

```

def median_of_medians(arr, k):
    # Base case: small list → just sort and return
    if len(arr) <= 5:
        return sorted(arr)[k]

    # Step 1: split arr into chunks of 5 and find their medians
    chunks = [arr[i:i+5] for i in range(0, len(arr), 5)]
    medians = [sorted(chunk)[len(chunk)//2] for chunk in chunks]

    # Step 2: recursively find pivot (median of medians)
    pivot = median_of_medians(medians, len(medians)//2)

    # Step 3: partition into three parts
    low = [x for x in arr if x < pivot]
    high = [x for x in arr if x > pivot]
    equal = [x for x in arr if x == pivot]

    # Step 4: decide where k lies
    if k < len(low):
        return median_of_medians(low, k)
    elif k < len(low) + len(equal):
        return pivot
    else:
        return median_of_medians(high, k - len(low) - len(equal))

# Example usage
nums = [12, 3, 5, 7, 4, 19, 26]
k = 3 # 0-based → 4th smallest element
print(f"{k+1}-th smallest element is:", median_of_medians(nums, k))

```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit
AMD64] on win32

Enter "help" below or click "Help" above for more information.

>>>

===== RESTART: C:/Users/DELL/pui-41.py =====

4-th smallest element is: 7

>>>

===== RESTART: C:/Users/DELL/pui-41.py =====

4-th smallest element is: 7

>>>

```
def fullJustify(words, maxWidth):
    res, cur, num_of_letters = [], [], 0

    for w in words:
        # if adding this word exceeds the width, justify the current line
        if num_of_letters + len(w) + len(cur) > maxWidth:
            for i in range(maxWidth - num_of_letters):
                cur[i % (len(cur) - 1 or 1)] += " "
            res.append("".join(cur))
            cur, num_of_letters = [], 0
        cur.append(w)
        num_of_letters += len(w)

    # last line (left-justified)
    res.append(" ".join(cur).ljust(maxWidth))
    return res

----- Example Usage -----
ds1 = ["This", "is", "an", "example", "of", "text", "justification."]
Width1 = 16

ds2 = ["What", "must", "be", "acknowledgment", "shall", "be"]
Width2 = 16

print(fullJustify(words1, maxWidth1))
print(fullJustify(words2, maxWidth2))
```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information

>>>

===== RESTART: C:/Users/DELL/piu56.py =====

```
['This    is    an', 'example of text', 'justification. ']
['What    must    be', 'acknowledgment ', 'shall be    ']
```

>>>

```
F = float('inf')
```

```
def floyd_warshall(n, dist):
    """Floyd-Warshall Algorithm"""
    for k in range(n):
        for i in range(n):
            for j in range(n):
                if dist[i][k] + dist[k][j] < dist[i][j]:
                    dist[i][j] = dist[i][k] + dist[k][j]
    return dist
```

```
def print_matrix(dist):
    for row in dist:
        print(row)
```

```
----- Main -----
print("=== Floyd's Algorithm for Routers ===")
```

```
n = 6 # Routers A-F
```

```
# Initial distance matrix
INF = float('inf')
dist = [[INF]*n for _ in range(n)]
for i in range(n):
    dist[i][i] = 0
```

```
# Given edges
edges = [
    (0, 1, 1), # A -> B
    (0, 2, 5), # A -> C
    (1, 2, 2), # B -> C
    (1, 3, 1), # B -> D
    (2, 4, 3), # C -> E
    (3, 4, 1), # D -> E
    (3, 5, 6), # D -> F
    (4, 5, 2), # E -> F
]
```

```
# Fill adjacency matrix
for u, v, w in edges:
```

```
=== Floyd's Algorithm for Routers ===
```

```
Initial Distance Matrix:
```

```
[0, 1, 5, inf, inf, inf]
[1, 0, 2, 1, inf, inf]
[5, 2, 0, inf, 3, inf]
[inf, 1, inf, 0, 1, 6]
[inf, inf, 3, 1, 0, 2]
[inf, inf, inf, 6, 2, 0]
```

```
Distance Matrix After Floyd-Warshall:
```

```
[0, 1, 3, 2, 3, 5]
[1, 0, 2, 1, 2, 4]
[3, 2, 0, 3, 3, 5]
[2, 1, 3, 0, 1, 3]
[3, 2, 3, 1, 0, 2]
[5, 4, 5, 3, 2, 0]
```

```
Shortest Path Router A to Router F (before failure): 5
```

```
=== Simulating Link Failure: Router B-D removed ===
```

```
Distance Matrix After Link Failure (before Floyd-Warshall):
```

```
[0, 1, 5, inf, inf, inf]
[1, 0, 2, inf, inf, inf]
[5, 2, 0, inf, 3, inf]
[inf, inf, inf, 0, 1, 6]
[inf, inf, 3, 1, 0, 2]
[inf, inf, inf, 6, 2, 0]
```

```
Distance Matrix After Floyd-Warshall (with B-D failure):
```

```
[0, 1, 3, 7, 6, 8]
[1, 0, 2, 6, 5, 7]
[3, 2, 0, 4, 3, 5]
[7, 6, 4, 0, 1, 3]
[6, 5, 3, 1, 0, 2]
[8, 7, 5, 3, 2, 0]
```

```
Shortest Path Router A to Router F (after failure): 8
```

