = 3 \times 10^8$ m/s)
- Characterized by wavelength (λ) or frequency (ν)

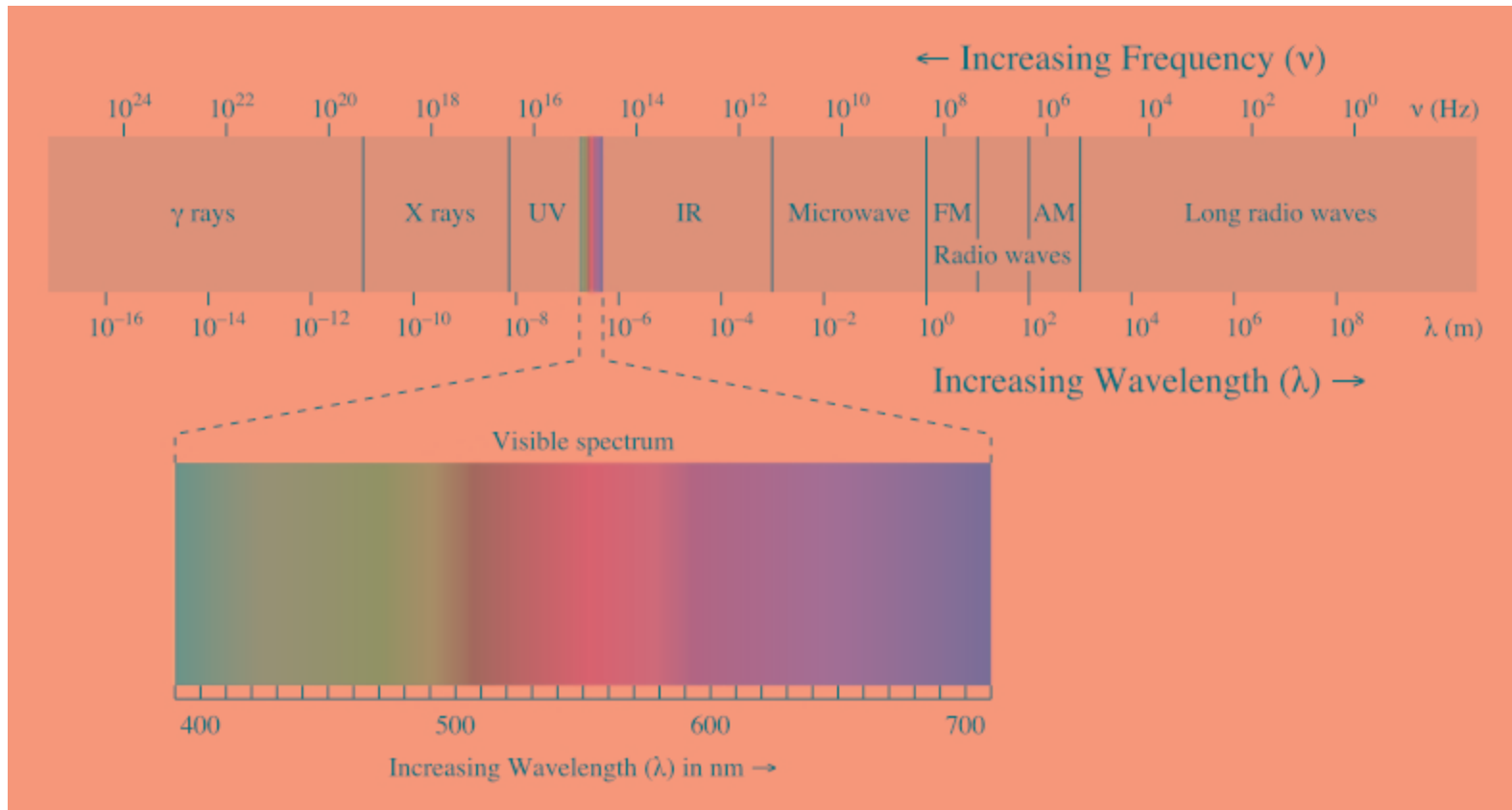


- Frequency is inversely proportional to wavelength:

$$\nu = \frac{c}{\lambda}$$

Electromagnetic spectrum

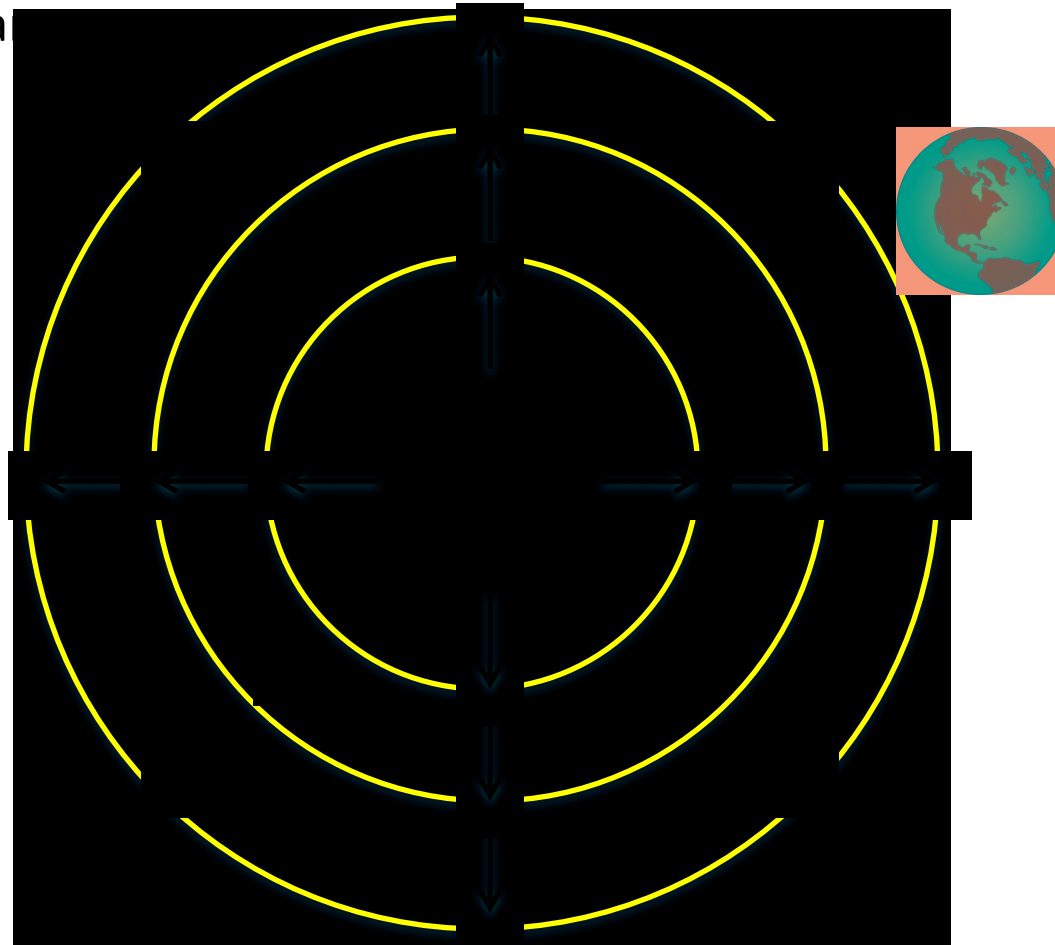
Electromagnetic spectrum: full range of electromagnetic radiation



Inverse square law

Newton's inverse square law: solar flux is inversely proportional to the square of the distance from Sun

- As energy moves away from Sun, it is spread over a greater and greater area



Inverse square law

Newton's inverse square law: solar flux is inversely proportional to the square of the distance from Sun

- As energy moves away from Sun, it is spread over a greater and greater area
- Spread over the area of a sphere, $4\pi r^2$, where r is distance from the Sun
- Solar flux is the luminosity divided by the sphere of incidence:

