```
61.py - C:/Users/HP/61.py (3.4.3)
                                                                                                                                                                          o x
File Edit Format Run Options Window Help
def optimal bst(keys, freq):
   for i in range(1, n+1):
                                                                                  Python 3.4.3 Shell
                                                                                                                                                       def sum freq(i, j):
                                                                                  File Edit Shell Debug Options Window Help
       return prefix[j] - prefix[i-1]
                                                                                  Python 3.4.3 (v3.4.3:9b73flc3e601, Feb 24 2015, 22:44:40) [MSC v.1600 64 bit (AM *
   # Fill cost for single keys
                                                                                  D64)] on win32
                                                                                  Type "copyright", "credits" or "license()" for more information.
   for i in range(1, n+1):
                                                                                  cost[i][i] = freq[i-1]
       root[i][i] = i
                                                                                  For Keys = ['A', 'B', 'C', 'D'] Freq = [0.1, 0.2, 0.4, 0.3]
   # Chain length L
                                                                                  Cost Table:
   for L in range (2, n+1):
                                                                                  [0.1, 0.4, 1.1, 1.7]
       for i in range(1, n-L+2):
                                                                                  [0, 0.2, 0.8, 1.4]
          j = i + L - 1
                                                                                  [0, 0, 0.4, 1.0]
           cost[i][j] = float("inf")
                                                                                  [0, 0, 0, 0.3]
           # Try making all keys in interval [i..j] as root
                                                                                  Root Table:
           for r in range(i, j+1):
                                                                                  [1, 2, 3, 3]
              c = cost[i][r-l] + cost[r+l][j] + sum_freq(i, j)
                                                                                  [0, 2, 3, 3]
              if c < cost[i][j]:
                                                                                  [0, 0, 3, 3]
                  cost[i][j] = c
                                                                                  [0, 0, 0, 4]
                  root[i][j] = r
                                                                                  Minimum Cost of OBST: 1.7
   # Print Cost Table
   print("\nCost Table:")
                                                                                  Test Case (a):
   for i in range(1, n+1):
       print(cost[i][1:n+1])
                                                                                  Cost Table:
                                                                                  [34, 118]
   # Print Root Table
                                                                                  [0, 50]
   print ("\nRoot Table:")
   for i in range(l, n+l):
                                                                                  Root Table:
       print(root[i][1:n+1])
                                                                                  [1, 2]
                                                                                  [0, 2]
   print("\nMinimum Cost of OBST:", cost[1][n])
   return cost, root, cost[1][n]
                                                                                  Minimum Cost of OBST: 118
                                                                                  Test Case (b):
# ----- MAIN EXECUTION -----
                                                                                  Cost Table:
# Problem input
                                                                                  [34, 50, 142]
keys = ["A", "B", "C", "D"]
                                                                                  [0, 8, 66]
freq = [0.1, 0.2, 0.4, 0.3]
                                                                                  [0, 0, 50]
print ("For Keys =", keys, "Freq =", freq)
cost, root, min cost = optimal bst(keys, freq)
                                                                                                                                                        Ln: 46 Col: 4
# Tast mass /s/
                                                                                                                                                                           Ln: 45 Col: 33
  6 Sports headline
                                                                               Y L O O E O S
                                                                                                                                                    Q Search
```

Max Verstappen.