>>>


```
= float('inf')
```

```
floyd_warshall_with_path(n, edges, src, dest):
# Step 1: Initialize distance and next matrices
dist = [[INF] * n for _ in range(n)]
next_hop = [[-1] * n for _ in range(n)]
```

```
for i in range(n):
    dist[i][i] = 0
    next_hop[i][i] = i
```

```
for u, v, w in edges:
    dist[u][v] = w
    next_hop[u][v] = v
```

```
print("Initial Distance Matrix:")
for row in dist:
    print(row)
```

```
# Step 2: Floyd-Warshall
for k in range(n):
    for i in range(n):
        for j in range(n):
            if dist[i][k] + dist[k][j] < dist[i][j]:
                dist[i][j] = dist[i][k] + dist[k][j]
                next_hop[i][j] = next_hop[i][k]
```

```
print("\nDistance Matrix After Floyd-Warshall:")
for row in dist:
    print(row)
```

```
# Step 3: Reconstruct path from src to dest
if next_hop[src][dest] == -1:
    return None, dist[src][dest]
```

```
path = [src]
while src != dest:
    src = next_hop[src][dest]
    path.append(src)
```

```
return path, dist[path[0]][path[-1]]
```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

>>>

```
===== RESTART: C:/Users/DELL/piu59.py =====
```

```
==== Test Case (a): 4 Cities ====
```

```
Initial Distance Matrix:
```

```
[0, 3, 8, -4]
[inf, 0, 4, 1]
[2, inf, 0, inf]
[inf, 6, -5, 0]
```

```
Distance Matrix After Floyd-Warshall:
```

```
[-7, -4, -9, -11]
[-2, 0, -4, -6]
[-5, -2, -7, -9]
[-10, -7, -12, -14]
```

```
Shortest Path City 1 to City 3: [0, 3, 2], Distance = -9
```

```
==== Test Case (b): 6 Routers ====
```

```
Initial Distance Matrix:
```

```
[0, 1, 5, inf, inf, inf]
[inf, 0, 2, 1, inf, inf]
[inf, inf, 0, inf, 3, inf]
[inf, inf, inf, 0, 1, 6]
[inf, inf, inf, inf, 0, 2]
[inf, inf, inf, inf, inf, 0]
```

```
Distance Matrix After Floyd-Warshall:
```

```
[0, 1, 3, 2, 3, 5]
[inf, 0, 2, 1, 2, 4]
[inf, inf, 0, inf, 3, 5]
[inf, inf, inf, 0, 1, 3]
[inf, inf, inf, inf, 0, 2]
[inf, inf, inf, inf, inf, 0]
```

```
Shortest Path Router A to Router F: [0, 1, 3, 4, 5], Distance = 5
```