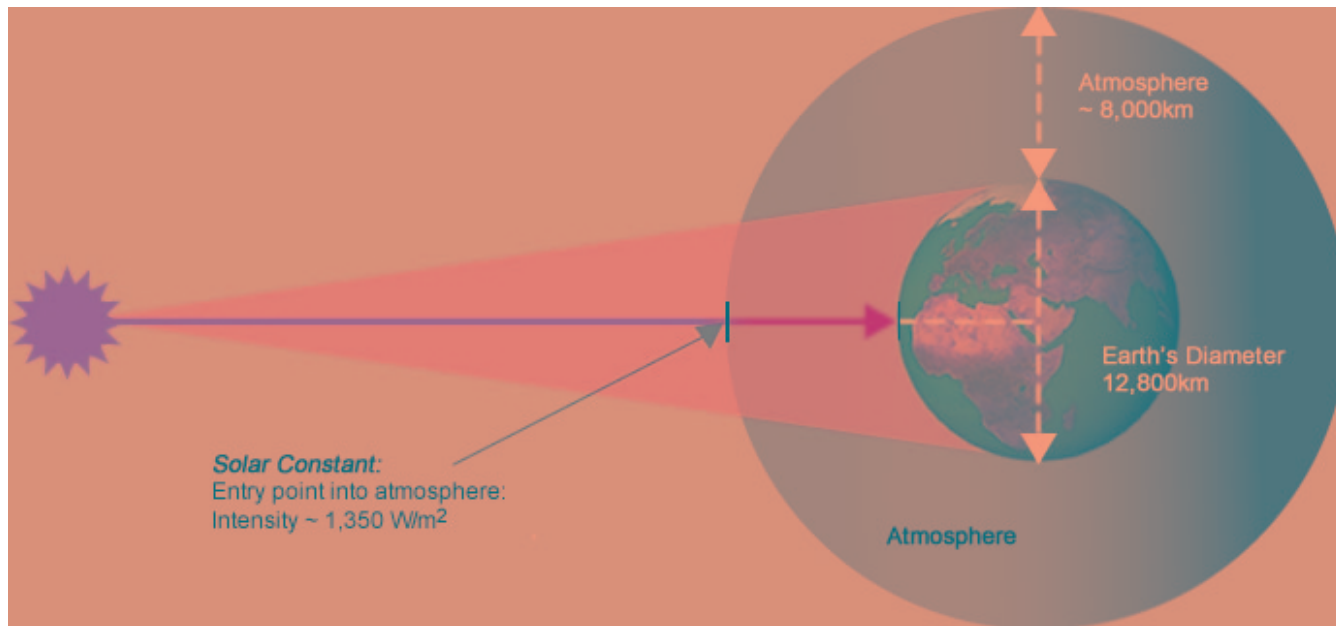
$$S = \frac{L}{4\pi r^2}$$

- What is Earth's solar flux (S_0)?
 - $L = 3.839 \times 10^{26} \text{ W}$
 - $r_0 = 1.496 \times 10^{11} \text{ m}$

Solar flux

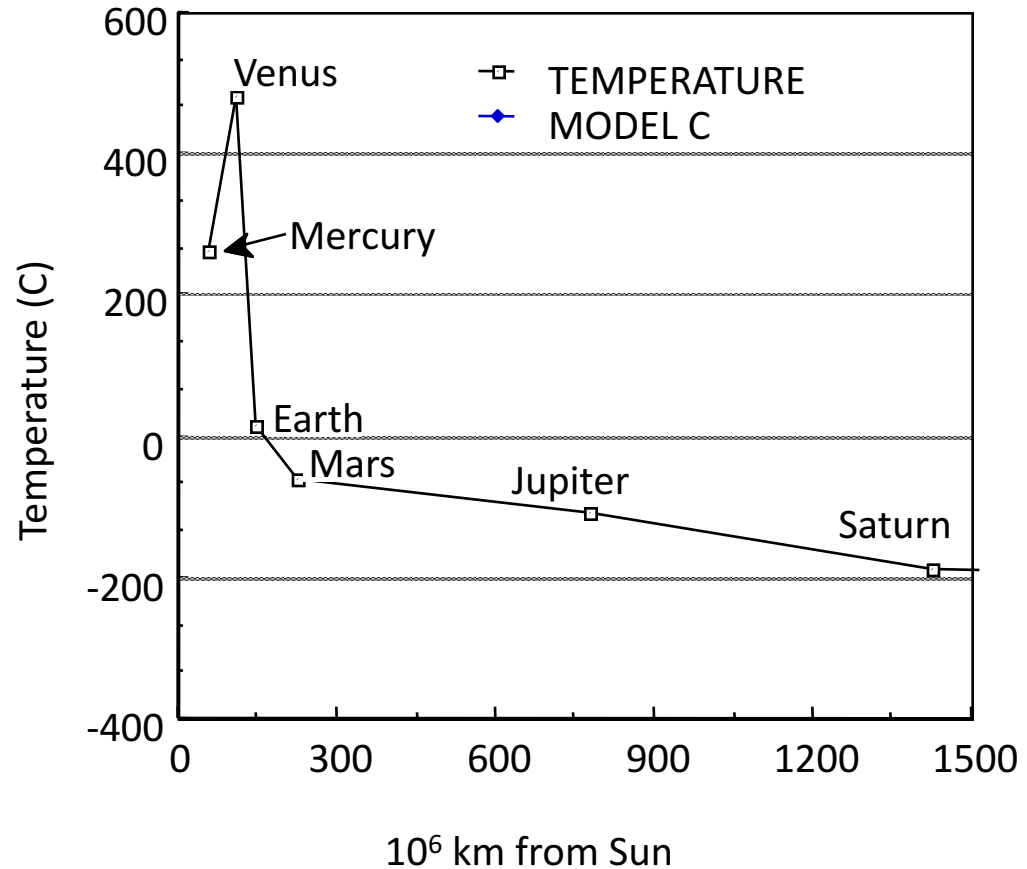
Solar flux: amount of solar energy that reaches a unit area of surface per unit time

- Solar flux is measured in units of $\text{Js}^{-1}\text{m}^{-2}$ or Wm^{-2}
- $S_0 = 1367 \text{ Wm}^{-2}$ – equivalent to $\sim 13\ 100 \text{ W}$ light bulbs illuminating a square meter



Inverse square law model

Is planetary temperature explained by distance from the Sun?



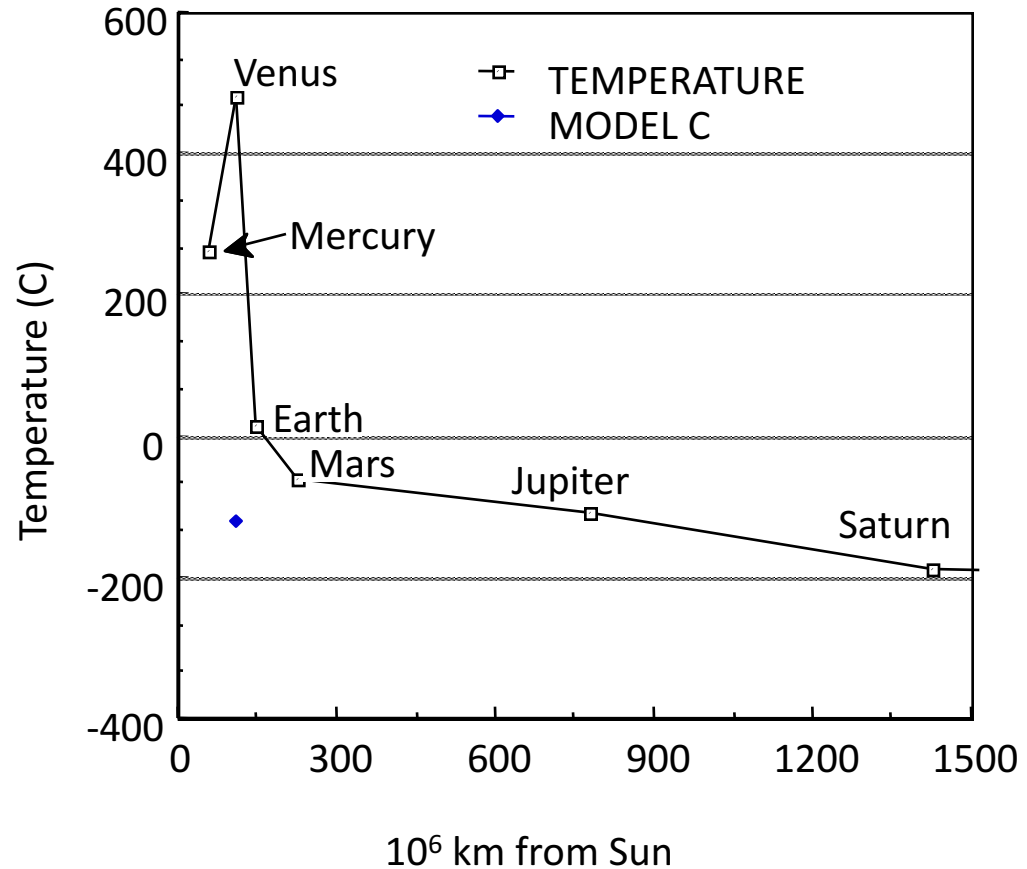
Inverse square law model

Is planetary temperature explained by distance from the Sun?

