

Math 1231 Summer 2024

Practice Midterm 1

- You will have 90 minutes for this test.
- You are not allowed to consult books or notes during the test, but you may use a one-page, one-sided, handwritten cheat sheet you have made for yourself ahead of time.
- You may not use a calculator. You may leave answers unsimplified, except you should compute trigonometric functions as far as possible.
- The exam has 5 problems, one on each mastery topic we've covered. The exam has 5 pages total.
- Each part of each topic is worth ten points, except the M2 questions are worth 15 points. The whole test is scored out of 100 points.
- Read the questions carefully and make sure to answer the actual question asked. Make sure to justify your answers—math is largely about clear communication and argument, so an unjustified answer is much like no answer at all. When in doubt, show more work and write complete sentences.
- If you need more paper to show work, I have extra at the front of the room.
- Good luck!

	a	b	c	d
M1:				
M2:			S1:	
S2:		S3:		/100

Name:

Name: _____

Problem 1 (M1). Compute the following limits if they exist. Show enough work to justify your computation.

(a) $\lim_{x \rightarrow +\infty} \frac{\sqrt{5x^4 + x + 1}}{x^2 + 3x + 4}$

(b) $\lim_{x \rightarrow 0} \frac{\sin(3x) \tan(2x)}{5x^2}$

(c) $\lim_{x \rightarrow 3} \frac{x^2 - 5x + 4}{x^2 - 2x - 3}$

(d) $\lim_{x \rightarrow 5} \frac{\sqrt{x+4} - 3}{x - 5}$

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Problem 2 (M2). Compute the derivatives of the following functions using any of the methods we have learned in class. Show enough work to justify your answers.

(a) $\frac{d}{dx} \cos^2(\tan^2(\sec^2(\sqrt{x} + x)))$

(b) $\frac{d}{dx} \frac{\csc(x^2 + 1)}{x^4 + \sqrt{\cos(x)}}$

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Problem 3 (S1). If $f(x) = (x - 3)^2$, find $f'(5)$, directly from the definition of derivative.

Problem 4 (S2). Give the equation for the linear approximation of the function $f(x) = x \sin(x)$ near the point $a = \pi/2$. Use it to estimate $f(1.5)$.

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Problem 5 (S3). Find a formula for the line tangent to the curve $x^2y^2 = 5 + x + y$ at the point $(1, 3)$.