

Exploring graphs

- Have seen examples of finding paths through graphs that represent physical networks
- Can also use graph search to explore changes to state of a physical system
 - Nodes represent states of system
 - Edges represent actions that cause a change of state
 - Want to find sequence of actions to convert system to desired state

Solving the 8-puzzle

1	2	5
6	3	8
	4	7

	1	2
3	4	5
6	7	8

- Slide any tile into blank space
- Find sequence of slides to reach goal

An example solution

1	2	5
6	3	8
	4	7

An example solution

1	2	5
	3	8
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An example solution

1	2	5
3		8
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An example solution

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An example solution

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An example solution

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An example solution

	1	2
3	4	5
6	7	8

How could we solve this?

- Each node in graph is a state of the puzzle
 - Specific layout of tiles in puzzle
- Each edge of the graph specifies which tile to slide to get to a new state of the puzzle
- Solution space is very large:
 - $9!$ or 362880 nodes
 - Each node has 2, 3, or 4 edges
 - Graph has almost 1 million edges
- Is there another way?