>>>

```
= float("inf")
```

```
floyd_warshall(n, edges):
```

```
# Step 1: Initialize distance matrix
```

```
dist = [[INF] * n for _ in range(n)]
```

```
next_node = [[-1] * n for _ in range(n)] # for path reconstruction
```

```
for i in range(n):
```

```
    dist[i][i] = 0
```

```
# fill initial edges
```

```
for u, v, w in edges:
```

```
    dist[u][v] = w
```

```
    next_node[u][v] = v
```

```
print("Initial Distance Matrix:")
```

```
for row in dist:
```

```
    print(row)
```

```
# Step 2: Floyd-Warshall update
```

```
for k in range(n):
```

```
    for i in range(n):
```

```
        for j in range(n):
```

```
            if dist[i][k] + dist[k][j] < dist[i][j]:
```

```
                dist[i][j] = dist[i][k] + dist[k][j]
```

```
                next_node[i][j] = next_node[i][k]
```

```
print("\nFinal Distance Matrix (after Floyd-Warshall):")
```

```
for row in dist:
```

```
    print(row)
```

```
return dist, next_node
```

```
Function to reconstruct path
```

```
def get_path(u, v, next_node):
```

```
    if next_node[u][v] == -1:
```

```
        return []
```

```
    path = [u]
```

```
    while u != v:
```

```
        u = next_node[u][v]
```

```
        path.append(u)
```

```
    return path
```

File Edit Shell Debug Options Window Help

```
Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11)
[MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.
```

>>>

```
===== RESTART: C:/Users/DELL/piu58.py =
```

```
Initial Distance Matrix:
```

```
[0, 3, inf, inf]
```

```
[inf, 0, 1, 4]
```

```
[inf, inf, 0, 1]
```

```
[inf, inf, inf, 0]
```

```
Final Distance Matrix (after Floyd-Warshall):
```

```
[0, 3, 4, 5]
```

```
[inf, 0, 1, 2]
```

```
[inf, inf, 0, 1]
```

```
[inf, inf, inf, 0]
```

```
Shortest path from City 0 to City 3:
```

```
[0, 1, 2, 3]
```

```
Distance: 5
```

```
=== Test Case 2 ===
```

```
Initial Distance Matrix:
```

```
[0, 3, 8, -4]
```

```
[inf, 0, 4, 1]
```

```
[2, inf, 0, inf]
```

```
[inf, 6, -5, 0]
```

```
Final Distance Matrix (after Floyd-Warshall):
```

```
[-7, -4, -9, -11]
```

```
[-2, 0, -4, -6]
```

```
[-5, -2, -7, -9]
```

```
[-10, -7, -12, -14]
```

```
Shortest path from City 0 to City 2:
```

```
[0, 3, 2]
```

```
Distance: -9
```

>>>


```

class WordFilter:
    def __init__(self, words):
        self.lookup = {}
        for i, word in enumerate(words):
            # generate all prefix + suffix combinations
            for p in range(len(word) + 1):
                for s in range(len(word) + 1):
                    key = (word[:p], word[len(word) - s:])
                    self.lookup[key] = i # store largest index (overwrite old one)

    def f(self, pref, suff):
        return self.lookup.get((pref, suff), -1)

```

```

----- Example Usage -----
dFilter = WordFilter(["apple"])
print(wordFilter.f("a", "e")) # Output: 0
print(wordFilter.f("ap", "le")) # Output: 0
print(wordFilter.f("b", "e")) # Output: -1

```

Python 3.13.7 (tags/v3.13.7:bcee1c3, Aug 14 2025, 14:15 :11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

>>>

===== RESTART: C:/Users/DELL/piu57.p

```

y
0
0
-1

```

>>>

```

word_break_with_segmentation(s, wordDict):
word_set = set(wordDict)
n = len(s)

# dp[i] stores list of words that end at position i (for backtracking)
dp = [[] for _ in range(n + 1)]
dp[0] = [""] # base case: empty string

for i in range(1, n + 1):
    for j in range(i):
        word = s[j:i]
        if dp[j] and word in word_set:
            for prev in dp[j]:
                if prev:
                    dp[i].append(prev + " " + word)
                else:
                    dp[i].append(word)

# If we have any segmentation ending at n, return Yes and examples
if dp[n]:
    print("Yes")
    print("Possible segmentations:")
    for seg in dp[n]:
        print(seg)
else:
    print("No")

----- Example Usage -----
wordDict = {"i", "like", "sam", "sung", "samsung", "mobile",
            "ice", "cream", "icecream", "man", "go", "mango"}

s1 = "ilike"
s2 = "ilikesamsung"

print(f"Input: {s1}")
word_break_with_segmentation(s1, wordDict)
print("\nInput:", s2)
word_break_with_segmentation(s2, wordDict)

```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64-bit AMD64] on win32
Enter "help" below or click "Help" above for more information.