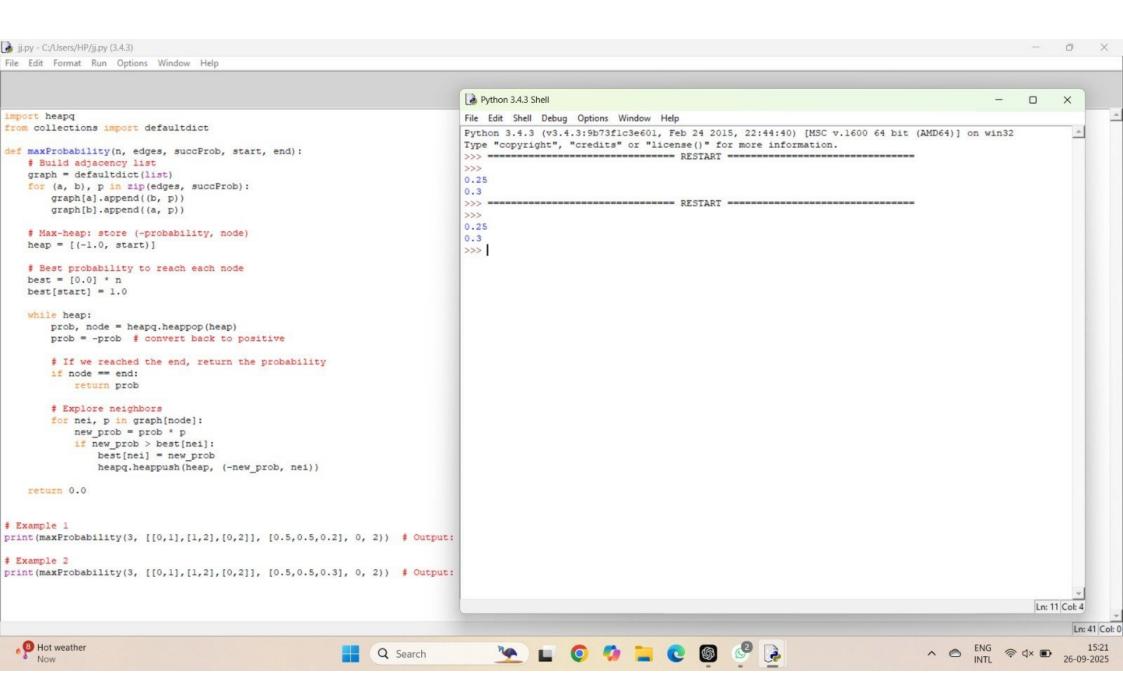
```
62.py - C:/Users/HP/62.py (3.4.3)
                                                                                                                                                                                o X
File Edit Format Run Options Window Help
def optimal bst(keys, freq):
                                                                                           Python 3.4.3 Shell
                                                                                                                                                                  for L in range(2, n+1):
       for i in range(1, n-L+2):
                                                                                           File Edit Shell Debug Options Window Help
           J = 1 + L - 1
                                                                                           Python 3.4.3 (v3.4.3:9b73flc3e601, Feb 24 2015, 22:44:40) [MSC v.1600 64 bit (AM ...
           cost[i][j] = float("inf")
                                                                                           D64)] on win32
                                                                                           Type "copyright", "credits" or "license()" for more information.
           # Try all roots
                                                                                           for r in range(i, j+1):
               c = cost[i][r-1] + cost[r+1][j] + sum_freq(i, j)
                                                                                           For Keys = [10, 12, 16, 21] Freq = [4, 2, 6, 3]