Mercury's temperature = 539 K, Venus is about 2x as far away from the Sun.

Using the inverse square law, we estimate that Venus should receive $\frac{1}{4}$ as much solar radiation.

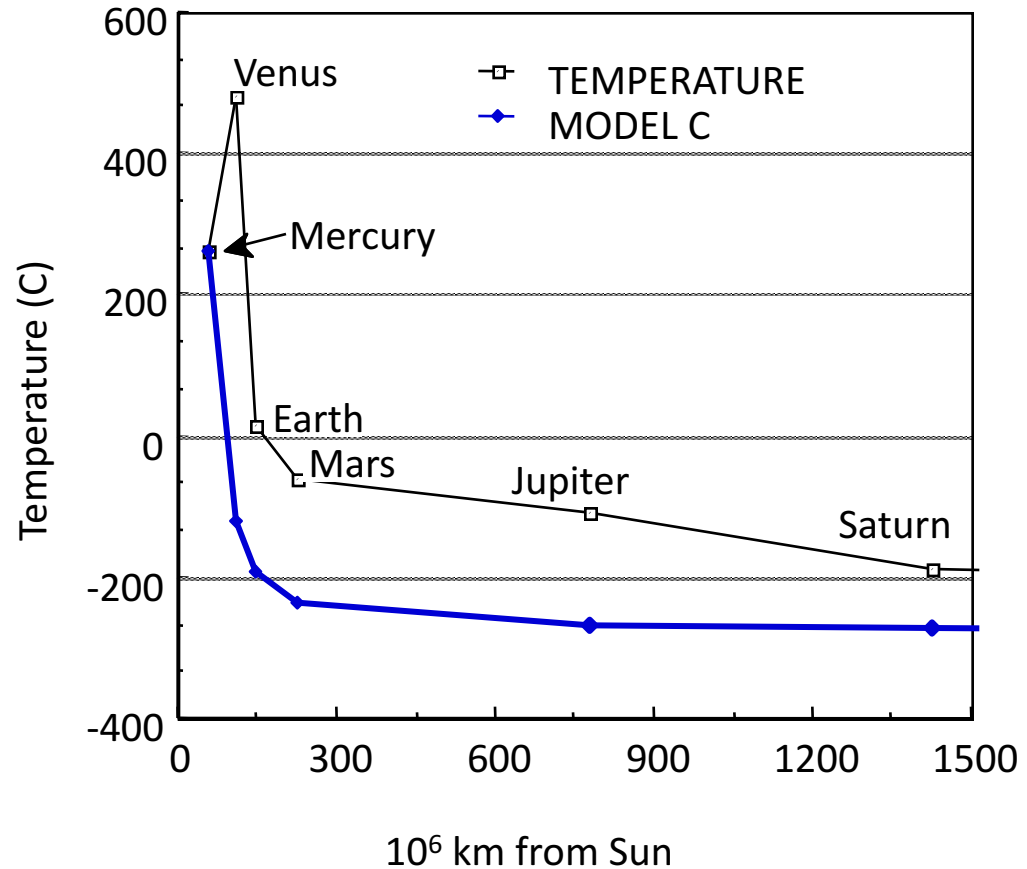
Venus' temperatures would be 539 K ($\frac{1}{4}$) = 135 K or -138 C.



Inverse square law model

Is planetary temperature explained by distance from the Sun?

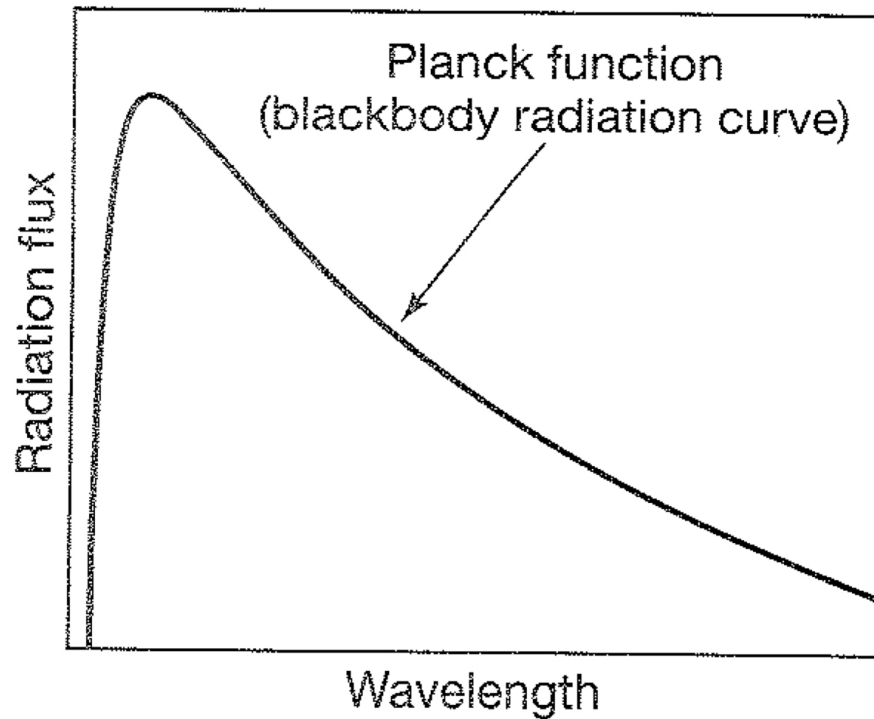
Distance from the Sun does a poor job of estimating planetary temperatures.



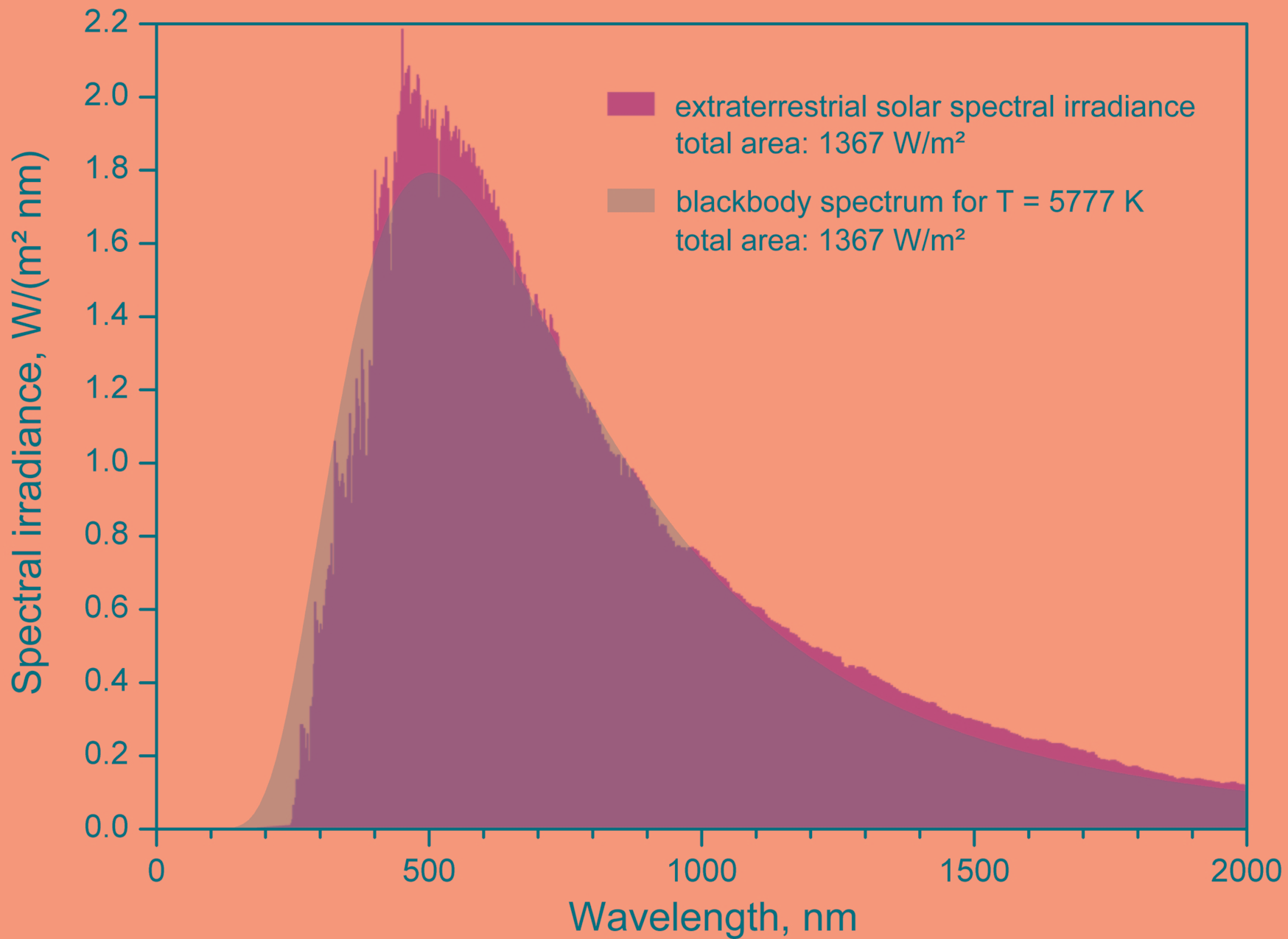
Planck's function

Planck's law of black body radiation: describes the electromagnetic radiation of a black body in thermal equilibrium.

