



Matrix Calculus





Matrix Calculus

- colSums(), rowSums()
- Standard arithmetic possible
- Element-wise computation





lotr_matrix

```
> the_fellowship <- c(316, 556)</pre>
> two_towers <- c(343, 584)</pre>
> return_king <- c(378, 742)
> lotr_matrix <- rbind(the_fellowship, two_towers, return_king)</pre>
> colnames(lotr_matrix) <- c("US", "non-US")</pre>
> rownames(lotr_matrix) <- c("Fellowship", "Two Towers",
                               "Return King")
> lotr_matrix
              US non-US
Fellowship 316
                  556
Two Towers 343
Return King 378
                    742
```





Matrix - Scalar Calculus

```
> lotr_matrix / 1.12
                 US
                      non-US
Fellowship 282.1429 496.4286
Two Towers 306.2500 521.4286
Return King 337.5000 662.5000
> lotr_matrix - 50
            US non-US
Fellowship 266
                  506
Two Towers 293 534
Return King 328
                 692
```

```
> lotr_matrix
US non-US
Fellowship 316 556
Two Towers 343 584
Return King 378 742
```





Matrix - Matrix Calculus

```
> # Definition of theater_cut omitted
> theater_cut
    [,1] [,2]
[1,] 50 50
[2,] 80 80
[3,]
     100
          100
> lotr_matrix - theater_cut
            US non-US
Fellowship 266
                  506
Two Towers 263
                504
Return King 278
                642
```

```
> lotr_matrix
US non-US
Fellowship 316 556
Two Towers 343 584
Return King 378 742
```





Matrix Calculus

```
> lotr_matrix - c(50, 80, 100)
            US non-US
Fellowship 266 506
Two Towers 263 504
Return King 278 642
> matrix(c(50, 80, 100), nrow = 3, ncol = 2)
    [,1] [,2]
[1,] 50 50
[2,] 80 80
[3,]
     100
          100
```

```
> lotr_matrix
US non-US
Fellowship 316 556
Two Towers 343 584
Return King 378 742
```





Matrix Multiplication

```
> # Definition of rates omitted
> rates
     [,1] [,2]
[1,] 1.11 1.11
[2,] 0.99 0.99
[3,] 0.82 0.82
> lotr_matrix * rates
                US non-US
Fellowship 350.76 617.16
Two Towers 339.57 578.16
Return King 309.96 608.44
```

```
> lotr_matrix
US non-US
Fellowship 316 556
Two Towers 343 584
Return King 378 742
```





Matrices and Vectors

- Very similar
- Vector = 1D, matrix = 2D
- Coercion if necessary
- Recycling if necessary
- Element-wise calculus





Let's practice!