               if c < cost[i][j]:
                   cost[i][j] = c
                                                                                           Cost Table:
                   root[i][j] = r
                                                                                           [4, 8, 20, 26]
                                                                                           [0, 2, 10, 16]
   # Print Cost Table
                                                                                           [0, 0, 6, 12]
   print("\nCost Table:")
                                                                                           [0, 0, 0, 3]
   for i in range(1, n+1):
       print(cost[i][1:n+1])
                                                                                           Root Table:
                                                                                           [1, 1, 3, 3]
   # Print Root Table
                                                                                           [0, 2, 3, 3]
   print("\nRoot Table:")
                                                                                           [0, 0, 3, 3]
   for i in range(1, n+1):
                                                                                           [0, 0, 0, 4]
       print(root[i][1:n+1])
                                                                                           Minimum Cost of OBST: 26
   print("\nMinimum Cost of OBST:", cost[1][n])
   return cost, root, cost[1][n]
                                                                                           Test Case (a):
                                                                                           Cost Table:
# ----- MAIN EXECUTION -----
                                                                                           [34, 118]
                                                                                           [0, 50]
# Problem input
keys = [10, 12, 16, 21]
                                                                                           Root Table:
freq = [4, 2, 6, 3]
                                                                                           [1, 2]
print ("For Keys =", keys, "Freq =", freq)
                                                                                           [0, 2]
cost, root, min_cost = optimal_bst(keys, freq)
                                                                                           Minimum Cost of OBST: 118
# Test case (a)
print("\nTest Case (a):")
                                                                                           Test Case (b):
keys = [10, 12]
freq = [34, 50]
                                                                                           Cost Table:
optimal_bst(keys, freq)
                                                                                           [34, 50, 142]
                                                                                           [0, 8, 66]
# Test case (b)
                                                                                           [0, 0, 50]
print("\nTest Case (b):")
keys = [10, 12, 20]
                                                                                                                                                                   Ln: 132 Col: 4