>>>

===== RESTART: C:/Users/DELL/Pictures/screenshots/pyi-55.py =====

Input: ilike

Yes

Possible segmentations:

i like

Input: ilikesamsung

Yes

Possible segmentations:

i like samsung

i like sam sung

>>>

```

word_break(s: str, wordDict: list) -> bool:
word_set = set(wordDict) # for O(1) lookups
n = len(s)

# dp[i] = True if s[0:i] can be segmented into words in wordDict
dp = [False] * (n + 1)
dp[0] = True # empty string can be segmented

for i in range(1, n + 1):
    for j in range(i):
        if dp[j] and s[j:i] in word_set:
            dp[i] = True
            break # no need to check further

return dp[n]

----- Example Usage -----
s1 = "leetcode"
wordDict1 = ["leet", "code"]

s2 = "applepenapple"
wordDict2 = ["apple", "pen"]

s3 = "catsanddog"
wordDict3 = ["cats", "dog", "sand", "and", "cat"]

print(word_break(s1, wordDict1)) # True
print(word_break(s2, wordDict2)) # True
print(word_break(s3, wordDict3)) # False

```

```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit
AMD64] on win32
Enter "help" below or click "Help" above for more information.

>>>
===== RESTART: C:/Users/DELL/pyi-54.py =====
True
True
False
>>>

```



```
length_of_longest_substring(s: str) -> int:
char_index = {} # stores last index of each character
max_len = 0
left = 0 # left pointer of sliding window

for right, char in enumerate(s):
    if char in char_index and char_index[char] >= left:
        # Move left pointer past the last occurrence
        left = char_index[char] + 1
    char_index[char] = right
    max_len = max(max_len, right - left + 1)

return max_len

----- Example Usage -----
s1 = "abcabcbb"
s2 = "bbbbb"
s3 = "pwwkew"

print(f"Input: {s1} -> Output: {length_of_longest_substring(s1)}")
print(f"Input: {s2} -> Output: {length_of_longest_substring(s2)}")
print(f"Input: {s3} -> Output: {length_of_longest_substring(s3)}")
```

IDLE Shell 3.13.7

File Edit Shell Debug Options Window Help

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

>>> ===== RESTART: C:/Users/DELL/pyi-53.py =====
Input: abcabcbb -> Output: 3
Input: bbbbbb -> Output: 1
Input: pwwkew -> Output: 3
>>> |

```

File Edit Shell Debug Options Window Help
longest_palindrome(s: str) -> str:
if not s or len(s) == 0:
    return ""

start, end = 0, 0

def expand(left, right):
    # Expand while characters match
    while left >= 0 and right < len(s) and s[left] == s[right]:
        left -= 1
        right += 1
    return left + 1, right - 1

for i in range(len(s)):
    # Odd length palindrome
    l1, r1 = expand(i, i)
    # Even length palindrome
    l2, r2 = expand(i, i + 1)

    if r1 - l1 > end - start:
        start, end = l1, r1
    if r2 - l2 > end - start:
        start, end = l2, r2

return s[start:end+1]

----- Example Usage -----
s1 = "babad"
s2 = "cbbsd"

int("Input:", s1, "-> Longest palindrome:", longest_palindrome(s1))
int("Input:", s2, "-> Longest palindrome:", longest_palindrome(s2))

```

IDLE Shell 3.13.7

File Edit Shell Debug Options Window Help

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

```

>>>
===== RESTART: C:/Users/DELL/p
yi-52.py =====
Input: babad -> Longest palindrome: bab
Input: cbbsd -> Longest palindrome: bb
>>>

```

Ln: 7 Col: 0

from itertools

cities

cities = ['A', 'B', 'C', 'D', 'E']

Symmetric distance matrix

Order: A, B, C, D, E

```
dist = [
    [0, 10, 15, 20, 25], # A
    [10, 0, 35, 25, 30], # B
    [15, 35, 0, 30, 20], # C
    [20, 25, 30, 0, 15], # D
    [25, 30, 20, 15, 0]  # E
]
```

n = len(cities)

min_distance = float('inf')

best_route = []

Generate all permutations of cities excluding starting city A (index 0)

for perm in itertools.permutations(range(1, n)):

route = [0] + list(perm) + [0] # Start and end at A

total_dist = sum(dist[route[i]][route[i+1]] for i in range(n))

if total_dist < min_distance:

min_distance = total_dist

best_route = route

Print result

best_route_names = [cities[i] for i in best_route]

print("Shortest route:", " -> ".join(best_route_names))

print("Total distance:", min_distance)

File Edit Shell Debug Options Window Help

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit
AMD64] on win32

Enter "help" below or click "Help" above for more information.