Relates radiation flux to wavelength at equilibrium T



(a)



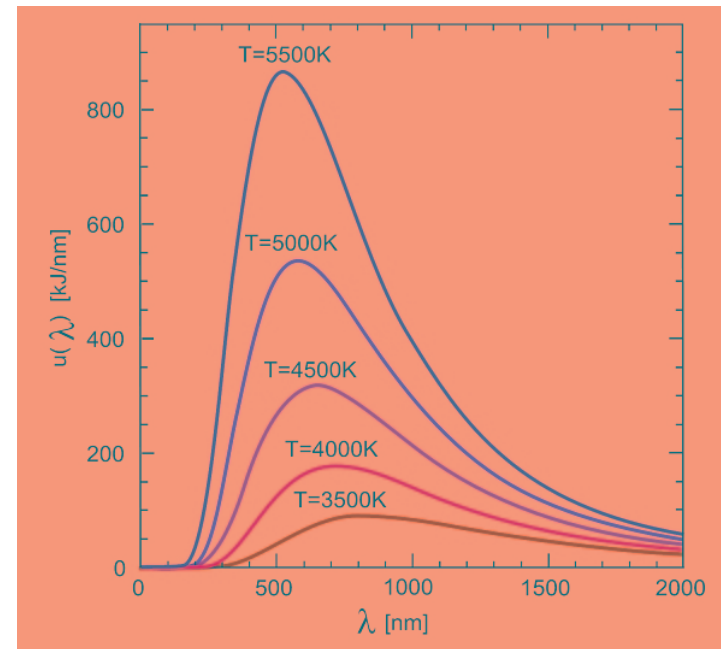
Wien's law

Wien Law: the peak electromagnetic radiation is inversely related to the temperature of a black body

A hot body will radiate at shorter peak wavelengths than a cold one:

$$\lambda_{\max} = B/T$$

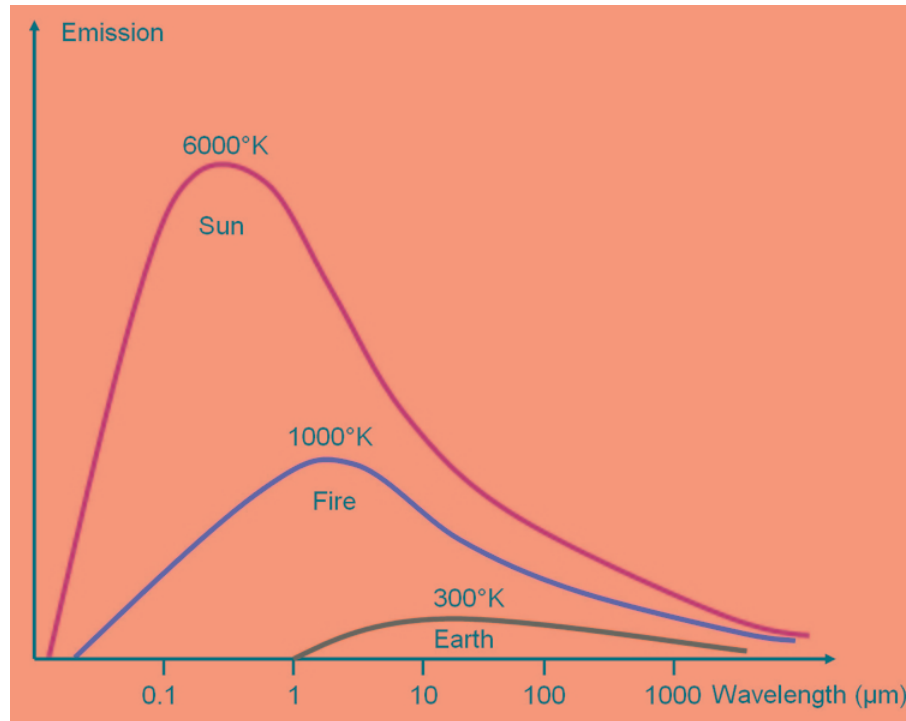
where $B=0.0029$ K m is Wien's constant



Wien's law

Wien Law: the peak electromagnetic radiation is inversely related to the temperature of a black body

- Sun – radiates in the shortwave (visible) spectra
- Earth – radiates in the longwave (ir) spectra



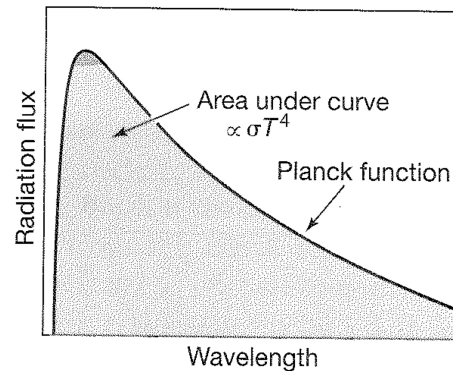
Stefan-Boltzmann law

Stefan-Boltzmann law: the total energy emitted by an object is proportional to its temperature:

$$I = \sigma T^4$$

where $\sigma = 5.67e-8 \text{ Wm}^{-2}\text{K}^{-4}$. Note that I is an energy flux (energy per time per area)! Units = $\text{Wm}^{-2} = \text{Jm}^{-2}\text{s}^{-1}$.

Stefan-Boltzmann Law is derived by integrating Planck's Function.



(c)



Radiation characteristics

	T (K)	λ_{\max} (μm)	region in spectrum	F (W/m²)
Sun	6000			
Earth	300			

Radiation characteristics

	T (K)	λ_{\max} (μm)	region in spectrum	F (W/m²)
Sun	6000	0.5		
Earth	300	10		

Radiation characteristics

	T (K)	λ_{\max} (μm)	region in spectrum	F (W/m²)
Sun	6000	0.5	visible	
Earth	300	10	infrared	