freq = [34, 8, 50]
optimal bst(keys, freq)
                                                                                                                                                                                 Ln: 67 Col: 0
```

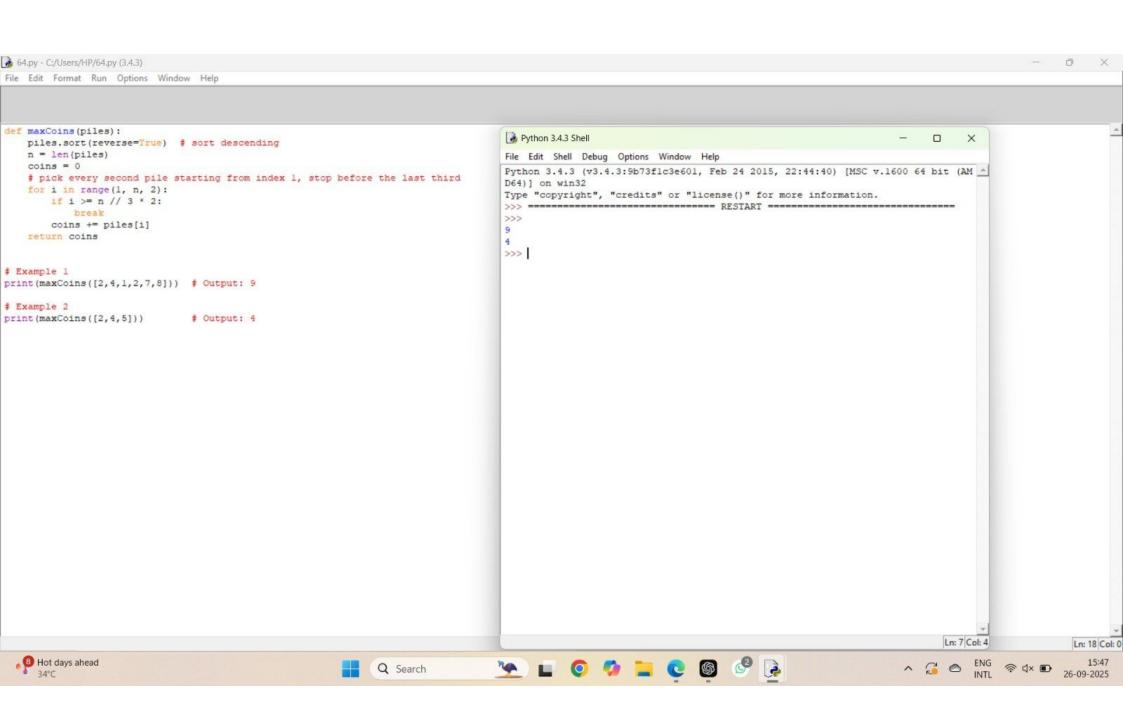
Q Search

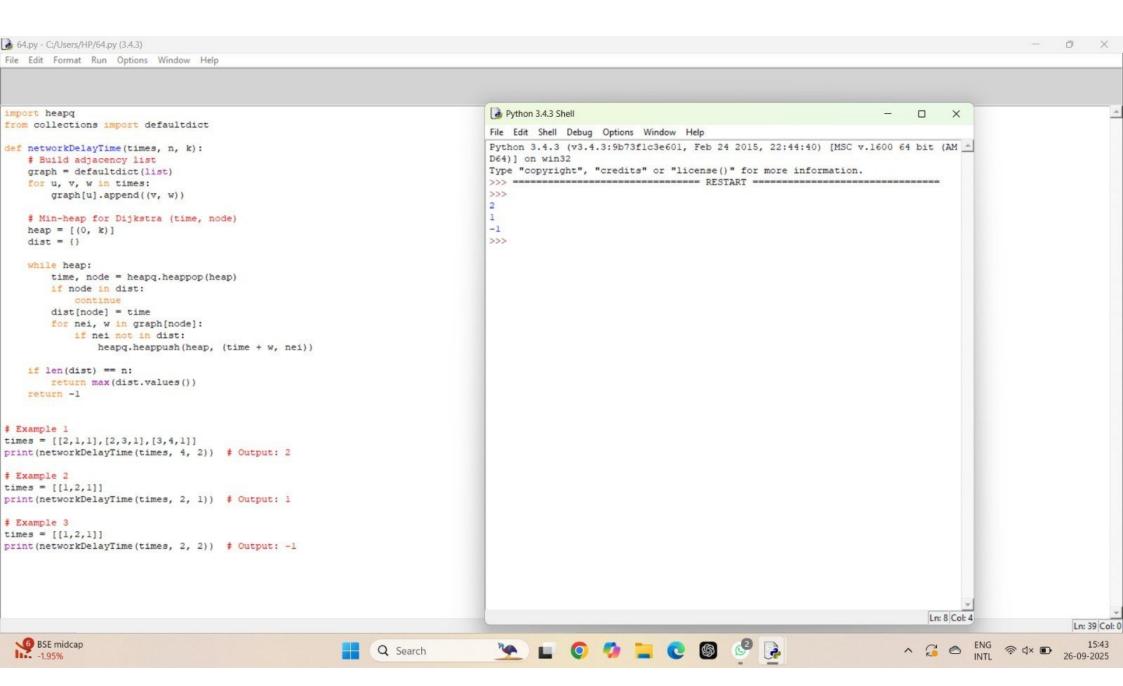
💁 🗀 🏮 🦪 📮 🙋 🚳 😟 🝃

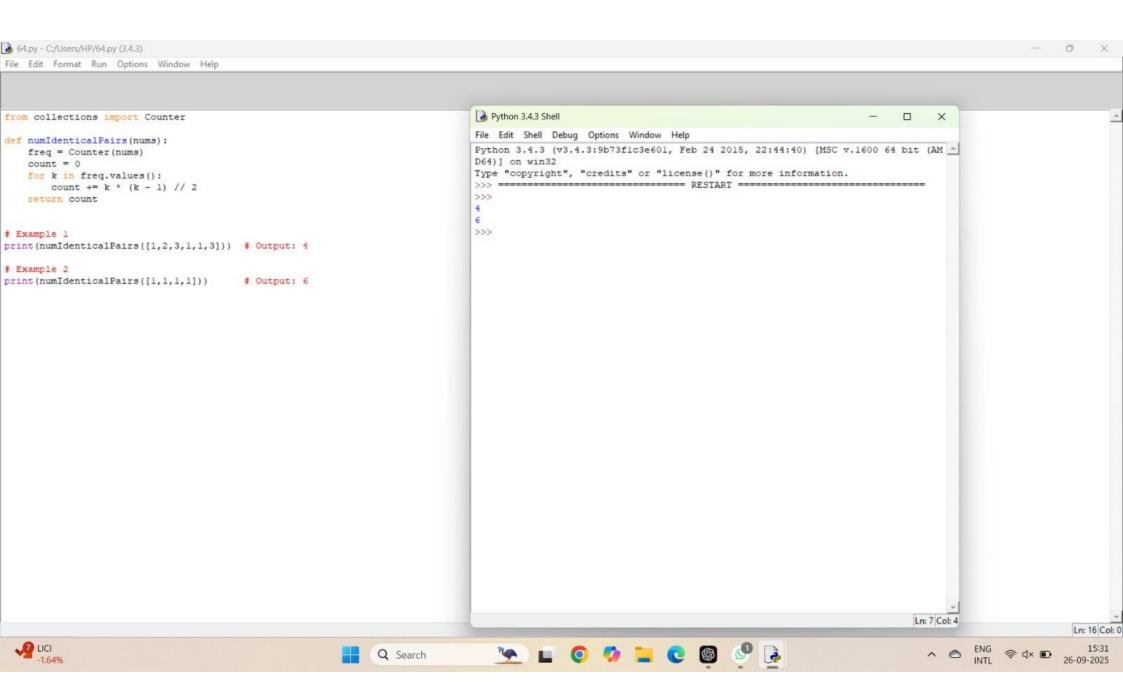
Light rain

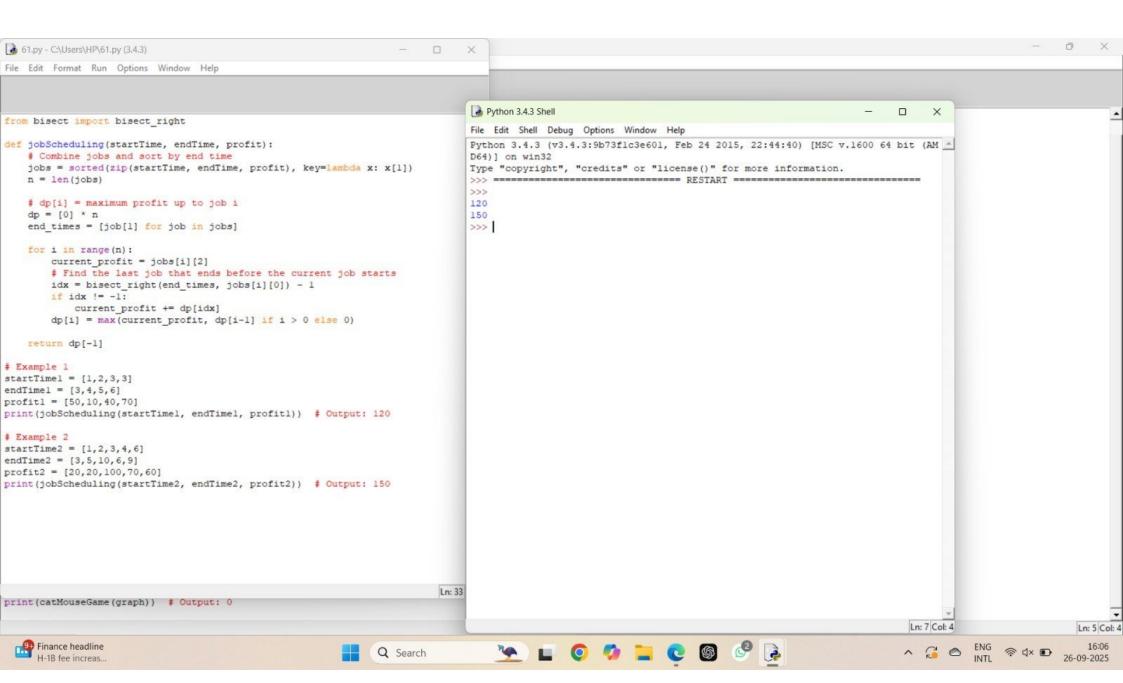
In the afternoon











```
33.py - C:/Users/HP/33.py (3.4.3)
File Edit Format Run Options Window Help
                                                                                           Python 3.4.3 Shell
                                                                                                                                                              X
def huffman codes (characters, frequencies):
                                                                                           File Edit Shell Debug Options Window Help
   neap = [Node(cnaracters[1], frequencies[1]) for 1 in range(ten(cnaracters))]
   heapq.heapify(heap)
                                                                                           Python 3.4.3 (v3.4.3:9b73f1c3e601, Feb 24 2015, 22:44:40) [MSC v.1600 64 bit (AM
                                                                                           D64)] on win32
   # Step 2: Build Huffman Tree
                                                                                           Type "copyright", "credits" or "license()" for more information.