>>>

===== RESTART: C:/Users/DELL/pyi-51.py =====

Shortest route: A -> B -> D -> E -> C -> A

Total distance: 85

>>>

t sys

function to find minimum of two numbers

```

min_val(a, b):
    return a if a < b else b

```

Recursive TSP function

```

tsp(dist, visited, pos, n):
    # Base case: all cities visited, return to starting city
    if visited == (1 << n) - 1:
        return dist[pos][0]

```

ans = sys.maxsize

```

for city in range(n):
    if (visited & (1 << city)) == 0: # if city not visited
        new_ans = dist[pos][city] + tsp(dist, visited | (1 << city),
        ans = min_val(ans, new_ans)

```

return ans

----- Test Cases -----

4 # Number of cities

Test Case 1

```

t1 = [
    [0, 10, 15, 20],
    [10, 0, 35, 25],
    [15, 35, 0, 30],
    [20, 25, 30, 0]

```

Test Case 2

```

t2 = [
    [0, 10, 10, 10],
    [10, 0, 10, 10],
    [10, 10, 0, 10],
    [10, 10, 10, 0]

```

Test Case 3

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit AMD64] on win32

Enter "help" below or click "Help" above for more information.

>>>

===== RESTART: C:/Users/DELL/pyi-50.py =====

Test Case 1: Minimum path distance = 80

Test Case 2: Minimum path distance = 40

Test Case 3: Minimum path distance = 14

>>>

```

min_time_three_lines(station_times, transfer, entry=None, exit=None)
"""
station_times: list of lists, station_times[line][station]
transfer: matrix transfer[i][j] cost to move from line i to line j
entry: list of entry times for each line (optional, default 0)
exit: list of exit times for each line (optional, default 0)
Returns: (min_time, path_lines) where path_lines is list of chosen lines
"""
m = len(station_times) # number of lines
n = len(station_times[0]) # number of stations (assumes all lines have same number of stations)
if entry is None:
    entry = [0]*m
if exit is None:
    exit = [0]*m

# dp[l][s] = minimum time to complete station s on line l
dp = [[float('inf')]*n for _ in range(m)]
parent = [[None]*n for _ in range(m)] # to reconstruct path

# Base case: first station
for l in range(m):
    dp[l][0] = entry[l] + station_times[l][0]
    parent[l][0] = -1 # start

# Fill DP table
for s in range(1, n):
    for l in range(m):
        best_prev = None
        best_val = float('inf')
        for p in range(m):
            cand = dp[p][s-1] + transfer[p][l] + station_times[l][s]
            if cand < best_val:
                best_val = cand
                best_prev = p
        dp[l][s] = best_val
        parent[l][s] = best_prev

# Add exit times and find best final line
best_final = None
best_total = float('inf')
for l in range(m):
    total = dp[l][n-1] + exit[l]

```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

>>>

===== RESTART: C:/Users/DELL/pyi-49.py =====

Minimum total production time: 17
Chosen line for each station (0-based indices): [0, 0, 0]
Chosen line names (1-based): [1, 1, 1]