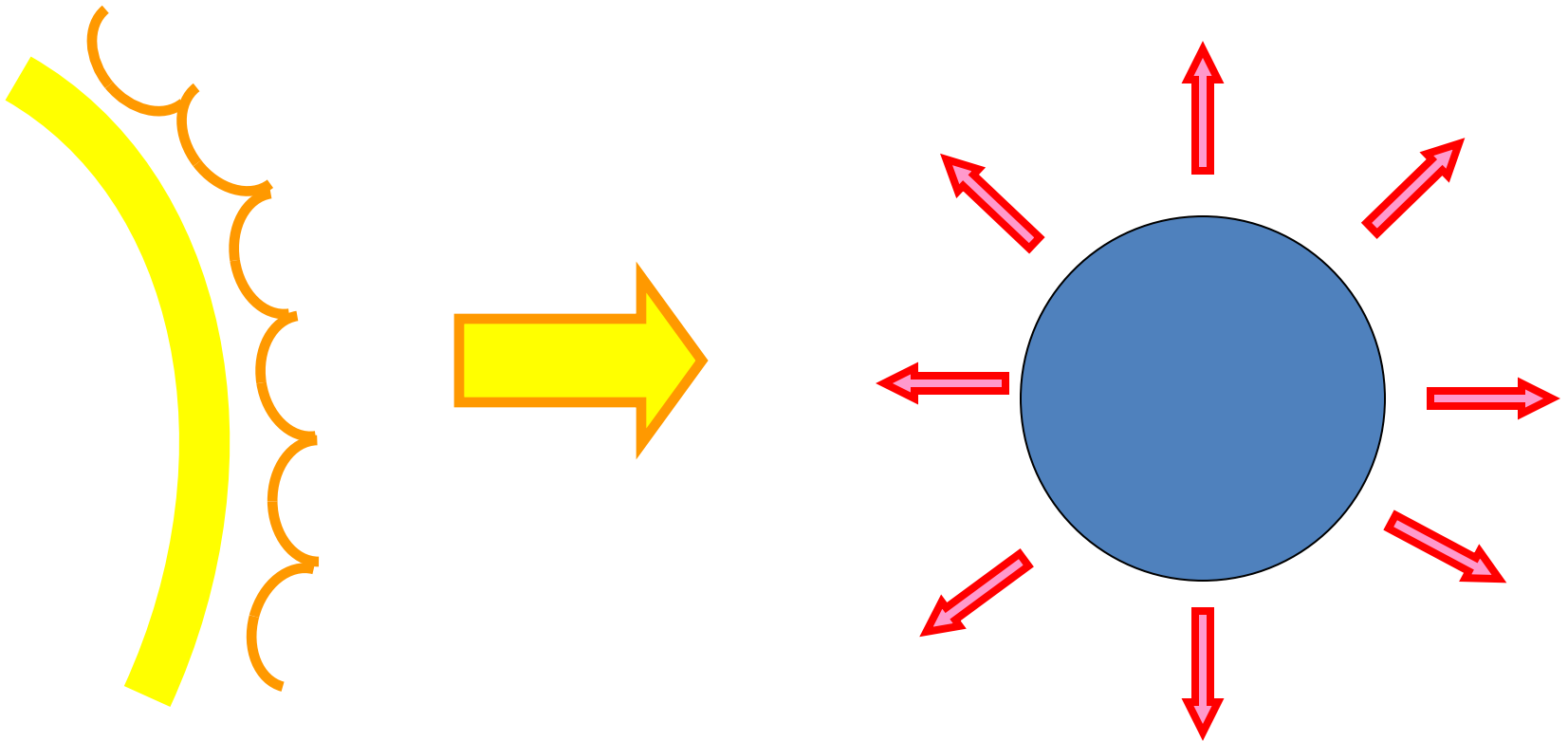
Radiation characteristics

	T (K)	λ_{\max} (μm)	region in spectrum	F (W/m²)
Sun	6000	0.5	visible	7×10^7
Earth	300	10	infrared	460

Planetary energy balance

Radiative equilibrium: assumes energy balance, incoming radiation equals outgoing radiation

- If incoming and outgoing radiation are not in balance, Earth's temperature will rise or fall.



Earth's radiative temperature

Let's calculate the radiative equilibrium temperature for Earth!

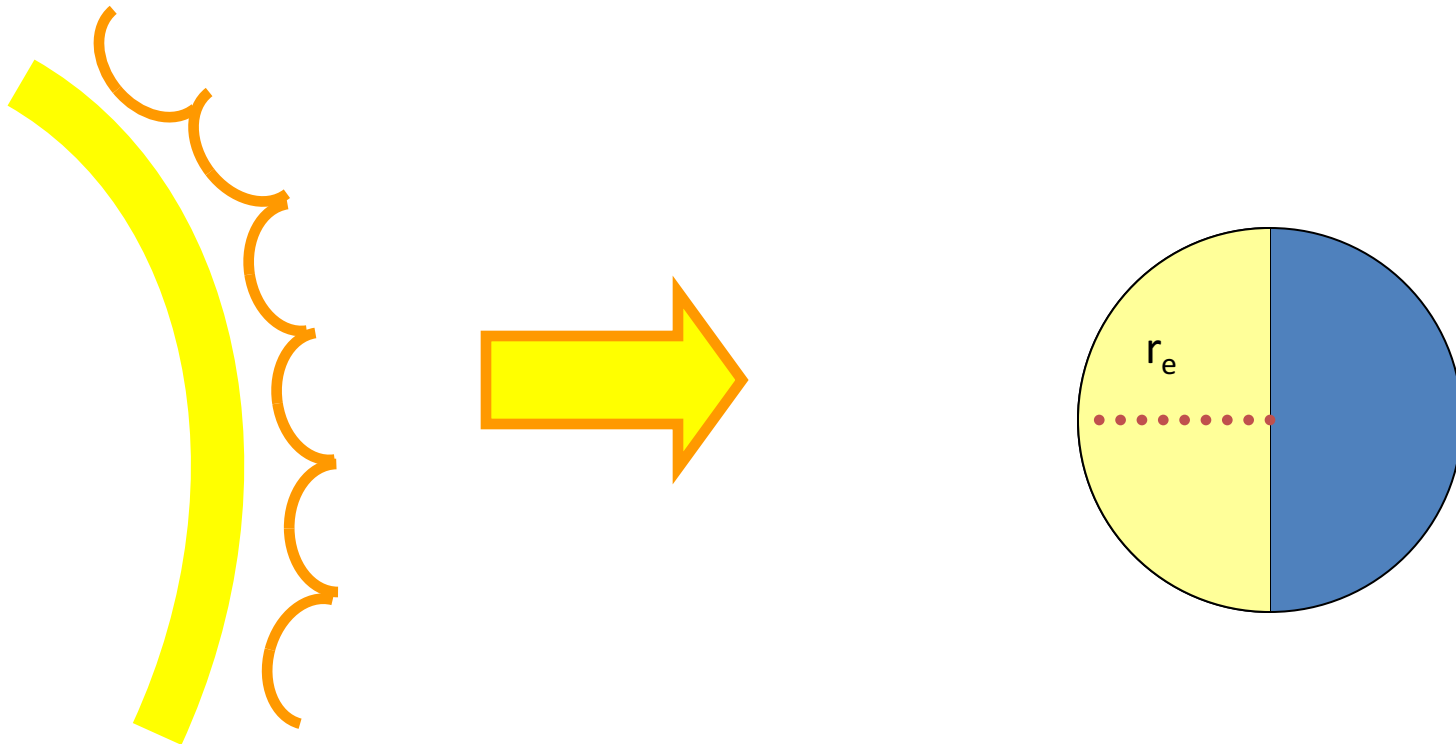
- Start from our equation for radiative equilibrium:

$$\text{Incoming Radiation} = \text{Outgoing Radiation}$$

- Write equation for Incoming Radiation
- Write equation for Outgoing Radiation
- Solve

