**Title**: Analytic continuation of Laurent series to domains of minimal capacity

**Abstract**: Let f(z) be a function defined by Laurent series

$$f(z) = \sum_{k=-\infty}^{\infty} a_k z^k, \tag{1}$$

which is analytic on the unit circle  $\mathbb{T}$ . By the classical theorem of Pierre Alphonse Laurent (1843), the series (1) converges on an annulus  $A(r,R) = \{z : r < |z| < R\}$  with some r and  $R, 0 \le r < 1 < r < R$  $R \leq \infty$ , and diverges for all  $z \in \overline{\mathbb{C}} \setminus \overline{A(r,R)}$ . It is also well-known that often the function f(z) defined by the series (1) can be analytically/meromorphycally continued to a larger domain  $D \supset A(r,R)$ . The primary goal of this project is to study the largest domains  $D \subset \mathbb{C}$ , to which the function f can be extended as a single-valued meromorphic function. To clarify the term "largest", we note that the complement  $\overline{\mathbb{C}} \setminus D$  consists of two parts:  $E_0 = \{z \notin D : |z| \geq R\}$  and  $E_1 = \{z \notin D : |z| \le r\}$ . If  $E_0$  and  $E_1$  both are not empty, then the domain D can be considered as a field of the condenser  $(D, E_0, E_1)$ with plates  $E_0$  and  $E_1$ . Precisely, we want to identify all domains D to which the series (1) can be continued meromorphically and such that the corresponding condensers  $(D, E_0, E_1)$  have the **minimal possible capacity**. The capacity of a condenser can be defined as the minimum of the Dirichlet integral; i.e.,

$$cap(D) = \inf \int_{D} |\nabla u|^2 dA,$$

where the infimum is taken over all functions  $u \in Lip(D)$  such that u = 0 on  $E_0$  and u = 1 on  $E_1$ .

This project can be thought as an extension of recent work of Prof. H. Stahl who studied meromorphic extensions of Taylor series at  $z=\infty$  to domains  $D\ni\infty$  with minimal logarithmic capacity of their complement  $\mathbb{C}\setminus D$ .

In the first part of my talk, I will introduce our main problem and discuss several examples illustrating main ideas and concepts. Then I will present an existence theorem for extremal condensers and give a sketch of its proof. Also, a uniqueness theorem for extremal domains will be discussed. Finally, the topological structure of complementary sets (or plates)  $E_0$  and  $E_1$  of the condensers of minimal capacity will be discussed and analytic tools needed for their characterization will be presented.