>>>

```
assembly_line(a1, a2, t1, t2, e1, e2, x1, x2):
    n = len(a1)
```

```
# DP arrays
```

```
f1 = [0] * n
f2 = [0] * n
```

```
# Base case
```

```
f1[0] = e1 + a1[0]
f2[0] = e2 + a2[0]
```

```
# Fill DP
```

```
for i in range(1, n):
    f1[i] = min(f1[i-1] + a1[i], f2[i-1] + t2[i-1] + a1[i])
    f2[i] = min(f2[i-1] + a2[i], f1[i-1] + t1[i-1] + a2[i])
```

```
# Final answer
```

```
return min(f1[n-1] + x1, f2[n-1] + x2)
```

```
Example Test Case
```

```
n = 4
a1 = [4, 5, 3, 2]
a2 = [2, 10, 1, 4]
t1 = [7, 4, 5] # transfer from line1 -> line2
t2 = [9, 2, 8] # transfer from line2 -> line1
e1 = 10, 12 # entry times
e2 = 18, 7 # exit times
```

```
int("Minimum time required:", assembly_line(a1, a2, t1, t2, e1, e2, x1, x2))
```

```
Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.194
AMD64] on win32
```

```
Enter "help" below or click "Help" above for more information.
```

```
>>>
```

```
===== RESTART: C:/Users/DELL/pyi-48.py =====
```

```
Minimum time required: 35
```

```
>>>
```



```
File Edit Format Run Options Window Help
dice_throw(num_sides, num_dice, target):
# DP table: (num_dice+1) * (target+1)
dp = [[0] * (target + 1) for _ in range(num_dice + 1)]

# Base case
dp[0][0] = 1

# Fill DP table
for d in range(1, num_dice + 1):
    for t in range(1, target + 1):
        for face in range(1, num_sides + 1):
            if t - face >= 0:
                dp[d][t] += dp[d - 1][t - face]

return dp[num_dice][target]

Test Case 1
int("Test Case 1:")
ys1 = dice_throw(6, 2, 7)
int("Number of ways to reach sum 7:", ways1)

Test Case 2
int("\nTest Case 2:")
ys2 = dice_throw(4, 3, 10)
int("Number of ways to reach sum 10:", ways2)
```

```
IDLE Shell 3.13.7
File Edit Shell Debug Options Window Help
Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

>>> ===== RESTART: C:/Users/DELL/pyi-47.py =====
Test Case 1:
Number of ways to reach sum 7: 6

Test Case 2:
Number of ways to reach sum 10: 6
>>> |
```

```

File Edit Shell Debug Options Window Help
karatsuba(x, y):
# Base case for small numbers
if x < 10 or y < 10:
    return x * y

# Calculate size of numbers
n = max(len(str(x)), len(str(y)))
m = n // 2 # Split position

# Split x and y
high1, low1 = divmod(x, 10**m)
high2, low2 = divmod(y, 10**m)

# 3 recursive multiplications
z0 = karatsuba(low1, low2)
z2 = karatsuba(high1, high2)
z1 = karatsuba(low1 + high1, low2 + high2) - z2 - z0

# Combine results
return (z2 * 10**(2*m)) + (z1 * 10**m) + z0

# Test Case 1
x = 1234, y = 5678
z = karatsuba(x, y)
print(f"{x} * {y} = {z}")

```

IDLE Shell 3.13.7

File Edit Shell Debug Options Window Help

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

```

>>>
===== RESTART: C:/Users/DELL/pyi-46.py =====
1234 * 5678 = 7006652
>>>

```

```

Edit Format Run Options Window Help
strassen_2x2(A, B):
# Extract elements
a, b, c, d = A[0][0], A[0][1], A[1][0], A[1][1]
e, f, g, h = B[0][0], B[0][1], B[1][0], B[1][1]

# Strassen's formulas
M1 = (a + d) * (e + h)
M2 = (c + d) * e
M3 = a * (f - h)
M4 = d * (g - e)
M5 = (a + b) * h
M6 = (c - a) * (e + f)
M7 = (b - d) * (g + h)

# Compute result matrix
C11 = M1 + M4 - M5 + M7
C12 = M3 + M5
C21 = M2 + M4
C22 = M1 - M2 + M3 + M6

return [[C11, C12],
        [C21, C22]]

Test Case 1
A = [[1, 7],
      [3, 5]]
B = [[6, 8],
      [4, 2]]

C = strassen_2x2(A, B)
print("Result Matrix C =")
for row in C:
    print(row)

```

IDLE Shell 3.13.7

File Edit Shell Debug Options Window Help

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

```

>>>
===== RESTART: C:/Users/DELL/pyi-45.py =====
Result Matrix C =
[34, 22]
[38, 34]
>>>

```

Ln: 8, Col: 0


```

def meet_in_middle_exact(nums, target):
    n = len(nums)
    left, right = nums[:n//2], nums[n//2:]