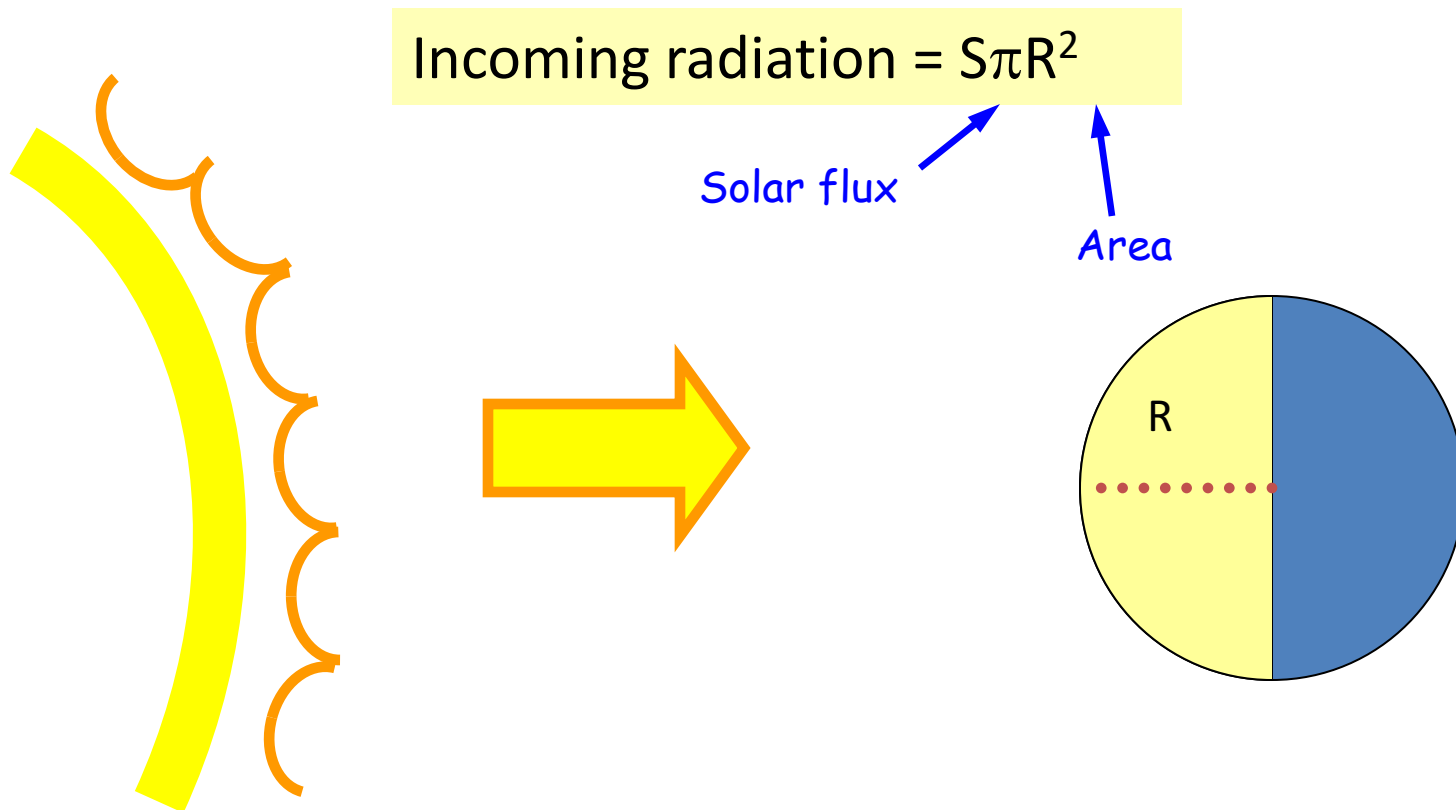
Earth's radiative temperature

Incoming radiation: energy received from the Sun



Earth's radiative temperature

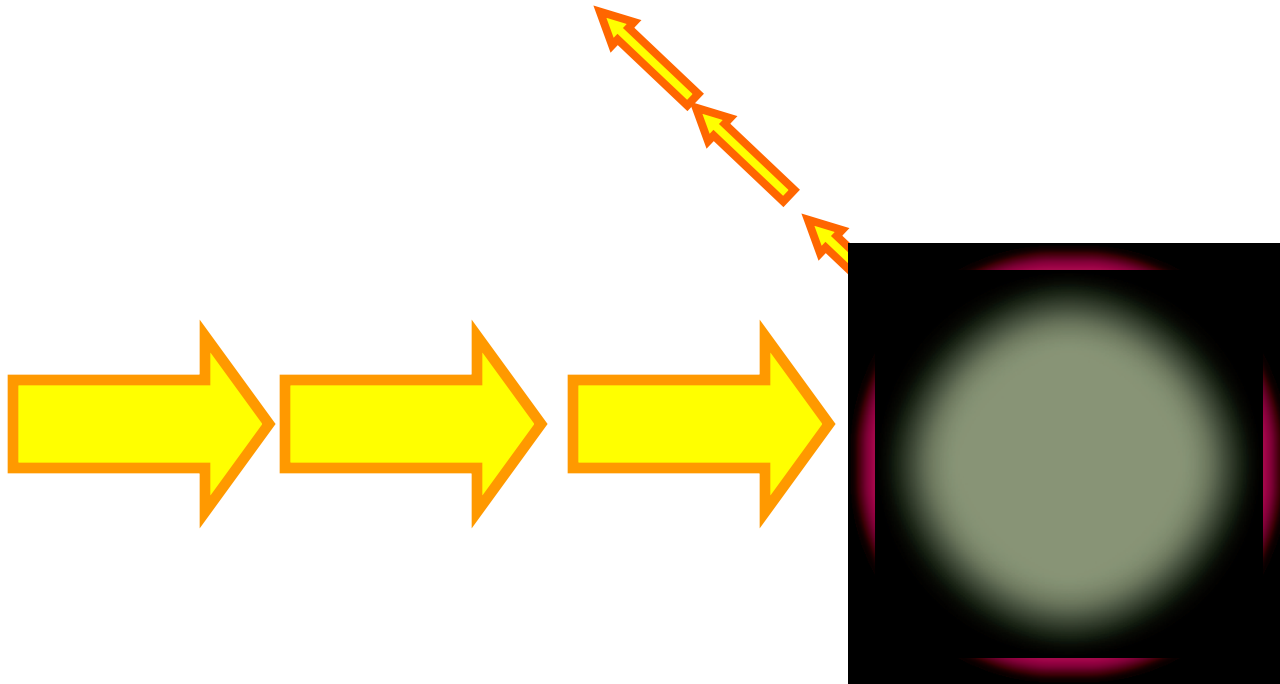
Incoming radiation: energy received from the Sun (S) covers the area of a circle defined by the radius of the Earth (R)



Albedo

Albedo: measure of visible light reflection

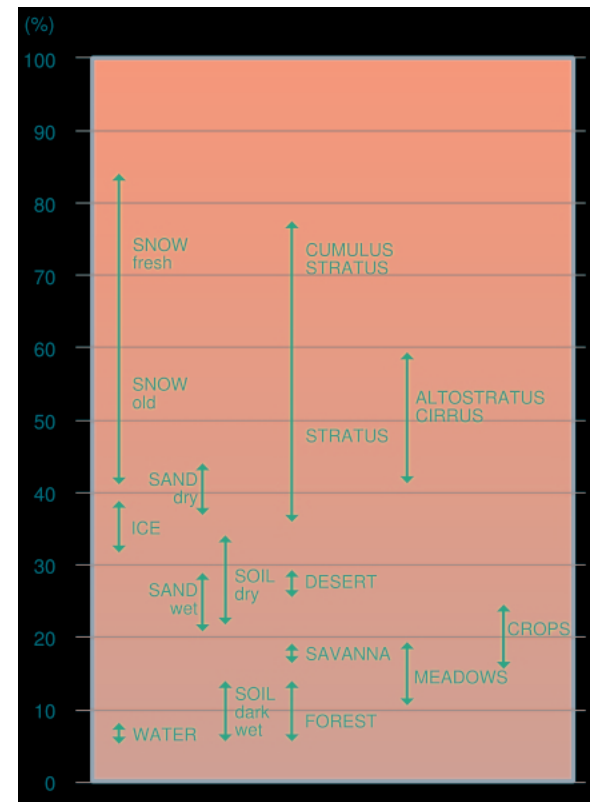
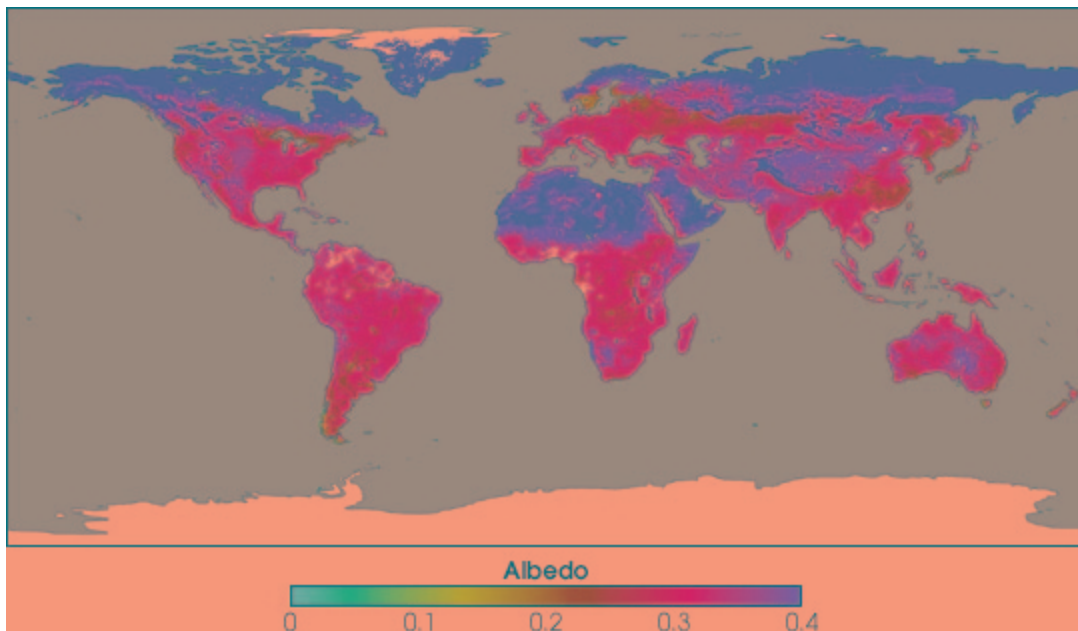
- Some of the incoming visible radiation is not absorbed, it is reflected



Albedo

Albedo: measure of visible light reflection

- Some of the incoming radiation is not absorbed, it is reflected
- Expressed as a fraction of the total incident radiation
- Varies from 0 (no reflection) to 1 (complete reflection)

