a) Describe the flow of messages through the concurrent system, the possible synchronisations, and the possible sequences of messages. Identify any problems. [15%]

The Keyboard process outputs key(x) to Plugboard. Plugboard receives this on its right channel (r) and outputs the mapped letter (the result of fplug(x)) on its left channel (l). Practically speaking, this is passed through three Rotors. In the context of CCS, each Rotor synchronises with the input that comes in on r and outputs a transformed value on l for the next (or, in the case of the final Rotor, the Reflector) to synchronise with.

The Reflector synchronises with the input to its input channel (in) and broadcasts an output on its output channel (out). This output is the original input from in transformed by the reflector function frefl(x). The input is then synchronised with by each Rotor on their right channel and output, transformed by frotor(p,x), for the next Rotor (or, in the case of the final Rotor, the Plugboard) to synchronise with. The

I identified the following problems:

- After Plugboard has output the result of $f_{plug}(x)$ to whichever channel it should use, it can still synchronise with messages on the same side of the board. This should be resolved by accepting from R first, then accepting from
 - L. Practically, this means that if multiple Keyboards were used with Enigma, more characters could be typed on other Keyboards and sent through the Plugboard.
- Rotors have a similar issue that would allow the characters to continue through Enigma to the point of displaying the character. In this instance, there could also be race conditions between incrementing the rotors and sending the encrypted character. These are made void by the fact that Keyboard cannot synchronise with inputs until the inc signal is received through the plugboard that is, any transmissions on the Rotors have already occurred.
- After a Rotor has synchronised with l or r once, it will not synchronise with inc_r again. It enters a recursion on RotorFunction(p), which cannot at any point synchronise with inc_r . What this means practically is that rotors, in this implementation, can be incremented only once.

b) Modify the model to make it a more accurate representation of the real Enigma system, and explain briefly how your version overcomes the problems you identified in (a).

RotorFunction should not be recursive:

$$RotorFunction(p) = l(x).\overline{r}(f_{rotor}(p, x)) + r(x).\overline{l}(\overline{f_{rotor}}(p, x))$$

Instead, choosing RotorFunction should result in a recursion on Rotor. This means that Rotor can respond to inc_r .

$$\begin{array}{lcl} Rotor(26,p) & = & inc_r.\overline{inc_l}.Rotor(0,p-26) + RotorFunction(p).Rotor(26,p) \\ Rotor(c,p) & = & inc_r.Rotor(c+1,p+1) + RotorFunction(p).Rotor(c,p) \end{array}$$

Plugboard should only respond from the right first.

$$Plugboard = r(x).\overline{l}(f_{plug}(x)).$$

$$l(x).\overline{r}(f_{plug}(x)).Plugboard$$

$$= in(x).\overline{out}(f_{refl}(x)).Reflector$$

$$Keyboard = \overline{key}(x).\overline{inc}.lamp(y).Keyboard$$

$$Plugboard = r(x).\overline{l}(f_{plug}(x)).$$

$$l(x).\overline{r}(f_{plug}(x)).Plugboard$$

$$Rotor(26, p) = inc_r.\overline{inc_l}.Rotor(0, p - 26) + RotorFunction(p).Rotor(0, p - 26)$$

$$RotorFunction(p) = l(x).\overline{r}(f_{rotor}(p, x))$$

$$+ r(x).\overline{l}(f_{rotor}(p, x))$$

$$Enigma = Reflector[ref/in, ref/out] | Rotor(c_2, p_2)[m1/l, m2/r, i3/inc_l, i2/inc_r] | Rotor(c_1, p_1)[m2/l, m3/r, i2/inc_l, i1/inc_r] | Plugboard[m3/l, keys/r] | Keyboard[keys/key, keys/lamp, i1/inc]$$

Figure 1: My modification to the abstract CCS/Pi-calculus model of the Enigma system components