```

Function to generate all subset sums

```

def subset_sums(arr):
    sums = []
    def backtrack(i, current):
        if i == len(arr):
            sums.append(current)
            return
        backtrack(i+1, current) # exclude
        backtrack(i+1, current + arr[i]) # include
    backtrack(0, 0)
    return sums

```

```

left_sums = subset_sums(left)
right_sums = subset_sums(right)
right_sums_set = set(right_sums) # for fast lookup

```

```

# Check if any pair forms the exact target
for s in left_sums:
    if target - s in right_sums_set:
        return True
return False

```

Example a)

```
arr1 = [1, 3, 9, 2, 7, 12]
```

```
target1 = 15
```

```
print("Subset with exact sum exists (Example a):", meet_in_middle_exact(arr1, target1))
```

Example b)

```
arr2 = [3, 34, 4, 12, 5, 2]
```

```
target2 = 15
```

```
print("Subset with exact sum exists (Example b):", meet_in_middle_exact(arr2, target2))
```

```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1
944 64 bit (AMD64)] on win32
Enter "help" below or click "Help" above for more information.

```

```
>>>
```

```
===== RESTART: C:/Users/DELL/pyi-44.py =====
```

```
Subset with exact sum exists (Example a): True
```

```
Subset with exact sum exists (Example b): True
```

```
>>>
```

```

median_of_medians(arr, k):
# Base case: if array small, just sort and return k-th
if len(arr) <= 5:
    return sorted(arr)[k-1] # k-1 because of 1-based indexing

# Step 1: split arr into chunks of 5
chunks = [arr[i:i+5] for i in range(0, len(arr), 5)]

# Step 2: find medians of each chunk
medians = [sorted(chunk)[len(chunk)//2] for chunk in chunks]

# Step 3: recursively find pivot (median of medians)
pivot = median_of_medians(medians, (len(medians)+1)//2)

# Step 4: partition array around pivot
low = [x for x in arr if x < pivot]
equal = [x for x in arr if x == pivot]
high = [x for x in arr if x > pivot]

# Step 5: choose where k falls
if k <= len(low):
    return median_of_medians(low, k)
elif k <= len(low) + len(equal):
    return pivot
else:
    return median_of_medians(high, k - len(low) - len(equal))

Example runs
r1 = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
k1 = 6
print(f"{k1}-th smallest element in arr1:", median_of_medians(arr1, k1))

r2 = [23, 17, 31, 44, 55, 21, 20, 18, 19, 27]
k2 = 5
print(f"{k2}-th smallest element in arr2:", median_of_medians(arr2, k2))

```

Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit AMD64] on win32
Enter "help" below or click "Help" above for more information.

>>>

===== RESTART: C:/Users/DELL/pui-42.py =====

6-th smallest element in arr1: 6

5-th smallest element in arr2: 21

>>>

```
port bisect
```

```
def meet_in_middle(nums, target):
    # Step 1: split into two halves
    n = len(nums)
    left, right = nums[:n//2], nums[n//2:]

    # Step 2: generate all subset sums
    def subset_sums(arr):
        sums = []
        def backtrack(i, current):
            if i == len(arr):
                sums.append(current)
                return
            backtrack(i+1, current) # exclude
            backtrack(i+1, current + arr[i]) # include
        backtrack(0, 0)
        return sums

    left_sums = subset_sums(left)
    right_sums = subset_sums(right)

    # Step 3: sort right sums
    right_sums.sort()

    # Step 4: find best sum close to target
    best_sum = None
    min_diff = float("inf")

    for s in left_sums:
        remaining = target - s
        # find closest in right_sums to 'remaining'
        pos = bisect.bisect_left(right_sums, remaining)

        # check candidate at pos
        if pos < len(right_sums):
            total = s + right_sums[pos]
            if abs(target - total) < min_diff:
                min_diff = abs(target - total)
                best_sum = total

    # check candidate before pos
```

File Edit Shell Debug Options Window Help

```
Python 3.13.7 (tags/v3.13.7:bceelc3, Aug 14 2025, 14:15:11) [MSC v.1944 64 bit (
AMD64)] on win32
Enter "help" below or click "Help" above for more information.

>>>
===== RESTART: C:/Users/DELL/pyi-43.py =====
Closest sum to 42 : 41
Closest sum to 10 : 10
>>>
```