   while len(heap) > 1:
                                                                                           left = heapq.heappop(heap)
       right = heapq.heappop(heap)
                                                                                           Test Case 1 Output: [('a', '00'), ('b', '01'), ('c', '10'), ('d', '11')]
                                                                                           Test Case 2 Output: [('a', '0'), ('b', 'lll'), ('c', 'l0l'), ('d', 'l00'), ('e',
       merged = Node (None, left.freq + right.freq)
                                                                                           '1101'), ('f', '1100')]
       merged.left = left
                                                                                           >>> ======
       merged.right = right
                                                                                           Test Case 1 Output: [('a', '00'), ('b', '01'), ('c', '10'), ('d', '11')]
       heapq.heappush(heap, merged)
                                                                                           Test Case 2 Output: [('a', '0'), ('b', '111'), ('c', '101'), ('d', '100'), ('e',
                                                                                           '1101'), ('f', '1100')]
   root = heap[0] # Final root of Huffman Tree
                                                                                          >>>
   # Step 3: Generate codes using DFS
   codes = {}
   def generate_codes(node, current_code):
       if node is None:
       if node.char is not None: # It's a leaf node
           codes[node.char] = current_code
       generate codes (node.left, current code + "0")
       generate_codes(node.right, current_code + "1")
   generate codes (root, "")
   return sorted(codes.items(), key=lambda x: x[0]) # Sort by character
# Test Case 1
chars1 = ['a', 'b', 'c', 'd']
freqs1 = [5, 9, 12, 13]
print("Test Case 1 Output:", huffman codes(charsl, freqsl))
# Expected: [('a', '110'), ('b', '10'), ('c', '0'), ('d', '111')]
# Test Case 2
chars2 = ['f', 'e', 'd', 'c', 'b', 'a']
freqs2 = [5, 9, 12, 13, 16, 45]
print("Test Case 2 Output:", huffman codes(chars2, freqs2))
                                                                                                                                                               Ln: 7 Col: 12
# Expected: [('a', '0'), ('b', '101'), ('c', '100'), ('d', '111'), ('e', '1101'), ('f', '1100')]
                                                                                                                                                                         Ln: 61 Col: 0
   32°C
                                                                            📲 🗖 🧿 🧖 📜 🕲 🚳 🔘 🍃
                                                                                                                                                  Q Search
```

Mostly sunny

```
64.py - C:/Users/HP/64.py (3.4.3)
                                                                                                                                                           0 X
File Edit Format Run Options Window Help
def uniquePaths(m, n):
   dp = [[1]*n for _ in range(m)] # first row & column = 1
   for i in range(1, m):
      for j in range(1, n):
          dp[i][j] = dp[i-1][j] + dp[i][j-1]
  return dp[m-1][n-1]
# Example 1
print(uniquePaths(3, 7)) # Output: 28
# Example 2
print(uniquePaths(3, 2)) # Output: 3
                                                                                                                                                            Ln: 9 Col: 0
 34°C
Mostly cloudy
                                                                             Q Search
```