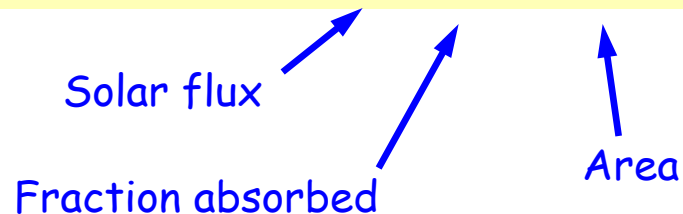


Earth's radiative temperature

Incoming radiation: energy received from the Sun

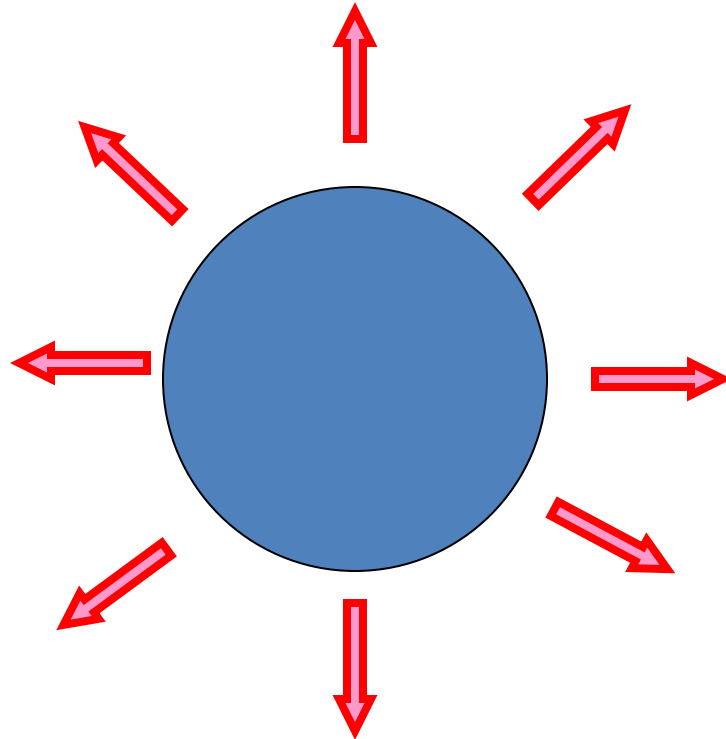
- Fraction of incoming radiation that is absorbed is $(1 - \alpha)$

$$\text{Incoming radiation} = S(1-\alpha)\pi R^2$$



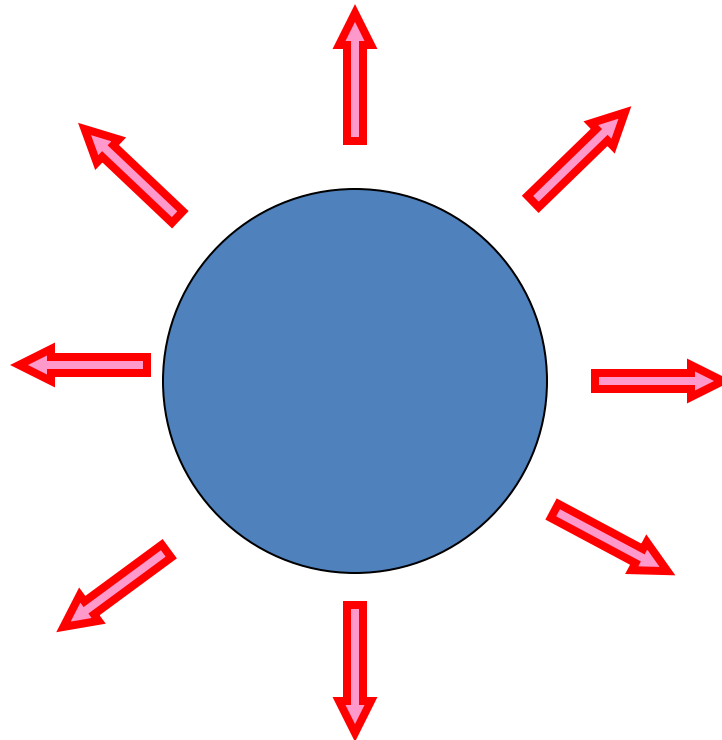
Earth's radiative temperature

Outgoing radiation: energy emitted by planet



Earth's radiative temperature

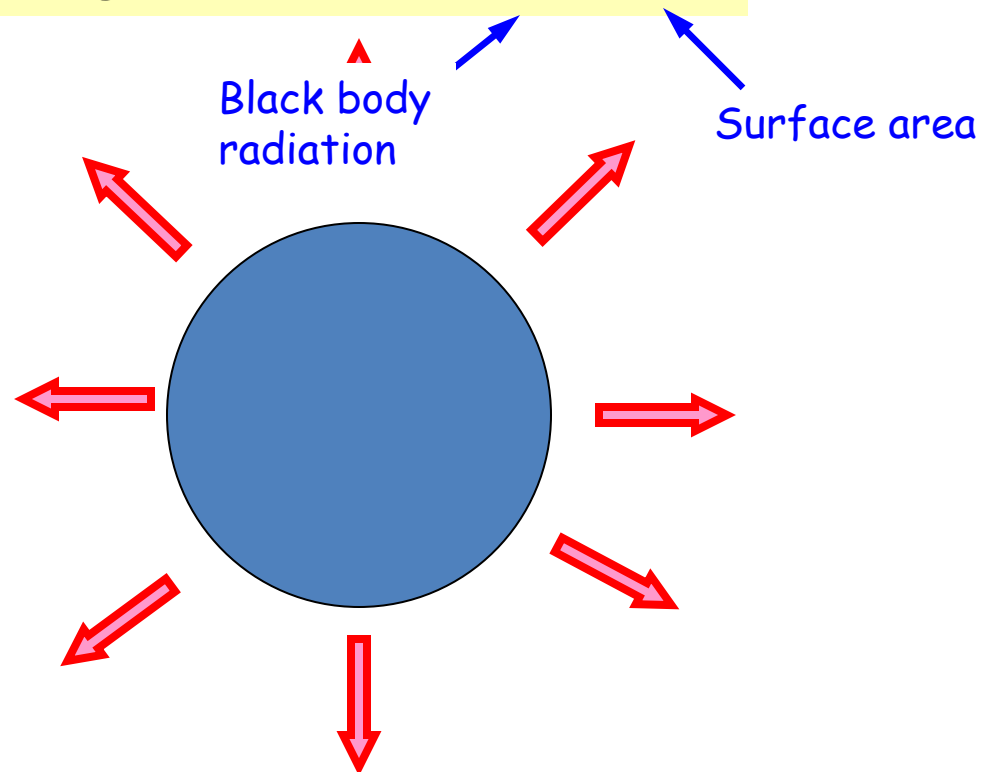
Outgoing radiation: energy emitted by planet is equal to its black body radiation over its surface area



Earth's radiative temperature

Outgoing radiation: energy emitted by planet is equal to its black body radiation over its surface area

$$\text{Outgoing radiation} = \sigma T^4 4\pi R^2$$



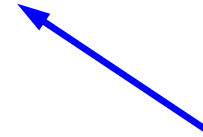
Earth's radiative temperature

- Radiative equilibrium model for planet:

Incoming solar radiation



$$S(1-\alpha)\pi R^2 = \sigma T^4 4\pi R^2$$



Outgoing black-body radiation

- Solve for T to estimate planetary temperature

Earth's radiative temperature

- Radiative equilibrium model for planet:

