

OLABISI ONABANJO UNIVERSITY, AGO-IWOYE
FACULTY OF SOCIAL AND MANAGEMENT SCIENCES
2015/2016 HARMATTAN SEMESTER EXAMINATION

Course Code / Title: ECO 301/Intermediate Microeconomics

Instruction: Attempt any four questions

Time Allowed: 2 Hours

1. (a) With the aid of well-labeled graphs and brief explanations, illustrate the substitution and income effects of a fall in price for: (i) normal good (ii) inferior good (iii) Giffen good (12 marks)

(b) Given a consumer's utility function $U = q_1 q_2$ and a budget constraint equation: $Y = p_1 q_1 + p_2 q_2$ where p_1 is the price of good q_1 and p_2 is the price of good q_2 , derive the consumer's Hicksian demand functions for goods q_1 and q_2 . (5.5 marks)

2. (a) Given the utility function $U = f(X_1, X_2) = 5 \log X_1 + 3 \log X_2$ and $M = P_1 X_1 + P_2 X_2$, where money income of the consumer is N100, price of commodity X_1 is N10 and price of commodity X_2 is N2, determine:

(i) The quantities of X_1 and X_2 that maximise his utility. (7 marks)

(ii) What is the marginal utility of last naira spent by the consumer? (2.5 marks)

(iii) Show that the consumer actually maximized his utility. (4 marks)

(b) With the aid of mathematical expression, illustrate the principle of equi-marginal utility (4 marks)

3(a) Given $q = AL^\alpha K^{1-\alpha}$ where L and K are variable inputs, show that total output would be exhausted if each input is paid its marginal physical product (5 marks)

(b) Show that elasticity of substitution equals one. (7.5 marks)

(c) With the aid of graphs and concise explanation highlight the relationship between long-run average cost and economies/diseconomies of scale. (5 marks)

4(a) Find the critical values for minimizing the costs of a firm producing two goods x and y when the total cost function is: $C = 5x^2 + 2xy + 3y^2 + 800$ subject to the production quota, $x + y = 39$ (6 marks)

(b) Given the inverse demand function of a multi-plant monopolist as $P = 50 - 0.25q$, where $q = q_1 + q_2$ and the cost facing the two plants as $C_1 = 5q_1$ and $C_2 = 0.125q_2^2$, determine:

(i) Equilibrium quantities to be produced in the two plants (5 marks)

(ii) Total profit of the monopolist (3.5 marks)

(c) Explain any **three** factors that could make monopoly power to arise

(3 marks)

5(a) A discriminating monopolist's cost function is expressed as $C = 50 + 20q$ while his demand functions in two sub-markets are $P_1 = 80 - 5q_1$ and $P_2 = 180 - 20q_2$ respectively, determine:

- (i) q_1 and q_2 (4 marks) (ii) p_1 and p_2 (3 marks) (iii) e_1 and e_2 (4 marks)
(iv) total output (1.5 marks) (v) total profit (2 marks)

(b) Explain any **three** conditions that could make price discrimination to occur (3 marks).

(6) Explain the following economic concepts/terms:

(i) Input and output expansion paths (4 marks)

(ii) Marginal rate of commodity substitution (2.5 marks)

(iii) Linear isoquant and kinked isoquant (4 marks)

(iv) Perfect competition (3 marks)

(v) Isocost and Isoquant (4 marks)

$$\begin{aligned}
 P_1 &= 80 - 5q_1 \\
 P_2 &= 180 - 20q_2 \\
 C &= 50 + 20q \\
 MR_1 &= 80 - 10q_1 \\
 MR_2 &= 180 - 40q_2 \\
 C' &= 20 \\
 MR_2 &= C' \\
 180 - 40q_2 &= 20 \\
 180 - 20 &= 40q_2 \\
 160 &= 40q_2 \\
 q_2 &= 4 \\
 P_2 &= 180 - 20(4) \\
 P_2 &= 180 - 80 \\
 P_2 &= 100 \\
 C &= 50 + 20(4) \\
 C &= 50 + 80 \\
 C &= 130 \\
 \text{Profit} &= TR - C \\
 \text{Profit} &= (P_1 q_1 + P_2 q_2) - C \\
 \text{Profit} &= (80 - 5q_1)q_1 + 100(4) - 130 \\
 \text{Profit} &= 80q_1 - 5q_1^2 + 400 - 130 \\
 \text{Profit} &= 80q_1 - 5q_1^2 + 270 \\
 \text{Profit}' &= 80 - 10q_1 \\
 \text{Profit}' &= 0 \\
 80 - 10q_1 &= 0 \\
 80 &= 10q_1 \\
 q_1 &= 8 \\
 P_1 &= 80 - 5(8) \\
 P_1 &= 80 - 40 \\
 P_1 &= 40 \\
 \text{Total Output} &= q_1 + q_2 \\
 \text{Total Output} &= 8 + 4 \\
 \text{Total Output} &= 12 \\
 \text{Total Profit} &= 80(8) + 100(4) - 130 \\
 \text{Total Profit} &= 640 + 400 - 130 \\
 \text{Total Profit} &= 910
 \end{aligned}$$

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 P_1 &= 80 - 5q_1 \\
 P_2 &= 180 - 20q_2 \\
 MR_1 &= 80 - 10q_1 \\
 MR_2 &= 180 - 40q_2 \\
 C &= 50 + 20q \\
 C' &= 20 \\
 MR_2 &= C' \\
 180 - 40q_2 &= 20 \\
 180 - 20 &= 40q_2 \\
 160 &= 40q_2 \\
 q_2 &= 4 \\
 P_2 &= 180 - 20(4) \\
 P_2 &= 180 - 80 \\
 P_2 &= 100 \\
 C &= 50 + 20(4) \\
 C &= 50 + 80 \\
 C &= 130 \\
 \text{Profit} &= TR - C \\
 \text{Profit} &= (P_1 q_1 + P_2 q_2) - C \\
 \text{Profit} &= (80 - 5q_1)q_1 + 100(4) - 130 \\
 \text{Profit} &= 80q_1 - 5q_1^2 + 400 - 130 \\
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 \text{Total Profit} &= 640 + 400 - 130 \\
 \text{Total Profit} &= 910
 \end{aligned}$$

$$\begin{aligned}
 e_1 &= \frac{P_1}{q_1} \cdot \frac{dq_1}{dP_1} \\
 e_1 &= \frac{80}{8} \cdot \frac{-5}{80 - 5(8)} \\
 e_1 &= 10 \cdot \frac{-5}{40} \\
 e_1 &= -1.25 \\
 e_2 &= \frac{P_2}{q_2} \cdot \frac{dq_2}{dP_2} \\
 e_2 &= \frac{100}{4} \cdot \frac{-20}{180 - 20(4)} \\
 e_2 &= 25 \cdot \frac{-20}{100} \\
 e_2 &= -5
 \end{aligned}$$