

# COLLOQUIUM

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## “On the best constant in Poincaré inequality”

Wednesday, November 19, 2014 at 3:30 p.m. in CH 101

Refreshments will be served in Math 238 at 3:00 p.m.

### Abstract

Let  $1 \leq p, q, r \leq \infty$ . We consider the following problem: to find the sharp constant in the generalized Poincaré inequality

$$\lambda_{pqr} = \min \frac{\|y'\|_{L_p[-1,1]}}{\|y\|_{L_q[-1,1]}}; \quad \int_{-1}^1 |y(t)|^{r-2} y(t) dt = 0 \quad (1)$$

(for  $r = \infty$  the last relation is understood in the limit sense).

Problem (1), so as its particular cases and some equivalent problems, arise, mostly for  $r = 2$ , in various fields of mathematics. We mention the problem of optimality of some goodness-of-fit criteria in non-parametric statistics and the estimation of critical values in the Lagrange problem.