$$S(1-\alpha)\pi R^2 = \sigma T^4 4\pi R^2$$

- Solve for T to estimate planetary temperature

$$S(1-\alpha) \cancel{\pi R^2} = \sigma T^4 4 \cancel{\pi R^2}$$

$$\sigma T^4 4 = S(1-\alpha)$$

$$T^4 = S(1-\alpha) / 4\sigma$$

$$T = (S(1-\alpha) / 4\sigma)^{1/4}$$

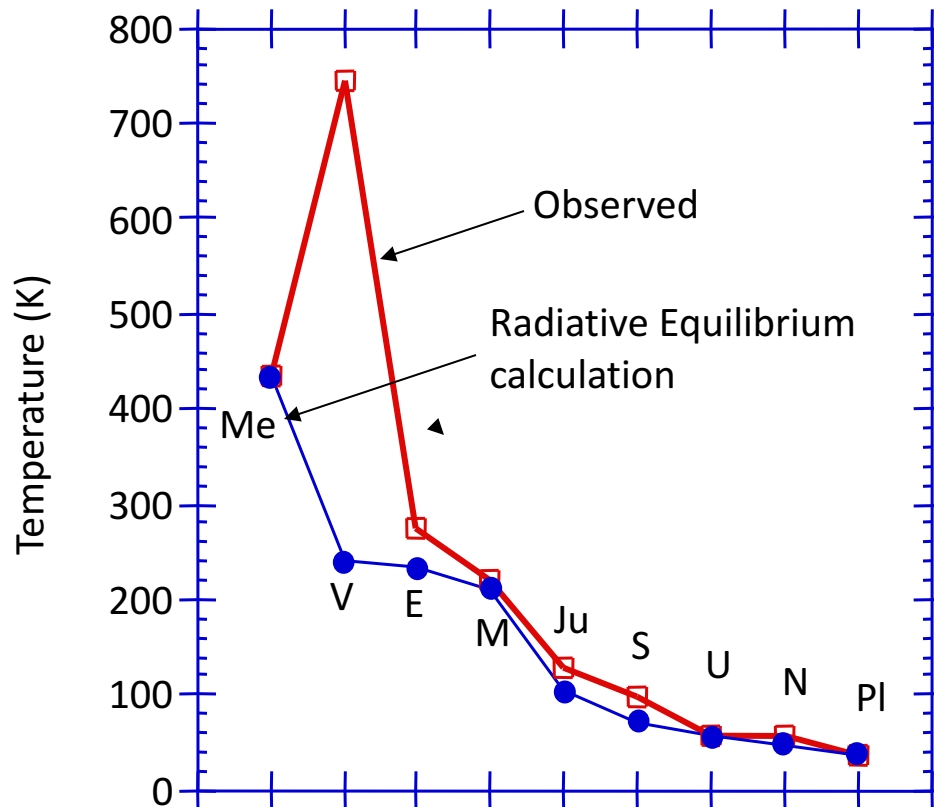
where $S = 1367 \text{ Wm}^{-2}$, $\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2}\text{K}^{-4}$, and $\alpha = 0.3$.

Earth's radiative temperature

255 K

Planetary radiative temperature

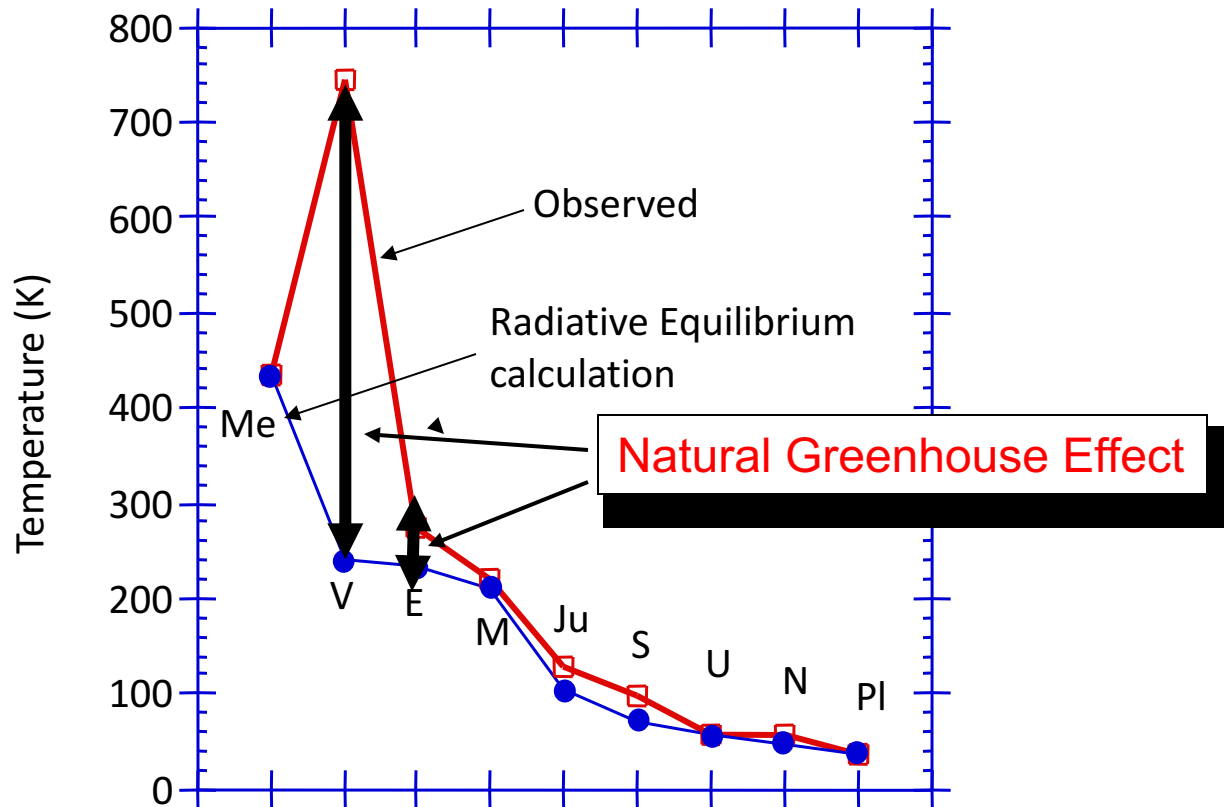
Can we use the radiative equilibrium model to predict planetary temperature?





Where did we go wrong?

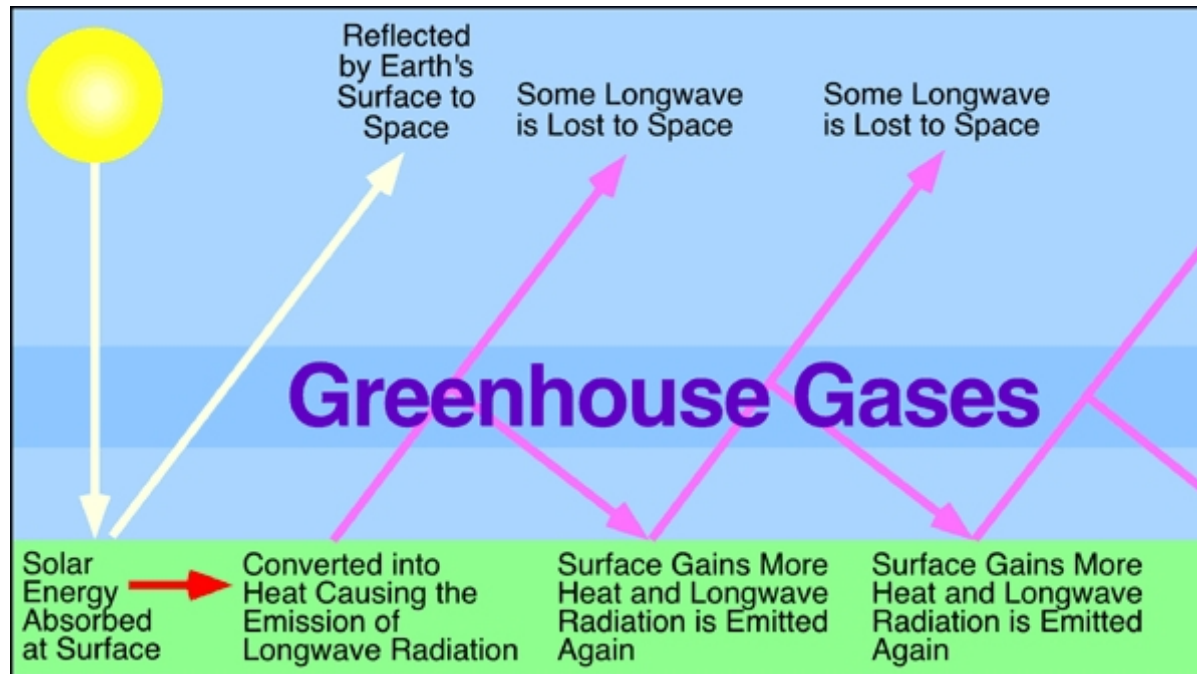
Greenhouse effect: not all radiation emitted by the surface escapes to space. Some is absorbed by gases in the atmosphere (greenhouse gases) and re-emitted back to the surface



Greenhouse effect

Greenhouse effect: traps heat in the lower atmosphere causing warming.

- Atmosphere is almost **transparent** to solar (shortwave) radiation!
- Greenhouse gases absorb infrared (longwave radiation) and re-emit radiation in all directions



Summary

- i. Earth receives its energy from the Sun in the form of electromagnetic radiation. Electromagnetic radiation varies by wavelength with warmer objects emitting more energy at shorter wavelengths.
- ii. Earth's global temperature is determined by its energy budget, the difference between the incoming and outgoing energy.
- iii. The greenhouse effect exists because gases in our atmosphere are transparent to shortwave radiation, but absorb longwave radiation. The greenhouse effect reduces the amount of outgoing energy, increasing Earth's temperature.