

Figure 1: The superexponentials to base  $b = \exp(1/)$  versus real argument by equations `e1e1` and `e1e3`; the horizontal line shows the asymptotic  $y = 0$ .

In this section, the holomorphic solutions  $F$  of equation  $F(z+1) = \exp\left(\frac{F(z)}{b}\right)$  are reconsidered.

At the traditional approach, the iterative procedure for the approximation of the solution converges slowly if at all.

TODO: Henryk, please, copy-paste here your explanation why the traditional approach fails.

DODO: Dmitrii plans to type there the description of figures.

As usually, we specify the superexponential, indicating the value at zero as subscript. We consider the two superexponentials,  $F = F_1$  and  $F = F_3$  such that  $F_1(0) = 1$ ,

$d_3(0) = 3$ ; as in the case of  $b=2$ , we choose the smallest integer among

The algorithm of evaluation described below does not

imply that the argument of the superexponential is real; so, in figure 2, functions  $F_1$  and  $F_3$  and their inverse functions  $G_1 = F_1^{-1}$  and  $G_3 = F_3^{-1}$  are shown in the complex plane.

$1\Im(z)$

18

16

14

12


10

1-2

1-4

1-6

1-8

  
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